

Exam 1

Tuesday, February 22, 2022

10:22 AM



midterm1

Need practice on time domain analysis. (52)
Don't get discouraged.
ECE 406 Midterm 1
Come to my office hour Name: Sydney Johnson
if you'd like to PID: AS2A05298
February 21, 2022

- Don't forget to write your name.
- Open textbook.
- Read carefully and write legibly. For the problems with partial credit, show your work.
- For those of you who are remotely solving the exam:
 - You can solve your exam in a-4 sheets or on your tablet.
 - You need to send a scanned pdf or image until 11:45 AM, Tuesday 22nd, to sofoglu@msu.edu. Otherwise, your exam will not be accepted.
 - Make sure your answers are legible from pdf or scanned image.

1. No partial points for the following.

(a) [15 Points] Check if the following systems fits the classifications on the columns.	System Equation	Linear	Time Invariant	Stable	Causal	Stable
$y[n] = x[-n]$			✓	✗	✗	✓
$y[n] = 2n^2x[n] + nx[n+1]$		✗	✗	✗	✗	✗

- (b) [5 Points] The sequence $x[n] = \cos\left(\frac{\pi}{4}n\right)$ was obtained by sampling an analog signal $x(t) = \cos(\Omega t)$ at a sampling rate of $F_s = 100$ Hz. What are two possible values of Ω ? missing it

$$2\pi \cdot \frac{2}{F_s} = 4K \quad \frac{100\pi/2}{4} = 25\pi/2 \quad \omega = \frac{\pi}{2} \quad N = \frac{2\pi}{\pi/2} = 4K \quad K=1, 2, 3, 4, \dots$$

- (c) [5 Points] What is the ideal sampling frequency of $x'(t) = u(t)$? not possible?

$$f_s = \frac{1}{T}$$

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- (d) [5 Points] The causal sequence $x[n] = \{3, 1\}$ is input to a system with impulse response $h[n]$, producing the zero-state response $y[n] = \{0, -1, 2, 1\}$. Determine $h[n]$. n(0)=z

$$h(n) = \begin{cases} 2, & n=0 \\ 0, & n=1 \\ 3, & n=2 \\ 1, & n=3 \end{cases}$$

tran out of time use convolution.

- (e) [5 Points] The impulse response of a DT (Discrete Time)-LTI system is given by $h[n] = A(0.7)^n u[n]$. Suppose $x[n] = B \cos(0.2\pi n)u[n]$ is input to the system. Which of the following could be the output signal $y[n] = h[n] * x[n]$? Total z Norm. + Part.

- i. $K_1(0.7)^n u[n] + K_2 \cos(0.2\pi n + \theta)u[n]$.
ii. $K_1(0.14)^n u[n] + K_2 \cos(0.14\pi n\theta)u[n]$.
iii. $K_1(0.7)^n u[n] + K_2 \cos(0.2\pi n + \theta)u[n]$.
iv. $K_1(0.7)^n u[n] + K_2 \cos(0.2\pi n + \theta)u[n]$.

2. [30 Points] Consider a causal LTI system described by the difference equation $y[n] = \frac{2}{15}y[n-1] + \frac{1}{15}y[n-2] + x[n]$ with $y[-1] = 1$, $y[-2] = -1$.

- (a) [6] Find the impulse response $h[n]$.
(b) [4] Determine if the system is (1) FIR or IIR, and (2) stable.
(c) [8] Find the zero state response for $x[n] = u[n]$. (Decide on particular response's K first.)
(d) [8] Find the total response.

- (e) [4] Find the total response for $x[n] = u[n]$. Identify the steady state and transient responses.

$$\frac{Y(z)}{X(z)} = \frac{h(n)}{1 - \frac{2}{15}z^{-1} - \frac{1}{15}z^{-2}} = \frac{\left(\frac{2}{15}\right)^n}{1 - \left(\frac{2}{15}\right)^{-1}z^{-1}}$$

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Extra page for Question 2

3. [30 points] A causal LTI system has a system function $H(z) = \frac{1+z^{-1}}{1-\frac{2}{5}z^{-1}+\frac{2}{5}z^{-2}}$.

- (a) [5] Determine the difference equation that this system function describes.
(b) [2] What is the gain of the system?
(c) [5] Plot the pole-zero map.
(d) [5] Determine the region of convergence (ROC).
(e) [5] Is the system stable? Why?
(f) [8] Find the input signal $x[n]$ that will produce the output $y[n] = 2\left(\frac{2}{5}\right)^n u[n] - \left(\frac{1}{5}\right)^n u[n]$.



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Extra page for Question 3

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