

①

5.1 Fundamentals of Replacement Analysis



- Replacement analysis is carried out when there is a need to replace the current owned equipment or any assets.
- Concepts of replacement analysis refers to selection of similar but new assets to replace the existing assets to meet the current and future requirement more economically.
(defender → old asset | challenger → new asset)

Reasons for Replacement

- ① Deterioration: loss of value due aging
- ② Obsolescence: outdated or no longer used
- ③ Inadequacy: lacking the quality
- ④ Depletion: gradual loss of value
- ⑤ Physical impairment: wear and tear due to chemical changes

Approaches for comparing defender and challenger

- ⑥ Cash flow approach
- ⑦ Opportunity cost approach.

batches

pura ~~batches~~



(a) Cash flow approach

Icharcha garega

naya samman hoga

- Treat the proceeds from sale of the old machine as down payment towards purchasing the new machine.
- Use NPV or AB analysis to decide.

(b) Opportunity cost Approach

- Treat the proceeds from sale of the old machine as the investment requirement to keep the old machine.

Batches bhayo & aune jin paisa
cha tellai purao machine me invent
garne)

For the replacement analysis of an asset at a company the following information is available. By using cash flow approach decide whether replacement is justified or not take MARR = 12%.

Soln:

Q



Defender

Challenger

IP Rs 15000

IC Rs 20,000

n = 3 yrs

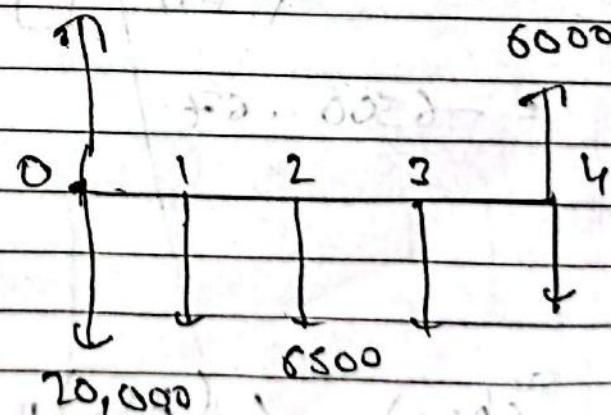
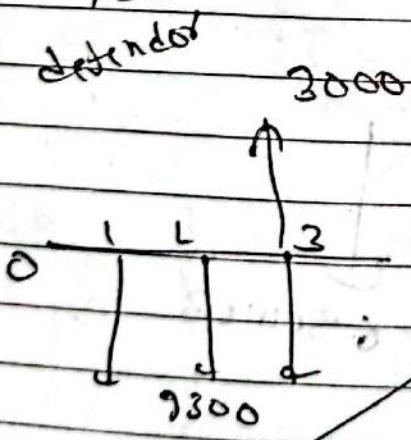
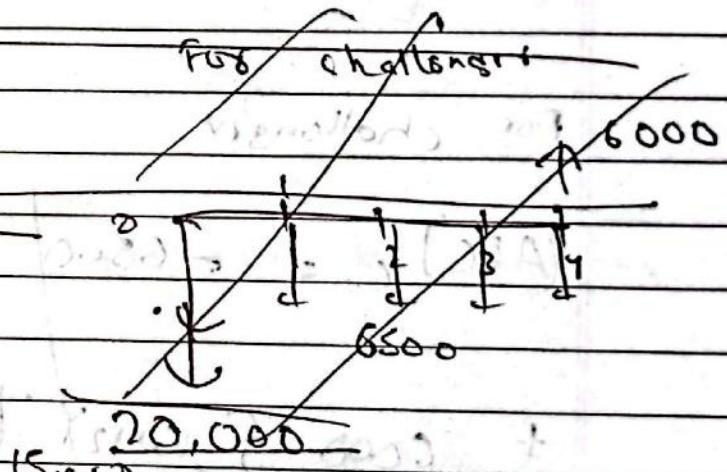
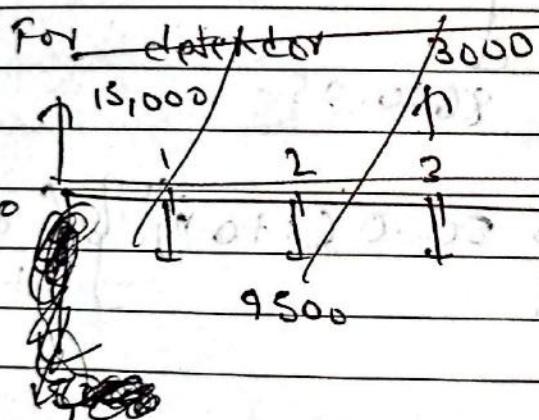
n = 4 yrs

SV Rs 3000 + 0.02C SV = 6000

OM Rs. 9500

OM = 6500

ROI %



L cash flow diagram:

Rs 15000 use same may not have same is
cash flow approach

(1)

Now find ABC of both:

for defenders

$$\begin{aligned}
 (ABC)_A &= -9500 + 3000 \left(A/F, 9\%, n \right) \\
 &= -9500 + 3000 \times \boxed{\frac{0.12}{0.12^8 - 1}} \\
 &= -8610.75
 \end{aligned}$$

for challenger

$$\begin{aligned}
 (ABC)_C &= -6500 - \left\{ 5000 \left(i + 0.12 \right)^4 \right\} \left\{ \frac{0.12}{0.12^4 - 1} \right\} \\
 &\quad + 6000 \left\{ \frac{0.12}{0.12^4 - 1} \right\} \\
 &= -6500.67
 \end{aligned}$$

$$\text{so } (ABC)_C < (ABC)_A$$

so we replace defender by challenger.

(2)

for challenge

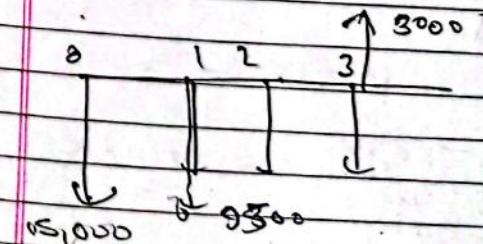
(ABC)_C

$$\begin{aligned}
 &= -6500 + 1867 \\
 &= -6890.76
 \end{aligned}$$

$$(ABC)_C < (ABC)_A$$

so replace defn

now by opportunity
market price

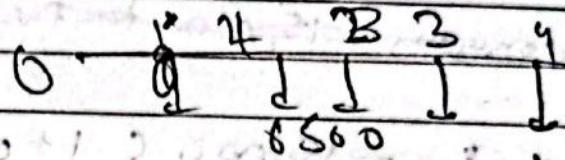


for
defender

③

for challenger

(ABC)



$$= -6500 + 1867.5968$$

$$\begin{pmatrix} 0.12 \\ 1.12^4 - 1 \end{pmatrix}$$

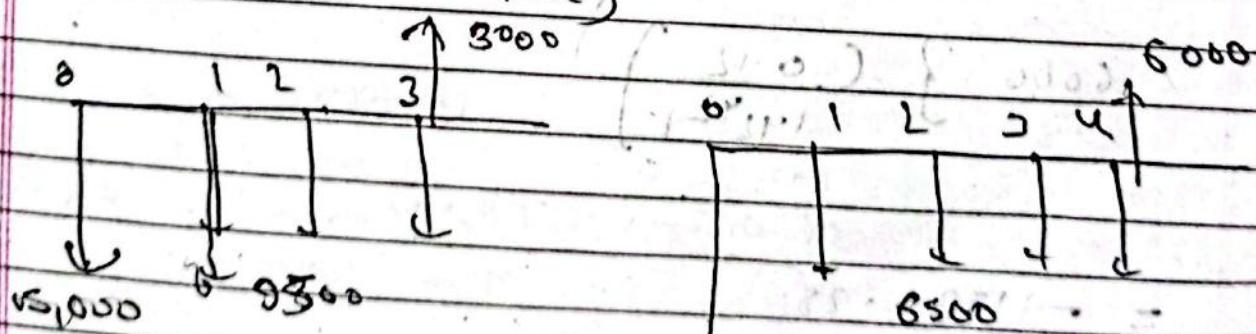
$$= 6 - 6890.76$$

$$1867.5968$$

(ABC) < (ABC)

so replace defencer defender by challenger.

now by opportunity cost approach #
(new \rightarrow profit at defender)
Market price)



for
defender

(b)

Date _____
Page _____

For defender

~~costing 15,000 b.p.s~~

$$= P - 15,000 (1 + 0.12)^3 + 2000$$

$$= -18073.02$$

Now

(AFC)

$$(AEC)_0 = -9500 - 18073.02 \left[\frac{0.12}{1.12^3 - 1} \right]$$

$$= \cancel{\dots} -14856.18$$

For challenger

$$(AEC)_c \approx -6500 + \frac{-20,000 \times 1.12^4}{1.12^4 - 1}$$

$$\left\{ \begin{array}{l} (0.12) \\ 1.12^4 - 1 \end{array} \right.$$

$$= -11829.28$$

 $(AEC)_0 > (AEC)_c$

~~Keep defender~~

Replace defender
by challenger

(P)

A Determine the replacement challenger with the one when MARR is 12

Year Defender

0	5000
1	1700
2	2000
3	2500

just find $(AEC)_0$

Now, for defender

$$FW = -5000 \times 1.12^3 - 2500$$

$$= -13897.12$$

$$(AEC)_0 = -13897.12$$

$$(AEC)_c = -13961.16$$

$$(AEC)_c < (AEC)_0$$

so replace D by



Determine the replacement between defender and challenger with the following cost information when MARR is 12%

Year Defender Challenger

0	5000	7500
1	1700	500
2	2000	1100
3	2500	1300

cost cost cost

just find $(ABC)_D$ and $(ABC)_C$

all cost

Now, for defender

$$FW = -5000 \times 1.12^3 + 1700 \times 1.12^2 + 2000 \times 1.12^1 - 2500$$

$$= -13897.12$$

$$(ABC)_D = -13897.12 \times \frac{0.12}{1.12^3 - 1} = -4117.50$$

$$(ABC)_C = -13896.16 \times \frac{0.12}{1.12^3 - 1} = -41058.84$$

$$(ABC)_C < (ABC)_D$$

so replace D by C

(8)

Replacement Analysis under the finite planning horizon (pw approach)

① Calculate AW_D and AW_E over study period. Select lowest AW.

② It is necessary to develop all viable defender challenger combinations and calculate AW or PW for each one over study period.

③ Select option with lowest cost or highest income.

~~Cost~~
The annual equivalent cost of defender and challengers are given in the table below, what is the best replacement strategy? Use MARR = 10%^{efb}. The planning horizon of the project is 8 years.

Ex (c)	1	2	3	4	5	6
(ABC) _b	5400	5200	5500	5700	6200	6600
(ABC) _c	7700	6200	5700	5100	5680	5900



Defender least cost (PSat) & min Chg \rightarrow Econ

Economic
Service Life

Challenger least cost 4 min chg

make combination so that (Defender 1st
min 2 yrs, Challenger 1st 4 yrs
(Challenger min))

(make at least 3-4 combinations)

Now,

BSL at Defend = 2

BSL at challenge = 4

Option 1

$(C_0, 0)$

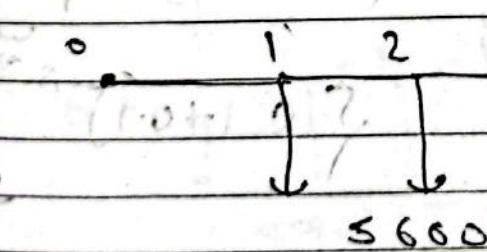
$(C_1, 4)$

$(C_1, 4)$ some comm
(challenger for year 4 lai 4 %
appat)

Defender 2x2

challenge - 4

challenger - 4



$$PW = -5600(P/A, 9\%, 8)$$

$$= -29875.58$$

(all negative
so sign
not taken here)

C.8 years (no lagi sara purcha)

16

Date _____
Page _____

Option 2; (0,2) (6,6)

0 1 2 3 4 5 6 7 8

inf value is 5200
 cash infl 5900

$$PW = \{5200 \left[\frac{1 - 1.1^{-6}}{0.1} \right] + 5900 \left[\frac{1 - 1.1^{-1}}{0.1} \right]\}$$

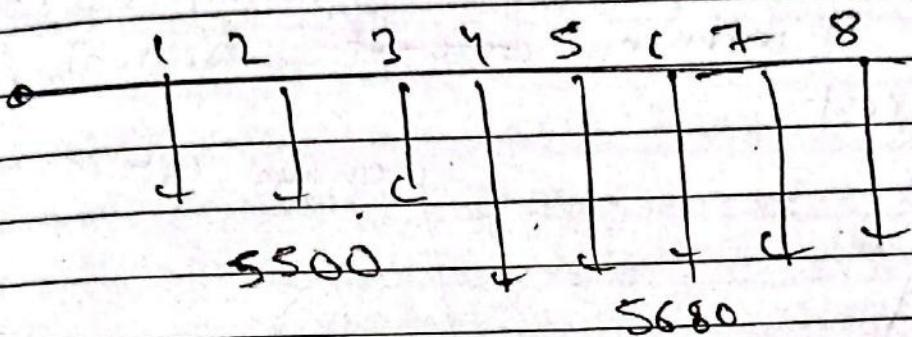
+ 5900

$$PW = 5200 \left[\frac{1 - 1.1^{-6}}{0.1} \right] + \{ 5900 \left[\frac{1 - 1.1^{-1}}{0.1} \right] \}$$

$$\{ C(1+0.1)^{-6} \}$$

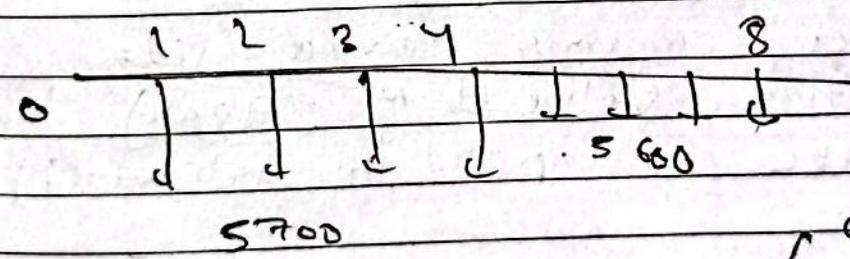
$$= 30261.18$$

① Option 3: \rightarrow $(D_1, 3)$ $((1, 5))$



$$PW = \$5500 \left(\frac{1.1^3 - 1}{1.1^3 \times 0.1} \right) + \left\{ \$5680 \left[\frac{1.1^5 - 1}{0.1} \right] \right. \\ \left. \left\{ (1+0.1)^{-8} \right\} \right\} \\ = 29854.74$$

Option 4: \rightarrow $(D_1, 4)$ $((1, 4))$



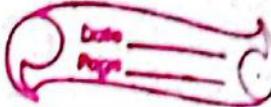
$$PW = 30,193$$

option 3 ($D_1, 3$)
 $((1, 5))$

is selected \neq

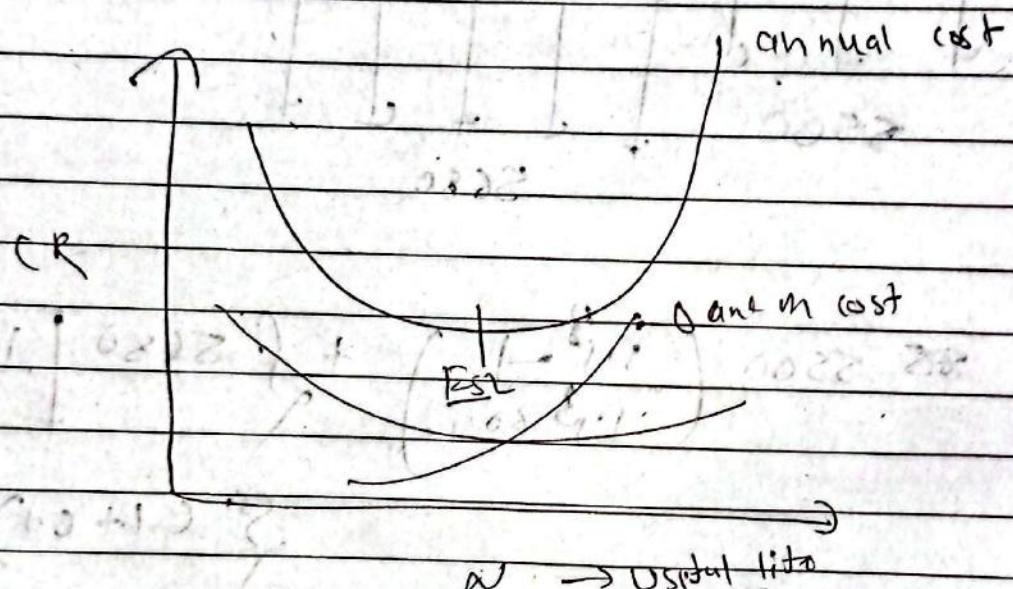
Since this is at cost we select the combination at lowest cost. Investment being highest investment. income
income

(12) ~~W.M.~~



Economic service life (E.S.L) ~~fall~~ ; ~~higher~~

- It is the remaining useful life of an assets that resolves in minimum amount annual equivalent cost.



$$ABC = CR + OC \quad \text{--- (i)}$$

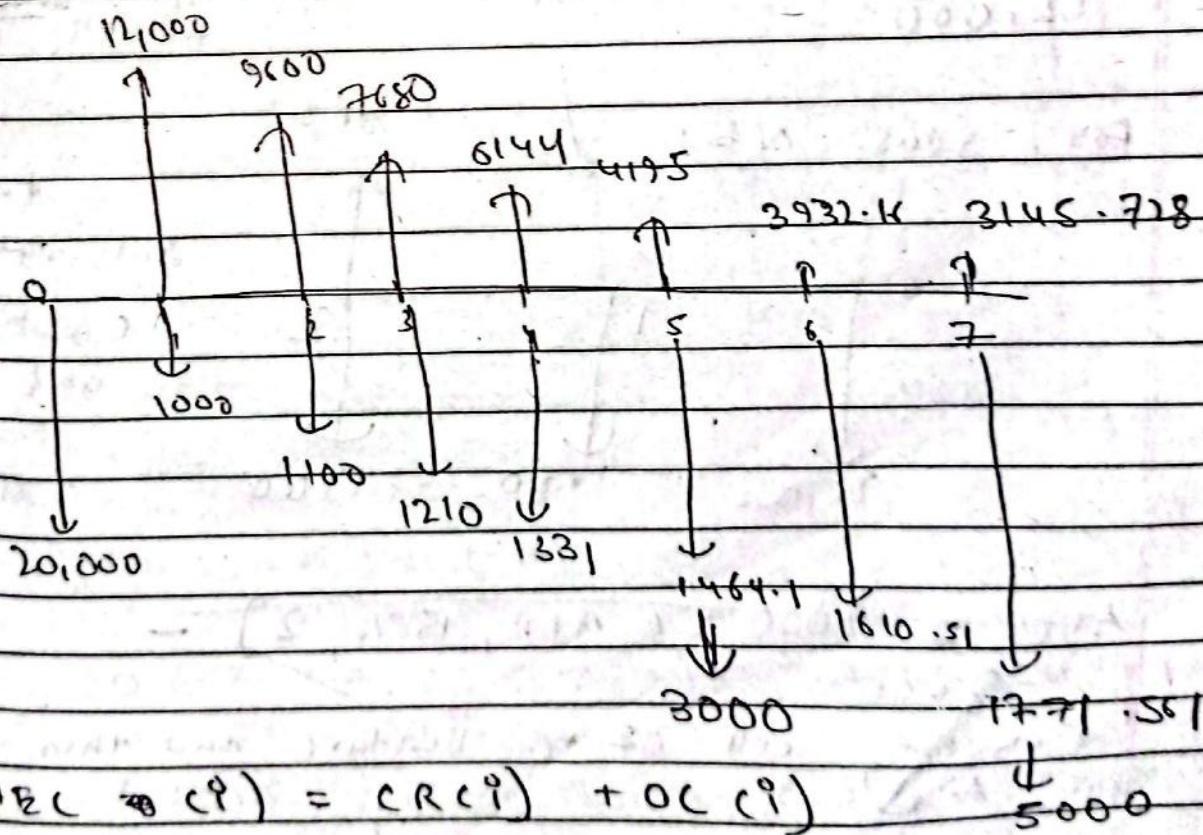
$\frac{1}{n}$ \uparrow
capital revenue
 \downarrow operating cost

To get exact economic service life we need to find value of n (year) has minimized ABC as expressed in eqn --- (i)

(13)

Find the economic service life of a new electric lift truck which costs \$ 20,000 has a operation cost \$ 1000 in 1st year and SV of \$ 12000 at the end of 1st year. For the remaining years, O.C. increase by 10% each year over previous year O.C. similarly SV declines every year by 200% of previous year SV. The lift truck has a minimum life of 7 yrs. An overhaul costing \$ 3000 and \$ 5000 will be required during 5th and 7th year of service. The firms require rate of return is 13% per year. (8)

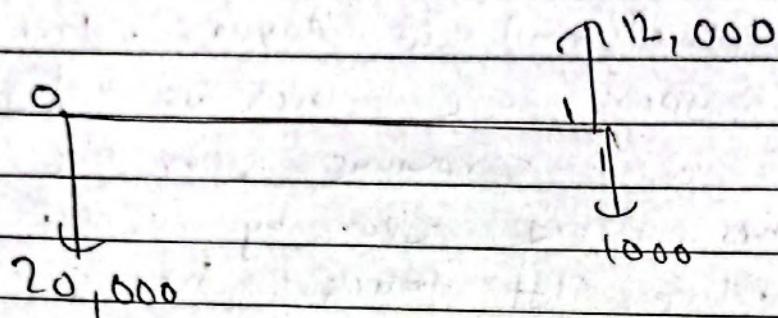
Solt:



(4)

For year $N=1$

$$AEC(15\%) = CR(15\%) + OC(15\%)$$

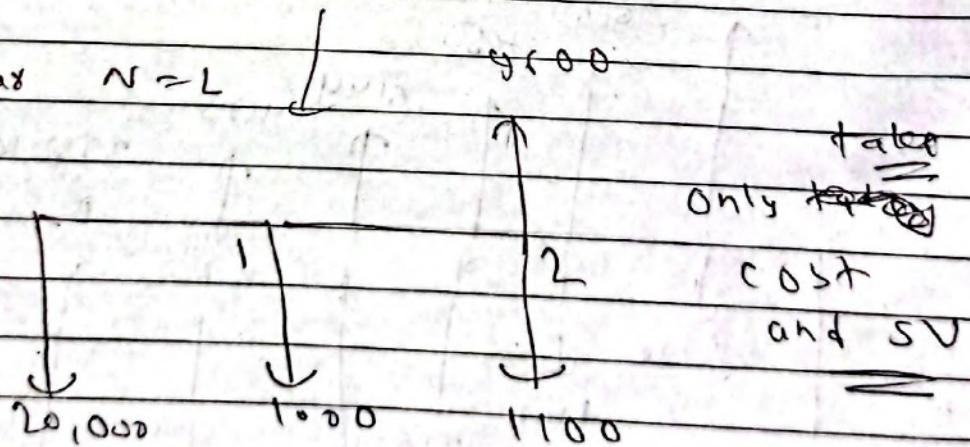


$$AEC(15\%) = 20,000 (AIP, 15\%, 1) -$$

$$12,000 (AIF, 15\%, 1) + 1000 (AF, 15\%, 1)$$

$$= 12,000$$

1st year of SV
machining 2 mg

for years $N=2$ 

$$ABC = 20,000 (AIP, 15\%, 2) -$$

9600

Convert all CF to future and then to A \textcircled{A}

(converting everything to PW and PW mg
using formulae)

$$= 20,000 \times 1.15^2 + 1000 \times 1.15 + 1100 - 960$$

$$= 19100$$

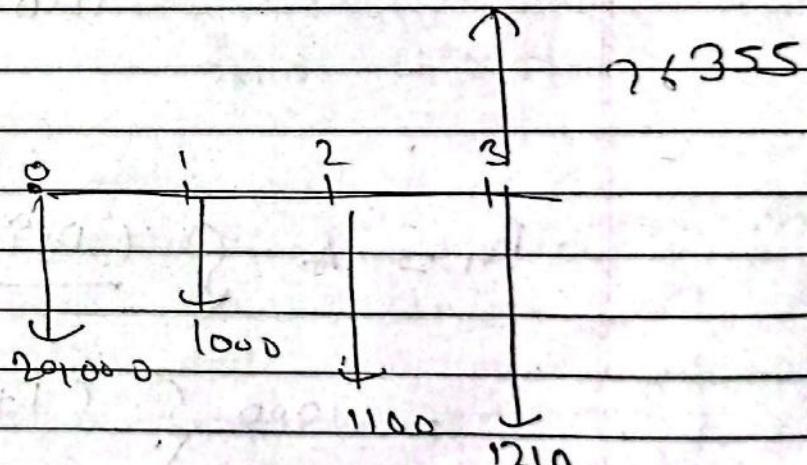
$$AFC (AFCL) = 19100 (AIF, 15\%, 2)$$

$$= 19100 \left[\frac{0.15}{1.15^2 - 1} \right] (AIP)$$

$$= 8883.72$$

Similarly

$$\text{Now, } N = 3$$



Now

8

PW2

$$(P-E)_3 = CR + OM$$

$$= 20,000 (AIF, 15\%, 3) - 7860 (AIF, 15\%, 3)$$

$$+ (1000 \times 1.15^2 + 1100 \times 1.15 + 1210) (AIF, 15\%, 3)$$

$$= 2606.94 \quad 7589.63$$

(16)

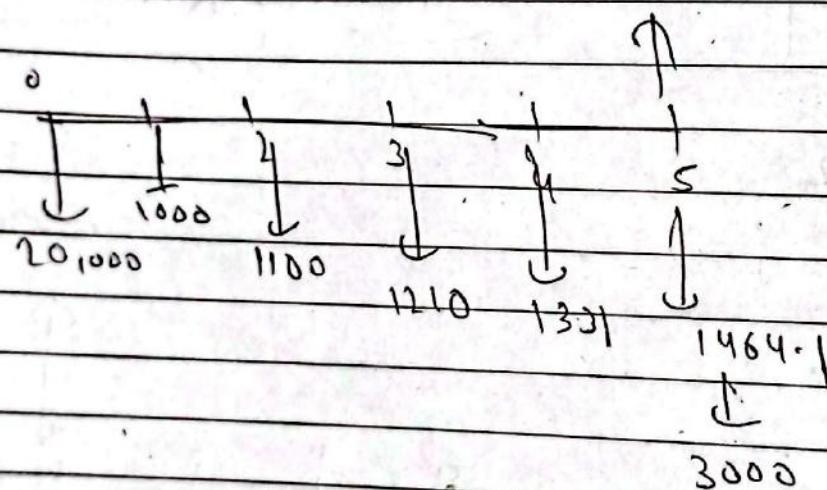
for year $N=4$

$$A_{F2C} = 8916.0$$

for year $N=5$

$$A_{F2C} =$$

$$5615$$



$$\begin{aligned}
 F_5 &= A \left\{ \frac{(1+i)^5 - (1+s)^5}{i-s} \right\} \\
 &= 1000 \left\{ \frac{(1+0.15)^5 - (1+0.1)^5}{0.15 - 0.1} \right\} \\
 &= 8016.94
 \end{aligned}$$

$$(-8016.94)$$

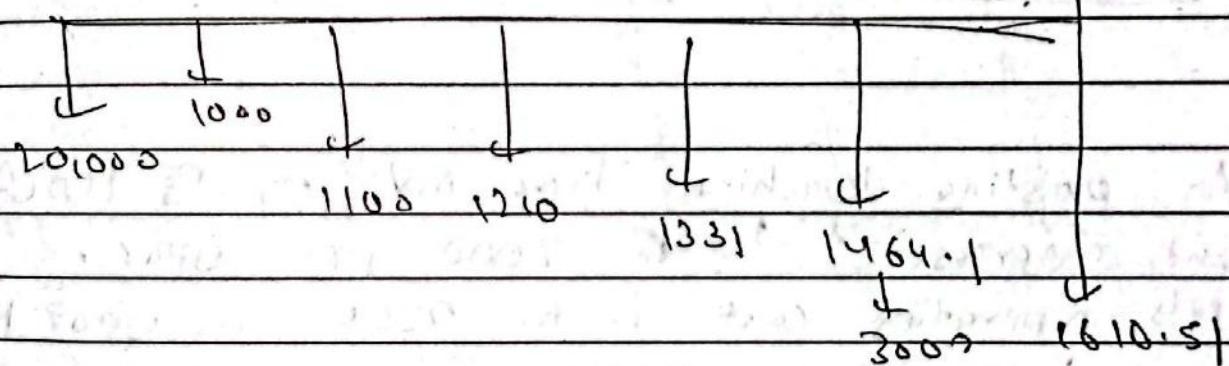
$$\begin{aligned}
 OIM (PW)_{m1} &= 8016.94 + 3000 \\
 &= 11016.94
 \end{aligned}$$

$$(ARC)_5 = 20,000 \left(A/F, 15\%, 5 \right) - 4195 \left(A/F, 15\%, 5 \right)$$

$$= 6978.11$$

$$3932.16$$

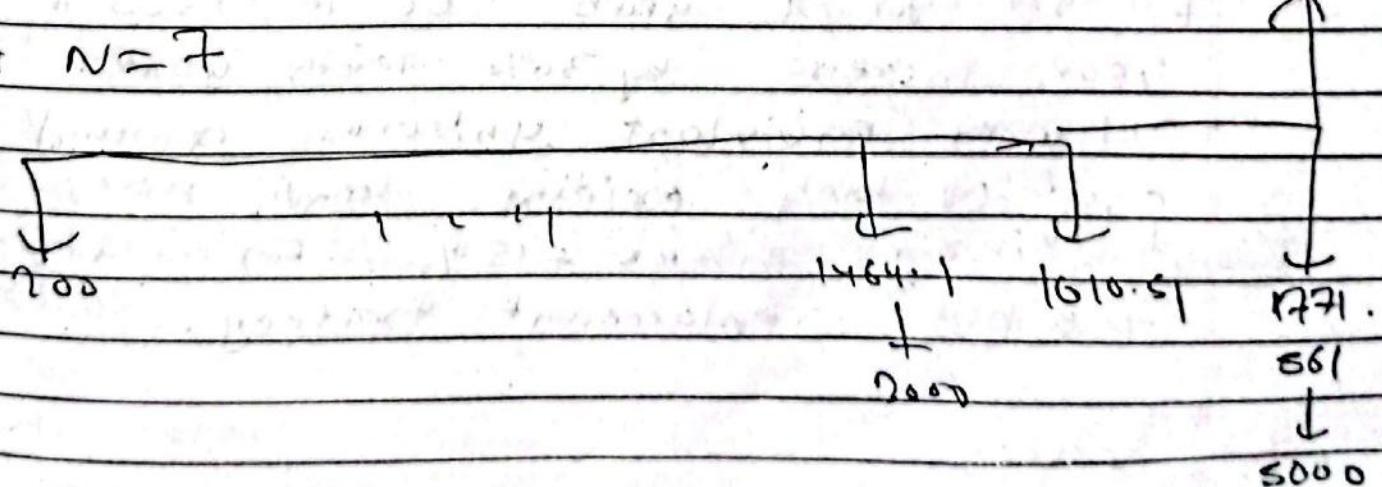
For $N=6$



$$(ARC)_6 = 6466.84$$

$$3143.72$$

For $N=7$



$$(ARC)_7 = \text{[Redacted]} 6618.73$$

(8)



(ABC) decreasing way \Rightarrow to

Hence

minimum ABC at 6th year

SD,

ESL = ~~at~~ 6 year

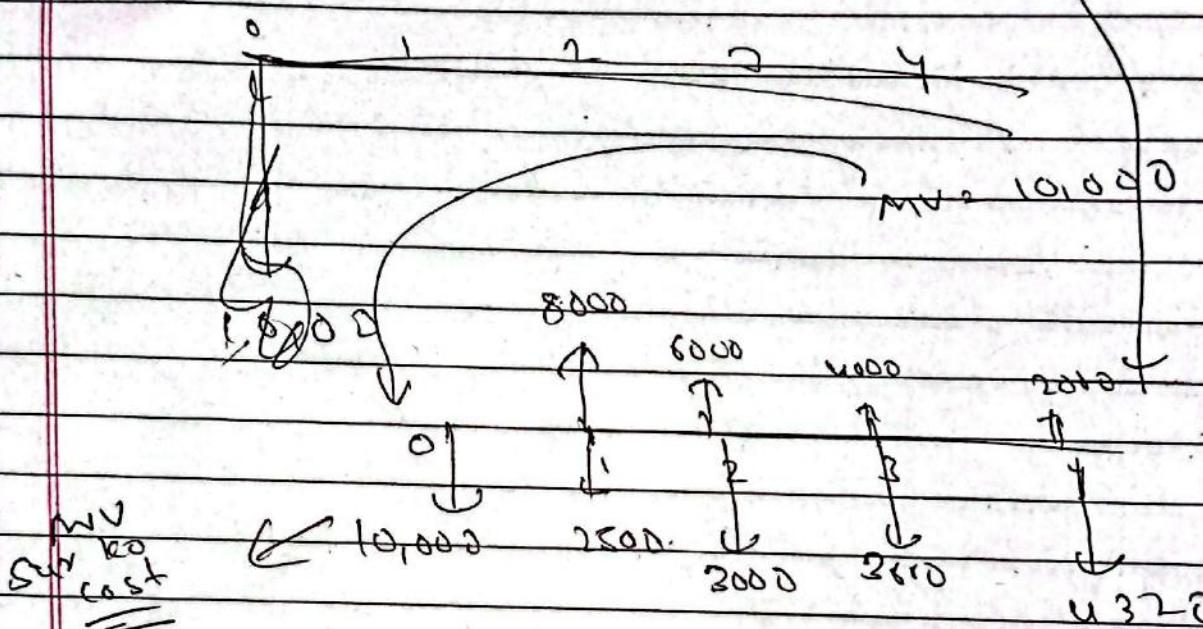
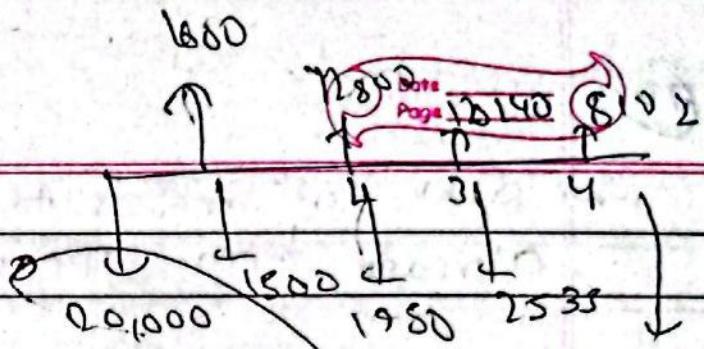
~~ESL = min ABC~~

#

An existing machine has MV. of Rs 10000 and decreases by Rs 2000 per year. Its operating cost is Rs 2800 in year 1 and increases by 20% each year for 4 years. New machine costs Rs 20,000 now and its MV will decrease 20% per year for 4 years. OC in 1st year increases by 30% each year. Calculate equivalent uniform annual cost w/ both existing and new machines. MARR = 15%. Formulate the best replacement strategy.

SOth

For defendor



AEC for

$N=2$

$N=3$

$N=4$

$N=1 = 6000$

6093.02

6210.22

6352.36

For new machine

$N=1$

85000

8500

$N=2$

8058.4

$N=3$

7757.74

$N=4$

7581.85

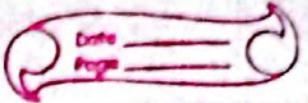
From both

ESL at defendor = 1 year

ESL at challenger = 4 years

AEC for challenger \rightarrow AEC of defendor for ESL
Max AEC of defendor $<$ AEC of challenger for ESL
(no need to replace defendor)

20



- sunk cost refers to the money that has already been spent and can't be recovered #