

# Exercise 7

1) 2002

$$\begin{array}{r}
 2002 \div 2 = 1001 \\
 1001 \div 2 = 500 \text{ r } 1 \\
 500 \div 2 = 250 \\
 250 \div 2 = 125 \\
 125 \div 2 = 62 \text{ r } 1 \\
 62 \div 2 = 31 \\
 31 \div 2 = 15 \text{ r } 1 \\
 15 \div 2 = 7 \text{ r } 1 \\
 7 \div 2 = 3 \text{ r } 1 \\
 3 \div 2 = 1 \text{ r } 1
 \end{array}$$

$$2002_{10} = 11111010010_2$$

$$1001_{10} = 1111101001_2$$

$$\begin{array}{r}
 11111010010 \\
 + 1111101001 \\
 \hline
 10000111011
 \end{array}$$

0 1 2 3 4 5 6 7 8 9 10

$$0: 1$$

$$1: 1 + 0 = 1$$

$$2: 1 + 0 + 0 = 1$$

$$3: 1$$

$$4: 1$$

$$5: 1 + 0 + 0 + 0 + 0 + 1 = 0$$

$$6: 1 + 0 + 0 + 0 + 0 + 1 + 1 = 1$$



$$7: 1 + 0 + 0 + 0 + 0 + 1 + 1 + 1 = 0$$

$$8: 0$$

$$9: 1 + 0 + 0 + 0 + 0 + 1 + 1 + 1 + 0 + 1 =$$

$$10: 1 + 0 + 0 + 0 + 0 + 1 + 1 + 1 + 0 + 1 + 1 = 0$$

$$\begin{array}{r} 10^9 8^8 7^7 6^6 5^5 4^4 3^3 2^2 1^1 0^0 \\ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1 \ 0 \ 0 \ 1 \ 0 \end{array} = 1024 + 512 + 256 +$$

$$+ 128 + 64 + 16 + \cancel{8} + 2 = 1336 +$$

$$+ 384 + \cancel{80} + \cancel{16} = 1420 + \cancel{8} =$$

$$= \cancel{2014} \quad 2002_{10}$$

$$\text{Answer: } 10000111011$$

$$2) \ 323$$

$$\begin{array}{r} 323 \div 2 \\ \underline{1} \phantom{00} \\ 161 \div 2 \\ \underline{1} \phantom{00} \\ 80 \div 2 \\ \underline{0} \phantom{00} \\ 40 \div 2 \\ \underline{0} \phantom{00} \\ 20 \div 2 \\ \underline{0} \phantom{00} \\ 10 \div 2 \\ \underline{0} \phantom{00} \\ 5 \div 2 \\ \underline{2} \phantom{00} \\ 7 \div 2 \\ \underline{2} \phantom{00} \\ 5 \div 2 \\ \underline{2} \phantom{00} \\ 3 \div 2 \\ \underline{1} \phantom{00} \\ 1 \end{array}$$

$$323_{10} = 101000011_2$$

$$161_{10} = 10100001_2$$



$$\begin{array}{r}
 10100 \quad 0011 \\
 01010 \quad 0001 \\
 \hline
 11110 \quad 0010 \\
 01234 \quad 5678
 \end{array}$$

$$0: 1$$

$$1: 1 + 1 = 0$$

$$2: 1 + 1 + 1 = 1$$

$$3: 1 + 1 + 1 + 1 = 0$$

$$4: 0$$

$$5: 0$$

$$6: 0$$

$$7: 1 + 1 + 1 + 1 + 0 + 0 + 0 + 1 = 1$$

$$8: 1$$

$$\begin{array}{cccccccc}
 8 & 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\
 1 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 1
 \end{array}
 = 256 + 64 + 2 + 1 =$$

$$= 320 + 3 = 323_{10}$$

$$\text{Answer: } 111100010.$$



$$3) \quad 20 + 09 = 29$$

$$\begin{array}{r} 29 \overline{) 2} \\ 7 \overline{) 14} \\ 0 \overline{) 2} \\ 7 \overline{) 14} \\ 0 \overline{) 2} \\ 7 \overline{) 14} \\ 0 \overline{) 2} \end{array}$$

$$29_{10} = 11101_2$$

$$14_{10} = 1110_2$$

$$\begin{array}{r} 11101 \\ + 01110 \\ \hline 10011 \\ 01234 \end{array}$$

$$0: 1$$

$$1: 1$$

$$2: 1$$

$$3: 1 + 0 + 0 + 1 = 0$$

$$4: 1 + 0 + 0 + 1 + 1 = 1$$

$$\begin{array}{c} 4 \quad 3 \quad 2 \quad 1 \quad 0 \\ 11101_2 = 16 + 8 + 4 + 1 = 24 + 5 = \\ = 29_{10} \end{array}$$

$$\text{Answer: } 10011$$



4) 1

$$\begin{array}{r|l} 1 & 2 \\ \hline 1 & 0 \end{array}$$

$$1_{10} = 01_2$$

$$0_{10} = 00_2$$

$$\begin{array}{r} 01 \\ + 00 \\ \hline 01 \\ 01 \end{array}$$

$$0_2 = 0$$

$$1_2 = 1$$

$$\begin{array}{r} 10 \\ 01_2 = 1_{10} \end{array}$$

Answer: 01