

The University Interscholastic League
Number Sense Test • HS District • 2025

Contestant's Number _____

Read directions carefully
before beginning test

**DO NOT UNFOLD THIS SHEET
UNTIL TOLD TO BEGIN**

Final _____

2nd _____

1st _____

Score _____

Initials _____

Directions: Do not turn this page until the person conducting this test gives the signal to begin. This is a ten-minute test. There are 80 problems. Solve accurately and quickly as many as you can in the order in which they appear. ALL PROBLEMS ARE TO BE SOLVED MENTALLY. Make no calculations with paper and pencil. Write only the answer in the space provided at the end of each problem. Problems marked with a (*) require approximate integral answers; any answer to a starred problem that is within five percent of the exact answer will be scored correct; all other problems require exact answers.

The person conducting this contest should explain these directions to the contestants.

STOP -- WAIT FOR SIGNAL!

- (1) _____ — 429 = 2025 (19) MMCDXXIX — XV = _____ (Arabic Numeral)
- (2) 24×25 = _____ *(20) $\sqrt{242} \times \sqrt{925}$ = _____
- (3) $2429 \div 6$ = _____ (mixed number) (21) If $A^4 \times A^{-2} \div A^9 = A^k$ and $A > 1$, then k = _____
- (4) $4\frac{2}{9} + 20\frac{2}{5}$ = _____ (mixed number) (22) $1492 \times 8 + 64$ = _____
- (5) $4\frac{1}{4}\%$ = _____ (decimal) (23) $6^3 + \sqrt[3]{729}$ = _____
- (6) 0.0625 = _____ (fraction) (24) $[24 + 29 \times 20 - 25] \div 7$ has a remainder of _____
- (7) $42.9 \times 10^2 - 25$ = _____ (25) $5\frac{4}{5} \times 5\frac{1}{5}$ = _____ (mixed number)
- (8) $4\frac{1}{2}$ minutes = _____ (seconds) (26) 24 base 6 is written as _____ base 9
- (9) $4 \times 6 \div 8 + 9 \times 10 - 12$ = _____ (27) $[\{f, o, u, r\} \cup \{f, i, v, e\}] \cap \{e, i, g, h, t\}$ contains how many distinct elements? _____
- *(10) 292.5×42.4 = _____ (28) One and a fourth million plus two thousand nine hundred twenty-five is _____
- (11) $24 + 53 + 82 + 111 + 140$ = _____ (29) $53^2 + 57^2$ = _____
- (12) GCD 34 and 51 is _____ *(30) $520292 \div 424$ = _____
- (13) $2429 \div 4$ has a remainder of _____ (31) 24% of $266\frac{2}{3}$ = _____
- (14) If almonds sell for \$1.60 an ounce, what will a pound of almonds cost? \$ _____ (32) $(3^5 + 6^5) \div 9$ has a remainder of _____
- (15) 93×102 = _____ (33) The quadratic equation, $9x^2 - 6x + k = 0$, has two equal roots. Find k . _____
- (16) $\$4.24 + \$4.29 + \$20.25$ = \$ _____ (34) The 16th term of the sequence 1, 3, 6, 10, 15, ... is 136. The 15th term is _____
- (17) $\$4.24 - \$4.29 + \$20.25$ = \$ _____
- (18) $\$4.20 + \$4.33 + \$20.47$ = \$ _____

- (35) Let $5x + y = 8$ and $2x + y = 4$. Find y . _____
- (36) If $f(x) = x^2 + 14x + 49$, then $f(13) =$ _____
- (37) Set $A = \{4, 2, 4, 2, 9, 2, 0, 2, 5\}$. The range of set A minus the mode of set A is _____
- (38) $\sqrt[3]{6859} =$ _____
- (39) $0.9222\dots =$ _____ (proper fraction)
- *(40) The circumference of a circle is 424 cm. The area of the circle is _____ sq. cm
- (41) $(2x - 9)^2 = ax^2 + bx + c$ and $a + b + c =$ _____
- (42) Find x , if $4^{3x} = 256$. _____
- (43) $9^B + 3B = 87$ and $B^9 =$ _____
- (44) $429 \times 13 =$ _____
- (45) $23^2 + 73^2 =$ _____
- (46) $(8^3 - 11^3) \div (8 - 11) =$ _____
- (47) $424 \text{ base } 9 \times 2 \text{ base } 9 =$ _____ base 9
- (48) $424 \text{ base } 9 \times 2 \text{ base } 9 + 25 \text{ base } 9 =$ _____ base 9
- (49) $424 \text{ base } 9 \times 3 \text{ base } 9 + 25 \text{ base } 9 =$ _____ base 9
- *(50) $4\frac{3}{4}$ "leagues of land" in Texas is _____ acres
- (51) $2 + 9 + 11 + 20 + 31 + 51 + 82 + 133 + 215 + 348 + 563 =$ _____
- (52) If a 4" by 8" picture is enlarged to a 12" by 24" picture, its perimeter is multiplied by _____
- (53) How many integers greater than 1 and less than 29 are relatively prime to 29? _____
- (54) $(\frac{1}{3} + \frac{1}{6} + \frac{1}{10} + \dots + \frac{1}{45} + \frac{1}{55}) \times 99 =$ _____
- (55) $11^{44} \div 29$ has a remainder of _____
- (56) The point $(-2, -9)$ is reflected across the line $y = x$ to the point (h, k) . Find $h - k$. _____
- (57) The sum of the digits of a 3-digit number is 8. How many such numbers exist? _____
- (58) $2025_8 \div 7_8$ has a remainder of _____
- (59) The multiplicative inverse of 0.9166... is _____
- *(60) If \$10.00 can buy 1564.69 yen, then \$2429.00 can buy _____ yen
- (61) If $\frac{2x+9}{2x} + \frac{2x+4}{2x-5} = \frac{ax^2+bx+c}{dx^2+ex+f}$, then $(a + b + c) \div (d + e + f) =$ _____
- (62) $\text{Arccsc}(-2) = k\pi$ rads and $k =$ _____
- (63) $6 = 110_2$, $28 = 11100_2$, and $496 =$ _____₂
- (64) Change $0.13444\dots_6$ to a base 6 fraction. _____₆
- (65) The Greatest Integer Function is written as $f(x) = [x]$. Find $[\sqrt{2} + \sqrt{3} + \sqrt{5} + \sqrt{7}]$. _____
- (66) If $A = \begin{bmatrix} 1 & 0 & 1 \\ 2 & 3 & 5 \\ 4 & 6 & 8 \end{bmatrix}$, then $|A| =$ _____
- (67) Let $i^{(19)} = a\sqrt{b}$. Find $b - a$. _____
- (68) If $\sqrt{16 - \sqrt{18\sqrt{20 - 22x}}} = 2$, then $x =$ _____
- (69) Two dice are thrown. What are the odds that their sum is divisible by 4? _____
- *(70) $\sqrt[3]{424292025} =$ _____
- (71) The directrix of $x = y^2$ is $x =$ _____
- (72) The remainder when $f(x) = x^4 - 3x^3 + 2x - 1$ is divided by $2x + 1$ is _____
- (73) If $f(x) = \frac{4x+24}{29}$ and $f^{-1}(x) = ax + b$, then $b =$ _____
- (74) The initial point of vector v is $(2, 3)$ and the terminal point is $(5, -7)$. If $\|v\| = k$, then $k^2 =$ _____
- (75) Let $h(x) = (2x + 3)^4$. Find $h'(-5)$. _____
- (76) $\int_0^1 \int_1^2 xy \, dy \, dx =$ _____
- (77) 440 feet per second = _____ miles per hour
- (78) Given: 2, 8, 18, 32, k , 72, Find k . _____
- (79) $\lim_{x \rightarrow \infty} \left(\frac{x-1}{x^2+5} \right) =$ _____
- *(80) 42925 varas (Texas) = _____ yards

DO NOT DISTRIBUTE TO STUDENTS BEFORE OR DURING THE CONTEST

University Interscholastic League - Number Sense Answer Key HS • District • 2025

*number) $x - y$ means an integer between x and y inclusive

NOTE: If an answer is of the type like $\frac{2}{3}$ it cannot be written as a repeating decimal

- | | | | |
|-----------------------|-----------------------|----------------------------------|---|
| (1) 2,454 | (19) 2,414 | (35) $\frac{4}{3}, 1\frac{1}{3}$ | (59) $\frac{12}{11}, 1\frac{1}{11}$ |
| (2) 600 | *(20) 450 — 496 | (36) 400 | *(60) 361,061 —
399,066 |
| (3) $404\frac{5}{6}$ | (21) — 7 | (37) 7 | (61) $3.5, \frac{7}{2}, 3\frac{1}{2}$ |
| (4) $24\frac{28}{45}$ | (22) 12,000 | (38) 19 | (62) $-\frac{1}{6}$ |
| (5) .0425 | (23) 225 | (39) $\frac{83}{90}$ | (63) 111110000 |
| (6) $\frac{1}{16}$ | (24) 5 | *(40) 13,591 — 15,021 | (64) $\frac{121}{500}$ |
| (7) 4,265 | (25) $30\frac{4}{25}$ | (41) 49 | (65) 8 |
| (8) 270 | (26) 17 | (42) $\frac{4}{3}, 1\frac{1}{3}$ | (66) — 6 |
| (9) 81 | (27) 2 | (43) 512 | (67) 0 |
| *(10) 11,782 — 13,022 | (28) 1,252,925 | (44) 5,577 | (68) — 2 |
| (11) 410 | (29) 6,058 | (45) 5,858 | (69) $\frac{1}{3}$ |
| (12) 17 | *(30) 1,166 — 1,288 | (46) 273 | *(70) 714 — 789 |
| (13) 1 | (31) 64 | (47) 848 | (71) $-.25, -\frac{1}{4}$ |
| (14) 25.60 | (32) 0 | (48) 874 | (72) $-1.5625, -\frac{25}{16},$
$-1\frac{9}{16}$ |
| (15) 9,486 | (33) 1 | (49) 1408 | (73) — 6 |
| (16) 28.78 | (34) 120 | *(50) 19,984 — 22,086 | (74) 109 |
| (17) 20.20 | | (51) 1,465 | (75) — 2,744 |
| (18) 29.00 | | (52) 3 | (76) $.75, \frac{3}{4}$ |
| | | (53) 27 | (77) 300 |
| | | (54) 81 | (78) 50 |
| | | (55) 24 | (79) 0 |
| | | (56) — 7 | |
| | | (57) 36 | |
| | | (58) 2 | |
| | | | *(80) 37,759 — 41,732 |