

KEPLER-91b IS A GIANT LOW-DENSITY PLANET ORBITING A GIANT LOW-DENSITY STAR

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Abstract

Kepler-91b was detected using data from the Kepler spacecraft and its planetary nature was confirmed through analysis of the light curve. Recently these data have been reanalyzed and questions have been raised as to whether a planet actually orbits Kepler-91. We simultaneously modeled the Kepler data and ground-based radial velocity observations from the Hobby-Eberly Telescope and find that Kepler-91b is unambiguously a planet orbiting a red giant host star. The star exhibits temporally correlated noise which we model as a Gaussian process. It is this noise component that we hypothesize led previous studies to suspect Kepler-91b as a false positive. This work validates the conclusions presented in the discovery paper that Kepler-91b is a $0.73 \pm 13 M_{Jup}$ planet.

Subject headings: planetary systems; stars: individual (Kepler-91, KIC 8219268, KOI-2133); techniques: photometric, radial velocities; methods: data analysis, statistical

1. INTRODUCTION

The first discovered exoplanets were Jupiter-sized (Campbell et al. 1988) and most orbited just a few stellar radii from their host star (Mayor & Queloz 1995; Marcy & Butler 1996). This was a milestone moment that unambiguously demonstrated that planetary systems need not resemble our own. While data from the Kepler spacecraft has revealed planetary systems come in many flavors (e.g. Lissauer et al. 2011; Carter et al. 2012; Barclay et al. 2013), hot Jupiter's remain a key area of interest because the large size of these planet and their short orbital periods yield the highest signal to noise light curve data with which otherwise undetectable effects can be observed. Examples of this include the detection of inhomogeneous clouds (Demory et al. 2013) and the determination of planet masses from Doppler boosting (Shporer et al. 2011; Barclay et al. 2012).

Kepler-91 was given the designation in the Kepler Input Catalog (KIC) 8219268 (Brown et al. 2011). The star was observed for the entire four year duration of the Kepler mission in long cadence mode. It was shown to display solar-like oscillations from which stellar mass of $1.3 M_{\odot}$ and radius of $6.3 R_{\odot}$ was derived, indicating this is a K-type giant with a density of 0.0073 g cc^{-3} (Huber et al. 2013a; Lillo-Box et al. 2014).

A transiting planet candidate with an orbital period of 6.3 days was detected by the Kepler team and assigned Kepler Object of Interest (KOI) number 2133.01 (Batalha et al. 2013). Lillo-Box et al. (2014) confirmed the planetary nature of the apparently transiting body. However, the status of this planet has recently been called into question by both Esteves et al. (2013), who

TABLE 1
 STELLAR PROPERTIES ADOPTED FROM LILLO-BOX ET AL. (2014)

Property	Adopted value
Effective temperature, T_{eff} (K)	4550 ± 75
Metallicity, $[\text{Fe}/\text{H}]$ (dex)	0.11 ± 0.07
Mean stellar density, ρ (g/cc)	0.0073 ± 0.0001
Surface gravity, $\log g$ (dex, cgs)	2.953 ± 0.007
Stellar mass, M_{\star} (M_{\odot})	1.31 ± 0.10
Stellar radius, R_{\star} (R_{\odot})	6.30 ± 0.16

use phase variations to deduce that the occulting body is self-luminous, and Sliski & Kipping (2014) who find that the stellar density derived from a transit model differs significantly from the density calculated using asteroseismic techniques. In this paper we present the results of a light curve model combined with radial velocity observations obtained from the ground and find that the transit-signal is unambiguously caused by a Jupiter-sized planet orbiting the red giant target star.

2. OBSERVATIONAL DATA USED IN THIS STUDY

2.1. Stellar properties

Solar-like oscillations were detected in the Kepler time series data of Kepler-91 (Huber et al. 2013a). By combining these observations with a temperature and metallicity derived from optical spectroscopy, it was determined that Kepler-91b was unambiguously a giant star. Lillo-Box et al. (2014) performed a more detailed asteroseismic analysis by fitting individual frequencies. The stellar properties adopted in this paper from Lillo-Box et al. are reported in Table 1.

2.2. Kepler data

In this work we utilize the full set of Kepler long cadence (29.4-min) observation from the Kepler spacecraft obtained over 4 years. These data consist of 17 observational Quarters (Q1–Q17) where all but the first and last Quarter consist of around 90 days of near continuous data. Q1 lasted 40 days and Q17 consists of 31 days of data after which Kepler suffered the failure of a reaction wheel.

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TABLE 2
RADIAL VELOCITIES

Time (BJD-2454833)	Velocity ^a (m/s)	Uncertainty (m/s)
1208.86670891	113.92	4.31
1266.71041653	21.31	17.52
1267.70865078	-24.61	19.74
1268.70698350	-45.59	16.88
1271.68968502	67.27	18.45
1275.69264679	-25.59	25.04
1300.86443801	-9.10	27.11
1358.70858740	96.36	18.44
1382.63282948	0.00	14.93

^athe values presented here have had an arbitrary offset subtracted to enforce a median of zero

We use data that has undergone Presearch Data Conditioning (Stumpe et al. 2012; Smith et al. 2012) using the multi scale maximum a priori (MS-MAP) method (Stumpe et al. 2014). This preprocessing removes signals related to the spacecraft while retaining variability of an astrophysical origin.

2.3. Radial velocity data

We obtained precise radial velocity measurements using the High-Resolution-Spectrograph (HRS) (Tull 1998) instrumental setup for Kepler follow-up observations and data reduction algorithms as described in Endl et al. (2011). Nine spectra were obtained using an iodine (I_2) cell. The data have a resolving power of $R = \lambda/\delta\lambda = 30,000$ and were sky background subtracted. We also obtained two template spectra (without the I_2 cell) of Kepler-91, one at $R = 30,000$ and a second spectrum with $R = 60,000$. The second template yielded better RV precision and the RV data reported here were obtained using this template.

We also measured bisectors and bisector velocity spans (BVS) for the 9 spectra used for the RV computation. We measured the bisector and BVS of the cross-correlation-function (CCF) for 11 orders that do not contain significant I_2 lines. We cross-correlated each spectrum with the $R = 30,000$ template to search for variability of the BVS that could indicate a false positive and computed the BVS as the velocity difference of 2 arbitrary points on the CCF bisector at flux values of 0.4 and 0.84, following Hatzes et al. (1998). The BVS results are displayed in Figure 1. Excluding the poor quality measurement from the lowest S/N spectrum, the remaining data have a total rms-scatter of 15 m s^{-1} with a mean uncertainty of 35 m s^{-1} . The BVS results are consistent with no variability and they also do not correlate with either the orbital phase or the RV measurements.

3. SIMULTANEOUS MODELING OF KEPLER AND RV DATA

To provide a self-consistent model of both the light curve and the radial velocity observations we chose to model both datasets simultaneously using the orbital model described in Rowe et al. (2014).

Significant planet-induced variability outside of the transit of Kepler-91b has been noted in previous work (Lillo-Box et al. 2014; Esteves et al. 2013). We chose to model these light curve variations rather than remove them via filtering. We include 5 physical components in our model of the light curve: a transit, an occultation,

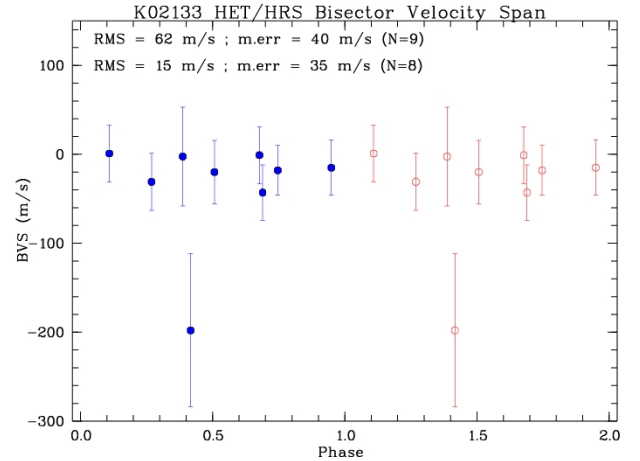


FIG. 1.— The bisector velocity spans of the nine HET observations of Kepler-91. There is a single outlier point which has a very large uncertainty. Excluding this leaves an rms scatter in the bisector velocity spans of 15 m/s. There is not obvious correlation with orbital phase.

ellipsoidal modulation, Doppler boosting and reflection from the planet. We additionally include the radial velocity data as an additional component in the model and finally we include a model for the correlated noise.

3.1. Parameterization

We used a limb darkened transit model (Mandel & Agol 2002) following a quadratic limb darkening law, and a uniform disk model for the occultation. The ellipsoidal variations, Doppler boosting and reflection off the planet were modeled in the manner described by Lillo-Box et al. (2014), but we parameterized the Doppler beaming in terms of K , the radial velocity semi-amplitude, to retain a consistent solution between the light curve data and the spectroscopic radial velocities. The scaling between the radial velocity semi-amplitude and the Doppler beaming amplitude is proportional to a ‘beaming factor’ B such that

$$A_b = B \frac{K}{c} (e \cos \omega) \quad (1)$$

where A_b is the semi-amplitude of the Doppler beaming signal c is the speed of light and e is the eccentricity and ω is the argument of periastron. We calculated B in the manner described by ? to find a value of 5.46 which we kept fixed.

We parameterized the combined model in terms of ρ the mean stellar density, zp a photometric zero point nuisance parameter, linear (γ_1) and quadratic (γ_2) limb darkening coefficients, T_0 the mid-point of transit, P the orbital period of the planet, b the impact parameter, R_p/R_\star the planet-to-star radius ratio, eccentricity vectors $e \cos \omega$ and $e \sin \omega$ where e is eccentricity and ω is the argument of periastron, the amplitude of the ellipsoid variations A_e , the amplitude of the reflection from the planet A_r , the occultation depth F_e , radial velocity semi-amplitude K , and V a radial velocity zero-point.

Because we are using disparate data sets it is useful to include a parameter for both the light curve and radial velocity data that is an additional noise term which is added in quadrature with the formal uncertainty (σ_{lc} and σ_{rv}). These account for missing physics on our model in addition to dealing with underestimation of the reported

TABLE 3
MODEL PARAMETERS

Property	Prior
ρ	$N(0.0073; 0.0001)$
zp	$U(-\infty; +\infty)$
γ_1	$N(0.67; 0.6)$
γ_2	$N(0.09; 0.6)$
T_0	$U(-\infty; +\infty)$
P	$U(-\infty; +\infty)$
b	$U(0; 1 + R_p/R_\star)$
R_p/R_\star	$U(0; 1)$
$e \cos \omega$	$U(-1; 1)$
$e \sin \omega$	$U(-1; 1)$
A_e	$U(-\infty; +\infty)$
A_r	$U(-\infty; +\infty)$
F_e	$U(-\infty; +\infty)$
V	$U(-\infty; +\infty)$
K	$U(-\infty; +\infty)$
σ_{lc}	$U(0; +\infty)$
σ_{rv}	$U(0; +\infty)$
A_{GP}	$U(0; +\infty)$
l_{GP}	$U(0; +\infty)$

uncertainties. This creates a flexible model that enables us to scale the two data sets appropriately.

3.2. Gaussian Process noise model

After examining the PDC data we noted the presence of a broad low frequency noise component in the time series. Red giants are known to show granulation (cite) to which we attribute the low frequency noise component. Not accounting for this correlated noise component can bias the observed planet parameters (Carter & Winn 2009). Huber et al. (2013b) have shown this type of noise is *can* be modeled by a two component (pink) noise model: a white Gaussian noise and a red noise component.

We opted to model the noise using squared exponential Gaussian Process... **Dan FM to write GP section. I've called the GP components A_{GP} and l_{GP} , lets think of better symbols for these.** is the lag in days?? cite this guy: Ambikasaran et al. (2014)

3.3. Priors

Priors on our model parameters are shown in Table 3. On particular note is ρ where we enforce a normal prior constrained from the probability density found from asteroseismology. We enforce a $1/e$ prior because without this our parameterization in terms of $e \sin \omega$ and $e \cos \omega$ would bias e high (cite Eastman). We use a normal prior on limb darkening with the expectation obtained through interpolation of model limb darkening in the Kepler bandpass with T_{eff} , $\log g$ and $[Fe/H]$ fixed at the values shown in Table 3, and with a standard deviation of 0.1. Finally, we set a number of prior constraints on linear combinations of γ_1 and γ_2 that prevent them taking unphysical values (Burke et al. 2008).

3.4. Markov-Chain Monte Carlo modeling

We numerically integrated the posterior probability using an efficient affine invariant Markov-Chain Monte Carlo (MCMC) algorithm (Goodman & Weare 2010; Foreman-Mackey et al. 2013). This method utilizes many walkers to reduce autocorrelation time; we opted to use 700 walkers each taking 15,000 steps for a total of

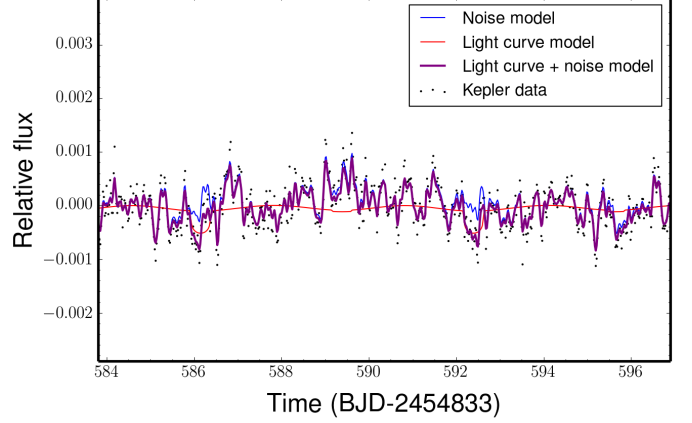


FIG. 2.— A small section of the observed Kepler data shown to demonstrate our noise model. The observed data is shown as black points, the noise model in blue, the light curve model in red and the combined light curve and noise model in purple. Two transit are shown in plot.

10.5×10^6 samples of the posterior probability. However, we toss the first 5,000 samples in each walker as burn-in which leaves 7×10^6 samples use to calculate posterior distributions.

In Figure ?? we show two transits in Kepler data, the mean noise model, light curve model and the combined light curve and noise model. The noise model does a good job of matching red noise component of the noise.

4. RESULTS

We were able to produce a self consistent model that well described the data. Parameters from the modeling are reported in Table 4, we give the median and central 68% bounds of the marginalized posterior distribution for each parameter. In addition we state the most probably model we sampled which provides a self consistent set of parameters. Our parameter estimates are largely consistent with Lillo-Box et al. (2014). While we obtain a slightly lower estimate for R_p/R_\star , we are still consistent with Lillo-Box et al. (2014) at the level of $<1.5\sigma$. Our estimate of R_p/R_\star is inconsistent with that found by Sliski & Kipping (2014).

We derive a planet mass of $0.73 \pm 13 M_{Jup}$ which, combined with a planet radius of $1.308^{+0.061}_{-0.074} R_{Jup}$ yields a density of $0.40^{+0.10}_{-0.09} \text{ g cm}^3$ implying that Kepler-91b is somewhat inflated. Specifically, we highlight the consistency between the planet mass we obtain with radial velocity observations and the mass Lillo-Box et al. (2014) obtains from the phase alone. Kepler-91b is one of a growing number of examples showing that hot Jupiter densities can be estimated from Kepler data alone (?Barclay et al. 2012; ?).

Lillo-Box et al. (2014) suggest that Kepler-91b may be on an eccentric orbit. In Figure ?? we show our posterior distribution for eccentricity derived from our $e \sin \omega$ and $e \cos \omega$ samples. While the data prefers an eccentric model, a circular orbit is not formally ruled out.

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5. DISCUSSION

We obtained good fits to both the radial velocity and light curve data with our model. The radial velocity observations phase well with the orbital period defined

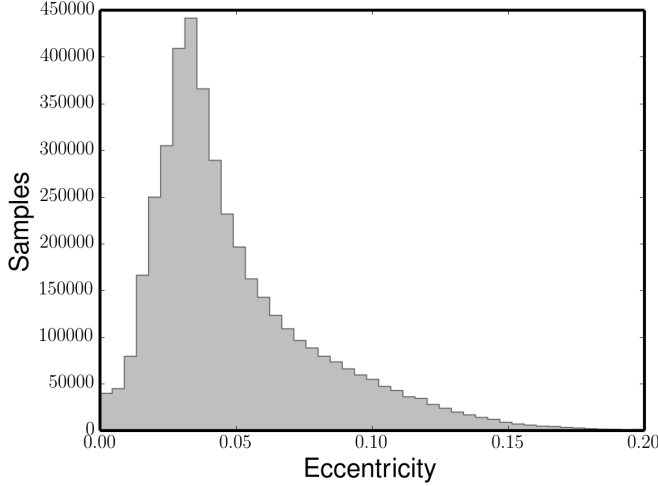


FIG. 3.— The posterior distribution for orbital eccentricity for Kepler-91b. While a slightly eccentric orbit is preferred by the data, we cannot rule out a circular orbit model.

TABLE 4

SUMMARY OF POSTERIOR PROBABILITIES FROM THE MCMC MODELING. PARAMETERS BELOW THE LINE BREAK ARE DERIVED FROM THE PARAMETERS SAMPLED BY THE MODEL

Parameter	Best fit	Median	84.1%	15.9%
ρ (g/cc)	0.00724	0.00730	+0.00010	-0.00010
zp (ppm)	-56.8	-57.5	+7.4	-8.8
γ_1	0.43	0.50	+0.48	-0.35
γ_2	0.27	0.19	+0.37	-0.49
T_0 (BKJD ^a)	136.3837	136.3824	+0.0043	-0.0042
P (days)	6.246696	6.246716	+0.000034	-0.000034
b	0.865	0.863	+0.011	-0.015
R_p/R_\star	0.0212	0.0213	+0.0011	-0.0008
$e \cos \omega$	0.0134	0.0234	+0.0086	-0.0086
$e \sin \omega$	0.0118	0.0176	+0.054	-0.036
A_e (ppm)	50.8	51.5	+4.8	-5.0
A_r (ppm)	27.4	29	+21	-16
F_e (ppm)	49	39	+15	-15
V (m/s)	15.6	16.5	+8.2	-8.0
K (m/s)	70	67	+11	-11
σ_{lc} (ppm)	0.6	1.3	+1.4	-0.9
σ_{rv} (m/s)	8.3	11	+12	-8
A_{GP} (ppm)	301.6	301.2	+2.0	-2.0
l_{GP} (days ²)	0.03717	0.03711	+0.00031	-0.00030
R_p (R_{Jup})	1.300	1.308	+0.061	-0.074
M_p (M_{Jup})	0.76	0.73	+0.13	-0.13
a/R_\star	2.463	2.469	+0.011	-0.011
A_g	0.66	0.52	+0.22	-0.20
e	0.018	0.040	+0.040	-0.016
i (deg)	69.17	69.12	+0.58	-0.88
ρ_p (g/cc)	0.43	0.40	+0.10	-0.09

^aBKJD is the time system used by Kepler and is defined by Barycentric Julian Date (BJD) - 2454833

by the transit and therefore almost certainly are caused by a reflex motion of the star that the planet orbits. The transit model fits the data well with low eccentricity. If the density constraint from asteroseismology were to be bad prior we would need a model with high eccentricity, which is not seen. The mass we derive is consistent with a planetary body. We therefore conclude Kepler-91b is unambiguously a planet.

This leads us to try to answer the question, what caused this to be classified as a false positive? We begin

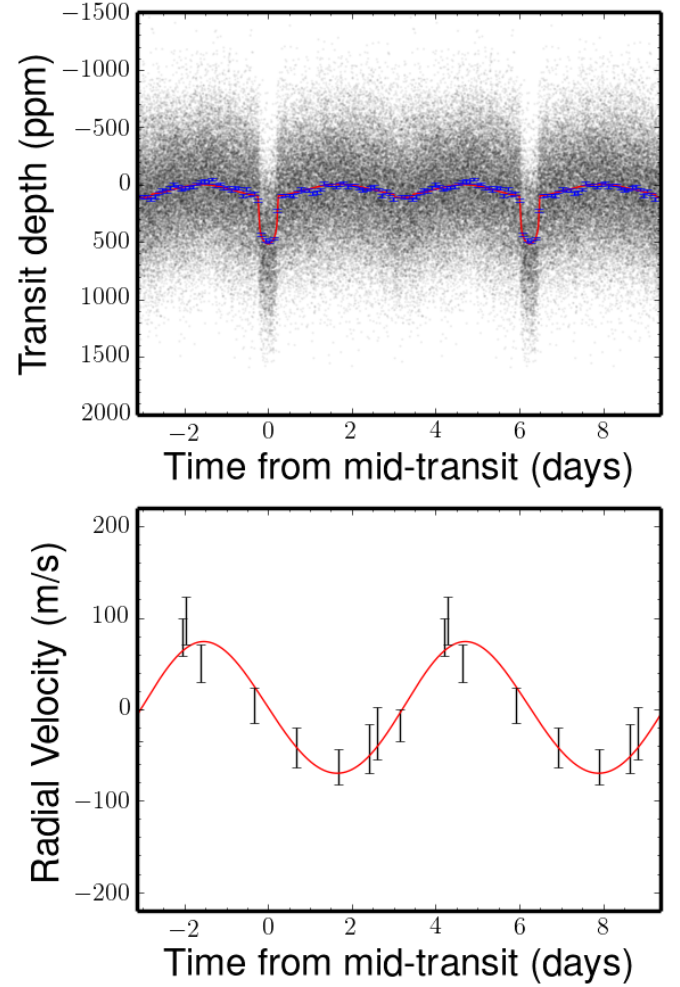


FIG. 4.— The upper panel shows the observed data as black semi-transparent points. The blue points show are binned observed data with 1000 observed points included per bin. The red curve is the best fitting light curve model, excluding the noise model. The data have been folded on the orbital period of the planet and repeated twice to fully show the entire phase curve. The fit to the data does not appear especially good. However, in this figure we have not included the Gaussian Process noise model. The large scatter is owing to correlated noise in the observe data. The lower panel shows our observed radial velocity data in blue and the best fitting model in red.

by considering the work of Esteves et al. (2013) who conclude that Kepler-91b is false positive based on a phase curve fit where they find a night-side temperature inconsistent with a body that is not self luminous. We do not draw the same conclusions. Using the same equation as Esteves et al for geometric albedo, we derived a value of $0.52^{+0.22}_{-0.20}$ compared with $2.49^{+0.55}_{-0.60}$ from Esteves et al.. We hypothesize that the disparate parameter estimates arises from using different detrending techniques. Specifically we point to their use of a median filter which could result in the significantly smaller transit depth than we measure. The method we use to calculate the geometric albedo (and we presume Esteves et al. use also) is

$$A_g = F_e \left(\frac{a}{R_p} \right)^2 = F_e \left(\frac{a}{R_\star} \frac{R_\star}{R_p} \right)^2. \quad (2)$$

Therefore, underestimating R_p/R_\star will overestimate the

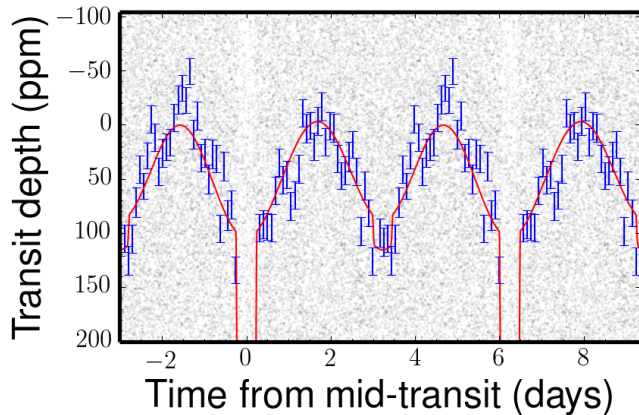


FIG. 5.— This plot shows the phase variations from Kepler-91b. Is it the same data as shown in the upper panel of Figure 4 but only showing the phase variations and the occultation. Similarly to in Figure 4, the correlated noise in the data implies a misleadingly poor fit of the model to the data.

albedo A_g . We caution that it is only because we were in possession of the radial velocity data, which raised doubts on the interpretation of Esteves et al., that we considered the more sophisticated noise model described here. We suggest that extreme caution should be used in deriving planet parameters where the host star is noisy on timescales comparable to the transit duration.

Sliski & Kipping (2014) only include data less than three transit durations from a transit and fit a standard transit model ignoring the out-of-transit ellipsoidal variations. They find that the mean stellar density derived purely from a transit model is not consistent with the asteroseismic density of the star. We suspect that Sliski & Kipping find a higher stellar density because they neglected to include phase variations, particularly the high amplitude ellipsoidal variations found by Lillo-Box et al. (2014). The density parameter is sensitive to the duration of the transit, we hypothesize that not including out-of-transit variations caused an underestimate of the transit duration. This theory is strengthened because they report a significantly smaller planet-to-star radius ratio than we find. We caution against using just a short amount of data on either side of the transit as correctly estimating the out-of-transit flux level is essential to estimating the planet properties.

6. CONCLUSIONS

We combined Kepler data presented in previous studies of Kepler-91 with radial velocity data obtained from the Hobby-Eberly Telescope. We find that these data can be fit in a self consistent manner and the results lead us to conclude that Kepler-91b is a planet, validating the work of Lillo-Box et al. (2014). We hypothesize that recent work claiming this as a false positive erred owing to the challenge of modeling a star with a strong correlated noise component and relatively high amplitude out-of-transit variations. We use a Gaussian Process to model the correlated noise present in the light curve of this red giant star. Our choice of the squared exponential kernel...

lets say how clever we are for using a GP...

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