# Parameters: physical and computational

### beta (of the ions)

$$\beta_i = \frac{n_i k_B T_i}{B^2/(8\pi)} = \frac{\text{thermal pressure}}{\text{magnetic pressure}}$$

### sigma (of the ions)

$$\sigma_i = \frac{B^2/(4\pi)}{n_i m_i c^2} = \frac{\text{magnetic pressure} (\times 2)}{\text{rest-mass energy density}}$$

## temperature ratio

$$\frac{T_e}{T_i} = \frac{\text{electron temperature}}{\text{ion temperature}}$$

#### Computational

dstripe

**dv**stripe

**n**stripe

My

**n**times

 $m_i/m_e$ 

ppc

c/wpe

### Full relativistic definition of sigma includes enthalpy

## sigma, including enthalpy

$$\sigma_w = \frac{\frac{m_i}{m_e} + 1}{\frac{m_i}{m_e} \left(1 + \frac{\hat{\gamma}_i}{\hat{\gamma}_i - 1} \frac{k_B T_i}{m_i c^2}\right) + \left(1 + \frac{\hat{\gamma}_e}{\hat{\gamma}_e - 1} \frac{k_B T_e}{m_e c^2}\right)} \frac{B^2}{4\pi (n_i m_i + n_e m_e)c^2}$$

pprox 1 for a cold plasma

$$\approx \frac{B^2}{4\pi n_i m_i c^2} \equiv \sigma_i$$

For a high-beta (thermally 'hot') plasma, the contribution from the thermal pressure is non-negligible

One more important definition: Alfvén velocity, which describes the speed of magnetic waves

### Alfvén velocity

$$\frac{v_A}{c} = \sqrt{\frac{\sigma_w}{1 + \sigma_w}}$$