

**The University Interscholastic League**  
**Number Sense Test • HS B • 2025**

Contestant's Number \_\_\_\_\_

Final	_____	_____
2nd	_____	_____
1st	_____	_____
Score	_____	Initials

Read directions carefully  
before beginning test

**DO NOT UNFOLD THIS SHEET  
UNTIL TOLD TO BEGIN**

**Directions:** Do not turn this page until the person conducting this test gives the signal to begin. This is a ten-minute test. There are 80 problems. Solve accurately and quickly as many as you can in the order in which they appear. ALL PROBLEMS ARE TO BE SOLVED MENTALLY. Make no calculations with paper and pencil. Write only the answer in the space provided at the end of each problem. Problems marked with a (\*) require approximate integral answers; any answer to a starred problem that is within five percent of the exact answer will be scored correct; all other problems require exact answers.

**The person conducting this contest should explain these directions to the contestants.**

**STOP -- WAIT FOR SIGNAL!**

- (1)  $2725 + \underline{\hspace{2cm}} = 3825$       (19)  $104 \times 109 = \underline{\hspace{2cm}}$
- (2)  $528.3 - 27.25 = \underline{\hspace{2cm}}$  (decimal)      \*(20)  $\sqrt{2738} \times 2025 = \underline{\hspace{2cm}}$
- (3)  $\frac{2}{7} \times \frac{3}{8} \times \frac{2}{5} = \underline{\hspace{2cm}}$       (21) The additive inverse of  $(6)^{-1}$  is \_\_\_\_\_
- (4)  $2738 \div (-5) = \underline{\hspace{2cm}}$  (mixed number)      (22)  $27\frac{3}{7} \div 3 = \underline{\hspace{2cm}}$  (improper fraction)
- (5)  $\frac{27}{25} = \underline{\hspace{2cm}} \%$       (23) Write two and a fifth million twenty-five thousand five hundred two in digits. \_\_\_\_\_
- (6)  $27 \times 25 - 38 \times 25 = \underline{\hspace{2cm}}$       (24)  $\sqrt{5041} = \underline{\hspace{2cm}}$
- (7)  $13.5 \times 10^2 - 25 = \underline{\hspace{2cm}}$       (25)  $8\frac{1}{5} \times 2\frac{1}{5} = \underline{\hspace{2cm}}$  (mixed number)
- (8)  $12 - 10 \times 9 + 8 \times 6 \div 4 = \underline{\hspace{2cm}}$       (26) 275 base 8 is written as \_\_\_\_\_ base 10
- (9)  $23^2 = \underline{\hspace{2cm}}$       (27)  $|2 - 7| - |2 - 5| - |3 - 8| - 25 = \underline{\hspace{2cm}}$
- \*(10)  $207 + 2025 + 308 + 2025 = \underline{\hspace{2cm}}$       (28)  $24^2 \div 12^2 \times 6^2 = \underline{\hspace{2cm}}$
- (11)  $27 + 38 + 49 + 60 + 71 = \underline{\hspace{2cm}}$       (29)  $207308 \div 11$  has a remainder of \_\_\_\_\_
- (12)  $\frac{3}{4}$  of 3 gallons 2 quarts = \_\_\_\_\_ pints      \*(30)  $\sqrt{20252738} = \underline{\hspace{2cm}}$
- (13)  $2738 \div 4$  has a remainder of \_\_\_\_\_
- (14)  $1996 \times 4 + 16 = \underline{\hspace{2cm}}$
- (15) The largest prime divisor of  $38 \times 27$  is \_\_\_\_\_
- (16) If 3 pens cost 42¢, then 10 pens cost \$ \_\_\_\_\_
- (17) The LCM of 8, 20, and 32 is \_\_\_\_\_
- (18)  $(5 \times 3^2 \times 2^3) \div (2 \times 5) = \underline{\hspace{2cm}}$
- (32) If  $x = 7$  and  $y = 8$ , then  $(x - y)(x^2 + xy + y^2) = \underline{\hspace{2cm}}$
- (33) If  $f(x) = 2x^2 + 4x + 1$ , then  $f(-0.5) = \underline{\hspace{2cm}}$
- (34) How many of the first six hexagonal numbers are triangular numbers? \_\_\_\_\_

(35)  $\frac{1}{5}$  of 275 is \_\_\_\_\_

(36)  $\frac{4}{5}$  of 275 is \_\_\_\_\_

(37)  $\frac{2}{5}$  of 275 +  $\frac{3}{5}$  of 275 is \_\_\_\_\_

(38) Set A = {2, 7, 3, 8, 2, 0, 2, 5}. The range of set A minus the mode of set A is \_\_\_\_\_

(39) If  $f(x) = x^3 + 3x^2 + 3x + 1$ , then  $f(-4)$  is \_\_\_\_\_

\*(40)  $(0.151515\dots \times 2738)^2 =$  \_\_\_\_\_

(41) 48 is what percent greater than 36? \_\_\_\_\_ %

(42) The modulus of  $7 + 23i = k$  and  $k^2 =$  \_\_\_\_\_

(43) The product of the roots of  $2x^2 + 7x - 8 = 0$  is \_\_\_\_\_

(44)  $207 \times 14 =$  \_\_\_\_\_

(45)  $71^2 + 13^2 =$  \_\_\_\_\_

(46) If 75 cows need 120 acres to graze sufficiently, how many acres will 125 cows need? \_\_\_\_\_

(47) The point  $(-3, 8)$  is reflected across the line  $y = 7$  to the point  $(h, k)$ . Find  $h + k$ . \_\_\_\_\_

(48)  $B^4 - 4B = 8$  and  $4^B =$  \_\_\_\_\_

(49) Let  $(7x - 8)^2 = ax^2 + bx + c$ . Find  $a + b + c$ . \_\_\_\_\_

\*(50)  $\sqrt[3]{207308} + 2025 =$  \_\_\_\_\_

(51) Let  $\frac{7!}{8!} = \frac{(x)!}{(x+1)!}$ . Find x. \_\_\_\_\_

(52) If a 3" by 6" picture is enlarged to a 9" by 18" picture, its perimeter is multiplied by \_\_\_\_\_

(53)  $24^2 + 25^2 =$  \_\_\_\_\_

(54)  $1.1 + 2.2 + 3.3 + 5.5 + 8.8 + 13.13 + 21.21 + 34.34 =$  \_\_\_\_\_ (decimal)

(55)  $(7^3 - 8^3) \div (7 - 8) =$  \_\_\_\_\_

(56)  $207_9 + 308_9 + 2025_9 =$  \_\_\_\_\_<sub>9</sub>

(57) The probability of drawing a black king or an ace from a standard deck is \_\_\_\_\_

(58)  $2345_7 \div 67$  has a remainder of \_\_\_\_\_

(59) 105 miles per hour = \_\_\_\_\_ feet per second

\*(60)  $[0.2666\dots \times 4444]^2 =$  \_\_\_\_\_

(61)  $\text{Arccos}\left(-\frac{1}{2}\right) = k\pi$  rads,  $0 < k < 1$ , and  $k =$  \_\_\_\_\_

(62)  $1^3 + 3^3 + 5^3 + 7^3 =$  \_\_\_\_\_

(63) The Greatest Integer Function is written as  $f(x) = [x]$ . Find  $[\sqrt{10} + \sqrt{7}]$ . \_\_\_\_\_

(64)  $f(x) = x - 2$ ,  $g(x) = 3x + 4$ , and  $f(g(-1)) =$  \_\_\_\_\_

(65) The coefficient in the  $x^2y^2$  term if  $(2x + y)^4$  is \_\_\_\_\_

(66) The total surface area of a hemisphere with a 10 inch diameter is  $k\pi$  sq. inches.  $k =$  \_\_\_\_\_

(67) If  $\sqrt{6 + 5\sqrt{18\sqrt{9-x}}} = 6$ , then  $x =$  \_\_\_\_\_

(68) If  $\frac{3x-1}{x+3} - \frac{2x-1}{x+2} = \frac{ax^2+bx+c}{dx^2+ex+f}$ , then  $(a + b + c) + (d + e + f) =$  \_\_\_\_\_

(69) If  $\frac{3}{11}$  base 7 = 0.ababab... base 7, then  $a + b =$  \_\_\_\_\_

\*(70)  $1^3 + 2^3 + 3^3 + 4^3 + \dots + 13^3 =$  \_\_\_\_\_

(71) The sum of the digits of a 3-digit number is 11. How many such numbers exist? \_\_\_\_\_

(72)  $354 \times 356 =$  \_\_\_\_\_

(73) If  $N \div 3$  has a remainder of 2, then  $5N \div 3$  has a remainder of \_\_\_\_\_

(74) If the initial point of vector v is  $(1, 3)$  and the terminal point is  $(1, -4)$ , then  $\|v\| =$  \_\_\_\_\_

(75)  $\int_1^3 (4x - 2) dx + \int_3^5 (4x - 2) dx =$  \_\_\_\_\_

(76) Let  $f(x) = (3x + 4)^2$ . Find  $f'(-2)$ . \_\_\_\_\_

(77) The ratio of p to q is 1 to 3 and  $p - q = 6$ .  $p =$  \_\_\_\_\_

(78) Given: 2, 2, 5, 8, 14, k, 38, 62, ... . Find k. \_\_\_\_\_

(79) The harmonic mean of 1, 4, and 4 is \_\_\_\_\_

\*(80) 2738 yards = \_\_\_\_\_ varas (Texas)

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\*number)  $x - y$  means an integer between  $x$  and  $y$  inclusive

NOTE: If an answer is of the type like  $\frac{2}{3}$  it cannot be written as a repeating decimal

- |                       |                            |                                     |                                |
|-----------------------|----------------------------|-------------------------------------|--------------------------------|
| (1) 1,100             | (19) 11,336                | (35) 55                             | (59) 154                       |
| (2) 501.05            | *(20) 100,662 —<br>111,257 | (36) 220                            | *(60) 1,334,164 —<br>1,474,602 |
| (3) $\frac{3}{70}$    | (21) $-\frac{1}{6}$        | (37) 275                            | (61) $\frac{2}{3}$             |
| (4) $-547\frac{3}{5}$ | (22) $\frac{64}{7}$        | (38) 6                              | (62) 496                       |
| (5) 108               | (23) 2,225,502             | (39) —27                            | (63) 5                         |
| (6) —275              | (24) 71                    | *(40) 163,495 —<br>180,704          | (64) —1                        |
| (7) 1,325             | (25) $18\frac{1}{25}$      | (41) $\frac{100}{3}, 33\frac{1}{3}$ | (65) 24                        |
| (8) —66               | (26) 189                   | (42) 578                            | (66) 75                        |
| (9) 529               | (27) —28                   | (43) —4                             | (67) 5                         |
| *(10) 4,337 — 4,793   | (28) 144                   | (44) 2,898                          | (68) 7                         |
| (11) 245              | (29) 2                     | (45) 5,210                          | (69) 6                         |
| (12) 21               | *(30) 4,276 — 4,725        | (46) 200                            | *(70) 7,867 — 8,695            |
| (13) 2                | (31) $37\frac{1}{3}$       | (47) 3                              | (71) 61                        |
| (14) 8,000            | (32) —169                  | (48) 16                             | (72) 126,024                   |
| (15) 19               | (33) $-.5, -\frac{1}{2}$   | (49) 1                              | (73) 1                         |
| (16) 1.40             | (34) 6                     | *(50) 1,980 — 2,188                 | (74) 7                         |
| (17) 160              |                            | (51) 7                              | (75) 40                        |
| (18) 36               |                            | (52) 3                              | (76) —12                       |
|                       |                            | (53) 1,201                          | (77) —3                        |
|                       |                            | (54) 89.58                          | (78) 23                        |
|                       |                            | (55) 169                            | (79) 2                         |
|                       |                            | (56) 2542                           | *(80) 2,810 — 3,104            |
|                       |                            | (57) $\frac{3}{26}$                 |                                |
|                       |                            | (58) 2                              |                                |