

# TRIGONOMETRIC IDENTITIES

## MULTIPLE CHOICE QUESTIONS

- (1)  $\sin 2\alpha =$
- |                                   |                                   |
|-----------------------------------|-----------------------------------|
| (a) $\cos^2\alpha - \sin^2\alpha$ | (b) $2\sin^2\alpha + 1$           |
| (c) $2\sin\alpha \cos\alpha$      | (d) $\sin\alpha \cdot \cos\alpha$ |
- [Lahore Board 2005-08, Lahore Board 2015]
- (2)  $\cos 3\alpha =$
- |                                   |                             |
|-----------------------------------|-----------------------------|
| (a) $4\cos^3\alpha - 3\cos\alpha$ | (b) $3\cos\alpha - 4\cos^3$ |
| (c) $3\cos\alpha + 4\cos^3\alpha$ | (d) None of these           |
- [Lahore Board 2005]
- (3)  $\sec x =$
- |                      |                     |
|----------------------|---------------------|
| (a) $\sec(x + 2\pi)$ | (b) $\sec(x + \pi)$ |
| (c) $\cos x$         | (d) $\sin x$        |
- [Lahore Board 2005]
- (4)  $\sin P + \sin Q =$
- |   |  |
|---|--|
| (a) $2 \sin \frac{P+Q}{2} \cos \frac{P-Q}{2}$       | (b) $-2 \sin \frac{P+Q}{2} \cdot \sin \frac{P-Q}{2}$ |
| (c) $2 \cos \frac{P+Q}{2} \cdot \cos \frac{P-Q}{2}$ | (d) None of these                                    |
- [Lahore Board 2005]
- (5)  $\cos(\alpha - \beta) =$
- |   |   |
|---|---|
| (a) $\cos\alpha \cos\beta + \sin\alpha \sin\beta$ | (b) $\cos\alpha \cos\beta - \sin\alpha \sin\beta$ |
| (c) $\sin\alpha \cos\beta + \cos\alpha \sin\beta$ | (d) $\sin\alpha \cos\beta - \cos\alpha \sin\beta$ |
- [Gujranwala Board 2005]

(6)  $\operatorname{cosec}(\pi - \alpha) =$

- (a)  $\sin \alpha$   
(c)  $\cot \alpha$

- (b)  $\cos \alpha$   
(d)  $\operatorname{cosec} \alpha$

[Gujranwala Board 2005]

(7)  $1 + \cos 2\alpha =$

- (a)  $\cos^2 \alpha$   
(c)  $\sin^2 \alpha$

- (b)  $2\cos^2 \alpha$   
(d)  $2\sin \alpha$

[Gujranwala Board 2005]

(8)  $\cos\left(\frac{\pi}{2} - \beta\right) =$

- (a)  $\cos \beta$   
(c)  $\sin \beta$

- (b)  $\cos \frac{\pi}{2}$   
(d)  $-\sin \beta$

[Gujranwala Board 2005]

(9)  $2\sin \alpha \cos \beta =$

- (a)  $\sin(\alpha + \beta) + \cos(\alpha - \beta)$   
(c)  $\sin(\alpha + \beta) - \sin(\alpha - \beta)$

- (b)  $\sin(\alpha + \beta) + \sin(\alpha - \beta)$   
(d) None of these

[Gujranwala Board 2006]

(10)  $\sec\left(\frac{3\pi}{2} - \theta\right) =$

- (a)  $\operatorname{cosec} \theta$   
(c)  $-\sec \theta$

- (b)  $-\operatorname{cosec} \theta$   
(d) None of these

[Gujranwala Board 2006]

(11)  $\pm \sqrt{\frac{1 + \cos \alpha}{2}} =$

- (a)  $\cos \frac{\alpha}{2}$   
(c)  $\tan \frac{\alpha}{2}$

- (b)  $\sin \frac{\alpha}{2}$   
(d) None of these

[Gujranwala Board 2006]

(12)  $\sin 3\alpha =$

- (a)  $3\sin \alpha + 4\sin^3 \alpha$   
(c)  $3\sin \alpha - 4\sin^3 \alpha$

- (b)  $4\sin \alpha + 3\sin^3 \alpha$   
(d)  $3\sin \alpha + 4\sin^3 \alpha$

[Lahore Board 2006]

[Gujranwala Board 2006]

(13) If  $r \cos\theta = 3$ ,  $r \sin\theta = 4$  then  $r$  is:

- |        |         |
|--------|---------|
| (a) 25 | (b) -5  |
| (c) 5  | (d) -25 |

[Lahore Board 2006]

(14)  $\tan(180^\circ + \alpha)$  is equal to:

- |                  |                   |
|------------------|-------------------|
| (a) $\tan\alpha$ | (b) $-\tan\alpha$ |
| (c) $\cot\alpha$ | (d) $-\cot\alpha$ |

[Lahore Board 2006]

(15)  $\cos 2\theta$  is equal to:

- |   |   |
|---|---|
| (a) $\frac{1 - \tan^2\theta}{1 + \tan^2\theta}$ | (b) $\frac{1 - \tan^2\theta}{1 - \tan^2\theta}$ |
| (c) $\frac{2\tan\theta}{1 + \tan^2\theta}$      | (d) $\frac{1 + \tan^2\theta}{2\tan\theta}$      |

[Gujranwala Board 2007]

(16)  $\sin\theta =$

- |                                 |   |
|---------------------------------|---|
| (a) $2 \sin \frac{\theta}{2}$   | (b) $\sin \frac{\theta}{2} \cdot \cos \frac{\theta}{2}$   |
| (c) $2 \cos^2 \frac{\theta}{2}$ | (d) $2 \sin \frac{\theta}{2} \cdot \cos \frac{\theta}{2}$ |

[Lahore Board 2007]

(17) co-ratio of cosine is:

- |           |          |
|-----------|----------|
| (a) sec   | (b) sine |
| (c) cosec | (d) cos  |

[Lahore Board 2008]

(18)  $\tan 2\alpha$  equals:

- |  |   |
|--|---|
| (a) $\frac{\tan\alpha}{1 - \tan^2\alpha}$  | (b) $\frac{\tan 2\alpha}{1 - \tan^2\alpha}$ |
| (c) $\frac{2\tan\alpha}{1 - \tan^2\alpha}$ | (d) $\frac{2\tan\alpha}{1 + \tan^2\alpha}$  |

[Gujranwala Board 2008]

(19)  $\tan(270^\circ + \theta)$  is equal to:

- |                   |                   |
|-------------------|-------------------|
| (a) $\cot\theta$  | (b) $\tan\theta$  |
| (c) $-\cot\theta$ | (d) $-\tan\theta$ |

[Lahore Board 2014, Gujranwala Board 2009]

(20)  $\tan \frac{\alpha}{2}$  is equal to:

(a)  $\pm \sqrt{\frac{1 - \cos \alpha}{1 + \cos \alpha}}$

(b)  $\sqrt{\frac{1 + \cos \alpha}{1 - \cos \alpha}}$

(c)  $\pm \sqrt{\frac{1 - \cos \alpha}{2}}$

(d)  $\sqrt{\frac{1 + \cos \alpha}{2}}$

[Gujranwala Board 2009]

(21)  $\cos \left( \frac{\pi}{2} + \theta \right)$  equals:

(a)  $\cos \theta$

(b)  $-\sin \theta$

(c)  $\sin \theta$

(d)  $-\cos \theta$

[Lahore Board 2009]

(22)  $2\sin 12^\circ \sin 46^\circ$  equals:

(a)  $\cos 34^\circ + \cos 58^\circ$

(b)  $\sin 34^\circ - \sin 58^\circ$

(c)  $\sin 34^\circ + \sin 58^\circ$

(d)  $\cos 34^\circ - \cos 58^\circ$

[Lahore Board 2009]

(23)  $\sin \left( \frac{\pi}{2} - \theta \right)$  equals:

(a)  $\cos \theta$

(b)  $\sin \theta$

(c)  $-\cos \theta$

(d)  $-\sin \theta$

[Lahore Board 2009]

(24)  $2\sin \alpha \cos \beta$  equals:

(a)  $\sin(\alpha + \beta) - \sin(\alpha - \beta)$

(b)  $\cos(\alpha + \beta) + \cos(\alpha - \beta)$

(c)  $\sin(\alpha + \beta) + \sin(\alpha - \beta)$

(d)  $\cos(\alpha + \beta) - \cos(\alpha - \beta)$

[Lahore Board 2009]

(25)  $\sin \left( \frac{3\pi}{2} + \theta \right) =$

(a)  $\cos \theta$

(b)  $-\cos \theta$

(c)  $\sin \theta$

(d)  $-\sin \theta$

[Lahore Board 2010]

(26)  $2\cos 5\theta \cdot \sin 3\theta =$

(a)  $\sin 8\theta - \sin 2\theta$

(b)  $\sin 8\theta + \sin 2\theta$

(c)  $\cos 8\theta + \cos 2\theta$

(d)  $\sin 4\theta - \sin \theta$

[Lahore Board 2010]

(27)  $\cos \frac{\alpha}{2}$  is equal to:

(a)  $\frac{1 + \cos \alpha}{2}$

(b)  $\frac{1 - \cos \alpha}{2}$

(c)  $\frac{1 + \sin \alpha}{2}$

(d)  $\pm \sqrt{\frac{1 + \cos \alpha}{2}}$

[Gujranwala Board 2010]

(28)  $\tan 2\alpha =$  \_\_\_\_\_

(a)  $\frac{2 \tan \alpha}{1 - \tan^2 \alpha}$

(b)  $\frac{2 \tan \alpha}{1 + \tan^2 \alpha}$

(c)  $\frac{\tan \alpha}{1 - \tan^2 \alpha}$

(d)  $\frac{\tan \alpha}{1 + \tan^2 \alpha}$

[Lahore Board 2012]

(29)  $\cos(\pi - \theta) =$

(a)  $\sin \theta$

(b)  $-\sin \theta$

(c)  $\cos \theta$

(d)  $-\cos \theta$

[Lahore Board 2012]

(30)  $\cos(\pi - \theta) =$

(a)  $\sin \theta$

(b)  $-\sin \theta$

(c)  $\cos \theta$

(d)  $-\cos \theta$

[Lahore Board 2013]

(31)  $\sin(-300^\circ) =$

(a)  $-\frac{\sqrt{3}}{2}$

(b)  $\frac{\sqrt{3}}{2}$

(c)  $\frac{2}{\sqrt{3}}$

(d) 0

[Lahore Board 2013]

(32) Distance between the points A(3, 8) and B(5, 6) is:

(a)  $\sqrt{2}$

(b)  $2\sqrt{2}$

(c)  $\sqrt{3}$

(d)  $3\sqrt{3}$

(33) Fundamental law of trigonometry is \_\_\_\_\_ where  $\alpha, \beta$  are any two angles:

(a)  $\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$

(b)  $\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$

(c)  $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$

(d)  $\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$

(34)  $\cos \frac{\pi}{12} =$

(a)  $\frac{\sqrt{3}}{2}$

(b)  $\frac{\sqrt{3}-1}{\sqrt{2}}$

(c)  $\frac{\sqrt{3}+1}{\sqrt{2}}$

(d)  $\frac{\sqrt{3}+1}{2\sqrt{2}}$

(35)  $\sec (-300^\circ) =$

(a) 1

(b) -1

(c) 2

(d) -2

(36) If  $\alpha, \beta, \gamma$  are angles of triangle then  $\cos (\alpha + \beta) =$  \_\_\_\_\_

(a)  $\cos \gamma$

(b)  $-\cos \gamma$

(c)  $\sin \gamma$

(d)  $\sin \frac{\gamma}{2}$

(37)  $\sin(\alpha + \beta) \cdot \sin(\alpha - \beta) =$

(a)  $\sin^2 \alpha - \sin^2 \beta$

(b)  $\sin^2 \alpha + \sin^2 \beta$

(c)  $\cos^2 \alpha - \cos^2 \beta$

(d)  $\cos^2 \alpha + \cos^2 \beta$

(38)  $\frac{\cos 11^\circ + \sin 11^\circ}{\cos 11^\circ - \sin 11^\circ} =$

(a)  $\tan 65^\circ$

(b)  $\tan 54^\circ$

(c)  $\tan 56^\circ$

(d)  $\tan 37^\circ$

(39)  $\frac{\sin A + \sin 2A}{1 + \cos A + \cos 2A} =$

(a)  $\sin A$

(b)  $\cos A$

(c)  $\cot A$

(d)  $\tan A$

(40)  $2 \sin 7\theta \cos 3\theta =$

(a)  $\sin 10\theta + \sin 4\theta$

(b)  $\sin 10\theta - \sin 4\theta$

(c)  $\cos 10\theta + \cos 4\theta$

(d)  $\cos 10\theta - \cos 4\theta$

(41)  $\sin 5x + \sin 7x =$

(a)  $2 \sin 3x \cos x$

(b)  $2 \sin x \cos x$

(c)  $2 \sin x \cos 6x$

(d)  $2 \sin 6x \cos x$

(42)  $\sin \left( \frac{\pi}{4} - \theta \right) \sin \left( \frac{\pi}{4} + \theta \right) =$

(a)  $\frac{1}{2} \cos 2\theta$

(b)  $\frac{1}{2} \sin 2\theta$

(c)  $\frac{1}{2} \sin \theta \cos \theta$

(d)  $2 \sin \theta \cdot \cos 2\theta$

- (43) If  $x > y > 0$  then point  $P(x, y)$  lies in quadrant:  
 (a) I (b) II (c) III (d) IV
- (44)  $\tan\left(-\alpha + \frac{\pi}{2} - \beta\right) =$   
 (a)  $\tan(\alpha + \beta)$  (b)  $\tan(\alpha - \beta)$   
 (c)  $\cot(\alpha + \beta)$  (d)  $\cot(\alpha - \beta)$
- (45) If  $\cot\alpha + \cot\theta = 0$  then  $\alpha = ?$   
 (a)  $\frac{\pi}{2} - \theta$  (b)  $\pi - \theta$   
 (c)  $\pi + \theta$  (d) None of these
- (46) If  $\frac{2\cos\theta(1 - \cos^2\theta)}{\sin 2\theta} > 0$  and  $\frac{\sec^2\theta - 1}{\tan^2\theta \cdot \cot\theta} < 0$  then ' $\theta$ ' lies in the quadrant:  
 (a) I (b) II  
 (c) III (d) IV
- (47)  $\sec\theta \neq$   
 (a)  $\frac{\sqrt{1 + \cot^2\theta}}{\cot\theta}$  (b)  $\frac{1}{\sqrt{1 - \sin^2\theta}}$   
 (c)  $\sqrt{\operatorname{cosec}^2\theta - 1}$  (d)  $\frac{\operatorname{cosec}\theta}{\sqrt{\operatorname{cosec}^2\theta - 1}}$
- (48)  $\tan \frac{5\alpha}{2} =$   
 (a)  $\pm \sqrt{\frac{1 - \cos 5\alpha}{1 + \cos 5\alpha}}$  (b)  $\pm \sqrt{\frac{1 - \cos \frac{5\alpha}{2}}{1 + \cos \frac{5\alpha}{2}}}$   
 (c)  $\pm \sqrt{\frac{1 + \cos 5\alpha}{1 - \cos 5\alpha}}$  (d) None of these
- (49)  $\cos\alpha - 2\cos \frac{\alpha + \beta}{2} \cdot \cos \frac{\alpha - \beta}{2} + \cos\beta =$   
 (a)  $\sin\alpha \cos\beta$  (b) 0  
 (c)  $\sin(\alpha - \beta) + \cos\alpha$  (d)  $\cos\alpha \cdot \cos\beta$
- (50) The value of  $\cos 315^\circ$  is:  
 (a) 0 (b) 1  
 (c)  $\frac{\sqrt{3}}{2}$  (d)  $\frac{1}{\sqrt{2}}$
- (51)  $\cos 2\alpha =$  \_\_\_\_\_  
 (a)  $2 \cos^2\alpha + 1$  (b)  $2 \cos^2\alpha - 1$   
 (c)  $2 \sin^2\alpha + 1$  (d)  $2 \sin^2\alpha - 1$

*Answers*

(1)	c	(2)	a	(3)	a	(4)	a	(5)	a
(6)	d	(7)	b	(8)	c	(9)	b	(10)	b
(11)	a	(12)	c	(13)	c	(14)	a	(15)	a
(16)	d	(17)	b	(18)	c	(19)	c	(20)	a
(21)	b	(22)	d	(23)	a	(24)	c	(25)	b
(26)	a	(27)	d	(28)	a	(29)	d	(30)	d
(31)	b	(32)	b	(33)	b	(34)	d	(35)	c
(36)	d	(37)	c	(38)	c	(39)	d	(40)	a
(41)	d	(42)	a	(43)	a	(44)	c	(45)	b
(46)	b	(47)	c	(48)	a	(49)	b	(50)	d
(51)	b								



# SOLUTION

**Q.6**  $\operatorname{cosec}(\pi - \alpha)$

$$\begin{aligned}
 &= \frac{1}{\sin(\pi - \alpha)} = \frac{1}{\sin\pi \cos\alpha - \cos\pi \sin\alpha} \\
 &= \frac{1}{0 - (-1) \sin\alpha} \\
 &= \frac{1}{\sin\alpha} = \operatorname{cosec}\alpha
 \end{aligned}$$

**Q.7** As,  $\cos 2\alpha = 2\cos^2\alpha - 1$   
 $1 + \cos 2\alpha = 2\cos^2\alpha$

**Q.8**  $\cos\left(\frac{\pi}{2} - \beta\right)$

$$\begin{aligned}
 &= \cos\frac{\pi}{2} \cos\beta + \sin\frac{\pi}{2} \cdot \sin\beta \\
 &= 0 + (1) \sin\beta \\
 &= \sin\beta
 \end{aligned}$$

**Q.13**  $r \cos\theta = 3$  ,  $r \sin\theta = 4$   
 $r^2 \cos^2\theta = 9$  ..... (1)  $r^2 \sin^2\theta = 16$  ..... (2)

Adding (1) and (2).

$$\begin{aligned}
 r^2 \cos^2\theta + r^2 \sin^2\theta &= 9 + 16 \\
 r^2 (\cos^2\theta + \sin^2\theta) &= 25 \\
 r^2 &= 25 \\
 r &= 5
 \end{aligned}$$

**Q.14**  $\tan(180^\circ + \alpha)$   
 $= \tan(\pi + \alpha)$   
 $= \tan\alpha$

**Q.15**  $\cos 2\theta$   
 $= \cos^2\theta - \sin^2\theta$   
 $= \frac{\cos^2\theta - \sin^2\theta}{1}$

$$\begin{aligned}
 &= \frac{\cos^2\theta - \sin^2\theta}{\cos^2\theta + \sin^2\theta} \\
 &= \frac{\frac{\cos^2\theta - \sin^2\theta}{\cos^2\theta}}{\frac{\cos^2\theta + \sin^2\theta}{\cos^2\theta}} \\
 &= \frac{\frac{\cos^2\theta}{\cos^2\theta} - \frac{\sin^2\theta}{\cos^2\theta}}{\frac{\cos^2\theta}{\cos^2\theta} + \frac{\sin^2\theta}{\cos^2\theta}} \\
 &= \frac{1 - \tan^2\theta}{1 + \tan^2\theta}
 \end{aligned}$$

**Q.16** As,

$$\begin{aligned}
 \sin 2\theta &= 2\sin\theta \cos\theta \\
 \Rightarrow \sin\theta &= 2\sin\frac{\theta}{2} \cdot \cos\frac{\theta}{2}
 \end{aligned}$$

**Q.19**  $\tan(270^\circ + \theta)$

$$\begin{aligned}
 &= \tan\left(\frac{3\pi}{2} + \theta\right) \\
 &= -\cot\theta
 \end{aligned}$$

**Q.22** As,

$$\begin{aligned}
 -2\sin\alpha \sin\beta &= \cos(\alpha + \beta) - \cos(\alpha - \beta) \\
 2\sin\alpha \sin\beta &= -\cos(\alpha + \beta) + \cos(\alpha - \beta) \\
 \Rightarrow 2\sin 12^\circ \sin 46^\circ &= -\cos(12^\circ + 46^\circ) + \cos(12^\circ - 46^\circ) \\
 &= -\cos 58^\circ + \cos(-34^\circ) \\
 &= -\cos 58^\circ + \cos 34^\circ \\
 &= \cos 34^\circ - \cos 58^\circ
 \end{aligned}$$

**Q.26** As,

$$\begin{aligned}
 2\cos\alpha \sin\beta &= \sin(\alpha + \beta) - \sin(\alpha - \beta) \\
 2\cos 5\theta \sin 3\theta &= \sin(5\theta + 3\theta) - \sin(5\theta - 3\theta) \\
 &= \sin 8\theta - \sin 2\theta
 \end{aligned}$$

**Q.30**

$$\begin{aligned}
 |AB| &= \sqrt{(5-3)^2 + (6-8)^2} \\
 &= \sqrt{(2)^2 + (-2)^2} \\
 &= \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}
 \end{aligned}$$

**Q.32**  $\cos \frac{\pi}{12}$

$$\frac{\pi}{12} = \frac{\pi}{12} \times \frac{180}{\pi} = 15^\circ$$

$$\begin{aligned}\cos \frac{\pi}{12} &= \cos 15^\circ \\ &= \cos (45^\circ - 30^\circ) \\ &= \cos 45^\circ \cdot \cos 30^\circ + \sin 45^\circ \sin 30^\circ \\ &= \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \cdot \frac{1}{2} \\ &= \frac{\sqrt{3}}{2\sqrt{2}} + \frac{1}{2\sqrt{2}} \\ &= \frac{\sqrt{3} + 1}{2\sqrt{2}}\end{aligned}$$

**Q.33**  $\sec(-300^\circ)$

$$\begin{aligned}&= \frac{1}{\cos(-300^\circ)} \\ &= \frac{1}{\cos(300^\circ)} \\ &= \frac{1}{\cos(360^\circ - 60^\circ)} \\ &= \frac{1}{\cos\left(2\pi - \frac{\pi}{3}\right)} \\ &= \frac{1}{\cos \frac{\pi}{3}} = \frac{1}{\frac{1}{2}} = 2\end{aligned}$$

**Q.34** As,  $\alpha + \beta + \gamma = 180^\circ$   
 $\alpha + \beta = 180^\circ - \gamma$   
 $\Rightarrow \cos(\alpha + \beta)$   
 $= \cos(180^\circ - \gamma)$   
 $= -\cos \gamma$

**Q.35**  $\sin(\alpha + \beta) \cdot \sin(\alpha - \beta)$

$$\begin{aligned}
 &= (\sin\alpha \cos\beta + \cos\alpha \sin\beta)(\sin\alpha \cos\beta - \cos\alpha \sin\beta) \\
 &= (\sin\alpha \cos\beta)^2 - (\cos\alpha \sin\beta)^2 \\
 &= \sin^2\alpha \cos^2\beta - \cos^2\alpha \sin^2\beta \\
 &= \sin^2\alpha (1 - \sin^2\beta) - (1 - \sin^2\alpha) \sin^2\beta \\
 &= \sin^2\alpha - \sin^2\alpha \sin^2\beta - \sin^2\beta + \sin^2\alpha \sin^2\beta \\
 &= \sin^2\alpha - \sin^2\beta
 \end{aligned}$$

**Q.36** As,

$$\begin{aligned}
 \tan 56^\circ &= \tan(45^\circ + 11^\circ) = \frac{\sin(45^\circ + 11^\circ)}{\cos(45^\circ + 11^\circ)} \\
 &= \frac{\sin 45^\circ \cos 11^\circ + \cos 45^\circ \sin 11^\circ}{\cos 45^\circ \cos 11^\circ - \sin 45^\circ \sin 11^\circ} \\
 &= \frac{\frac{1}{\sqrt{2}} \cdot \cos 11^\circ + \frac{1}{\sqrt{2}} \sin 11^\circ}{\frac{1}{\sqrt{2}} \cos 11^\circ - \frac{1}{\sqrt{2}} \sin 11^\circ} \\
 &= \frac{\cos 11^\circ + \sin 11^\circ}{\cos 11^\circ - \sin 11^\circ}
 \end{aligned}$$

**Q.37**  $\frac{\sin A + \sin 2A}{1 + \cos A + \cos 2A}$

$$\begin{aligned}
 &= \frac{\sin A + \sin 2A}{1 + \cos A + 2\cos^2 A - 1} \\
 &= \frac{\sin A + 2\sin A \cos A}{\cos A + 2\cos^2 A} \\
 &= \frac{\sin A(1 + 2\cos A)}{\cos A(1 + 2\cos A)} \\
 &= \frac{\sin A}{\cos A} = \tan A
 \end{aligned}$$

**Q.38** As,

$$\begin{aligned}
 2\sin\alpha \cos\beta &= \sin(\alpha + \beta) + \sin(\alpha - \beta) \\
 2\sin 70^\circ \cos 30^\circ &= \sin(70^\circ + 30^\circ) + \sin(70^\circ - 30^\circ) \\
 &= \sin 100^\circ + \sin 40^\circ
 \end{aligned}$$

**Q.39** As,

$$\begin{aligned}\sin P + \sin Q &= 2\sin \frac{P+Q}{2} \cdot \cos \frac{P-Q}{2} \\ \Rightarrow \sin 5x + \sin 7x &= 2\sin \frac{5x+7x}{2} \cos \frac{5x-7x}{2} \\ &= 2\sin \frac{12x}{2} \cdot \cos \frac{-2x}{2} \\ &= 2\sin 6x \cdot \cos x\end{aligned}$$

**Q.40** As,

$$\begin{aligned}-2\sin\alpha \sin\beta &= \cos(\alpha + \beta) - \cos(\alpha - \beta) \\ \sin\alpha \sin\beta &= -\frac{1}{2} [\cos(\alpha + \beta) - \cos(\alpha - \beta)] \\ \Rightarrow \sin\left(\frac{\pi}{4} - \theta\right) \cdot \sin\left(\frac{\pi}{4} + \theta\right) &= -\frac{1}{2} \left[ \cos\left(\frac{\pi}{4} - \theta + \frac{\pi}{4} + \theta\right) - \cos\left(\frac{\pi}{4} - \theta - \frac{\pi}{4} - \theta\right) \right] \\ &= -\frac{1}{2} \left[ \cos\left(2\frac{\pi}{4}\right) - \cos(-2\theta) \right] \\ &= -\frac{1}{2} \left[ \cos\frac{\pi}{2} - \cos 2\theta \right] \\ &= -\frac{1}{2} [0 - \cos 2\theta] \\ &= -\frac{1}{2} \cos 2\theta\end{aligned}$$

$$\begin{aligned}\text{Q.42 } \tan\left(-\alpha + \frac{\pi}{2} - \beta\right) \\ &= \tan\left(\frac{\pi}{2} - (\alpha + \beta)\right) \\ &= \cot(\alpha + \beta)\end{aligned}$$

$$\begin{aligned}\text{Q.43 } \text{As, } \cot\alpha + \cot\theta &= 0 \\ \Rightarrow \cot\alpha &= -\cot\theta\end{aligned}$$

Which is possible only if  $\alpha = \pi - \theta$ **Q.44**

$$\frac{2\cos\theta(1 - \cos^2\theta)}{\sin 2\theta} > 0$$

$$\Rightarrow \frac{2\cos\theta \cdot \sin^2\theta}{2\sin\theta \cdot \cos\theta} > 0$$

$$\Rightarrow \sin\theta > 0$$

Also,

$$\frac{\sec^2\theta - 1}{\tan^2\theta \cdot \cot\theta} < 0$$

$$\Rightarrow \frac{\tan^2\theta}{\tan^2\theta \cdot \cot\theta} < 0$$

$$\Rightarrow \frac{1}{\cot\theta} < 0$$

$$\Rightarrow \tan\theta < 0$$

$$\Rightarrow \text{Quadrant will be II}$$

**Q.45** As,

$$\begin{aligned} & \sqrt{\operatorname{cosec}^2\theta - 1} \\ &= \sqrt{\cot^2\theta} = \cot\theta \neq \sec\theta \end{aligned}$$

**Q.46** As,

$$\begin{aligned} \tan \frac{\alpha}{2} &= \pm \sqrt{\frac{1 - \cos\alpha}{1 + \cos\alpha}} \\ \tan \frac{5\alpha}{2} &= \pm \sqrt{\frac{1 - \cos 5\alpha}{1 + \cos 5\alpha}} \end{aligned}$$

**Q.47**  $\cos\alpha - 2\cos \frac{\alpha + \beta}{2} \cdot \cos \frac{\alpha - \beta}{2} + \cos\beta$

$$= \cos\alpha - [\cos\alpha + \cos\beta] + \cos\beta$$

$$= \cos\alpha - \cos\alpha - \cos\beta + \cos\beta$$

$$= 0$$

**Q.50**  $\cos 315^\circ$

$$= \cos (3 \times 90^\circ + 45^\circ)$$

$$= \sin 45^\circ = \frac{1}{\sqrt{2}}$$