Data Mining Classification: Basic Concepts and Techniques

Lecture Notes for Business Intelligent Analytics Introduction to Data Mining - Classification

Introduction to Data Mining - Classification

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Classification: Definition

I Given a collection of records (training set)

- Each record is by characterized by a tuple (x,y), where x is the attribute set and y is the class label
 - lacktriangle x: attribute, predictor, independent variable, input
 - ◆ y: class, response, dependent variable, output

I Task:

— Learn a model that maps each attribute set \boldsymbol{x} into one of the predefined class labels \boldsymbol{y}

Task	Attribute set, x	Class label, y
Categorizing email messages	Features extracted from email message header and content	spam or non-spam
Identifying tumor cells	Features extracted from x-rays or MRI scans	malignant or benign cells
Cataloging galaxies	Features extracted from telescope images	Elliptical, spiral, or irregular-shaped galaxies

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General Approach for Building Classification Model

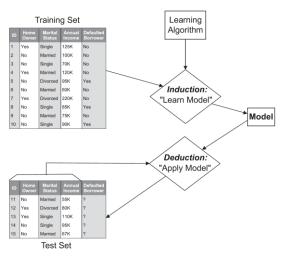


Figure 3.3. General framework for building a classification model.

Classification Techniques

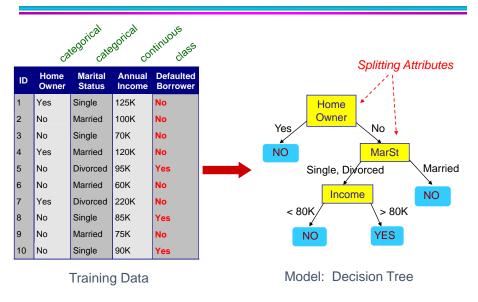
- Base Classifiers
 - Decision Tree based Methods
 - Rule-based Methods
 - Nearest-neighbor
 - Naïve Bayes and Bayesian Belief Networks
 - Support Vector Machines
 - Neural Networks, Deep Neural Nets
- Ensemble Classifiers
 - Boosting, Bagging, Random Forests

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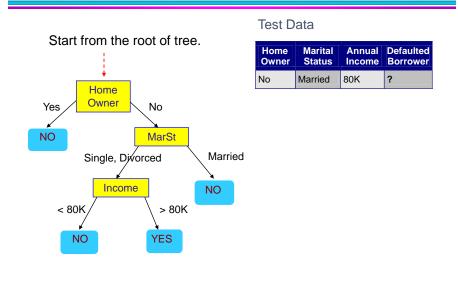
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Example of a Decision Tree



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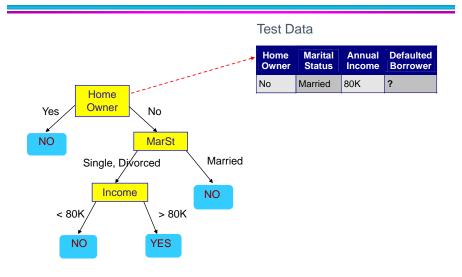
Apply Model to Test Data



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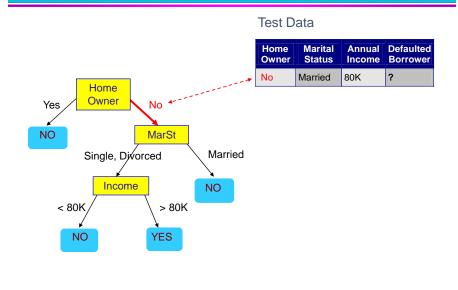
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Apply Model to Test Data



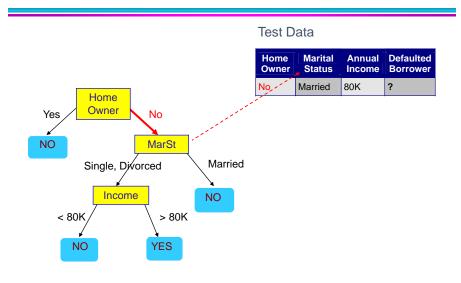
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Apply Model to Test Data



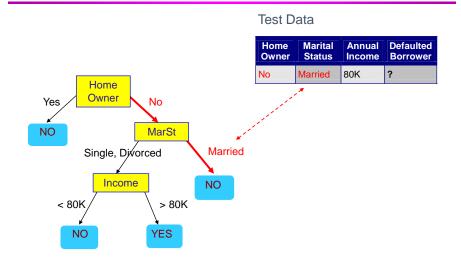
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Apply Model to Test Data



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Apply Model to Test Data

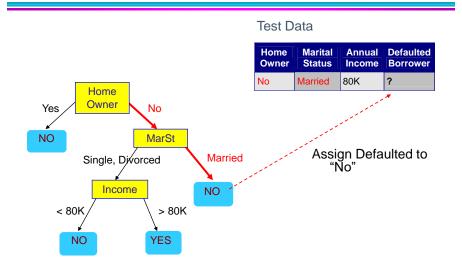


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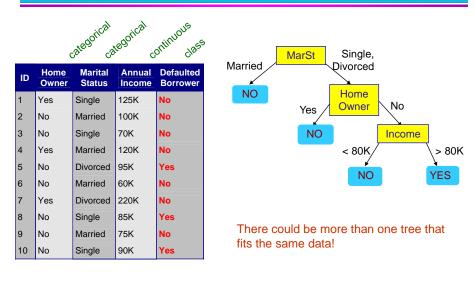
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Apply Model to Test Data



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Another Example of Decision Tree

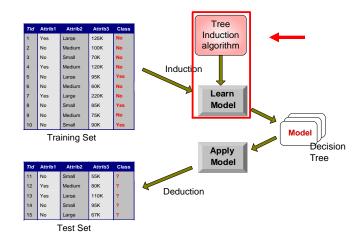


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Decision Tree Classification Task



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Decision Tree Induction

- Many Algorithms:
 - Hunt's Algorithm (one of the earliest)
 - CART
 - ID3, C4.5
 - SLIQ,SPRINT

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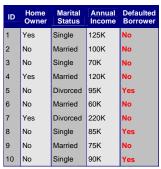
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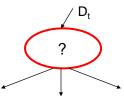
General Structure of Hunt's Algorithm

2 Let D_t be the set of training records that reach a node t

General Procedure:

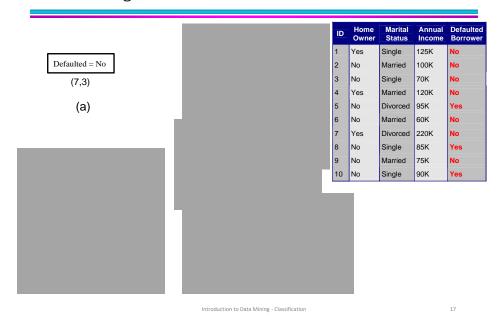
- If D_t contains records that belong the same class y_t, then t is a leaf node labeled as y_t
- If D_t contains records that belong to more than one class, use an attribute test to split the data into smaller subsets.
 Recursively apply the procedure to each subset.





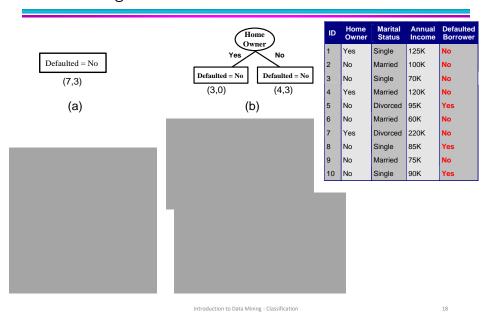
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Hunt's Algorithm

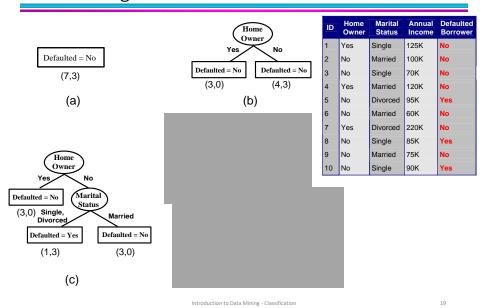


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Hunt's Algorithm

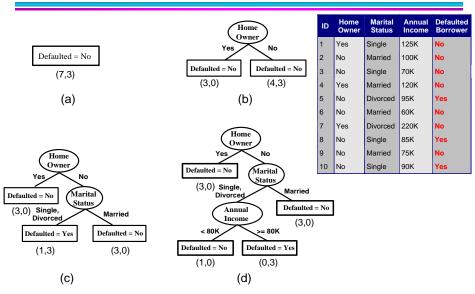


Hunt's Algorithm



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Hunt's Algorithm



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Design Issues of Decision Tree Induction

How should training records be split?

- Method for expressing test condition
 - depending on attribute types
- Measure for evaluating the goodness of a test condition

2 How should the splitting procedure stop?

- Stop splitting if all the records belong to the same class or have identical attribute values
- Early termination

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Methods for Expressing Test Conditions

② Depends on attribute types

- Binary
- Nominal
- Ordinal
- Continuous

Test Condition for Nominal Attributes

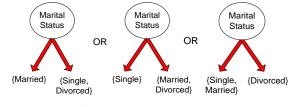
☐ Multi-way split:

Use as many partitions as distinct values.



☐ Binary split:

- Divides values into two subsets



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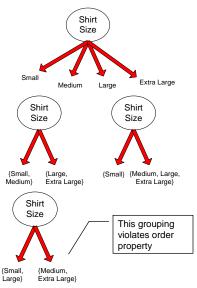
Test Condition for Ordinal Attributes

I Multi-way split:

Use as many partitions as distinct values

I Binary split:

- Divides values into two subsets
- Preserve order property among attribute values

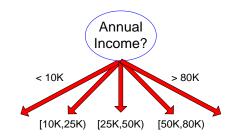


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Test Condition for Continuous Attributes



(i) Binary split



(ii) Multi-way split

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Splitting Based on Continuous Attributes

- · Different ways of handling
 - Discretization to form an ordinal categorical attribute

Ranges can be found by equal interval bucketing, equal frequency bucketing (percentiles), or clustering.

- Static discretize once at the beginning
- Dynamic repeat at each node
- Binary Decision: (A < v) or $(A \ge v)$
 - consider all possible splits and finds the best cut
 - can be more compute intensive

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How to determine the Best Split

Before Splitting: 10 records of class 0, 10 records of class 1







Customer Id	Gender	Car Type	Shirt Size	Class
1	M	Family	Small	C0
2	M	Sports	Medium	C0
3	M	Sports	Medium	C0
4	M	Sports	Large	C0
5	M	Sports	Extra Large	C0
6	M	Sports	Extra Large	C0
7	F	Sports	Small	C0
8	F	Sports	Small	C0
9	F	Sports	Medium	C0
10	F	Luxury	Large	C0
11	M	Family	Large	C1
12	M	Family	Extra Large	C1
13	M	Family	Medium	C1
14	M	Luxury	Extra Large	C1
15	F	Luxury	Small	C1
16	F	Luxury	Small	C1
17	F	Luxury	Medium	C1
18	F	Luxury	Medium	C1
19	F	Luxury	Medium	C1
20	F	Luxury	Large	C1

Which test condition is the best?

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How to determine the Best Split

- I Greedy approach:
 - Nodes with purer class distribution are preferred
- I Need a measure of node impurity:

C0: 5 C1: 5

High degree of impurity

C0: 9 C1: 1

Low degree of impurity

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Measures of Node Impurity

Gini Index $Gini Index = 1 - \sum_{i=0}^{c-1} p_i(t)^2$

Where $p_i(t)$ is the frequency of class i at node t, and c is the total number of classes

I Entropy

Entropy =
$$-\sum_{i=0}^{c-1} p_i(t) log_2 p_i(t)$$

I Misclassification error

Classification error =
$$1 - \max[p_i(t)]$$

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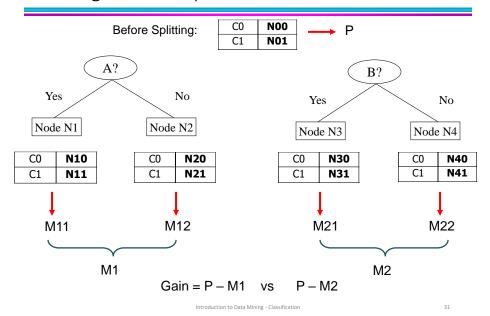
Finding the Best Split

- 1. Compute impurity measure (P) before splitting
- 2. Compute impurity measure (M) after splitting
 - I Compute impurity measure of each child node
 - I M is the weighted impurity of child nodes
- 3. Choose the attribute test condition that produces the highest gain

Gain = P - M

or equivalently, lowest impurity measure after splitting (M)

Finding the Best Split



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Measure of Impurity: GINI

• Gini Index for a given node t

Gini Index =
$$1 - \sum_{i=0}^{c-1} p_i(t)^2$$

Where $p_i(t)$ is the frequency of class i at node t, and c is the total number of classes

- Maximum of 1-1/c when records are equally distributed among all classes, implying the least beneficial situation for classification
- Minimum of 0 when all records belong to one class, implying the most beneficial situation for classification
- Gini index is used in decision tree algorithms such as CART, SLIQ, SPRINT

Measure of Impurity: GINI

• Gini Index for a given node t :

Gini Index =
$$1 - \sum_{i=0}^{c-1} p_i(t)^2$$

• For 2-class problem (p, 1 - p):

• GINI =
$$1 - p^2 - (1 - p)^2 = 2p (1-p)$$

C1	0
C2	6
Gini=	0.000

C1	1
C2	5
Gini=	0.278

C1	2
C2	4
Gini=	0.444

C1	3
C2	3
Gini=	0.500

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Computing Gini Index of a Single Node

Gini Index =
$$1 - \sum_{i=0}^{c-1} p_i(t)^2$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$
 $Gini = 1 - P(C1)^2 - P(C2)^2 = 1 - 0 - 1 = 0$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$
 $Gini = 1 - (1/6)^2 - (5/6)^2 = 0.278$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$
 $Gini = 1 - (2/6)^2 - (4/6)^2 = 0.444$

Computing Gini Index for a Collection of Nodes

I When a node p is split into k partitions (children)

$$GINI_{split} = \sum_{i=1}^{k} \frac{n_i}{n} GINI(i)$$

where, n_i = number of records at child i, n = number of records at parent node p.

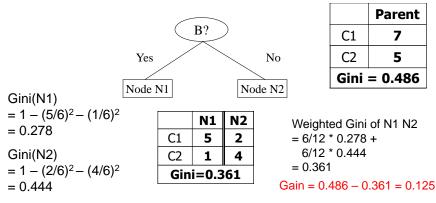
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Binary Attributes: Computing GINI Index

- □ Splits into two partitions (child nodes)
- Effect of Weighing partitions:
 - Larger and purer partitions are sought



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Categorical Attributes: Computing Gini Index

- I For each distinct value, gather counts for each class in the dataset
- I Use the count matrix to make decisions

 CarType

 Family
 Sports
 Luxury

 C1
 1
 8
 1

 C2
 3
 0
 7

0.163

Multi-way split

Two-way split (find best partition of values)

	CarType						
	{Sports, Luxury} {Family}						
C1	9	1					
C2	7 3						
Gini	0.468						

	CarType					
	{Sports}	{Family, Luxury}				
C1	8	2				
C2	0	10				
Gini	0.167					

Which of these is the best?

I

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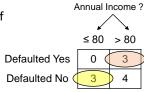
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Gini

Continuous Attributes: Computing Gini Index

- I Use Binary Decisions based on one value
- I Several Choices for the splitting value
 - Number of possible splitting values
 - = Number of distinct values
- I Each splitting value has a count matrix associated with it
 - —Class counts in each of the partitions, A ≤ v and A > v
- I Simple method to choose best v
 - For each v, scan the database to gather count matrix and compute its Gini index
 - Computationally Inefficient! Repetition of work.

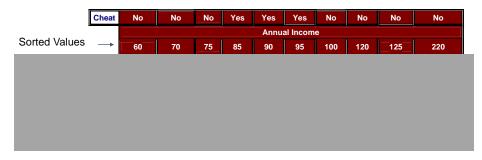




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Continuous Attributes: Computing Gini Index...

- I For efficient computation: for each attribute,
 - Sort the attribute on values
 - Linearly scan these values, each time updating the count matrix and computing gini index
 - Choose the split position that has the least gini index



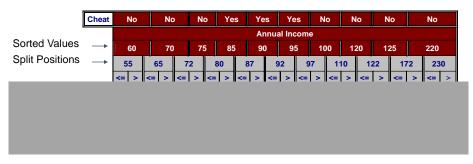
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Continuous Attributes: Computing Gini Index...

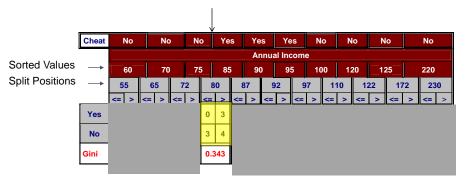
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Continuous Attributes: Computing Gini Index...

- I For efficient computation: for each attribute,
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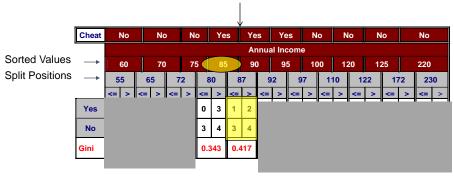
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Continuous Attributes: Computing Gini Index...

- For efficient computation: for each attribute,
 - Sort the attribute on values
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 - Choose the split position that has the least gini index



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Continuous Attributes: Computing Gini Index...

- I For efficient computation: for each attribute,
 - Sort the attribute on values
 - Linearly scan these values, each time updating the count matrix and computing gini index
 - Choose the split position that has the least gini index

	Cheat	I	No		No	,	N	0_	Ye	s	Ye	s	Υe	es	N	0	N	lo	N	lo		No	
Sorted Values	→		60	Ť	70		7:	5	85	;	Ar 90	nnua	ıl Ind		e 10	00	12	20		25	- 	220	
Split Positions	\rightarrow	5	5	6	5	7	2	8	0	8	7	9	2	9	7	11	10	12	22	17	72	23	0
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	Yes	0	3	0	3	0	3	0	3	1	2	2	1	3	0	3	0	3	0	3	0	3	0
	No	0	7	1	6	2	5	3	4	3	4	3	4	3	4	4	3	5	2	6	1	7	0
	Gini	0.4	120	0.4	00	0.3	75	0.3	43	0.4	117	0.4	100	<u>0.3</u>	<u>300</u>	0.3	143	0.3	75	0.4	00	0.4	20

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Measure of Impurity: Entropy

I Entropy at a given node t

$$Entropy = -\sum_{i=0}^{c-1} p_i(t) log_2 p_i(t)$$

Where $p_i(t)$ is the freque $h\overline{cy}$ of class i at node t, and c is the total number of classes

- ◆ Maximum of log₂c when records are equally distributed among all classes, implying the least beneficial situation for classification
- ◆ Minimum of 0 when all records belong to one class, implying most beneficial situation for classification
- Entropy based computations are quite similar to the GINI index computations

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Computing Entropy of a Single Node

$$Entropy = -\sum_{i=0}^{c-1} p_i(t)log_2p_i(t)$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$
Entropy = $-0 \log 0 - 1 \log 1 = -0 - 0 = 0$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$
Entropy = - (1/6) $\log_2 (1/6) - (5/6) \log_2 (1/6) = 0.65$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$
Entropy = - (2/6) $log_2(2/6) - (4/6) log_2(4/6) = 0.92$

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Computing Information Gain After Splitting

I Information Gain:

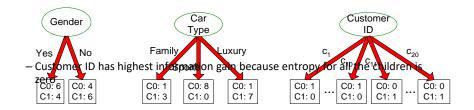
$$Gain_{split} = Entropy(p) - \sum_{i=1}^{k} \frac{n_i}{n} Entropy(i)$$

Parent Node, p is split into k partitions (children) n_i is number of records in child node i

- Choose the split that achieves most reduction (maximizes GAIN)
- Used in the ID3 and C4.5 decision tree algorithms
- Information gain is the mutual information between the class variable and the splitting variable

Problem with large number of partitions

□Node impurity measures tend to prefer splits that result in large number of partitions, each being small but pure



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Gain Ratio

I Gain Ratio:

$$Gain \ Ratio = \frac{Gain_{split}}{Split \ Info} \qquad Split \ Info = -\sum_{i=1}^{k} \frac{n_i}{n} log_2 \frac{n_i}{n}$$

Parent Node, p is split into k partitions (children) n_i is number of records in child node i

- Adjusts Information Gain by the entropy of the partitioning (Split Info).
 - ◆ Higher entropy partitioning (large number of small partitions) is penalized!
- Used in C4.5 algorithm
- Designed to overcome the disadvantage of Information Gain

Gain Ratio

I Gain Ratio:

$$Gain Ratio = \frac{Gain_{split}}{Split Info} \qquad Split Info = \sum_{i=1}^{k} \frac{n_i}{n} log_2 \frac{n_i}{n}$$

Parent Node, p is split into k partitions (children) n_i is number of records in child node i

	CarType							
	Family	Sports	Luxury					
C1	1	8	1					
C2	3 0 7							
Gini	0.163							

SplitINFO = 1.52



SplitINFO = 0.72

	CarType					
	{Sports}	{Family, Luxury}				
C1	8	2				
C2	0 10					
Gini	0.167					

SplitINFO = 0.97

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Measure of Impurity: Classification Error

I Classification error at a node t

$$Error(t) = 1 - \max_{i}[p_i(t)]$$

- Maximum of 1-1/c when records are equally distributed among all classes, implying the least interesting situation
- Minimum of 0 when all records belong to one class, implying the most interesting situation

Computing Error of a Single Node

$$Error(t) = 1 - \max_{i}[p_i(t)]$$

C1	0	P(C1) :
C2	6	Error =

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$
 $Error = 1 - max(0, 1) = 1 - 1 = 0$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$
 $Error = 1 - max (1/6, 5/6) = 1 - 5/6 = 1/6$

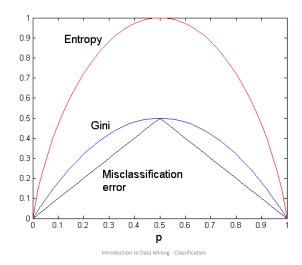
$$P(C1) = 2/6$$
 $P(C2) = 4/6$
 $Error = 1 - max (2/6, 4/6) = 1 - 4/6 = 1/3$

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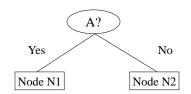
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Comparison among Impurity Measures

For a 2-class problem:



Misclassification Error vs Gini Index



	Parent
C1	7
C2	3
Gini = 0.42	

Gini(N1)
=
$$1 - (3/3)^2 - (0/3)^2$$

= 0

Gini(N2)
=
$$1 - (4/7)^2 - (3/7)^2$$

$$= 1 - (4/7)^2 - (3/7)^2$$
$$= 0.489$$

	N1	N2
C1	3	4
C2	0	3
Gini=0.342		

Gini(Children)

= 3/10 * 0

+ 7/10 * 0.489

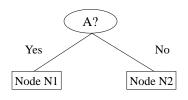
= 0.342

Gini improves but error remains the same!!

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Misclassification Error vs Gini Index



	Parent	
C1	7	
C2	3	
Gini = 0.42		

	N1	N2
C1	3	4
C2	0	3
Gini=0.342		

	N1	N2	
C1	3	4	
C2	1	2	
Gini=0.416			

Misclassification error for all three cases = 0.3!

Decision Tree Based Classification

I Advantages:

- Relatively inexpensive to construct
- Extremely fast at classifying unknown records
- Easy to interpret for small-sized trees
- Robust to noise (especially when methods to avoid overfitting are employed)
- Can easily handle redundant attributes
- Can easily handle irrelevant attributes (unless the attributes are interacting)

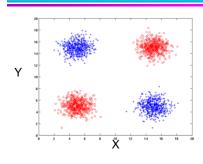
I Disadvantages: .

- Due to the greedy nature of splitting criterion, interacting attributes (that can
 distinguish between classes together but not individually) may be passed over in
 favor of other attributed that are less discriminating.
- Each decision boundary involves only a single attribute

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Handling interactions



+: 1000 instances

o: 1000 instances

Entropy (X): 0.99

Entropy (Y): 0.99

Handling interactions

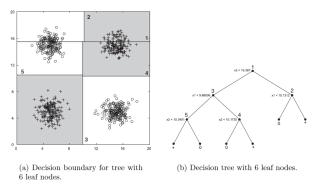


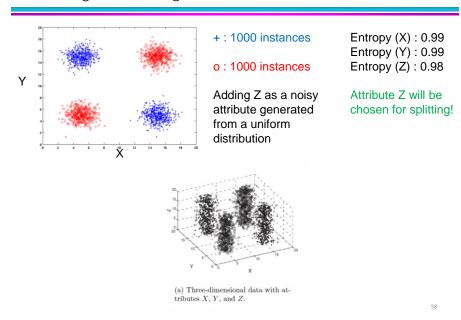
Figure 3.28. Decision tree with 6 leaf nodes using X and Y as attributes. Splits have been numbered from 1 to 5 in order of other occurrence in the tree.

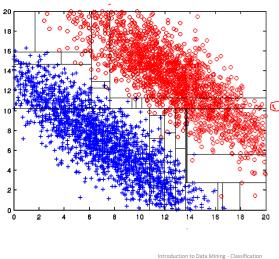
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Handling interactions given irrelevant attributes





Both positive (+) and negative (o) classes generated from skewed Gaussians with centers at (8,8) and (12,12) respectively.