

# Distributed Systems Assignment

s1140740

## 2.1

**Proof:** If  $V$  is a vector clock, prove that  $a \rightarrow b \iff V(a) \leq V(b)$ .

$$a \rightarrow b \implies V(a) \leq V(b)$$

There are three possibilities:

1. Event  $b$  was a local event of a process  $i$ , by definition  $V(b)[i] = V(a)[i] + 1$
2. Event  $b$  was a send message event of a process  $i$ .
3. Event  $b$  was a receive message event of a process  $i$ .

$$V(a) \leq V(b) \implies a \rightarrow b$$

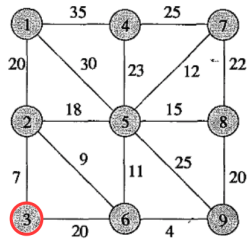
## 2.2

## 2.3

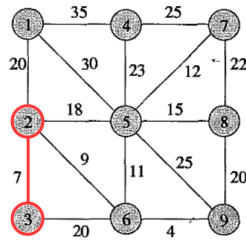
The weighted diameter of this graph is 7. The path realising this diameter is  $A \rightarrow C \rightarrow E \rightarrow G \rightarrow H$ .

If the graph was unweighted, the diameter would be 4 and the corresponding path would be  $A \rightarrow C \rightarrow F \rightarrow G \rightarrow I$ .

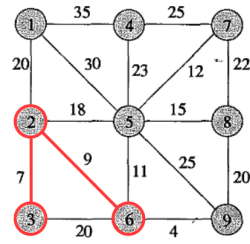
## 2.4



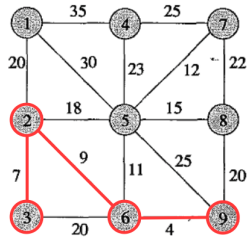
(a) Step 1



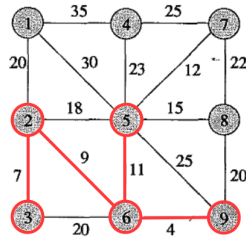
(b) Step 2



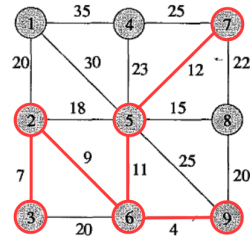
(c) Step 3



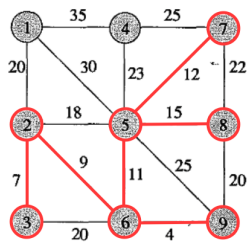
(d) Step 4



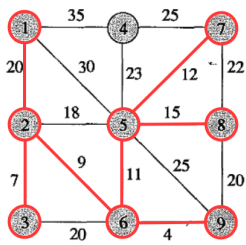
(e) Step 5



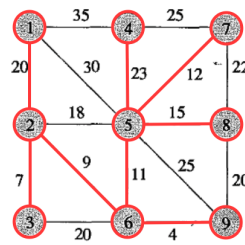
(f) Step 6



(g) Step 7



(h) Step 8



(i) Step 9

Figure 1: Prim's algorithm