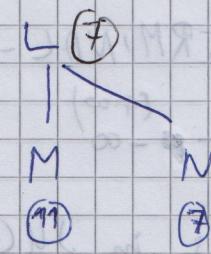
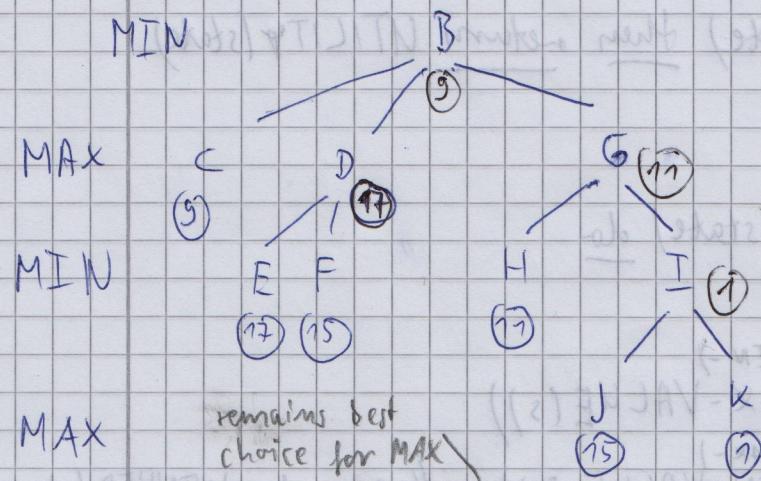


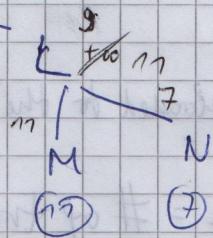
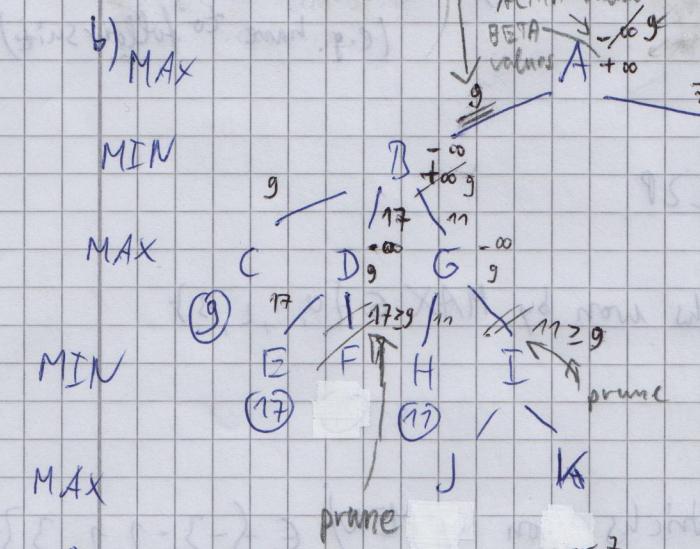
AI
using

Ex 3.1) MAX

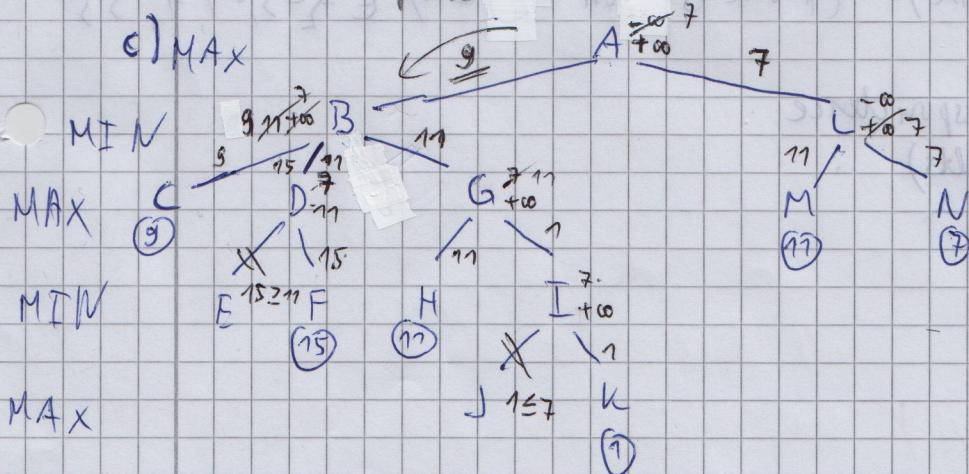
UB3



(cf. ALPHA-DETA-
Search version 2)



pruned: F, I, J, K



pruned: E, J

Complexity for Minimax: $\mathcal{O}(b^d)$

α - β with optimal ordering: $\mathcal{O}(b^{d/2})$

α - β on average: $\mathcal{O}(b^{3d/4})$

Ex 3.2) a) (MIN-)

function: MAX-VALUE(state) returns a utility value

If TERMINAL-TEST(state) then return UTILITY(state)

$$v \leftarrow \begin{cases} +\infty \\ -\infty \end{cases}$$

for a, s in SUCCESSORS(state) do

if WINNER(s) = MAX

(MIN)

(MIN-) (MAX-)

then $v \leftarrow \text{MAX}(v, \text{MAX-VALUE}(s))$

else $v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(s))$

// also when WINNER(s) = \emptyset

return v

(e.g. have to follow suit)

b) game-tree will be uploaded to the L2P

Note: utility value = # of tricks won by MAX $\in \{0, 1, 2, 3\}$

Alternative: utility value:

$$(\# \text{ tricks won by MAX}) - (\# \text{ tricks won by MIN}) \in \{-3, -1, 1, 3\}$$

\Rightarrow one-to-one correspondence

(yield same results)

AI $(t \times 3.3)$ a) / b)

tidung

ÜB3

A

B

A

B

A

B

A

B

$A - B$

(+1)

$- A - B$

(+1)

$- A B$

(+1)

\overline{BA}

(+1)

$A B -$

(-1)

$A - B$

(-1)

$- BA$

(-1)

$\overline{B - A -}$

(-1)

$- - AB$

(?)

$- A - B$

(?)

b) pass the (?) from button upwards

c) trivial answers:

- standard minimax cannot handle questionmarks
- If loop states would not have been considered as terminal states, then minimax would run into an infinite path (depth-first)

fix: keep track of all (loop) states, and

define max and min for each non-empty subset of $\{-1, ?, +1\}$

	$\{-1, ?, +1\}$	$\{+1, ?\}$	$\{+1, -1\}$	$\{?, -1\}$	$\{+1\}$	$\{?\}$	$\{-1\}$
$A = MAX$	+1	+1	+1	?	+1	?	-1
$B = MIN$	-1	?	-1	-1	+1	?	-1

Note: Exactly the same result will be obtained if "?" is replaced by "+0".



This will always work optimally for win/lose games

(i.e. when terminal states have values " $-n$ " or " $+n$ ")

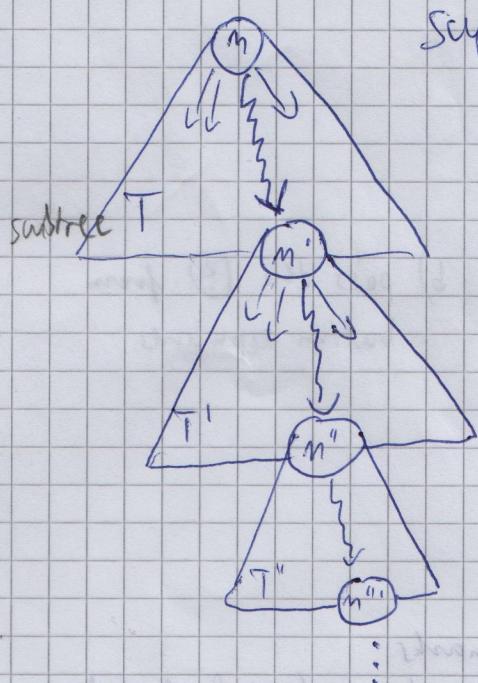
because " ± 0 " represents a draw.

More general: If there is a value that can represent a draw, then "?" can be replaced by this value and the standard minimax will work optimally.

"Proof": Minimax works optimally for all finite games.

\Rightarrow only to show: loop states lead to draws

Suppose: The best choices in T lead from n to n' and n' is like n .



Then T' equals T , and:

the best choices in T lead from n' to n'' , and n'' is like n' .

Then T'' equals T' , etc.

\Rightarrow If n' is reached, then it will lead to an infinite path.

Infinite paths are draws (nobody wins).

\Rightarrow Loop states lead to draws.