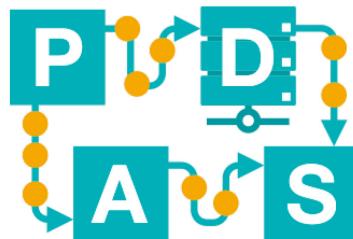


## Neural Networks (1/2)

Lecture 7

**IDS-L7**

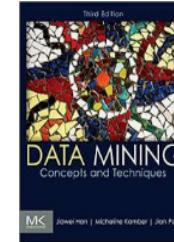


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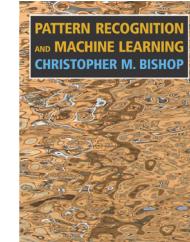
**RWTH**AACHEN  
UNIVERSITY

# Outline of Today's Lecture

- **Introduction to Neural Networks**
- **Human and Artificial Neurons**
- **What are Neural Networks?**
- **Model Representation**
- **Feedforward Networks**



Based on  
chapter 9 of  
“data mining  
concepts and  
techniques”  
by Jiawei  
Han

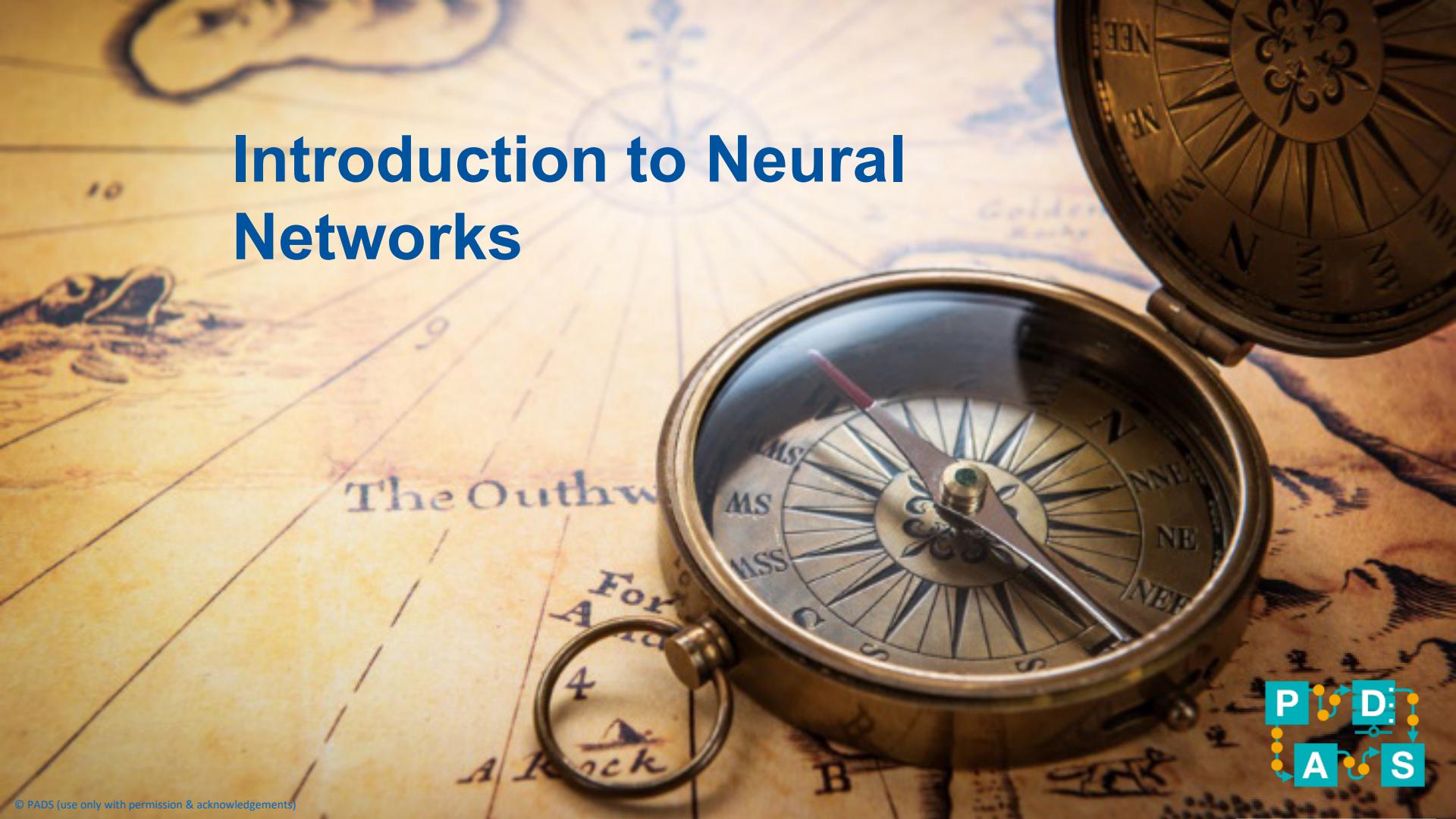


Chapter 5 of  
“pattern  
recognition  
and machine  
learning” by  
Christopher  
M. Bishop



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# Introduction to Neural Networks



# Positioning Neural Networks

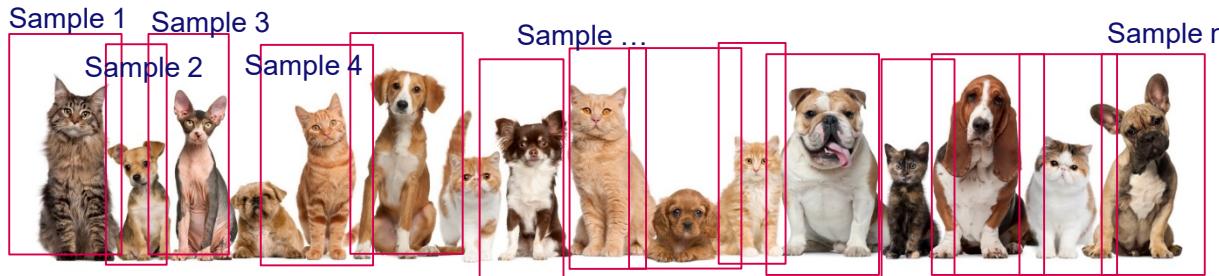
## Supervised learning techniques

- **Decision Trees**
  - Were initially developed for categorical features and then extended to continuous features.
- **Regression**
  - Followed the reverse path (most suitable for continuous data).
- **Support Vector Machines**
  - For large numbers of features while avoiding overfitting.
- **Today: Neural Networks**
  - Flexible in the types of data they can support.
  - Learns the important features from basically any data structure.



# Why Use Neural Networks?

**Linear machines are often not satisfactory when facing real world situations**



Is this a dog?



A five years old child simply knows, but how should a computer know?

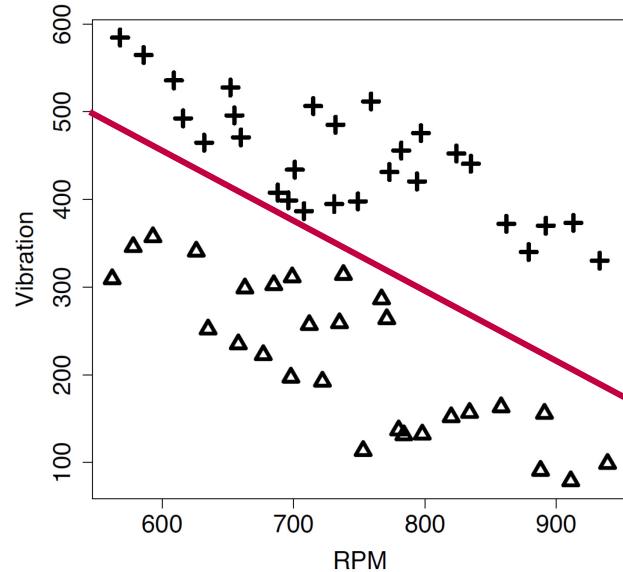
# Why Use Neural Networks?

## Linear Problem

For simple linear classification: one can use logistic regression or SVM to separate the instances

| ID | RPM | VIBRATION | STATUS |
|----|-----|-----------|--------|
| 1  | 568 | 585       | good   |
| 2  | 586 | 565       | good   |
| 3  | 609 | 536       | good   |
| 4  | 616 | 492       | good   |
| 5  | 632 | 465       | good   |
| 6  | 652 | 528       | good   |
| 7  | 655 | 496       | good   |
| 8  | 660 | 471       | good   |
| 9  | 688 | 408       | good   |
| 10 | 696 | 399       | good   |
| 11 | 708 | 387       | good   |
| 12 | 701 | 434       | good   |
| 13 | 715 | 506       | good   |
| 14 | 732 | 485       | good   |
| 15 | 731 | 395       | good   |
| 16 | 749 | 398       | good   |
| 17 | 759 | 512       | good   |
| 18 | 773 | 431       | good   |
| 19 | 782 | 456       | good   |
| 20 | 797 | 476       | good   |
| 21 | 794 | 421       | good   |
| 22 | 824 | 452       | good   |
| 23 | 835 | 441       | good   |
| 24 | 862 | 372       | good   |
| 25 | 879 | 340       | good   |
| 26 | 892 | 370       | good   |
| 27 | 913 | 373       | good   |
| 28 | 933 | 330       | good   |

| ID | RPM | VIBRATION | STATUS |
|----|-----|-----------|--------|
| 29 | 562 | 309       | faulty |
| 30 | 578 | 346       | faulty |
| 31 | 593 | 357       | faulty |
| 32 | 626 | 341       | faulty |
| 33 | 635 | 252       | faulty |
| 34 | 658 | 235       | faulty |
| 35 | 663 | 299       | faulty |
| 36 | 677 | 223       | faulty |
| 37 | 685 | 303       | faulty |
| 38 | 698 | 197       | faulty |
| 39 | 699 | 311       | faulty |
| 40 | 712 | 257       | faulty |
| 41 | 722 | 193       | faulty |
| 42 | 735 | 259       | faulty |
| 43 | 738 | 314       | faulty |
| 44 | 753 | 113       | faulty |
| 45 | 767 | 286       | faulty |
| 46 | 771 | 264       | faulty |
| 47 | 780 | 137       | faulty |
| 48 | 784 | 131       | faulty |
| 49 | 798 | 132       | faulty |
| 50 | 820 | 152       | faulty |
| 51 | 834 | 157       | faulty |
| 52 | 858 | 163       | faulty |
| 53 | 888 | 91        | faulty |
| 54 | 891 | 156       | faulty |
| 55 | 911 | 79        | faulty |
| 56 | 939 | 99        | faulty |



# Why Use Neural Networks?

## Non-Linear Problem

- Nonlinear classification may work fine.

GROWTH =  $0.3707 \times \phi_0(\text{RAIN}) + 0.8475 \times \phi_1(\text{RAIN}) + -1.717 \times \phi_2(\text{RAIN})$

from lecture on regression

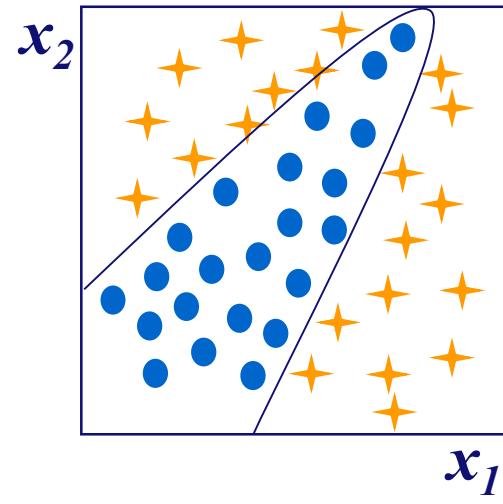
$$\min_{\vec{w}, b, \epsilon} \frac{1}{2} \|\vec{w}\|^2 + C \sum_{i=1}^m \epsilon_i$$

such that

$$y_i(\vec{w} \cdot \phi(\vec{x}_i) + b) \geq 1 - \epsilon_i \text{ for any } i$$

from lecture on SVMs

- But for most of the problems in practice:
  - The number of features is often more than two.
  - What if the number of features is 100?
  - Just the number of possible pairs is already  $n(n - 1) = 9900!$



# Why Neural Networks?

## Limitation of Simple Linear Models

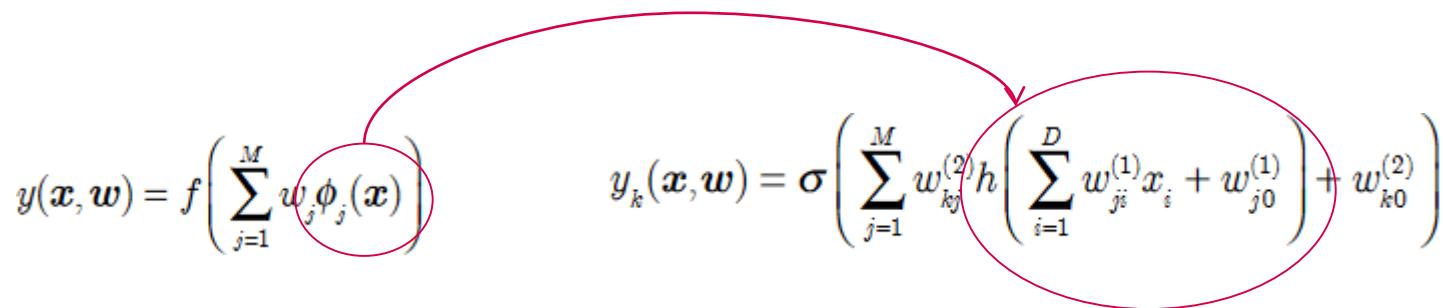
- Consider the following as a general form of Linear Models:
- Where:
  - $x$  represents input (vector describing the descriptive features)
  - $w$  represents the weight vector
  - $\phi_j(x)$  is:
    - $j$ th element of the feature vector
    - or a calculation to change input dimensions to a higher dimension
  - $f$  is:
    - a simple threshold-based function returning  $0$  or  $1$
    - or more sophisticated functions like the sigmoid function (to add nonlinearity)
  - $M$  represents the number of descriptive features

$$y(\mathbf{x}, \mathbf{w}) = f\left( \sum_{j=1}^M w_j \phi_j(\mathbf{x}) \right)$$

# Why Neural Networks?

## Limitation of Simple Linear Models

- SVM and Neural Networks try to address limitations of traditional purely linear approaches
  - SVM**
    - By varying number of  $\phi_j(x)$  functions on training data points
  - Neural Networks**
    - $\phi_j(x)$  functions may be based on other layers and can be learned

$$y(\mathbf{x}, \mathbf{w}) = f\left(\sum_{j=1}^M w_j \phi_j(\mathbf{x})\right)$$
$$y_k(\mathbf{x}, \mathbf{w}) = \sigma\left(\sum_{j=1}^M w_{kj}^{(2)} h\left(\sum_{i=1}^D w_{ji}^{(1)} x_i + w_{j0}^{(1)}\right) + w_{k0}^{(2)}\right)$$


- input  $\mathbf{x}$  has  $D$  dimensions (features)
- $\sigma$  and  $h$  are activation functions  
(will be explained later)

# Why Use Neural Networks?

## Example

- Automatic dog detection
- Provide many labeled sample of
  - Dogs
  - Non dogs



Non dogs



Dogs

- Is this a dog?

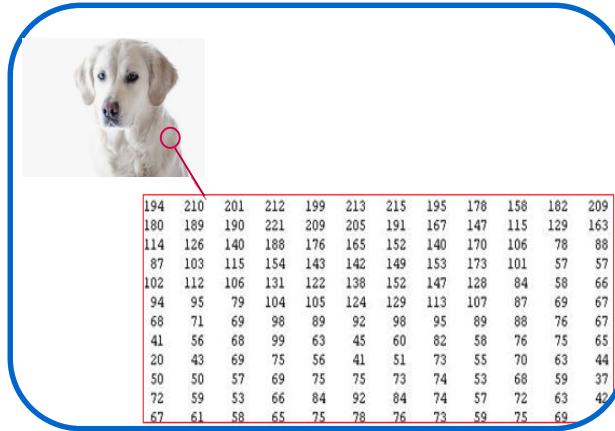


# Why Use Neural Networks?

Large number of features



What we see!



What the  
camera sees!

Consider the number of features!

# More Specific Example

## Number recognition

- To a computer, an image is really just a grid of numbers that represent how dark each pixel is:
  - Now imagine: handwriting of digit number 8
    - 18\*18 pixel image as an array of 324 numbers

The numbers inside pixels show the darkness of that pixel.  
In grey scale format ,the value of each pixel is between 0-255



```
[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 12, 0, 11, 39, 137, 37, 0, 152, 147, 84, 0, 0, 0, 0, 1, 0, 0, 0, 41, 160, 250, 255, 235, 162, 255, 238, 206, 11, 13, 0, 0, 0, 16, 9, 9, 150, 251, 45, 21, 184, 159, 154, 2, 55, 233, 40, 0, 0, 10, 0, 0, 0, 0, 145, 146, 3, 10, 0, 11, 124, 253, 255, 107, 0, 0, 0, 3, 0, 4, 15, 236, 216, 0, 0, 38, 109, 247, 240, 169, 0, 11, 0, 1, 0, 2, 0, 0, 0, 253, 253, 23, 62, 224, 241, 255, 164, 0, 5, 0, 0, 6, 0, 0, 4, 0, 3, 252, 250, 228, 255, 255, 234, 112, 28, 0, 2, 17, 0, 0, 2, 1, 4, 0, 21, 255, 253, 251, 255, 172, 31, 8, 0, 1, 0, 0, 0, 0, 0, 4, 0, 163, 225, 251, 255, 229, 120, 0, 0, 0, 0, 11, 0, 0, 0, 21, 162, 255, 255, 254, 255, 126, 6, 0, 10, 14, 6, 0, 0, 9, 0, 3, 79, 242, 255, 141, 66, 255, 245, 189, 7, 8, 0, 0, 5, 0, 0, 0, 26, 221, 237, 98, 0, 67, 251, 255, 144, 0, 8, 0, 0, 7, 0, 0, 11, 0, 125, 255, 141, 0, 87, 244, 255, 208, 3, 0, 0, 13, 0, 1, 0, 1, 0, 0, 145, 248, 228, 116, 235, 255, 141, 34, 0, 11, 0, 1, 0, 0, 0, 1, 3, 0, 85, 237, 253, 246, 255, 210, 21, 1, 0, 1, 0, 0, 6, 2, 4, 0, 0, 0, 6, 23, 112, 157, 114, 32, 0, 0, 0, 0, 2, 0, 8, 0, 7, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]
```

How computer sees this 8  
(Set of features)

```
8277577288570717593102799694741144880263  
0076344434232808297619004206643390473220  
2646475987190687719865210108347713096038  
028365767261026971958700616448623313094  
$102142209993134195543933585065182689228  
L197550722135848852571618380010302408662  
1339049154955269534730462940627103912604  
3411908211907574239990252138331676072005  
713128829424198480307883947331008721162  
6017236165078786923886311326060599102219
```

Training dataset for the number recognition classifier



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# What Is a Neural Network?

- **Motivation**
  - Simulation of the neuron system's information processing mechanisms (as used in the human brain).
- **Structure**
  - Huge amount of densely connected, mutually operating processing units (**neurons**)
- **It learns from experiences (training instances)**

# What Is a Neural Network?

- An information processing paradigm
- Inspired by biological nervous systems
  - such as the human brain ...
- Composed of a large number of highly interconnected processing elements (neurons)
- Through a learning process
  - Learning in biological systems involves adjustments to the synaptic connections that exist between the neurons.

# Historical Background

- First artificial neuron
  - 1943
  - Invented by the neurophysiologist **Warren McCulloch** and the logician **Walter Pits**
- But the technology available at that time did not allow them to use such artificial neurons on any meaningful manner.

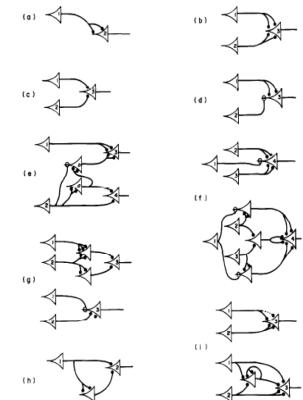
## A LOGICAL CALCULUS OF THE IDEAS IMMANENT IN NERVOUS ACTIVITY\*

■ WARREN S. McCULLOCH AND WALTER PITTS  
University of Illinois, College of Medicine,  
Department of Psychiatry at the Illinois Neuropsychiatric Institute,  
University of Chicago, Chicago, U.S.A.

Because of the "all-or-none" character of nervous activity, neural events and the relations among them can be treated by means of propositional logic. It is found that the behavior of every net can be described in these terms, with the addition of more complicated logical means for nets containing circles; and that for any logical expression satisfying certain conditions, one can find a net which behaves in the way it describes. It is shown that many particular choices among possible neurophysiological assumptions are equivalent, in the sense that for every net behaving under one assumption, there exists another net which behaves under the other and gives the same results, although perhaps not in the same time. Various applications of the calculus are discussed.

1. Introduction. Theoretical neurophysiology rests on certain cardinal assumptions. The nervous system is a net of neurons, each having a soma and an axon. Their adjunctions, or synapses, are always between the axon of one neuron and the soma of another. At any instant a neuron has some threshold, which excitation must exceed to initiate an impulse. This, except for the fact and the time of its occurrence, is determined by the neuron, not by the excitation. From the point of excitation the impulse is propagated to all parts of the neuron. The velocity along the axon varies directly with its diameter, from  $< 1 \text{ ms}^{-1}$  in thin axons, which are usually short, to  $> 150 \text{ ms}^{-1}$  in thick axons, which are usually long. The time for axonal conduction is consequently of little importance in determining the time of arrival of impulses at points unequally remote from the same source. Excitation across synapses occurs predominantly from axonal terminations to somata. It is still a moot point whether this depends upon reciprocity of individual synapses or merely upon prevalent anatomical configurations. To suppose the latter requires no hypothesis *ad hoc* and explains known exceptions, but any assumption as to cause is compatible with the calculus to come. No case is known in which excitation through a single synapse has elicited a nervous impulse in any neuron, whereas any neuron may be excited by impulses arriving at a sufficient number of neighboring synapses within the period of latent addition, which lasts  $< 0.25 \text{ ms}$ . Observed temporal summation of impulses at greater intervals

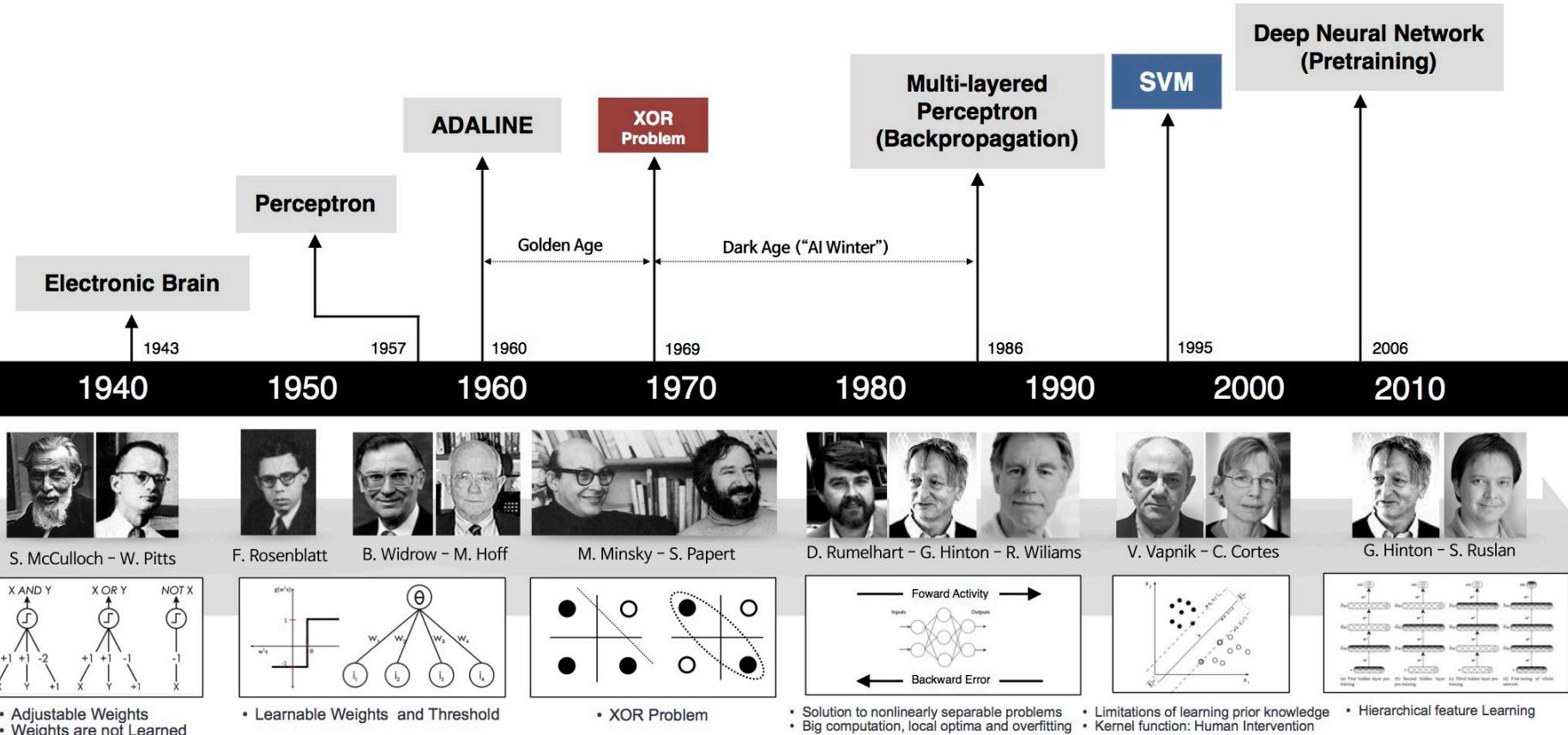
\* Reprinted from the *Bulletin of Mathematical Biophysics*, Vol. 5, pp. 115-133 (1943).



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# Brief History of Neural Networks

(taken from Sefik Ilkin Serengil's Blog on the "Evolution of Neural Networks" Oct. 2017)



# Why Use Neural Networks?

## Why

- Ability to derive meaning
- Complicated data
- Imprecise data

## Uses

- Extract pattern
- Detect trends that:
  - Humans and other computer techniques can't

## Advantages

- Adaptive learning
- Self-Organization
- Real Time Operation
- Fault Tolerance

## A trained neural network

- Is an expert that:
  - can be used to provide projections given:
    - New situations of interest
    - Answer "what if" question

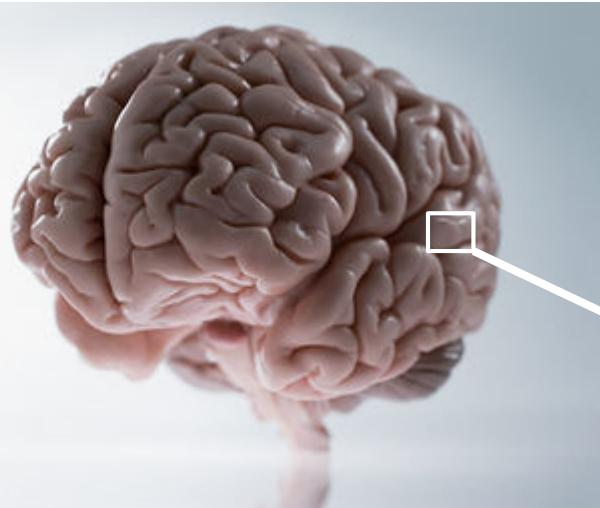
# Properties of Artificial Neural Networks

- High level abstraction of neural input-output transformation
  - Inputs → weighted sum of inputs → nonlinear function → output
    - Typically no spikes (neurons fire in each cycle)
    - Typically use additional constraints or learning rules
- Often used where data or functions are uncertain
  - Goal is to learn from a set of training data
  - And to generalize from learned instances to new unseen data

# Human and Artificial Neurons

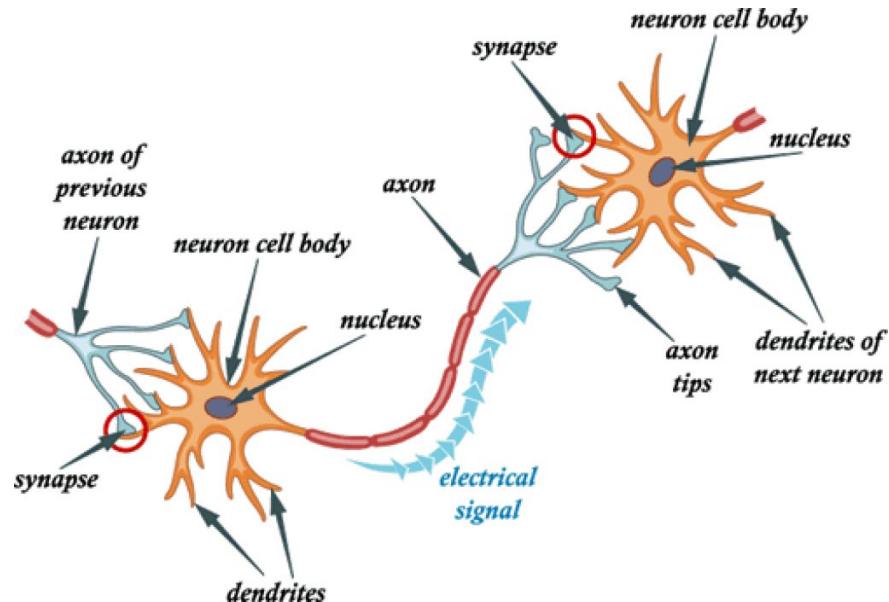


**The human brain contains around 100 billion neurons  
(give or take a few billion).**



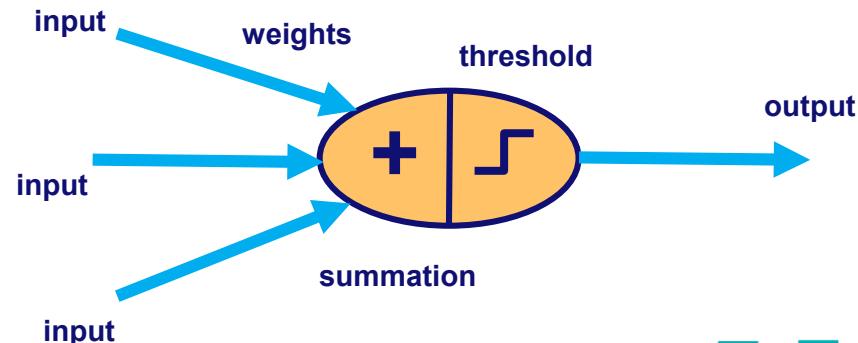
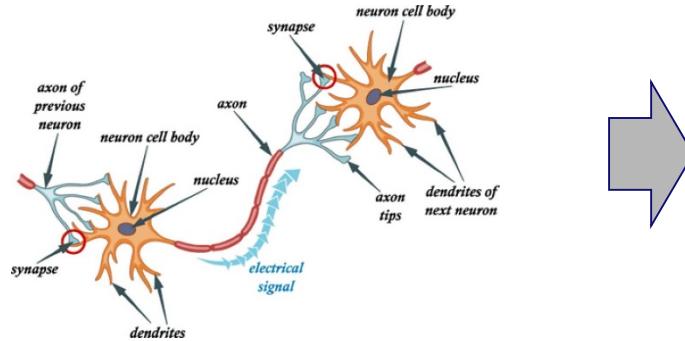
# How the Human Brain Learns

- Dendrites are sensitive to a certain kind of chemicals
- When there are a certain variety of chemical signals around these dendrites, they absorb them
  - When a certain amount of chemical is accumulated at the cell, it fires.
  - It generates an electrical pulse through an axon, into the synapse connected to the next neuron's dendrites.
  - The pulse is picked up as a signal by the dendrites of the next cell.



# From Human Neurons to Artificial Neurons

- When a neuron receives excitatory input
  - If is sufficiently large compared with its inhibitory input, then sends a spike of electrical activity down its axon.
- Learning occurs:
  - By changing the effectiveness of the synapses.
  - The influence of one neuron on another changes.



# From Human Neurons to Artificial Neurons

- “Imitating” neural networks
  - First
    - Deduce the essential features of neurons
    - Understand their interconnections
  - Then
    - Program a computer to simulate these features

Our knowledge of neurons is incomplete and our computing power is limited.  
Hence, our models are necessarily gross idealizations of real networks of neurons.

# How to Create and Represent a Neural Network?

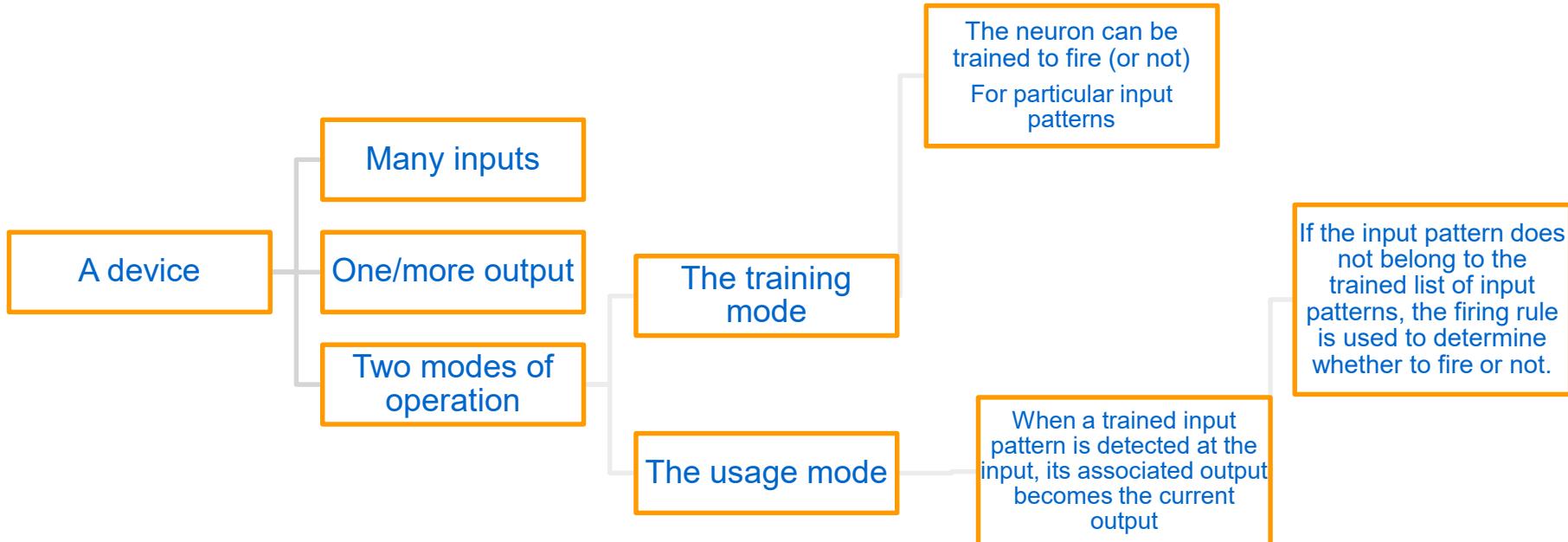


# Create Neural Networks

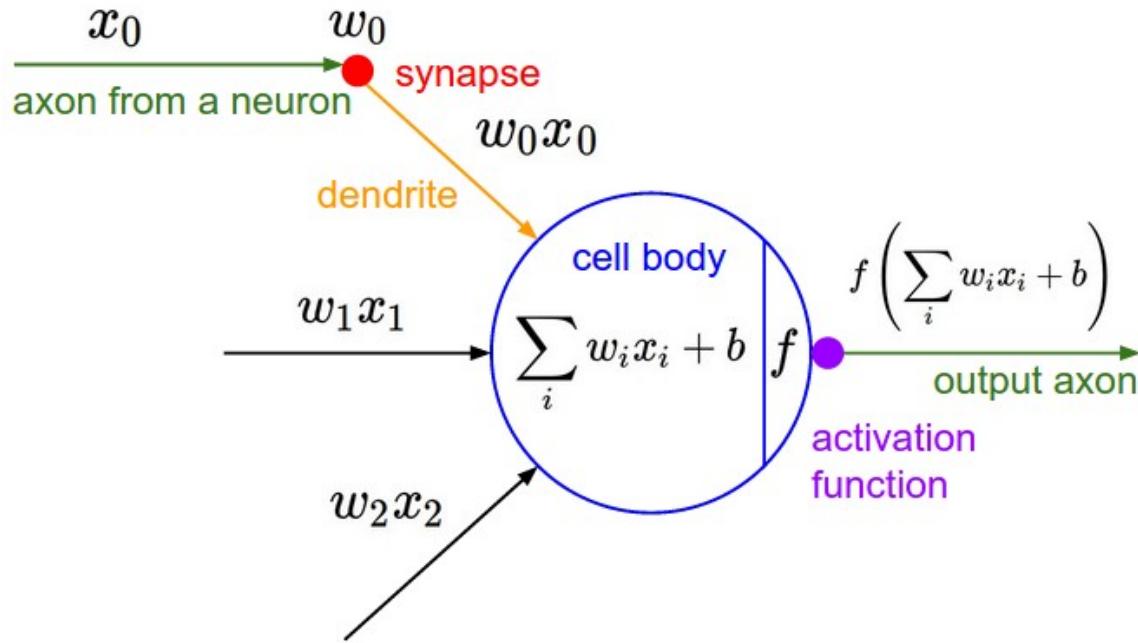
- Neural Networks belong to the class of error-based learning algorithms (like SVMs, etc.)
- First
  - We learn how to create a network (focus of this lecture)
- Then
  - How to train the network using error (next lecture).

# A Simple Neuron

## Description of a simple neuron



# A Simple Neuron



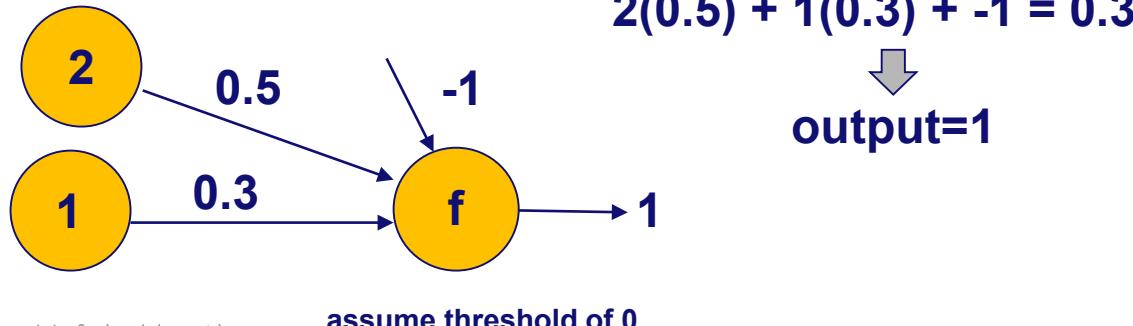
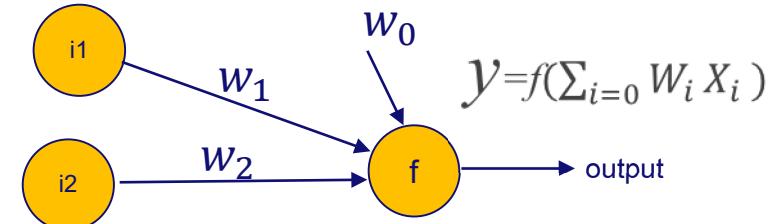
# A Simple Neuron

- Every simple neuron acts as an actual brain neuron
  - get input signals
    - Inputs
  - assign importance to each input
    - Weights
  - analyze all the incoming signals with respect to their importance
    - Cell body (summation of weighted inputs)
  - use a threshold to decide: fire or not
    - Activation function

# Simple Neuron Learning Process

## Perceptron Example

- Randomly assign weights (between 0-1)
- Present inputs from training data
- Get output
  - Nudge weights to get results toward our desired target output
  - Repeat; stop when no errors, or enough epochs completed



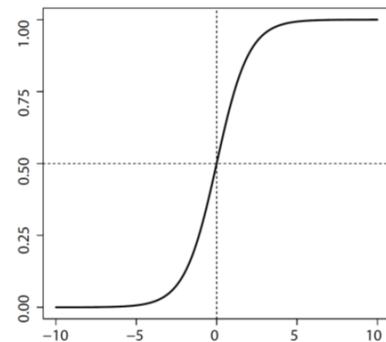
# How to use a perceptron network?

## Example

- Generally perceptron networks are used to learn how to make classifications
- For example
  - You have collected some data regarding the diagnosis of patients with heart disease
  - Age, Sex, Chest Pain Type, Resting BPS, Cholesterol, ..., Diagnosis (0/1))
    - 67,1,4,120,229,..., 1
    - 37,1,3,130,250,... ,0
    - 41,0,2,130,204,... ,0
  - Train network to predict heart disease of new patients

# Activation Function

- Neurons use a threshold to decide when to fire
  - In neural networks the sigmoid function (like in logistic regression) is commonly used as an activation function:



$$\text{sigmoid} = \frac{1}{1 + e^{-x}}$$

Remember: tends to go to 0 or 1.

- However, now for simplicity we use step function:

$$f(y) = \begin{cases} 0, & y < 0 \\ 1, & y \geq 0 \end{cases}$$



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# What is an artificial neuron doing when it learns?

## Logical OR example

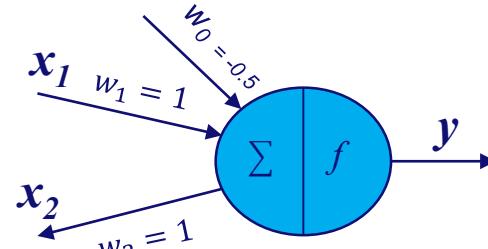
Logical OR function:

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| 0     | 0     | 0   |
| 0     | 1     | 1   |
| 1     | 0     | 1   |
| 1     | 1     | 1   |

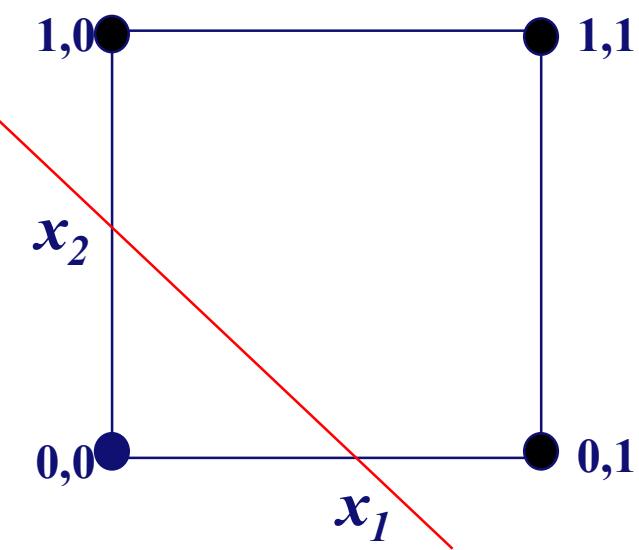
$$y = f(x_1, x_2)$$

$$1 * x_1 + 1 * x_2 - 0.5 = y : f(y) = \begin{cases} 0, & y < 0 \\ 1, & y \geq 0 \end{cases}$$

Simple Neural Network:



$$y = f(w_0 + w_1 x_1 + w_2 x_2)$$



# How neural networks are different?

## Logical XOR example

### Logical XOR function

| x1 | x2 | y |
|----|----|---|
| 0  | 0  | 0 |
| 0  | 1  | 1 |
| 1  | 0  | 1 |
| 1  | 1  | 0 |

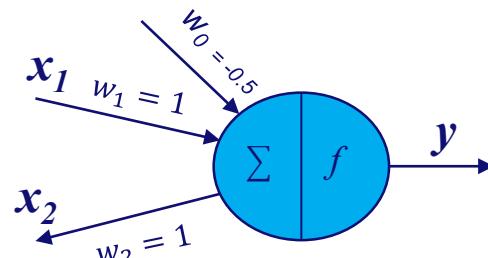
$$1 \quad \begin{cases} w_0 = -0.5 \\ w_1 = 1 \\ w_2 = 1 \end{cases}$$

$$1 * x_1 + 1 * x_2 - 0.5 = sum : f(sum) = \begin{cases} 0, & sum < 0 \\ 1, & sum \geq 0 \end{cases}$$

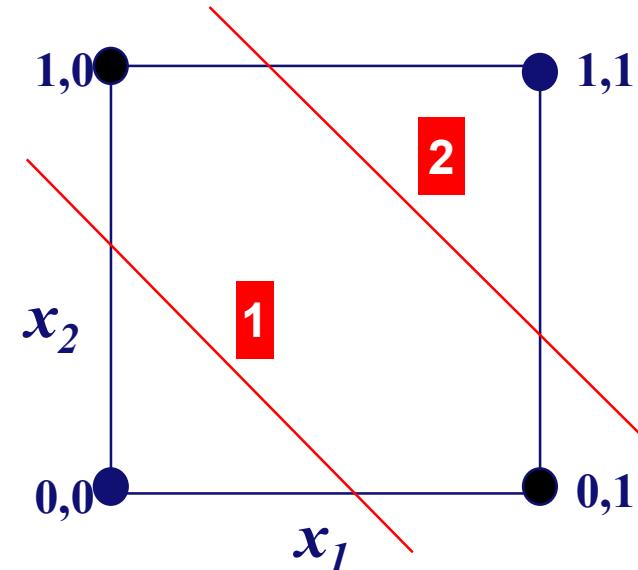
$$2 \quad \begin{cases} w_0 = -1.5 \\ w_1 = 1 \\ w_2 = 1 \end{cases}$$

$$1 * x_1 + 1 * x_2 - 1.5 = sum: f(sum) = \begin{cases} 0, & sum < 0 \\ 1, & sum \geq 0 \end{cases}$$

### Simple Neural Network:



$$y = f(w_0 + w_1 x_1 + w_2 x_2)$$



The simple Neural Network cannot produce proper classifications!

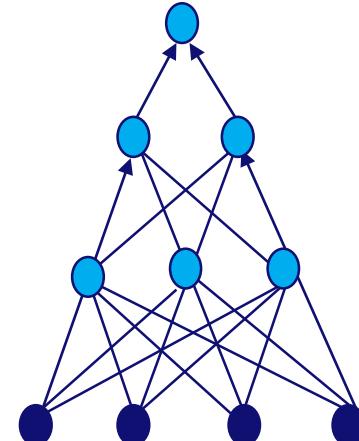
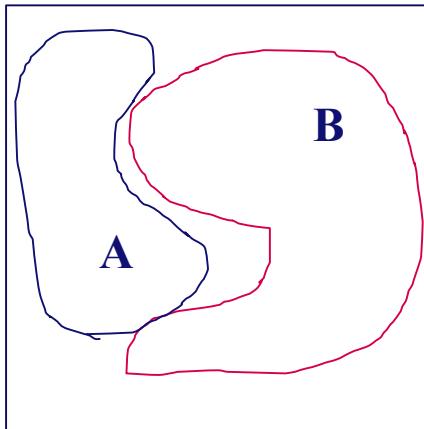
# Limitations of Simple Neural Networks

- **What is a Perceptron doing when it learns?**
  - A discrimination function (separating plane) is generated
  - Has the power to map input patterns to output class values
- **Limitations of the basic Perceptron**
  - Able to form only linear discriminate functions; i.e. classes which can be divided by a line or hyper-plane.
  - Most functions are more complex; i.e. they are non-linear or not linearly separable.

# Limitations of Simple Neural Networks

## Example

More difficult problems → More complex, multi-layer networks



# Feedforward Networks



# Different Topologies of Neural Networks

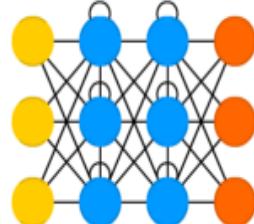
Feed Forward (FF)



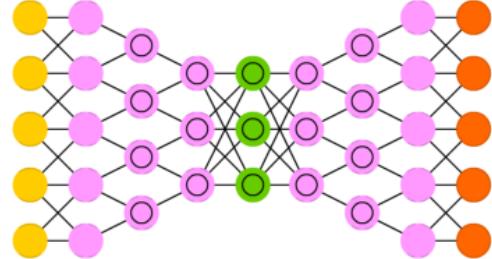
Deep Feed Forward (DFF)



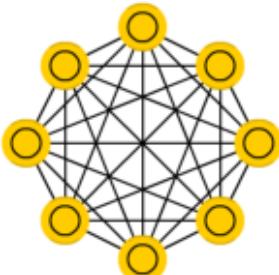
Recurrent Neural Network (RNN)



Deep Convolutional Inverse Graphics Network (DCIGN)



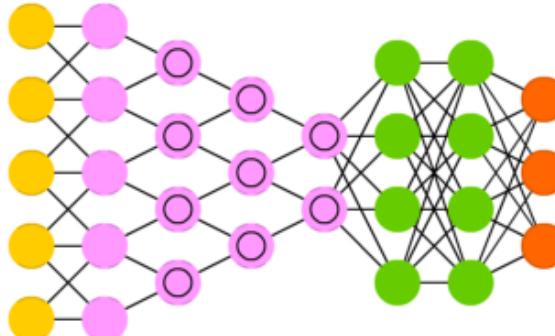
Hopfield Network (HN)



Markov Chain (MC)



Deep Convolutional Network (DCN)



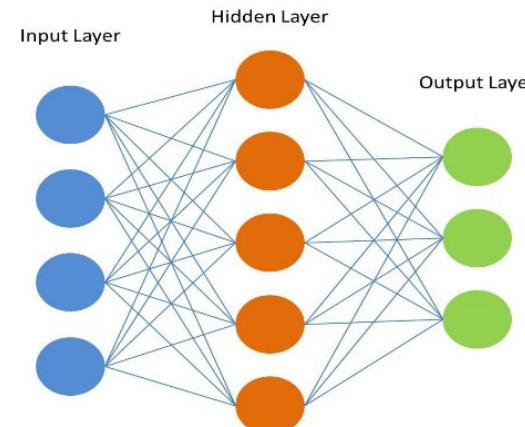
...

# Neural Networks in This Lecture

- There are different types of neural networks
- We are going to learn about the feedforward networks
  - and later about backpropagation algorithm for this type of networks
- Feedforward networks:
  - No loops
  - input → hidden layers → output

# Feedforward Neural Networks

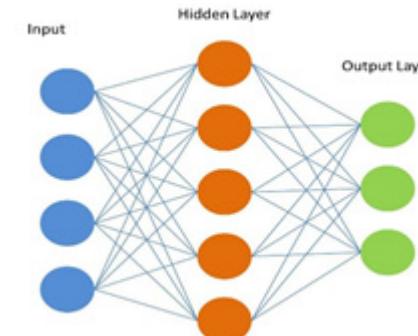
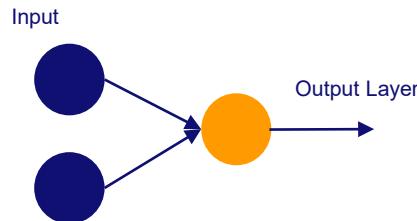
- Connection only to the next layer
- The weights of the connections (between two layers) can be changed
- Activation functions are used to calculate whether the neuron fires



# Feedforward Neural Networks

## Example

- Single-layer network:
  - Inputs
  - Output layer
- Two-layer network:
  - Inputs
  - Hidden layer
  - Output layer



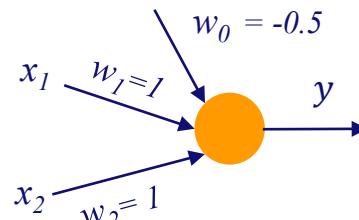
# Feedforward Neural Networks

## Example

### Single-Layer OR

Logical OR Function

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| 0     | 0     | 0   |
| 0     | 1     | 1   |
| 1     | 0     | 1   |
| 1     | 1     | 1   |



$$w_1x_1 + w_2x_2 + w_0 = \text{sum} : f(\text{sum}) = \begin{cases} 0, & \text{sum} < 0 \\ 1, & \text{sum} \geq 0 \end{cases}$$

$$x_1 + x_2 - 0.5 = \text{sum} : f(\text{sum}) = \begin{cases} 0, & \text{sum} < 0 \\ 1, & \text{sum} \geq 0 \end{cases}$$

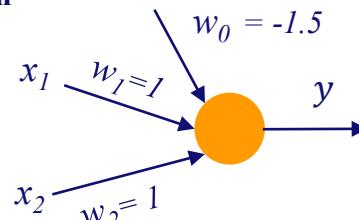
# Feedforward Neural Networks

## Example

### Single-Layer AND

Logical AND Function

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| 0     | 0     | 0   |
| 0     | 1     | 0   |
| 1     | 0     | 0   |
| 1     | 1     | 1   |



$$w_1 x_1 + w_2 x_2 + w_0 = \text{sum} : f(\text{sum}) = \begin{cases} 0, & \text{sum} < 0 \\ 1, & \text{sum} \geq 0 \end{cases}$$

$$x_1 + x_2 - 1.5 = \text{sum} : f(\text{sum}) = \begin{cases} 0, & \text{sum} < 0 \\ 1, & \text{sum} \geq 0 \end{cases}$$

# Feedforward Neural Networks

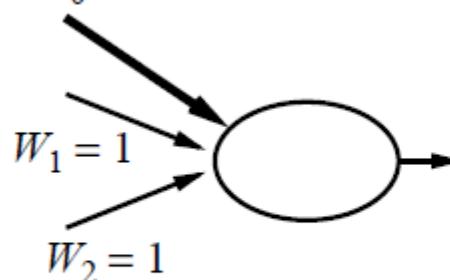
## Example

$$x_1 + x_2 - 1.5 = \text{sum} : f(\text{sum}) = \begin{cases} 0, & \text{sum} < 0 \\ 1, & \text{sum} \geq 0 \end{cases}$$

$$x_1 + x_2 - 0.5 = \text{sum} : f(\text{sum}) = \begin{cases} 0, & \text{sum} < 0 \\ 1, & \text{sum} \geq 0 \end{cases}$$

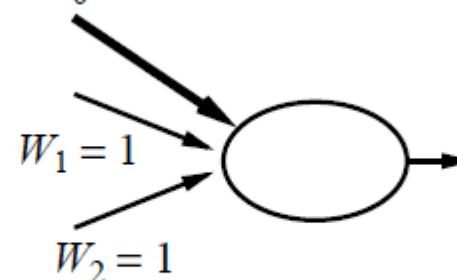
$$-x_1 + 0.5 = \text{sum} : f(\text{sum}) = \begin{cases} 0, & \text{sum} < 0 \\ 1, & \text{sum} \geq 0 \end{cases}$$

$$W_0 = -1.5$$



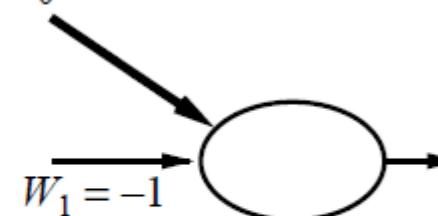
AND

$$W_0 = -0.5$$



OR

$$W_0 = 0.5$$



NOT

Every Boolean function can be implemented,  
... but not in one step.

# Feedforward Neural Networks

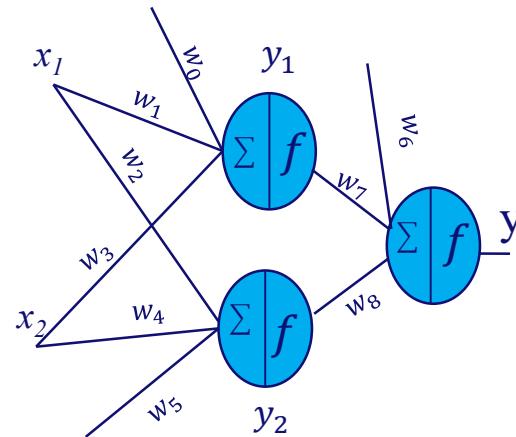
## Example (Solving XOR Problem )

Logical XOR function

| x1 | x2 | y |
|----|----|---|
| 0  | 0  | 0 |
| 0  | 1  | 1 |
| 1  | 0  | 1 |
| 1  | 1  | 0 |

$$f(x) = \begin{cases} 0, & x < 0 \\ 1, & x \geq 0 \end{cases}$$

Hidden layer of neurons



$$f(w_1 * x_1 + w_3 * x_2 + w_0) = y_1$$

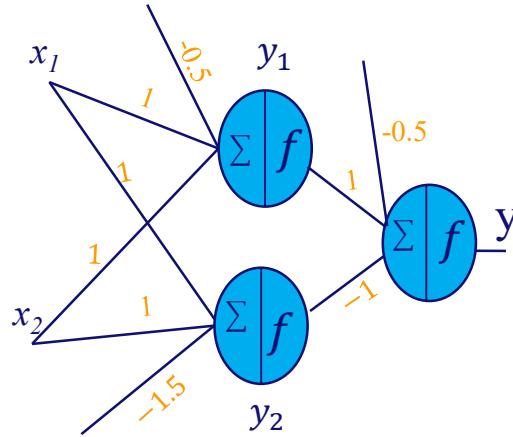
$$f(w_2 * x_1 + w_4 * x_2 + w_5) = y_2$$

$$f(w_7 * y_1 + w_8 * y_2 + w_6) = y$$

One more layer including two neurons is needed!  
Their combined results can produce proper classifications.

# Feedforward Neural Networks

## Example (Solving XOR Problem )

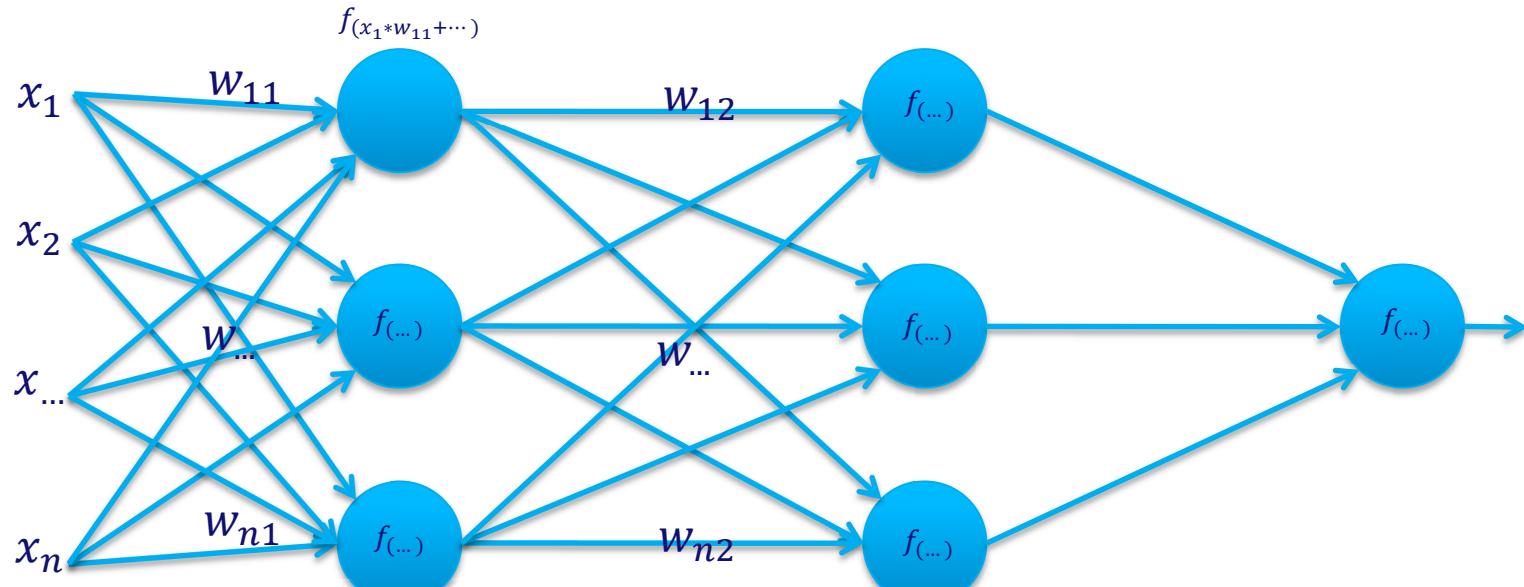


$$f(1 * x_1 + 1 * x_2 - 0.5) = y_1 \quad \text{“or”}$$
$$f(1 * x_1 + 1 * x_2 - 1.5) = y_2 \quad \text{“and”}$$
$$f(1 * y_1 - 1 * y_2 - 0.5) = y \quad \text{“and not”}$$

$$\begin{aligned} w_0 &= -0.5 \\ w_1 &= 1 \\ w_2 &= 1 \\ w_3 &= 1 \\ w_4 &= 1 \\ w_5 &= -1.5 \\ w_6 &= -1 \\ w_7 &= 1 \\ w_8 &= -0.5 \end{aligned}$$

$$f(x) = \begin{cases} 0, & x < 0 \\ 1, & x \geq 0 \end{cases}$$

# General Feedforward Network



# Sample Neural Network Model

## Two layer neural network

$$y_k(\mathbf{x}, \mathbf{w}) = f \left( \sum_{j=1}^M w_{kj}^{(2)} h \left( \sum_{i=1}^D w_{ji}^{(1)} x_i + w_{j0}^{(1)} \right) + w_{k0}^{(2)} \right)$$

Annotations:

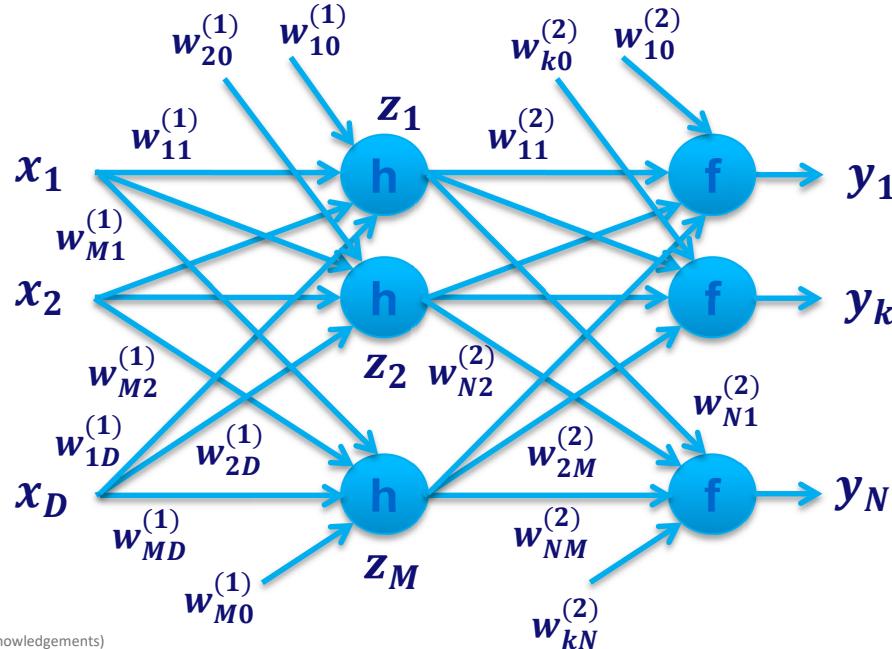
- A red arrow points to the term  $\sum_{j=1}^M w_{kj}^{(2)}$  with the label "linear combination".
- A red arrow points to the term  $\sum_{i=1}^D w_{ji}^{(1)} x_i$  with the label "D inputs".
- A red arrow points to the term  $w_{k0}^{(2)}$  with the label "Shows the element is in the first layer".

- $f$  and  $h$  are activation functions:
  - they can be different functions  
for simplicity imagine there is one  $h$  function for the hidden layer
- $w_{kj}$  shows the weight of the edge: from  $j$ th node of hidden layer to  $k$ th node of output layer
- $w_{ji}$  shows the weight of the edge: from  $i$ th element of input to  $j$ th node of hidden layer

# Sample Neural Network Model

## Two layer neural network

$$y_k(x, \mathbf{w}) = f \left( \sum_{j=1}^M w_{kj}^{(2)} h \left( \sum_{i=1}^D w_{ji}^{(1)} x_i + w_{j0}^{(1)} \right) + w_{k0}^{(2)} \right)$$



# General Feedforward Network

## Complete Two Layer Function

$$y_k(\mathbf{x}, \mathbf{w}) = f \left( \sum_{j=1}^M w_{kj}^{(2)} h \left( \sum_{i=1}^D w_{ji}^{(1)} x_i + w_{j0}^{(1)} \right) + w_{k0}^{(2)} \right)$$

- The hidden units with their activation functions can express non-linear functions
- The activation functions can be different at neurons

# When to Use Multilayer Perceptron?

In feedforward networks

- Comprised of one or more layers of neurons
- Data is fed to the input layer
- One or more hidden layers
  - Increase level of abstraction
- Prediction based on output layer
- Suitable for
  - Classification prediction problems
    - With labeled inputs
  - Regression prediction problems
    - A real-valued quantity is predicted given a set of inputs.

# When to Use Multilayer Perceptron?

In feedforward networks

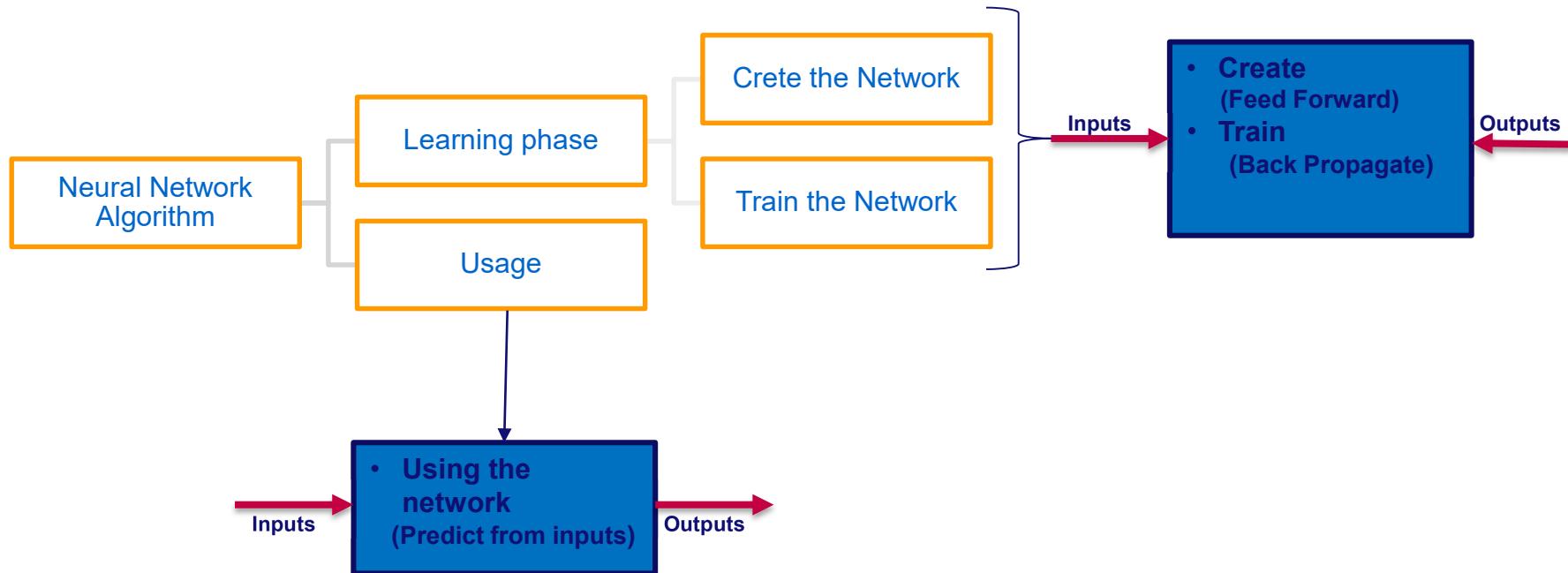
- Can be applied to different types of data
  - Text data
  - Time series data
  - Image data
    - Pixels of an image reduce to a row of data
  - Words of a document
    - Reduce to a row of data

# General View of a Neural Network

- You have already learned how to create a feedforward Network
- The next step is how to train your network using error-based back-propagation approach

# General View of a Neural Network

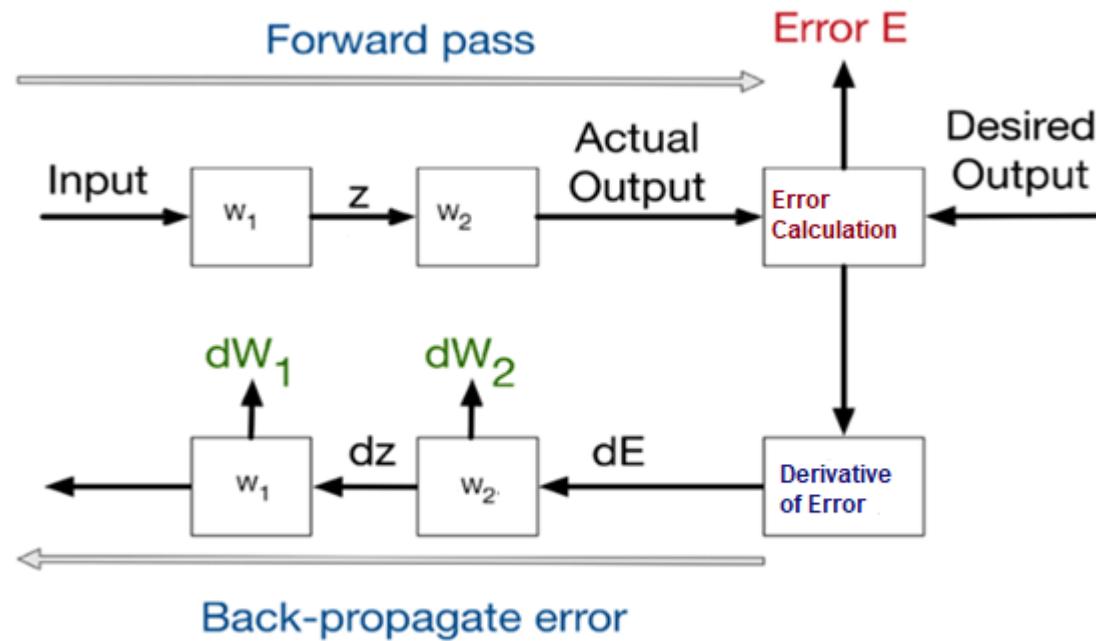
## Training and Using



# Next Lecture :

## How a Neural Network Learns?

### Training algorithm (Backpropagation)



# Conclusion

# Lecture Summary

- How to deal with non-linear problems
- A complete Neural Network elements:
  - A set of nodes (neurons)
  - A set of weight representing between each layer
  - Output and hidden layers
  - An activation function
- Network architecture
- How to build a network
- Possible usage of a simple and multilayer networks
- How to train a neural network? (Next Lecture)

| #                    | Lecture   | date              | day           |
|----------------------|---|-------------------|---------------|
|                      | <b>Lecture 1</b> Introduction                               | 10/10/2018        | Wednesday     |
|                      | <b>Lecture 2</b> Crash Course in Python                     | 11/10/2018        | Thursday      |
| <i>Instruction 1</i> | <i>Python</i>   | <i>12/10/2018</i> | <i>Friday</i> |
|                      | <b>Lecture 3</b> Basic data visualisation/exploration       | 17/10/2018        | Wednesday     |
|                      | <b>Lecture 4</b> Decision trees                             | 18/10/2018        | Thursday      |
| <i>Instruction 2</i> | <i>Decision trees and data visualization/exploration</i>    | <i>19/10/2018</i> | <i>Friday</i> |
|                      | <b>Lecture 5</b> Regression                                 | 24/10/2018        | Wednesday     |
|                      | <b>Lecture 6</b> Support vector machines                    | 25/10/2018        | Thursday      |
| <i>Instruction 3</i> | <i>Regression and support vector machines</i>               | <i>26/10/2018</i> | <i>Friday</i> |
|                      | <b>Lecture 7</b> Neural networks (1/2)                      | 31/10/2018        | Wednesday     |
| <i>Instruction 4</i> | <i>Neural networks and supervised learning</i>              | <i>02/11/2018</i> | <i>Friday</i> |
|                      | <b>Lecture 8</b> Neural networks (2/2)                      | 07/11/2018        | Wednesday     |
|                      | <b>Lecture 9</b> Evaluation of supervised learning problems | 08/11/2018        | Thursday      |
| <i>Instruction 5</i> | <i>Neural networks and supervised learning</i>              | <i>09/11/2018</i> | <i>Friday</i> |
|                      | <b>Lecture 10</b> Clustering                                | 14/11/2018        | Wednesday     |

|             |   |   |                   |               |
|-------------|---|---|-------------------|---------------|
|             | <b>Lecture 7</b> Neural networks (1/2)                      | 31/10/2018  | Wednesday         |               |
| <i>Inst</i> | <i>Instruction 4</i>  | <i>Neural networks and supervised learning</i>            | <i>02/11/2018</i> | <i>Friday</i> |
| <i>Inst</i> | <b>Lecture 8</b> Neural networks (2/2)                      | 07/11/2018  | Wednesday         |               |
| <i>Inst</i> | <b>Lecture 9</b> Evaluation of supervised learning problems | 08/11/2018  | Thursday          |               |
| <i>Inst</i> | <i>Instruction 5</i>  | <i>Neural networks and supervised learning</i>            | <i>09/11/2018</i> | <i>Friday</i> |
| <i>Inst</i> | <b>Lecture 10</b> Clustering                                | 14/11/2018  | Wednesday         |               |
| <i>Inst</i> | <b>Lecture 11</b> Frequent items sets                       | 15/11/2018  | Thursday          |               |
| <i>Inst</i> | <b>Lecture 12</b> Association rules                         | 21/11/2018  | Wednesday         |               |
| <i>Inst</i> | <b>Lecture 13</b> Sequence mining                           | 22/11/2018  | Thursday          |               |
| <i>Inst</i> | <i>Instruction 6</i>  | <i>Clustering, frequent items sets, association rules</i> | <i>23/11/2018</i> | <i>Friday</i> |

|                       |                        |            |           |
|-----------------------|------------------------|------------|-----------|
| <i>Instruction 12</i> | Example exam questions | 25/01/2018 | Friday    |
| backup                |                        | 30/01/2019 | Wednesday |
| backup                |                        | 31/01/2019 | Thursday  |
| extra                 | Question hour          | 01/02/2019 | Friday    |