

Key

7.4-7.5 Review: Logarithms

Use your notes and show all your work!

SKILL 5: Evaluate Logarithms (7.4)

Evaluate without a calculator:

1. $\log_2 16 = 4$

2. $\log_6 1 = 0$

3. $\log_4 \frac{1}{16} = -2$

4. $\log_{1/3} 81 = -4$

5. $\log_3 3 = 1$

6. $\log_{36} 6 = \frac{1}{2}$

7. $\log_{27} 1/3 = -\frac{1}{3}$

8. $\log 0.01 = -2$

SKILL 6: Inverse Properties of Logarithms (7.4)

Simplify:

9. $\log_6 6^{2x} = 2x$

10. $7^{\log_7 x} = x$

11. $\log 10^{-5y} = -5y$

12. $\log_2 32^4 = 20$

$$= \log_2 (2^5)^4$$

$$= \log_2 2^{20}$$

Find the inverse of the function:

13. $y = \log_2(x + 3)$

$$x = \log_2(y + 3)$$

$$2^x = y + 3$$

$$-3 \quad -3$$

$$2^x - 3 = y$$

$$y = 2^x - 3$$

14. $y = e^{x-2}$

$$y = \ln x + 2$$

15. $y = 2^x + 5$

$$y = \log_2(x - 5)$$

16. $y = 3^{x-7}$

$$y = \log_3 x + 7$$

17. $y = \log_5 x - 10$

$$y = 5^{x+10}$$

18. $y = \ln x$

$$y = e^x$$

SKILL 7: Use Properties of Logs and the Change of Base Formula (7.5)

Expand the expression

19. $\log_3 \frac{6x}{y}$

$$\log_3 6 + \log_3 x - \log_3 y$$

20. $\ln 4x^2y^5$

$$\ln 4 + 2\ln x + 5\ln y$$

21. $\log_2 \frac{9x}{7z^3}$

$$\log_2 9 + \log_2 x - \log_2 7 - 3\log_2 z$$

Condense the expression into one logarithm

22. $\log_5 24 - \log_5 6$

$$\log_5 4$$

23. $\log_8 6 + 2\log_8 x$

$$\log_8 \frac{6}{x^2}$$

24. $2(\log x - \log y) + 3\log z$

$$\log \frac{x^2 z^3}{y^2}$$

Use the change of base formula to evaluate. Round your answer to 3 decimal places:

25. $\log_4 12$

≈ 1.792

26. $\log_9 18$

≈ 1.315

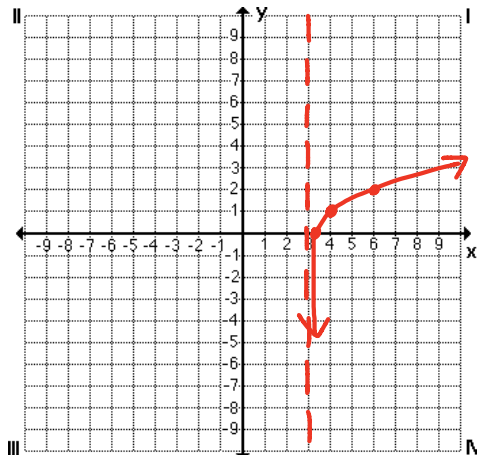
27. $\log_{20} 8$

≈ 0.694

SKILL 8: Graph Logarithmic Functions (7.4)

Graph each function. State the domain, range, and vertical asymptote

28. $y = \log_3(x - 3) + 1$

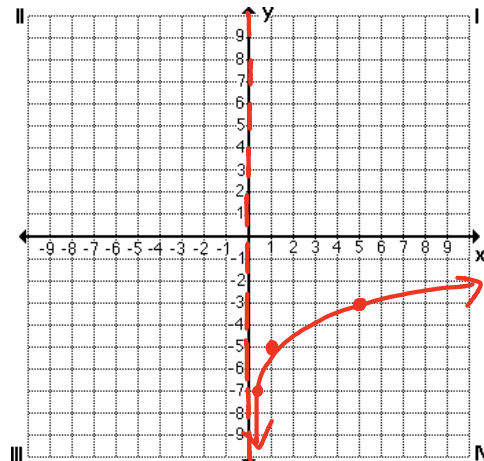


x	y
1	0
3	1
$\frac{1}{3}$	-1

Domain: $x > 3$

Range: \mathbb{R}

Asym: $x = 3$



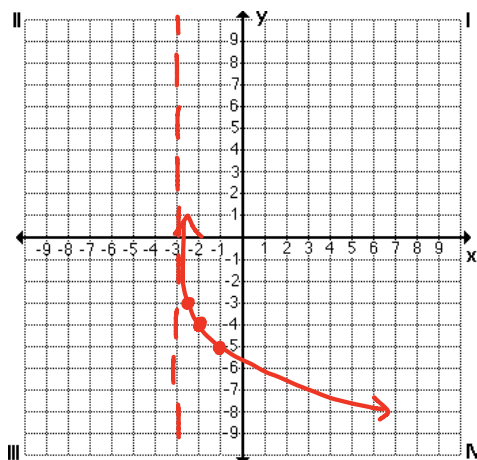
x	y
1	0
5	2
$\frac{1}{5}$	-2

Domain: $x > 0$

Range: \mathbb{R}

Asym: $x = 0$

30. $y = \log_{1/2}(x + 3) - 4$



x	y
1	0
$\frac{1}{2}$	1
2	-1

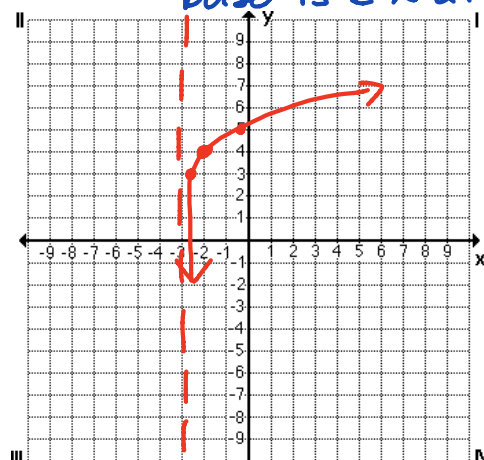
Domain: $x > -3$

Range: \mathbb{R}

Asym: $x = -3$

31. $y = \ln(x + 3) + 4$

base is $e \approx 2.718$



x	y
1	0
$e \approx 2.7$	1
$\frac{1}{e} \approx 0.37$	-1

Domain: $x > -3$

Range: \mathbb{R}

Asym: $x = -3$