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In[268]:= MQF[f_] := {{
    1, 0}, {
    1/f, 1}}
MQD[f_] := {{
    1, 0}, {
    -1/f, 1}}
MDrift[s_] := {{
    1, s}, {
    0, 1}}

MFodoHalfx[fQF_, fQD_, s1_, s2_] := MQF[fQF].MDrift[s1].MQD[fQD].MDrift[s2]
MFodox[fQF_, fQD_, s1_, s2_] := MFodoHalfx[fQF, fQD, s1, s2].MFodoHalfx[fQF, fQD, s1, s2]
MFodoHalfy[fQF_, fQD_, s1_, s2_] := MQD[fQD].MDrift[s1].MQF[fQF].MDrift[s2]
MFodoy[fQF_, fQD_, s1_, s2_] := MFodoHalfy[fQF, fQD, s1, s2].MFodoHalfy[fQF, fQD, s1, s2]
gamma[alpha_, beta_] := (1 + alpha^2) / beta
Mbeta0[alpha_, beta_] := {{
    beta, -alpha},
    {-alpha, gamma[alpha, beta]}
}}
MbetaHalfx[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
    (MFodoHalfx[fQF, fQD, s1, s2].Mbeta0[alpha, beta]).
    Transpose[MFodoHalfx[fQF, fQD, s1, s2]]
Mbetax[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
    MFodox[fQF, fQD, s1, s2].Mbeta0[alpha, beta].Transpose[MFodox[fQF, fQD, s1, s2]]
MbetaHalfy[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
    (MFodoHalfy[fQF, fQD, s1, s2].Mbeta0[alpha, beta]).
    Transpose[MFodoHalfy[fQF, fQD, s1, s2]]
Mbetay[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
    MFodoy[fQF, fQD, s1, s2].Mbeta0[alpha, beta].Transpose[MFodoy[fQF, fQD, s1, s2]]

alpha0 = 0;
alphaHalf = 0;
alphaEnd = 0;
MbetaHalfx[fQF, fQD, s1, s2, alpha0, beta0]
Solve[MbetaHalfx[fQF, fQD, s1, s2, alpha0, beta0] ==
    {{betaStar, 0}, {0, 1/betaStar}}, {fQF, fQD}]
ChromX = 1 / (4 * Pi) * (1 / fQF * beta0 - 1 / fQD * (beta0 + s1 ** 2 / beta0))

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$$\text{Out[284]} = \left\{ \left\{ \beta_0 \left(1 - \frac{s_1}{f_{QD}} \right)^2 + \frac{\left(s_1 + \left(1 - \frac{s_1}{f_{QD}} \right) s_2 \right)^2}{\beta_0}, \right. \right. \\ \left. \beta_0 \left(1 - \frac{s_1}{f_{QD}} \right) \left(\frac{1}{f_{QF}} - \frac{1 + \frac{s_1}{f_{QF}}}{f_{QD}} \right) + \frac{\left(s_1 + \left(1 - \frac{s_1}{f_{QD}} \right) s_2 \right) \left(1 + \frac{s_1}{f_{QF}} + \left(\frac{1}{f_{QF}} - \frac{1 + \frac{s_1}{f_{QF}}}{f_{QD}} \right) s_2 \right)}{\beta_0}, \right. \\ \left. \left\{ \beta_0 \left(1 - \frac{s_1}{f_{QD}} \right) \left(\frac{1}{f_{QF}} - \frac{1 + \frac{s_1}{f_{QF}}}{f_{QD}} \right) + \frac{\left(s_1 + \left(1 - \frac{s_1}{f_{QD}} \right) s_2 \right) \left(1 + \frac{s_1}{f_{QF}} + \left(\frac{1}{f_{QF}} - \frac{1 + \frac{s_1}{f_{QF}}}{f_{QD}} \right) s_2 \right)}{\beta_0}, \right. \right. \\ \left. \left. \beta_0 \left(\frac{1}{f_{QF}} - \frac{1 + \frac{s_1}{f_{QF}}}{f_{QD}} \right)^2 + \frac{\left(1 + \frac{s_1}{f_{QF}} + \left(\frac{1}{f_{QF}} - \frac{1 + \frac{s_1}{f_{QF}}}{f_{QD}} \right) s_2 \right)^2}{\beta_0} \right\} \right\}$$

$$\text{Out[285]} = \left\{ \left\{ f_{QF} \rightarrow \left(-\beta_0^2 \beta_{\text{Star}} s_1 + \beta_0 \beta_{\text{Star}}^2 s_1 - \beta_{\text{Star}} s_1^2 s_2 - \right. \right. \right. \\ \left. \beta_{\text{Star}} s_1 s_2^2 + \frac{\beta_0^4 \beta_{\text{Star}} s_1}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \right. \\ \frac{\beta_0^3 \beta_{\text{Star}}^2 s_1}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{\beta_0^2 \beta_{\text{Star}} s_1^3}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{3 \beta_0^2 \beta_{\text{Star}} s_1^2 s_2}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \\ \frac{\beta_0 \beta_{\text{Star}}^2 s_1^2 s_2}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{\beta_{\text{Star}} s_1^4 s_2}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{2 \beta_0^2 \beta_{\text{Star}} s_1 s_2^2}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \\ \frac{\beta_0 \beta_{\text{Star}}^2 s_1 s_2^2}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{3 \beta_{\text{Star}} s_1^3 s_2^2}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{3 \beta_{\text{Star}} s_1^2 s_2^3}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{\beta_{\text{Star}} s_1 s_2^4}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \\ \frac{\beta_0^2 \beta_{\text{Star}} \sqrt{\beta_0^3 \beta_{\text{Star}} s_1^2 - \beta_0^2 s_1^4 + \beta_0 \beta_{\text{Star}} s_1^2 s_2^2}}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} + \\ \frac{\beta_0 \beta_{\text{Star}}^2 \sqrt{\beta_0^3 \beta_{\text{Star}} s_1^2 - \beta_0^2 s_1^4 + \beta_0 \beta_{\text{Star}} s_1^2 s_2^2}}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \\ \frac{\beta_{\text{Star}} s_1^2 \sqrt{\beta_0^3 \beta_{\text{Star}} s_1^2 - \beta_0^2 s_1^4 + \beta_0 \beta_{\text{Star}} s_1^2 s_2^2}}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \\ \frac{2 \beta_{\text{Star}} s_1 s_2 \sqrt{\beta_0^3 \beta_{\text{Star}} s_1^2 - \beta_0^2 s_1^4 + \beta_0 \beta_{\text{Star}} s_1^2 s_2^2}}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \\ \left. \frac{\beta_{\text{Star}} s_2^2 \sqrt{\beta_0^3 \beta_{\text{Star}} s_1^2 - \beta_0^2 s_1^4 + \beta_0 \beta_{\text{Star}} s_1^2 s_2^2}}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} \right) / \\ \left(\beta_0^2 \beta_{\text{Star}} - \beta_0 \beta_{\text{Star}}^2 - \beta_0 s_1^2 + \beta_{\text{Star}} s_2^2 \right), f_{QD} \rightarrow \\ \frac{\beta_0^2 s_1 + s_1^2 s_2 + s_1 s_2^2 - \sqrt{\beta_0^3 \beta_{\text{Star}} s_1^2 - \beta_0^2 s_1^4 + \beta_0 \beta_{\text{Star}} s_1^2 s_2^2}}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} \left. \right\}, \\ \left\{ f_{QF} \rightarrow \left(-\beta_0^2 \beta_{\text{Star}} s_1 + \beta_0 \beta_{\text{Star}}^2 s_1 - \beta_{\text{Star}} s_1^2 s_2 - \right. \right. \\ \left. \beta_{\text{Star}} s_1 s_2^2 + \frac{\beta_0^4 \beta_{\text{Star}} s_1}{\beta_0^2 - \beta_0 \beta_{\text{Star}} + s_1^2 + 2 s_1 s_2 + s_2^2} - \right.$$

$$\begin{aligned}
& \frac{\text{beta0}^3 \text{betaStar}^2 s1}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{\text{beta0}^2 \text{betaStar} s1^3}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{3 \text{beta0}^2 \text{betaStar} s1^2 s2}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} - \\
& \frac{\text{beta0} \text{betaStar}^2 s1^2 s2}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{\text{betaStar} s1^4 s2}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{2 \text{beta0}^2 \text{betaStar} s1 s2^2}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} - \\
& \frac{\text{beta0} \text{betaStar}^2 s1 s2^2}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{3 \text{betaStar} s1^3 s2^2}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{3 \text{betaStar} s1^2 s2^3}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{\text{betaStar} s1 s2^4}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{\text{beta0}^2 \text{betaStar} \sqrt{\text{beta0}^3 \text{betaStar} s1^2 - \text{beta0}^2 s1^4 + \text{beta0} \text{betaStar} s1^2 s2^2}}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} - \\
& \frac{\text{beta0} \text{betaStar}^2 \sqrt{\text{beta0}^3 \text{betaStar} s1^2 - \text{beta0}^2 s1^4 + \text{beta0} \text{betaStar} s1^2 s2^2}}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{\text{betaStar} s1^2 \sqrt{\text{beta0}^3 \text{betaStar} s1^2 - \text{beta0}^2 s1^4 + \text{beta0} \text{betaStar} s1^2 s2^2}}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{2 \text{betaStar} s1 s2 \sqrt{\text{beta0}^3 \text{betaStar} s1^2 - \text{beta0}^2 s1^4 + \text{beta0} \text{betaStar} s1^2 s2^2}}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} + \\
& \frac{\text{betaStar} s2^2 \sqrt{\text{beta0}^3 \text{betaStar} s1^2 - \text{beta0}^2 s1^4 + \text{beta0} \text{betaStar} s1^2 s2^2}}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} \Big) / \\
& \left(\text{beta0}^2 \text{betaStar} - \text{beta0} \text{betaStar}^2 - \text{beta0} s1^2 + \text{betaStar} s2^2 \right), \text{fQD} \rightarrow \\
& \frac{\text{beta0}^2 s1 + s1^2 s2 + s1 s2^2 + \sqrt{\text{beta0}^3 \text{betaStar} s1^2 - \text{beta0}^2 s1^4 + \text{beta0} \text{betaStar} s1^2 s2^2}}{\text{beta0}^2 - \text{beta0} \text{betaStar} + s1^2 + 2 s1 s2 + s2^2} \Big) \Big\}
\end{aligned}$$

$$\text{Out[286]= } \frac{\frac{\text{beta0}}{\text{fQF}} - \frac{\text{beta0} + \frac{s1 + 2}{\text{beta0}}}{\text{fQD}}}{4 \pi}$$

$$\begin{aligned}
& \left\{ \left\{ \text{Cos}[\omega]^2 \text{Cosh}[\omega], \frac{l^2 \text{Sin}[\omega]^2 \text{Sinh}[\omega]}{\text{Abs}[k]^{3/2}}, 0, 0 \right\}, \right. \\
& \left\{ 0, \text{Cos}[\omega]^2 \text{Cosh}[\omega], 0, 0 \right\}, \\
& \left\{ 0, 0, \text{Cos}[\omega] \text{Cosh}[\omega]^2, \frac{l^2 \text{Sin}[\omega] \text{Sinh}[\omega]^2}{\text{Abs}[k]^{3/2}} \right\}, \\
& \left. \left\{ 0, 0, 0, \text{Cos}[\omega] \text{Cosh}[\omega]^2 \right\} \right\}
\end{aligned}$$