

# Fixed assets lose their value even as they continue to function and contribute to engineering project that use them. This lost value is called depreciation.

→ Most assets lose their value over time (in other words they depreciate) and must be replaced once the end of their useful life is reached.

### Appreciable property.

(a) Tangible  
(seen or touched)

(b) Intangible  
(personal property)

Personal

Real

→ copyright

→ patent

→ goodwill

→ trademark

→ machinery

→ land

→ vehicles

(Because it does

→ furniture

not have  
determinable  
life]

## \* Economic Depreciation

- ① Physical : Reduction in asset capacity to performing its intended service due to physical impairment.  
(corrosion, chemical changes, wear and tear)
- ② Functional : Due to change in organization or technology that decrease or eliminate need for asset.

### # Some definitions

- ① Cost basis or Unadjusted cost
  - Initial cost of acquiring assets (purchase price + tax) + transportation or other normal cost. (like installation)
  - It represents the total cost that is claimed as expense over up asset life i.e. sum of annual depreciation assets.
- ② Book value (BV)



→ The worth of depreciable property as shown as accounting records of company.

① Recovery price

→ It is the depreciable life of the assets in years.

② Market value (MV)

→ The amount that will be paid by buyer to seller for property under no compulsion to buy or sell.

③ Salvage value

→ The estimated value of property at the end of useful life.

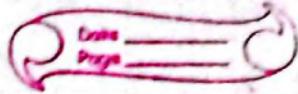
## # Basic methods of depreciation

① Straight line method

→ It assumes that a constant amount is depreciated each year over the useful life of the asset.

$$D_n = \frac{I - S}{N}$$

$D_n$  = Depreciation charge during year n  
 $I$  = Cost of the assets including installation expenses



$S$  = Salvage value at the end of useful life

$N$  = Useful life

Book value in a given year

= Cost Basis - total depreciation

Example 1:

consider the following data

$I = 10,000$

$N = 5 \text{ yrs}$

$S = 2000$

compute the annual depreciation allowance  
and the resulting book value using the  
SL line depreciation method?

Soln :-

$I = \text{Rs } 10,000 \quad N = 5 \text{ yrs}, \quad S = 2000$

$$D_n = \frac{I - S}{N} = \frac{10,000 - 2000}{5}$$

$$\therefore D_n = 1600$$

Date  
Page

Year	Book Value depreciation		Actual depreciation	BV
	D <sub>n</sub>	B <sub>n</sub>		
1	10,000	1600	8400	
2	8400	1600	6800	
3	6800	1600	5200	
4	5200	1600	3600	
5	3600	1600	2000	

# Sum of the year digit method

$$SOYD = 1 + 2 + 3 + \dots + N$$

$$= \frac{N(N+1)}{2}$$

$$D_n = \frac{(N-n+1)}{SOYD} (I-S)$$

respective year (1st year = 1)  
2nd year = 2

$$SOYD = \frac{N(N+1)}{2} = \frac{5 \times 6}{2} = 5 \times 3 = 15$$

$$* I = \text{Rs } 20,000 \quad N = 5 \text{ yrs}, \quad SV = 2000$$

$y_{(0)Y}$	$B_{n-1}$	$D_n$	$B_n$
1	20,000	$\frac{2(20,000 - 2000)}{15} (5-1+)$ = 6000	14000
2	14,000	$\frac{(5-2+1)}{15} \times (I-s) = 4000$	12000
3	9200	<del><math>\frac{3}{15} (I - (5-3+1)(1-s)) = 3600</math></del>	5600
4	5600	$\frac{5-4+1}{15} (I-s) = 2400$	3200
5	3200	$\frac{5-5+1}{5} (I-s) = 1200$	2000

(A)

### Doubling Balance method

- It is also known as fixed % or Uniform % method.
- In this method book value is multiplied by the fixed rate.

$$\alpha = \frac{1}{N} \times \text{multiplier}$$

The most commonly used multiplier is double the st line rate for this reason

It is called double declining method

$$\alpha = \frac{2}{N} \times 2$$

Ex:  $I = \text{Rs } 10,000$ ,  $N = 5 \text{ yrs}$ ,  $S = 778$  find

$B_n$  and  $D_n$  for  $n = 1 \text{ to } 5$  using DDB method

$$\alpha = \frac{2}{N} = 0.4 = 40\% \quad \text{decrease} \\ = (\alpha \times B_{n-1}) - (B_{n-1} - D_n)$$

1	10,000	4000	6000
2	6000	2400	3600
3	3600	1440	2160
4	2160	864	1296
5	1296	518.4	777.6 $\approx$

-778

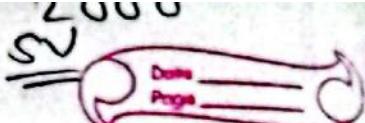
If  $SV = 2000$  in this Qn

(BV  $\angle S$ )

↓  
SV  $\angle S$   
case  
no extra  
case

p. 17.0

at year 4 it should be ₹ 2000



n	B_{n-1}	b_n	B_n
1	10000	4000	6000
2	6000	2400	3600
3	3600	1440	2160
→ 4	2160	160	2000
5	2000	-	2000

make  
change  
here

for full  
~~photum~~

2 ma 80 ₹ shadaya

mulchia at no  
chhey

final year ma

SV = BV ch

huny puryo

if BV > S

(switch from BDB DDB to SL)

O\_n = BV at begin - SV

Remaining useful life at beginning of year

R = Rs 10,000 N=5 S=0

(BDB with SL)

$$\alpha = \frac{2}{5} = 0.4$$



$$\alpha = \alpha_{n-1}$$

n

$B_{n-1}$

$D_n$

$B_n$

1	10,000	4000	6000
2	6000	2400	3600
3	3600	1440	2160
4	2160	864	1296
5	2000	518.4	778
	1296		

$B_n > S$

We have to switch the switch fundamental to S2

Box	$S_2 - \text{epoch}$	DDB $\downarrow 4^{th}$	Decision
1	$10,000 - 0$ = 2000	< 4000	Do not switch.
2	$6000 - 0 = 1500$	< 2400	1 ~ 2
3	$3600 - 0 = 1200$	< 1440	Do not switch
4	$2160 - 0 = 1080$	> 864	Switch to S2

optimal year for switching is year 4

$P_0 Y$	$B_{n-1}$	$B_n$	$B_{n+1}$
1	10,000	4000	6000
2	6000	24000	36000
3	3600	14400	21600
4	2160	1080	1080
5	1080	1080	0

↓  
SL depreciation →

$(SV = BV)$

Cost of asset = 1  
 $SV = 20000$   
 Useful life =  
 interest rate :

100 P-F

$A = (\cancel{100}) ($

$\cancel{1})$  \* year depreciation

the year best

$A = (100000,-$

= 6504.227

Dep at the end of 1.

### # Sinking fund method

→ Book value decreases at increasing rates with respect to the life of the asset.

ii compute the depreciation and BV in each year using sinking fund depreciation method.

$P_0 Y$	$Dep$
1	6504.227
2	
3	
4	
5	
6	
7	
8	

Cost of asset = 100000

SV = 20000

Useful life = 8 yrs

Interest rate = 12%

~~100 P-F (2-5)~~

$$A = (\text{~~100~~}) (A/F, 12\%, 8 \text{ yrs})$$

Up to 4th year depreciation amount

1st year but 12% to be deducted

$$A = (100000 - 20000) \left[ \frac{0.12}{1.12^8 - 1} \right]$$

$$= 6504.227$$

Dep at the end of 1st year = 6504

$$\text{1st 2nd year} = 6504 \times 1.12$$

$$= 7284.48$$

3rd year = 8158.6176

Year	Dep(A)
1	6504.227 6504
2	7284.48
3	8158.61
4	8137.65
5	10234.107
6	11462.27
7	12837.74
8	14378.27

Now!

	$B_{n-1}$	$n$	$B_n$
1	100 000	6564	93496
2	93496	7284.8044	86211.52
3	86211.52	8158.81	78052.91
4	78052.91	9137.65	68915.26
5	68915.26	10284.17	58681.12
6	58681.12	11452.27	47218.85
7	47218.85	12837.74	34381.11
8	34381.11	14378.27	20002.84
			$\times 20,000$
			$SV = SV$

\* Considering the  
the annual  
at each year

c) SL method  
method GRS

Cost basis

\$ 7000

① SL  $B_{n-1}$

8 years

1	700
2.	600
3	500
4	400
5	300

(n)

\* Considering the following information compute  
the annual depreciation and book value  
of each year by

- (i) SL method (ii) DB method (iii) SVD  
method (iv) sinking fund method

Cost basis	SV	n	MARR
\$ 7000	\$ 2000	5 yrs	10%

on  
 (i) SL       $B_{n-1}$        $D_n$        $B_n$

Year

1.	7000	1000	6000
2.	6000	1000	5000
3.	5000	1000	4000
4.	4000	1000	3000
5	3000	1000	2000

(BV > SV)

(n)

Bd DB

$$\alpha = \frac{2}{3} = 0.44\%$$

Year       $B_{n-1}$        $D_n$        $B_n$

1	7000	2800	4200
2	4200	1600	2520
3	2520	1008	1512
4	1512	604.8	907.2
5	907.2	362.88	544.32

$SU \cdot B_n \leftarrow SU$

Year       $B_{n-1}$        $D_n$        $B_n$

1	7000	2800	4200
2	4200	1600	5220
3	2520	173.33	2346.67
4	2346.67	173.33	2173.34
5	2173.34	173.33	2000

①  $SOD$

$$SOD = \frac{N(N+1)}{2} = 15$$

Year	$B_{n-1}$	$D_n = \left( \frac{n-n+1}{50 \times b} (1-s) \right)$	$B_n$
1	7000	1666.67	5333.33
2	5333.33	1333.33	4000
3	4000	1000	3000
4	3000	666.67	2333.33
5	2333.33	333.33	2000

$(BV = SV)$

### Slushing fund method

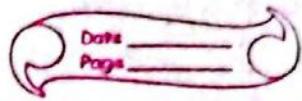
$$A = (P - F) (A/F, 10\%, 5)$$

$$= (7000 - 2000) \begin{pmatrix} 0.15 & 0.1 \\ 1.15 & 1 \end{pmatrix} \\ = 818.987$$

Year	$B_{n-1}$	$D_n$	$B_n$
1	7000	818.987	6181.013
2		900.886	5280.127
3		990.774	4289.153
4		1090.67	3199.083
5		1199.07	2000

$BV = SV$   $\Rightarrow$   $\#$

## (modified Accelerated Cost Recovery System)



### # MACRS Depreciation

- In US MACRS is launched from 1981 and from 1986 MACRS is implemented.
- It is a principle method for computing depreciation / deduction.
- The SV to be defined is zero and useful life estimates are not used directly in calculating depreciation amount.
- It includes eight categorized of assets and supposed useful life at 3 yrs, 5 yrs, 10, 15, 20, 27.5 and 30 yrs.

### # Half year convention of MACRS

- Assumes all the assets are placed in service at mid so only half of that years depreciation being taken in 1st year.
- MACRS assets is depreciated initially by declining balance method then by straight line method.

A firm plans to place in service Rs 10,000 assets that is assigned to 5 years class. Compute the MACRS % and depreciation amount for the assets.

$$N = 5 \text{ yrs}, \quad \text{B/F DDB} = \frac{2}{5} = 40\%$$

Year	Calculation %	MACRS %	Decision
1	$BD = \frac{1}{2} \times 40\% = 20\%$ x <u>half year</u> 1st year <u>to</u>	20%	
2	$DB = 0.4(100-20)40\% = 32\%$ $S.L = \frac{1}{5}(100-20)\% = 17.78\%$	32%	Do not switch
3	$BD = 0.4(100-20-32)40\% = 19.2\%$ $S.L = \frac{1}{5}(100-52)\% = 13.7\%$	19.2%	switch
4	$DB = 0.4(100-52-19.2)40\% = 11.52\%$ $S.L = \frac{1}{3}(100-52-19.2)40\% = 11.52\%$	11.52%	switch to SL
5	$S.L = \frac{1}{1.5}(100-82.72)40\% = 11.52\%$	11.52%	
①	$11.52 \times 0.5 = 5.76$ calc check garni muncing	5.76	directly 1/2 <u>of the</u> muncing



(8)

For now remaining 6 month

$$= \frac{1}{2} \times 11.52$$

$$= \boxed{5.76 \text{ ₦}}$$

PPR basis

n	%	Dep basic	Dep Amount
1	20%	10,000	2000
2	32	10,000	3200
3	19.2	10,000	1920
4	11.52	10,000	1152
5	11.52	10,000	1152
6	5.76	10,000	576

Dep schedule

n	B <sub>n-1</sub>	B <sub>n</sub>	B <sub>n</sub>
1	10,000	2000	8000
2	8000	3200	4800
3	4800	1920	2880
4	2880	1152	1728
5	1728	1152	576
6	576	576	0

## # Taxes

- Taxes are compulsory payment to government without exception of expectation of direct benefit in return to the tax paid.

## # Types of Taxes

### ① Direct tax

- The tax which cannot be shifted to others is called direct tax. These taxes are also known as personal tax. For example income tax, property tax, inheritance tax, land tax etc.

### ② Indirect tax

- The tax is legally imposed on one person but is actually paid by another person is called indirect tax. These taxes are also known as impersonal taxes for example VAT, custom duties, excise tax etc.

## b) Introduction to corporate income tax

- ### ① Income tax:
- income tax are assets as a function of gross revenue minus allowable reduction.

① property tax: Are assessed as a function of the value of property owned such as land, buildings, equipment.

② sales tax: are assessed as the basis of purchase of goods and/or services.

# Taxable income = Gross income (revenue) - All expenses except capital investment - Depreciable deducing.

# Net income after tax (NIAIT) = Net income before tax (NIBT) - Income tax

# Income tax = Tax rate  $\times$  taxable income

# Taxable income - Income tax = Net income

# Company buys a machine for Rs 78,000 and use for 5 yrs depreciation for 1st yr is Rs 4,000 suppose company estimated following revenue and expenses.

Gross income = Rs 50,000

Cost of good sold (expenses) = Rs 20,000

Operating expenses = Rs 6,000

What is the net income for the 1st year?

At the rate  $\times$

Taxable income  
expenses exc  
depreciable

$$= 50,000 - ?$$
$$= 20,000$$

40% of 20,

net income =

# General procedure  
Economic analysis

RK = Revenue

EI = Expenses

dk = Depreciation  
during period

t = income rate

Taxable income =  
Tax amount (Tk)

BTCF<sub>K</sub> = RK - EI

ATCF<sub>K</sub> = BTCF

If the tax rate is 40%.

Taxable income = Gross income - all expenses except capital investment - depreciable deductions

$$= \$50,000 - \$20,000 - \$6,000 - \$4,000 \\ = \$20,000$$

$$40\% \text{ of } \$20,000 = \$8,000$$

$$\text{Net income} = \$20,000 - \$8,000 = \$12,000$$

General procedures for making After tax economic analysis

$R_k$  = Revenue from the project during k

$E_k$  = Expenses from the project during period k

$d_k$  = Depreciation amount at the project during period k,

$t$  = income tax rate

$$\text{Taxable income} = R_k - E_k - d_k$$

$$\text{Tax amount (T}_k) = t (R_k - E_k - d_k)$$

$$\Delta TCF_k = R_k - E_k$$

$$\Delta TCF_k = \Delta TCF_k - T_k$$

$$= R_k - E_k - t(R_k - E_k - d_k)$$

$$= (1-t)(R_k - E_k) + t d_k$$

Tabular form to compute ATCFs

Year	BTCF	Depreciation	Taxable income	Tax amount
K	$R_k - E_k$	$d_k$	$BTCF - d_k$	$(R_k - E_k - d_k)$

$$\text{ATCF} = BTCF - \text{Tax amount}$$

$$(1-t)(R_k - E_k) + t d_k$$

# Suppose an asset was purchased for Rs 1,00,000. It is expected to produce net cash inflows of Rs 30,000 p.a. and effective income tax is 40%. Under the straight-line basis, the amount of taxes depreciation are as follows.

Year	1	2	3	4	5	6
Depreciation	10000	20000	20000	20000	20000	10000

calculate ATCFs and determine profitability  
 when MARR = 10% by using PW method  
 also calc IRR.

Soln:

Expenses = 0 in this

use

E = A - B

Year	A	B	C = A - B	D = t * C	AECF
Year	ATCF	Dep	taxable income	tax	
0	-100,000	0	-100,000	-	-100,000
1	30,000	10,000	20,000	8000	22,000
2	30,000	20,000	10,000	4000	26,000
3	30,000	20,000	10,000	4000	26,000
4	30,000	20,000	10,000	4000	26,000
5	30,000	20,000	10,000	4000	26,000
6	30,000	10,000	20,000	8000	22,000

22K      26K  
 ↑      ↑      ↑      ↑      ↑

↓  
 100,000

$$-PW = -7342 \text{ isl}$$

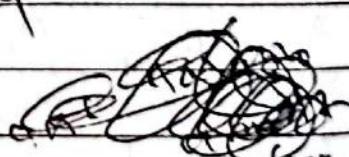
To find IRR

$$-100000 + 22000 (1+i)^{-1} + 22000 (1+i)^{-2} \\ + 26000 \left[ \frac{(1+i)^4 - 1}{i \times (1+i)^4} \right] (1+i)^{-1}$$

$$i = 12.5\%$$

$$IRR = 12.5\% \rightarrow MARR$$

Kunai On ma MA CRS  
ko sab nicalon  
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permo



Aesme B+C F

1st

2nd year 100 half hal

1st year

100

91%

Barber  
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2

1