

$$1) \quad 3575x + 1846y = 117 \quad |:13$$

$$3575 - 1846 = 1729$$

$$1846 - 1729 = 117$$

$$1729 - 117 \cdot 14 = 91$$

$$117 - 91 = 26$$

$$91 - 26 \cdot 3 = 13$$

$$26 - 2 \cdot 13 = 0$$

$$275x + 142y = 9$$

i	-1	0	1	2	3	4	
r	275	142	133	9	7	2	1 0
q		1	1	14	1	3	2
x_0	1	0	1	-1	15	-16	68 63
y_0	0	1	-1	2	-29	31	-122

$$567$$

$$x_0 = 63 \cdot 9 + 142k$$

$$y_0 = -1098 - 275k$$

Orbit: $x = 567 + 142k$

$$y = -1098 - 275k, k \in \mathbb{Z}$$

$$2) \sqrt{359} = 18 + (\sqrt{359} - 18) = 18 + \frac{1}{\sqrt{359} + 18}$$

$$= 18 + \frac{1}{\frac{1}{\sqrt{359} - 18}} = 18 + \frac{1}{\frac{\sqrt{359} + 18}{35}}$$

$$= 18 + \frac{1}{1 + \frac{\sqrt{359} - 17}{35}} = 18 + \frac{1}{1 + \frac{1}{\frac{35}{\sqrt{359} - 17}}}$$

$$= 18 + \frac{1}{1 + \frac{1}{18 + \frac{\sqrt{359} - 17}{2}}} = 18 + \frac{1}{1 + \frac{1}{17 + \frac{1}{\frac{2}{\sqrt{359} - 17}}}}$$

$$= 18 + \frac{1}{1 + \frac{1}{17 + \frac{1}{\frac{\sqrt{359} + 17}{35}}}} = 18 + \frac{1}{1 + \frac{1}{17 + \frac{1}{1 + \frac{\sqrt{359} - 18}{35}}}}$$

$$= 18 + \frac{1}{1 + \frac{1}{17 + \frac{1}{1 + \frac{1}{18 + \frac{\sqrt{359} + 18}{35}}}}} = 18 + \frac{1}{1 + \frac{1}{17 + \frac{1}{1 + \frac{1}{1 + \frac{1}{\sqrt{359} - 18}}}}}$$

$$= 18 + \frac{1}{1 + \frac{1}{17 + \frac{1}{1 + \frac{1}{\sqrt{359} + 18}}}}$$

$$= 1 + \frac{1}{36 + (\sqrt{359} - 18)}$$

Orbit:

$$\Rightarrow 18; 1, 17, 1, 36$$

$$3) \quad x_1 \equiv 7 \pmod{20}^{m_1}$$

$$x_2 \equiv 27 \pmod{39}^{m_2}$$

$$x_3 \equiv 9 \pmod{11}^{m_3}$$

$$x_4 \equiv 18 \pmod{31}^{m_4}$$

$$M = 20 \cdot 39 \cdot 11 \cdot 31 = 265980$$

$$M_1 = 39 \cdot 11 \cdot 31 = 13299$$

$$M_2 = 20 \cdot 11 \cdot 31 = 6820$$

$$M_3 = 20 \cdot 39 \cdot 31 = 24180$$

$$M_4 = 20 \cdot 39 \cdot 11 = 8580$$

$$M_1 x_1 \equiv 1 \pmod{m_1}$$

$$13299 x_1 + 20 y_1 = 1$$

$$i \quad -1 \quad 0 \quad 1 \quad 2 \quad 3$$

$$r \quad 13299 \quad 20 \quad 19 \quad 1 \quad 0$$

$$q \quad \quad 664 \quad 1 \quad 19$$

$$x \quad 1 \quad 0 \quad 1 \quad -1$$

$$y$$

$$x_1 \equiv -1 \pmod{20} \equiv 19 \pmod{20}$$

$$M_2 x_2 \equiv 1 \pmod{m_2}$$

$$6820 x_2 \equiv 1 \pmod{39}$$

$$6820 x_2 + 39 y' \equiv 1$$

i	-1	0	1	2	3
r	6820	39	34	5	4
q		174	1	6	1
x	1	0	1	-1	7
					-8

$$x_2 \equiv 28 \pmod{39} \equiv 31 \pmod{39}$$

$$M_3 x_3 \equiv 1 \pmod{m_3}$$

$$24180 x_3 + 11 y' \equiv 1$$

$$x_3 \equiv -5 \pmod{11} \equiv 6 \pmod{11}$$

i	-1	0	1	2	3
r	24180	11	2	1	
q		2198	5		
x	1	0	1	-5	

$$M_4 x_4 \equiv 1 \pmod{m_4}$$

$$1580 x_4 + 31 y' \equiv 1$$

$$x_4 \equiv -9 \pmod{31} \equiv 22 \pmod{31}$$

$$\equiv 22 \pmod{31}$$

i	-1	0	1	2	3
r	1580	31	24	7	3
q		48	1	3	2
x	1	0	1	-1	4
					-9

$$14634387$$

$$x = (13299 \cdot 19 \cdot 7 + 6820 \cdot 31 \cdot 27 + 24180 \cdot 6 \cdot 9 +$$

$$+ 1580 \cdot 22 \cdot 18) \pmod{265980} \equiv \cancel{5457 \pmod{265980}}$$

$$\equiv 12180507 \pmod{265980} \equiv 211407 \pmod{265980}$$

$$\text{Answer: } 211407 \pmod{265980}$$

4)

$$5) p(3) = -47$$

$$p(1) = -1$$

$$p(-1) = 5$$

$$p(4) = -40$$

$$p(2) = -22$$

$$f(x) = \frac{(x-1)(x+1)(x-4)(x-2)}{(3-1)(3+1)(3-4)(3-2)} \cdot (-47) +$$

$$+ \frac{(x-3)(x+1)(x-4)(x-2)}{(1-3)(1+1)(1-4)(1-2)} \cdot (-1) +$$

$$+ \frac{(x-3)(x-1)(x-4)(x-2)}{(-1-3)(-1-1)(-1-4)(-1-2)} \cdot 5 +$$

$$+ \frac{(x-3)(x-1)(x+1)(x-2)}{(4-3)(4-1)(4+1)(4-2)} \cdot (-40) +$$

$$+ \frac{(x-3)(x-1)(x+1)(x-4)}{(2-3)(2-1)(2+1)(2-4)} \cdot (-22) =$$

$$= \frac{47}{8}(x-1)(x+1)(x-4)(x-2) + \frac{1}{12}(x-3)(x+1).$$

$$\bullet (x-4)(x-2) + \frac{1}{24}(x-3)(x-1)(x-4)(x-2) +$$

$$+ \left(-\frac{4}{3}\right)(x-3)(x-1)(x+1)(x-2) + \left(-\frac{11}{3}\right)(x-3)(x-1) \bullet$$

$$\bullet (x+1)(x-4) \text{ (circled)} = \frac{47}{8}$$

$$\frac{47}{8}(x^2-8)(x-4)(x-2) = \frac{47}{8}(x^3-x-4x^2+4)(x-2) =$$

$$= \frac{47}{8}(x^3-4x^2-x+4)(x-2) = \frac{47}{8}(x^4-4x^3-x^2+4x-2x^3+8x^2+2x-8) =$$

$$= \frac{47}{8}(x^4-6x^3+7x^2+6x-8)$$

$$\frac{1}{12}(x^2-2x-3)(x-4)(x-2) = \frac{1}{12}(x^3-2x^2-3x-4x^2+8x+12)(x-2) =$$

$$= \frac{1}{12}(x^4-6x^3+5x^2+12x-2x^3+12x^2-10x-24) =$$

$$= \frac{1}{12}(x^4-8x^3+17x^2+2x-24)$$

$$\frac{1}{24}(x-3)(x-1)(x-4)(x-2) = \frac{1}{24}(x^2-4x+3)(x-4)(x-2) =$$

$$= \frac{1}{24}(x^3-4x^2+3x-4x^2+16x-12)(x-2) =$$

$$= \frac{1}{24}(x^4-8x^3+19x^2-12x-2x^3+16x^2-38x+24) =$$

$$= \frac{1}{24}(x^4-10x^3+35x^2-50x+24)$$

$$-\frac{4}{3}(x-3)(x-1)(x+1)(x-2) = -\frac{4}{3}(x^2-1)(x-3)(x-2) =$$

$$= -\frac{4}{3}(x^3-3x^2-x+3)(x-2) = -\frac{4}{3}(x^4-3x^3-x^2+3x-2x^3+6x^2+$$

$$+2x-6) = -\frac{4}{3}(x^4-5x^3+5x^2+5x-6)$$

$$-\frac{11}{3}(x-3)(x-1)(x+1)(x-4) = -\frac{11}{3}(x^3-3x^2-4x+12)$$

$$\cdot (x-4) = -\frac{11}{3}(x^4-3x^3-x^2+3x-4x^3+12x^2+4x-12)$$

$$= -\frac{11}{3}(x^4-7x^3+11x^2+7x-12)$$

$$\begin{aligned} \textcircled{E} & \left(\frac{47}{8} + \frac{1}{12} + \frac{1}{24} - \frac{4}{3} - \frac{11}{3} \right) x^4 + \left(\frac{47}{8}(-6) + \frac{1}{12}(-8) + \frac{1}{24}(-10) + \right. \\ & \left. + (-\frac{4}{3})(-5) + (-\frac{11}{3})(-3) \right) x^3 + \left(\frac{47}{8}(7) + \frac{1}{12}(17) + \right. \\ & \left. + \frac{1}{24}(35) + (-\frac{4}{3}) \cdot 5 + (-\frac{11}{3}) \cdot 11 \right) x^2 + \left(\frac{47}{8} \cdot 6 + \frac{1}{12} \cdot 2 + \right. \\ & \left. + \frac{1}{24} \cdot (-50) + (-\frac{4}{3}) \cdot 5 + (-\frac{11}{3}) \cdot 7 \right) x + \left(\frac{47}{8} \cdot (-8) + \right. \\ & \left. + \frac{1}{12}(-24) + \frac{1}{24}(24) + (-\frac{4}{3})(-6) + (-\frac{11}{3})(-12) \right) = \\ & = \frac{7523}{24} x^4 - \frac{2581}{4} x^3 + \frac{83513}{24} x^2 - \frac{119611}{12} x + \end{aligned}$$

$$\frac{7523}{24} x^4 - \frac{2581}{4} x^3 + \frac{83513}{24} x^2 - \frac{119611}{12} x + 673 = x^4 - 4x^3 - 3x^2 + x + 4$$

7) $7x + 127 = 703$ 6 s-puett CC

1.

$$7x = 703 - 127$$

$$\begin{array}{r} 703 \\ - 127 \\ \hline 554 \end{array}$$

$$7x = 554$$

$$x = 64,8$$

$$\begin{array}{r} 554 \overline{) 7} \\ \underline{52} \\ 34 \\ \underline{34} \\ 0 \end{array}$$

$$2. \quad 7x + 127 = 703$$

$$7x + 87 = 451$$

$$7x = 364$$

$$x = 52$$

Orber: $64_8; 52_{10}$

$$8) \quad x = \frac{11}{26} \pmod{99}$$

$$26x = 11 \pmod{99}$$

$$26x + 99y = 11$$

i	-1	0	1	2	3	4
r	26	99	26	21	5	1
q		0	3	1	4	
x	1	0	1	-3	4	-19

$$x = -11 \cdot 19 + 99k = -209 + 99k$$

$$~~x = 88 \pmod{99} \quad 1101 \cdot 8 \Rightarrow k=0~~$$

$$x = 88$$

$$9) \quad \frac{447}{202} = 2 + \frac{43}{202} = 2 + \frac{1}{\frac{202}{43}} = 2 + \frac{1}{4 + \frac{30}{43}} =$$

$$= 2 + \frac{1}{4 + \frac{1}{\frac{48}{30}}} = 2 + \frac{1}{4 + \frac{1}{1 + \frac{13}{30}}} = 2 + \frac{1}{4 + \frac{1}{1 + \frac{1}{2 + \frac{4}{13}}}}$$

$$= 2 + \frac{1}{4 + \frac{1}{1 + \frac{1}{2 + \frac{1}{3 + \frac{1}{4}}}}}$$

Orbit: 2, 4, 1, 2, 3, 4

$$10) \quad -2x^5 + x^3 + 2x^2 + x + 2 \quad | \quad x^3 + x^2 + x + 1$$

$$\begin{array}{r} 2x^5 + 0 \cdot x^4 + x^3 + 2x^2 + x + 2 \quad | \quad x^3 + x^2 + x + 1 \\ 2x^5 + 2x^4 + 2x^3 + 2x^2 \\ \hline x^4 + 2x^3 + 0 \cdot x^2 + x \\ - x^4 + x^3 + x^2 + x \\ \hline x^3 + 2x^2 + 0 \cdot x + 2 \\ - x^3 + x^2 + x + 1 \\ \hline x^2 + 2x + 1 \end{array}$$

Orbit: $x^2 + 2x + 1$