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ln[525]:= MQF[f_] := {{
    1, 0}, {
    1/f, 1}}
MQD[f_] := {{
    1, 0}, {
    -1/f, 1}}
MDrift[s_] := {{
    1, s}, {
    0, 1}}

MFodoHalfx[fQF_, fQD_, s1_, s2_] := MQF[fQF].MDrift[s1].MQD[fQD].MDrift[s2]
MFodox[fQF_, fQD_, s1_, s2_] :=
    MFodoHalfx[fQF, fQD, s1, s2].MDrift[s2].MQD[fQD].MDrift[s1].MQF[fQF]
MFodoHalfy[fQF_, fQD_, s1_, s2_] := MQD[fQD].MDrift[s1].MQF[fQF].MDrift[s2]
MFodoy[fQF_, fQD_, s1_, s2_] :=
    MFodoHalfy[fQF, fQD, s1, s2].MDrift[s2].MQF[fQF].MDrift[s1].MQD[fQD]
gamma[alpha_, beta_] := (1 + alpha^2) / beta
MKSHalfx[fQF_, fQD_, s1_, s2_] := {{
    MFodoHalfx[fQF, fQD, s1, s2][[1, 1]]^2, -2 * MFodoHalfx[fQF, fQD, s1, s2][[1, 1]] *
    MFodoHalfx[fQF, fQD, s1, s2][[1, 2]], MFodoHalfx[fQF, fQD, s1, s2][[1, 2]]^2},
    {-MFodoHalfx[fQF, fQD, s1, s2][[1, 1]] * MFodoHalfx[fQF, fQD, s1, s2][[2, 1]],
    MFodoHalfx[fQF, fQD, s1, s2][[1, 1]] * MFodoHalfx[fQF, fQD, s1, s2][[2, 2]] +
    MFodoHalfx[fQF, fQD, s1, s2][[1, 2]] * MFodoHalfx[fQF, fQD, s1, s2][[2, 1]],
    -MFodoHalfx[fQF, fQD, s1, s2][[2, 2]] * MFodoHalfx[fQF, fQD, s1, s2][[1, 2]]},
    {MFodoHalfx[fQF, fQD, s1, s2][[2, 1]]^2, -2 * MFodoHalfx[fQF, fQD, s1, s2][[2, 2]] *
    MFodoHalfx[fQF, fQD, s1, s2][[2, 1]], MFodoHalfx[fQF, fQD, s1, s2][[2, 2]]^2
    }}
MKSx[fQF_, fQD_, s1_, s2_] := {{
    MFodox[fQF, fQD, s1, s2][[1, 1]]^2, -2 * MFodox[fQF, fQD, s1, s2][[1, 1]] *
    MFodox[fQF, fQD, s1, s2][[1, 2]], MFodox[fQF, fQD, s1, s2][[1, 2]]^2},
    {-MFodox[fQF, fQD, s1, s2][[1, 1]] * MFodox[fQF, fQD, s1, s2][[2, 1]],
    MFodox[fQF, fQD, s1, s2][[1, 1]] * MFodox[fQF, fQD, s1, s2][[2, 2]] +
    MFodox[fQF, fQD, s1, s2][[1, 2]] * MFodox[fQF, fQD, s1, s2][[2, 1]],
    -MFodox[fQF, fQD, s1, s2][[2, 2]] * MFodox[fQF, fQD, s1, s2][[1, 2]]},
    {MFodox[fQF, fQD, s1, s2][[2, 1]]^2, -2 * MFodox[fQF, fQD, s1, s2][[2, 2]] *
    MFodox[fQF, fQD, s1, s2][[2, 1]], MFodox[fQF, fQD, s1, s2][[2, 2]]^2
    }}
MKSHalfy[fQF_, fQD_, s1_, s2_] := {{
    MFodoHalfy[fQF, fQD, s1, s2][[1, 1]]^2, -2 * MFodoHalfy[fQF, fQD, s1, s2][[1, 1]] *
    MFodoHalfy[fQF, fQD, s1, s2][[1, 2]], MFodoHalfy[fQF, fQD, s1, s2][[1, 2]]^2},
    {-MFodoHalfy[fQF, fQD, s1, s2][[1, 1]] * MFodoHalfy[fQF, fQD, s1, s2][[2, 1]],
    MFodoHalfy[fQF, fQD, s1, s2][[1, 1]] * MFodoHalfy[fQF, fQD, s1, s2][[2, 2]] +
    MFodoHalfy[fQF, fQD, s1, s2][[1, 2]] * MFodoHalfy[fQF, fQD, s1, s2][[2, 1]],

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    -MFodoHalfy[fQF, fQD, s1, s2][[2, 2]] * MFodoHalfy[fQF, fQD, s1, s2][[1, 2]]},
    {MFodoHalfy[fQF, fQD, s1, s2][[2, 1]]^2, -2 * MFodoHalfy[fQF, fQD, s1, s2][[2, 2]] *
      MFodoHalfy[fQF, fQD, s1, s2][[2, 1]], MFodoHalfy[fQF, fQD, s1, s2][[2, 2]]^2
    }}
  }}
MKSy[fQF_, fQD_, s1_, s2_] := {{
  MFodoy[fQF, fQD, s1, s2][[1, 1]]^2, -2 * MFodoy[fQF, fQD, s1, s2][[1, 1]] *
    MFodoy[fQF, fQD, s1, s2][[1, 2]], MFodoy[fQF, fQD, s1, s2][[1, 2]]^2},
  {-MFodoy[fQF, fQD, s1, s2][[1, 1]] * MFodoy[fQF, fQD, s1, s2][[2, 1]],
    MFodoy[fQF, fQD, s1, s2][[1, 1]] * MFodoy[fQF, fQD, s1, s2][[2, 2]] +
      MFodoy[fQF, fQD, s1, s2][[1, 2]] * MFodoy[fQF, fQD, s1, s2][[2, 1]],
    -MFodoy[fQF, fQD, s1, s2][[2, 2]] * MFodoy[fQF, fQD, s1, s2][[1, 2]]},
  {MFodoy[fQF, fQD, s1, s2][[2, 1]]^2, -2 * MFodoy[fQF, fQD, s1, s2][[2, 2]] *
    MFodoy[fQF, fQD, s1, s2][[2, 1]], MFodoy[fQF, fQD, s1, s2][[2, 2]]^2
  }}
Mbeta0[alpha_, beta_] := {{
  beta, -alpha},
  {-alpha, gamma[alpha, beta]}
}}
MbetaHalfx[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
  (MFodoHalfx[fQF, fQD, s1, s2].Mbeta0[alpha, beta]).
  Transpose[MFodoHalfx[fQF, fQD, s1, s2]]
Mbetax[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
  MFodox[fQF, fQD, s1, s2].Mbeta0[alpha, beta].Transpose[MFodox[fQF, fQD, s1, s2]]
MbetaHalfy[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
  (MFodoHalfy[fQF, fQD, s1, s2].Mbeta0[alpha, beta]).
  Transpose[MFodoHalfy[fQF, fQD, s1, s2]]
Mbetay[fQF_, fQD_, s1_, s2_, alpha_, beta_] :=
  MFodoy[fQF, fQD, s1, s2].Mbeta0[alpha, beta].Transpose[MFodoy[fQF, fQD, s1, s2]]
MFunc[beta0_, beta_, alpha00_, alpha_, phi_] := {{
  Sqrt[beta/beta0] * (Cos[phi] + alpha0 * Sin[phi]), Sqrt[beta * beta0] * Sin[phi]},
  {(alpha00 - alpha) * Cos[phi] - (1 + alpha00 * alpha) * Sin[phi] / Sqrt[beta * beta0]},
  Sqrt[beta0/beta] * (Cos[phi] - alpha * Sin[phi])}}

D0 = 10;
Ds = 0.05 * D0;
alpha0 = 0;
alphaHalf = 0;
alphaEnd = 0;
phase = 150 * Pi / 180.;
NSolve[MFodoy[fQF, fQD, Ds, D0][[1, 1]] == Cos[phase] &&
  MFodoy[fQF, fQD, Ds, D0][[1, 2]] == beta * Sin[phase], {fQF, fQD}]

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Solve: Solve was unable to solve the system with inexact coefficients. The answer was obtained by solving a corresponding exact system and numericizing the result.

$$\text{Out}[549]= \left\{ \left\{ \text{fQF} \rightarrow \frac{0.5 \left(41. - 1. \sqrt{1. + 40. \text{beta}} \right)}{-42. + \text{beta}}, \text{fQD} \rightarrow \left(2.93545 \times 10^7 \right. \right. \\ \left. \left(-2.35623 \times 10^9 \text{beta} - \frac{1.01097 \times 10^{11} \text{beta}}{-42. + \text{beta}} + 5.8709 \times 10^7 \text{beta}^2 + \frac{2.40707 \times 10^9 \text{beta}^2}{-42. + \text{beta}} + \right. \right. \\ \left. \left. \frac{2.46578 \times 10^9 \text{beta} \sqrt{1. + 40. \text{beta}}}{-42. + \text{beta}} - \frac{5.8709 \times 10^7 \text{beta}^2 \sqrt{1. + 40. \text{beta}}}{-42. + \text{beta}} \right) \right) / \\ \left. \left(-8.61688 \times 10^{14} - 1.319 \times 10^{17} \text{beta} + 3.44675 \times 10^{15} \text{beta}^2 \right) \right\}, \\ \left\{ \text{fQF} \rightarrow \frac{0.5 \left(41. + \sqrt{1. + 40. \text{beta}} \right)}{-42. + \text{beta}}, \text{fQD} \rightarrow \left(2.93545 \times 10^7 \right. \right. \\ \left. \left(-2.35623 \times 10^9 \text{beta} - \frac{1.01097 \times 10^{11} \text{beta}}{-42. + \text{beta}} + 5.8709 \times 10^7 \text{beta}^2 + \frac{2.40707 \times 10^9 \text{beta}^2}{-42. + \text{beta}} - \right. \right. \\ \left. \left. \frac{2.46578 \times 10^9 \text{beta} \sqrt{1. + 40. \text{beta}}}{-42. + \text{beta}} + \frac{5.8709 \times 10^7 \text{beta}^2 \sqrt{1. + 40. \text{beta}}}{-42. + \text{beta}} \right) \right) / \\ \left. \left(-8.61688 \times 10^{14} - 1.319 \times 10^{17} \text{beta} + 3.44675 \times 10^{15} \text{beta}^2 \right) \right\} \right\}$$

$$\left\{ \left\{ \text{Cos}[\omega]^2 \text{Cosh}[\omega], \frac{l^2 \text{Sin}[\omega]^2 \text{Sinh}[\omega]}{\text{Abs}[k]^{3/2}}, 0, 0 \right\}, \right. \\ \left\{ 0, \text{Cos}[\omega]^2 \text{Cosh}[\omega], 0, 0 \right\}, \\ \left\{ 0, 0, \text{Cos}[\omega] \text{Cosh}[\omega]^2, \frac{l^2 \text{Sin}[\omega] \text{Sinh}[\omega]^2}{\text{Abs}[k]^{3/2}} \right\}, \\ \left. \left\{ 0, 0, 0, \text{Cos}[\omega] \text{Cosh}[\omega]^2 \right\} \right\}$$