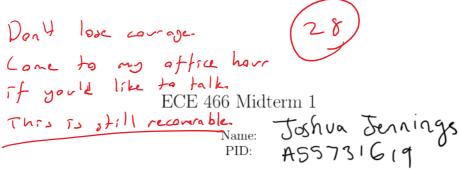
Joshua Jennings

Wednesday, February 23, 2022

10:42 PM



February 21, 2022

- Don't forget to write your name.
- Open textbook.
- Read carefully and write legibly. For the problems with partial credit, show your work.
- For those of you who are remotely solving the exam:
 - You can solve your exam in a-4 sheets or on your tablet.
 - You need to send a scanned pdf or image until 11:45 AM, Tuesday 22nd, to sofuoglu@msu.edu. Otherwise, your exam will not be accepted.
 - Make sure your answers are legible from pdf or scanned image.
- 1. No partial points for the following.
 - (a) [15 Points] Check if the following systems fits the classifications on the columns.

System Equation	Linear	Time Invariant	Static	Causal	Stable
y[n] = x[-n]	V	V(-1)		_	
$y[n] = 2n^2x[n] + nx[n+1]$	\Box			VO	10
$y[n] = cos(2\pi x[n])$	VA		(-)	(A)	V
					•

(b) [5 Points] The sequence $x[n] = \cos\left(\frac{\pi}{2}\eta\right)$ was obtained by sampling an analog signal $x(t) = \cos\left(\Omega t\right)$ at a sampling rate of $F_s = 100$ Hz. What are two possible values of Ω ?



$$S_{-} = F_{0} \cdot LR$$

$$f_{0} = \frac{F_{0}}{F_{0}} = \frac{F_{0}}{100} = \frac{1}{7} \Rightarrow \frac{F_{0} \cdot 2LS}{2-LS}$$

(c) [5 Points] What is the ideal sampling frequency of x(t) = u(t)?

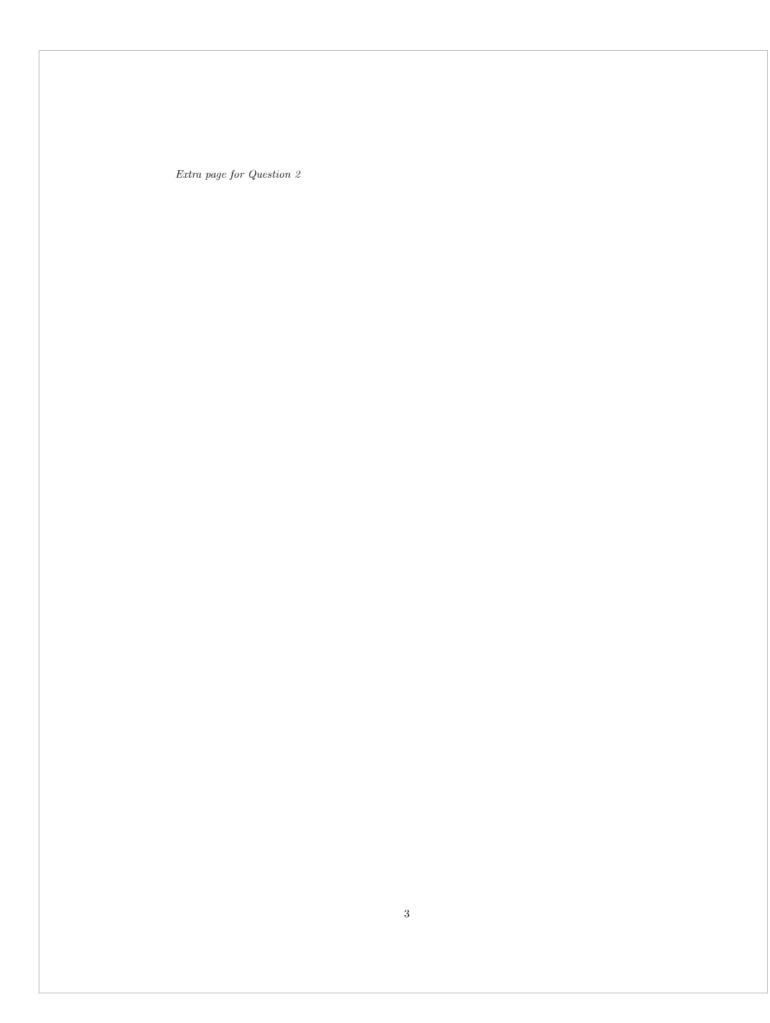
atteast 200 Hz -1 according to the Nyquist Freq theorem

(d) [5 Points] The causal sequence $x[n] = \{3, 1\}$ is input to a system with impulse response h[n], producing the zero-state response $y[n] = \{6, -1, 2, 1\}$. Determine h[n].

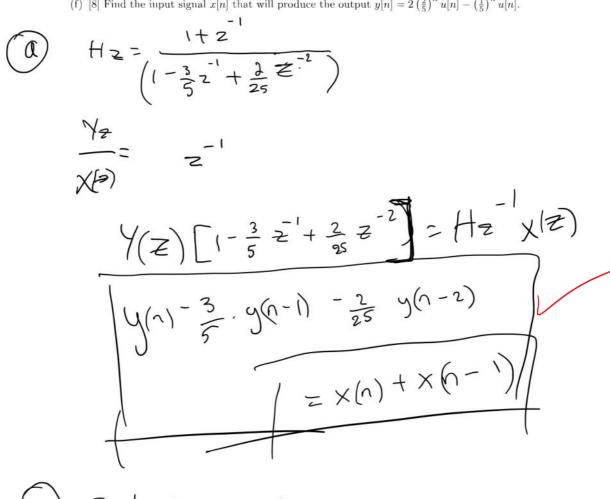
- 5

- (e) The impulse response of a DT (Discrete Time)-LTI system is given by $h[n] = A(0.7)^n u[n]$. Suppose $x[n] = B\cos(0.2\pi n)u[n]$ is input to the system. Which of the following could be the output signal y[n] = h[n] * x[n]?
 - i. $K_1(0.7)^n \cos(0.2\pi n + \theta)u[n]$.
 - ii. $K_1(0.14)^n u[n] + K_1 \cos(0.14\pi n\theta) u[n]$.
 - iii. $K_1(0.7)^n u[n] + K_2 \cos(0.2\pi n + \theta) u[n]$.
 - iv. $K_1(0.7)^n u[-n] + K_2 \cos(0.2\pi n + \theta) u[n]$.
- 2. [30 Points] Consider a causal LTI system described by the difference equation $y[n] = \frac{2}{15}y[n-1] + \frac{1}{15}y[n-2] + x[n]$ with y[-1] = 1, y[-2] = -1.
 - (a) [6] Find the impulse response h[n].
 - (b) [4] Determine if the system is (1) FIR or IIR, and (2) stable.
 - (c) [8] Find the zero state response for x[n] = u[n]. (Decide on particular response's K first.)
 - (d) [8] Find the zero input response.
 - (e) [4] Find the total response for x[n] = u[n]. Identify the steady state and transient responses.

$$y_1 = \frac{2}{15} \quad y_1 = \frac{1}{15} \quad y_2 = \frac{1}{15} \quad y_3 = \frac{1}{15} \quad y_3$$



- 3. [30 points] A causal LTI system has a system function $H(z) = \frac{1+z^{-1}}{1-\frac{3}{6}z^{-1}+\frac{2}{26}z^{-2}}$.
 - (a) [5] Determine the difference equation that this system function describes.
 - (b) [2] What is the gain of the system?
 - (c) [5] Plot the pole-zero map.
 - (d) [5] Determine the region of convergence (ROC).
 - (e) [5] Is the system stable? Why?
 - (f) [8] Find the input signal x[n] that will produce the output $y[n] = 2\left(\frac{2}{5}\right)^n u[n] \left(\frac{1}{5}\right)^n u[n]$.



Pole Za Map

