



midterm1

## ECE 466 Midterm 1

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- Don't forget to write your name.
- Open textbook.
- Read carefully and write legibly. For the problems with partial credit, show your work.
- For those of you who are remotely solving the exam:
  - You can solve your exam in a-4 sheets or on your tablet.
  - You need to send a scanned pdf or image until 11:45 AM, Tuesday 22nd, to sofuo@msu.edu. Otherwise, your exam will not be accepted.
  - Make sure your answers are legible from pdf or scanned image.

1. No partial points for the following.

- (a) [15 Points] Check if the following systems fits the classifications on the columns.

System Equation	Linear	Time Invariant	Static	Causal	Stable
$y[n] = x[-n]$	✓	✓	✓		✓
$y[n] = 2n^2 x[n] + n x[n+1]$	✓			✓	
$y[n] = \cos(2\pi x[n])$	✓				✓

- (b) [5 Points] The sequence
- $x[n] = \cos\left(\frac{\pi}{2}n\right)$
- was obtained by sampling an analog signal
- $x(t) = \cos(\Omega t)$
- at a sampling rate of
- $F_s = 100$
- Hz. What are two possible values of
- $\Omega$
- ?

$$2\pi \cdot \frac{\Omega}{T} = 4K \quad \frac{100Hz}{4} = 25Hz \quad \Omega = \frac{\pi}{2} \quad N = \frac{2\pi}{T/2} = 4K$$

$4.2 \rightarrow \frac{100Hz}{8} = 12.5Hz$   $K=1, 2, 3, 4, \dots$

- (c) [5 Points] What is the ideal sampling frequency of
- $x(t) = u(t)$
- ?

$$f_s = \frac{1}{T} \quad \text{not possible?}$$

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- (d) [5 Points] The causal sequence
- $x[n] = \{3, 1\}$
- is input to a system with impulse response
- $h[n]$
- , producing the zero-state response
- $y[n] = \{6, -1, 2, 1\}$
- . Determine
- $h[n]$
- .

$$h[n] = \{2, 0\}$$

transient of time

0	1	2	3
3	1	0	0
6	<del>2</del>	2	1

$n(0)=2$   
 $n(1)=0$   
 $n(2)=0$

- (e) The impulse response of a DT (Discrete Time)-LTI system is given by
- $h[n] = A(0.7)^n u[n]$
- . Suppose
- $x[n] = B \cos(0.2\pi n) u[n]$
- is input to the system. Which of the following could be the output signal
- $y[n] = h[n] * x[n]$
- ?

- $K_1(0.7)^n \cos(0.2\pi n + \theta) u[n]$ .
- $K_1(0.14)^n u[n] + K_1 \cos(0.14\pi n \theta) u[n]$ .
- $K_1(0.7)^n u[n] + K_2 \cos(0.2\pi n + \theta) u[n]$ .
- $K_1(0.7)^n u[-n] + K_2 \cos(0.2\pi n + \theta) u[n]$ .

2. [30 Points] Consider a causal LTI system described by the difference equation
- $y[n] = \frac{2}{15}y[n-1] + \frac{1}{15}y[n-2] + x[n]$
- with
- $y[-1] = 1$
- ,
- $y[-2] = -1$
- .

- [6] Find the impulse response  $h[n]$ .
- [4] Determine if the system is (1) FIR or IIR, and (2) stable.
- [8] Find the zero state response for  $x[n] = u[n]$ . (Decide on particular response's  $K$  first.)
- [8] Find the zero input response.
- [4] Find the total response for  $x[n] = u[n]$ . Identify the steady state and transient responses.

$$\frac{y[n]}{x[n]} = h[n] = \frac{\frac{2}{15}y[n] + \frac{1}{15}y[n-2] + x[n]}{x[n]}$$

a)  $\frac{2}{15}y[n] + \frac{1}{15}y[n-2] + x[n]$   
 b) FIR, ✓

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Extra page for Question 2

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3. [30 points] A causal LTI system has a system function
- $H(z) = \frac{1+z^{-1}}{1-\frac{1}{2}z^{-1}+\frac{1}{25}z^{-2}}$
- .

- [5] Determine the difference equation that this system function describes.
- [2] What is the gain of the system?
- [5] Plot the pole-zero map.
- [5] Determine the region of convergence (ROC).
- [5] Is the system stable? Why?
- [8] Find the input signal  $x[n]$  that will produce the output  $y[n] = 2\left(\frac{2}{5}\right)^n u[n] - \left(\frac{1}{5}\right)^n u[n]$ .

gain is 2

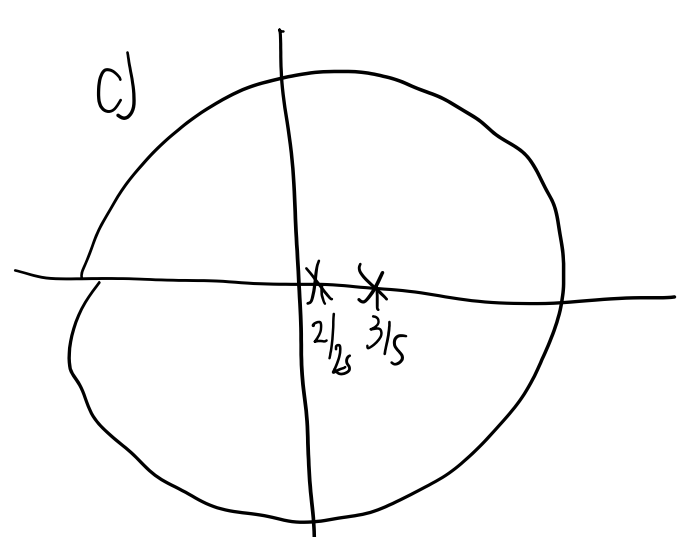
$$d) \text{ROC} = 2 > 3/5 \quad 2 > \frac{2}{5}$$

$$|z| > 3/5$$

e) yfs system is stable

$$a) n \geq 5 \quad u[n]$$

f)



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Extra page for Question 3

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