

Exercise 3

$$k = 4$$

$$C = 2003$$

$$d = 24$$

$$m = 6$$

$$x = 43$$

$$1. \quad \varphi(4) = 2$$

$$\varphi(2003) = 2002$$

$$\varphi(24) = \varphi(3) \cdot \varphi(8) = 2 \cdot 4 = 8$$

$$\varphi(6) = \varphi(2) \cdot \varphi(3) = 2$$

$$\varphi(43) = 42$$

$$3. \quad 43^{28} \bmod 2003$$

$$28 = 11100$$

$$C = 1 \quad 1^2 \cdot 43 \bmod 2003$$

$$C = 43 \quad 1^2 \cdot 43 \bmod 2003$$

$$C = 1390 \quad 1^2 \cdot 43 \bmod 2003$$

$$C = 1869 \quad 1^2 \bmod 2003$$

$$C = 1932 \quad 1^2 \bmod 2003 \quad (C = 1035)$$