

$$\begin{aligned}
\frac{\partial^2 U}{\partial r^2} = & \frac{r\sqrt{r^2 \sin^2(\theta)} \sin(\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} - \frac{2r\sqrt{r^2 \sin^2(\theta)} \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} + \frac{\sqrt{r^2 \sin^2(\theta)} \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} + \\
& \cos^2(\theta) \frac{\partial^2}{\partial r^2} U(r, \theta, \phi) + \frac{\sin^2(\theta) \frac{\partial^2}{\partial \theta^2} U(r, \theta, \phi)}{r^2} + \frac{\sin(2\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{2r^2}
\end{aligned}$$

$$\begin{aligned}
\frac{\partial^2 U}{\partial y^2} = & \frac{r^3 \sin^2(\theta) \cos^2(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{\sqrt{r^2 \sin^2(\theta)} (r^2)^{\frac{3}{2}}} + \frac{r^3 \sin(\theta) \cos^2(\phi) \cos^2(\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{\sqrt{r^2 \sin^2(\theta)} (r^2)^{\frac{3}{2}}} + \frac{r^3 \sin^4(\theta) \cos^2(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{(r^2 \sin^2(\theta))^{\frac{3}{2}} \sqrt{r^2}} - \\
& \frac{r^2 \sin(\phi) \cos(\phi) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} - \frac{r^2 \cos^2(\phi) \frac{\partial}{\partial r} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} + \frac{r^2 \frac{\partial}{\partial r} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} - \frac{r^2 \sin^4(\theta) \cos^2(\phi) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{(r^2 \sin^2(\theta))^{\frac{3}{2}} \sqrt{r^2}} + \\
& \sin^2(\theta) \cos^2(\phi) \frac{\partial^2}{\partial r^2} U(r, \theta, \phi) - \frac{\sin(\phi) \cos(\phi) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{\sqrt{r^2}} + \frac{2 \sin(\phi) \cos(\phi) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{-2r^2 \cos^2(\theta) + 2r^2} - \\
& \frac{2 \cos^2(\phi) \frac{\partial^2}{\partial \phi^2} U(r, \theta, \phi)}{-2r^2 \cos^2(\theta) + 2r^2} + \frac{2 \frac{\partial^2}{\partial \phi^2} U(r, \theta, \phi)}{-2r^2 \cos^2(\theta) + 2r^2} + \frac{\sin(\phi) \cos(\phi) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2}} - \frac{\sqrt{2} \sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r \sqrt{-2r^2 \cos^2(\theta) + 2r^2}} - \\
& \frac{\sqrt{2} \cos^2(\phi) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r \sqrt{-2r^2 \cos^2(\theta) + 2r^2}} + \frac{\sqrt{2} \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r \sqrt{-2r^2 \cos^2(\theta) + 2r^2}} - \frac{\sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2 \sin^2(\theta)}} + \\
& \frac{\sin(\phi) \cos(\phi) \cos^2(\theta) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2 \sin^2(\theta)} \sin(\theta)} - \frac{\sin(\theta) \cos^2(\phi) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^2} + \frac{\cos^2(\phi) \cos^2(\theta) \frac{\partial^2}{\partial \theta^2} U(r, \theta, \phi)}{r^2}
\end{aligned}$$

$$\begin{aligned}
\frac{\partial^2 U}{\partial z^2} = & \frac{r^3 \sin^2(\phi) \sin^2(\theta) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{\sqrt{r^2 \sin^2(\theta)} (r^2)^{\frac{3}{2}}} + \frac{r^3 \sin^2(\phi) \sin(\theta) \cos^2(\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{\sqrt{r^2 \sin^2(\theta)} (r^2)^{\frac{3}{2}}} + \frac{r^3 \sin^2(\phi) \sin^4(\theta) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{(r^2 \sin^2(\theta))^{\frac{3}{2}} \sqrt{r^2}} + \\
& \frac{r^2 \sin(\phi) \cos(\phi) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} + \frac{r^2 \cos^2(\phi) \frac{\partial}{\partial r} U(r, \theta, \phi)}{(r^2)^{\frac{3}{2}}} - \frac{r^2 \sin^2(\phi) \sin^4(\theta) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{(r^2 \sin^2(\theta))^{\frac{3}{2}} \sqrt{r^2}} + \\
& \sin^2(\phi) \sin^2(\theta) \frac{\partial^2}{\partial r^2} U(r, \theta, \phi) + \frac{\sin(\phi) \cos(\phi) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{\sqrt{r^2}} - \frac{2 \sin(\phi) \cos(\phi) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{-2r^2 \cos^2(\theta) + 2r^2} + \\
& \frac{2 \cos^2(\phi) \frac{\partial^2}{\partial \phi^2} U(r, \theta, \phi)}{-2r^2 \cos^2(\theta) + 2r^2} - \frac{\sin(\phi) \cos(\phi) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2}} + \frac{\sqrt{2} \sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r \sqrt{-2r^2 \cos^2(\theta) + 2r^2}} + \frac{\sqrt{2} \cos^2(\phi) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r \sqrt{-2r^2 \cos^2(\theta) + 2r^2}} + \\
& \frac{\sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2 \sin^2(\theta)}} - \frac{\sin(\phi) \cos(\phi) \cos^2(\theta) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2 \sin^2(\theta)} \sin(\theta)} - \frac{\sin^2(\phi) \sin(\theta) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^2} + \\
& \frac{\sin^2(\phi) \cos^2(\theta) \frac{\partial^2}{\partial \theta^2} U(r, \theta, \phi)}{r^2}
\end{aligned}$$

$$\begin{aligned}
\frac{\partial^2 U}{\partial x \partial y} = & \sin(\theta) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial r^2} U(r, \theta, \phi) + \frac{\sin(\phi) \sin(\theta) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2 \sin^2(\theta)}} - \frac{\sin(\theta) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta^2} U(r, \theta, \phi)}{r^2} - \\
& \frac{\cos(\phi) \cos^2(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^2} - \frac{(r^2)^{\frac{3}{2}} \sin^3(\theta) \cos(\phi) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{r^3 \sqrt{r^2 \sin^2(\theta)}} + \frac{(r^2)^{\frac{3}{2}} \sin(2\theta) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{2r^3 \sqrt{r^2 \sin^2(\theta)}} + \\
& \frac{(r^2)^{\frac{3}{2}} \cos(\phi) \cos(\theta) \cos(2\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{2r^3 \sqrt{r^2 \sin^2(\theta)}} - \frac{(r^2)^{\frac{3}{2}} \cos(\phi) \cos(\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{2r^3 \sqrt{r^2 \sin^2(\theta)}} - \frac{(r^2)^{\frac{3}{2}} \sin(\phi) \cos(\theta) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{r^4 \sin(\theta)} + \\
& \frac{(r^2)^{\frac{3}{2}} \sin^3(\theta) \cos(\phi) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^4 \sqrt{r^2 \sin^2(\theta)}}
\end{aligned}$$

$$\begin{aligned}
\frac{\partial^2 U}{\partial x \partial z} = & \sin(\phi) \sin(\theta) \cos(\theta) \frac{\partial^2}{\partial r^2} U(r, \theta, \phi) - \frac{\sin(\theta) \cos(\phi) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r \sqrt{r^2 \sin^2(\theta)}} - \frac{\sin(\phi) \sin(\theta) \cos(\theta) \frac{\partial^2}{\partial \theta^2} U(r, \theta, \phi)}{r^2} - \\
& \frac{\sin(\phi) \cos^2(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^2} - \frac{(r^2)^{\frac{3}{2}} \sin(\phi) \sin^3(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{r^3 \sqrt{r^2 \sin^2(\theta)}} + \frac{(r^2)^{\frac{3}{2}} \sin(\phi) \sin(2\theta) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{2r^3 \sqrt{r^2 \sin^2(\theta)}} + \\
& \frac{(r^2)^{\frac{3}{2}} \sin(\phi) \cos(\theta) \cos(2\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{2r^3 \sqrt{r^2 \sin^2(\theta)}} - \frac{(r^2)^{\frac{3}{2}} \sin(\phi) \cos(\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{2r^3 \sqrt{r^2 \sin^2(\theta)}} + \frac{(r^2)^{\frac{3}{2}} \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{r^4 \sin(\theta)} + \\
& \frac{(r^2)^{\frac{3}{2}} \sin(\phi) \sin^3(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^4 \sqrt{r^2 \sin^2(\theta)}}
\end{aligned}$$

$$\begin{aligned}
\frac{\partial^2 U}{\partial y \partial z} = & \sin(\phi) \sin^2(\theta) \cos(\phi) \frac{\partial^2}{\partial r^2} U(r, \theta, \phi) - \frac{\sin(\phi) \sin(\theta) \cos(\phi) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^2} + \frac{\sin(\phi) \cos(\phi) \cos^2(\theta) \frac{\partial^2}{\partial \theta^2} U(r, \theta, \phi)}{r^2} - \\
& \frac{\sin(\phi) \cos(\phi) \frac{\partial^2}{\partial \phi^2} U(r, \theta, \phi)}{r^2 \sin^2(\theta)} - \frac{\cos^2(\phi) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{r^2 \sin^2(\theta)} - \frac{(r^2)^{\frac{3}{2}} \sin^2(\phi) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{r^4} - \frac{(r^2)^{\frac{3}{2}} \sin(\phi) \cos(\phi) \frac{\partial}{\partial r} U(r, \theta, \phi)}{r^4} + \\
& \frac{(r^2)^{\frac{3}{2}} \cos^2(\phi) \frac{\partial^2}{\partial r \partial \phi} U(r, \theta, \phi)}{r^4} - \frac{(r^2 \sin^2(\theta))^{\frac{3}{2}} \sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^5 \sin^4(\theta)} + \frac{(r^2 \sin^2(\theta))^{\frac{3}{2}} \cos^2(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r^5 \sin^4(\theta)} + \\
& \frac{(r^2)^{\frac{3}{2}} \sin^2(\phi) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{r^5} - \frac{\sqrt{r^2 \sin^2(\theta)} (r^2)^{\frac{3}{2}} \sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial}{\partial \theta} U(r, \theta, \phi)}{r^6} - \frac{(r^2 \sin^2(\theta))^{\frac{5}{2}} \sin^2(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial \phi} U(r, \theta, \phi)}{r^7 \sin^6(\theta)} + \\
& \frac{(r^2 \sin^2(\theta))^{\frac{5}{2}} \sin^2(\phi) \cos^2(\theta) \frac{\partial}{\partial \phi} U(r, \theta, \phi)}{r^7 \sin^7(\theta)} + \frac{(r^2 \sin^2(\theta))^{\frac{3}{2}} (r^2)^{\frac{3}{2}} \sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{r^7 \sin^2(\theta)} + \\
& \frac{(r^2 \sin^2(\theta))^{\frac{7}{2}} (r^2)^{\frac{3}{2}} \sin(\phi) \cos(\phi) \cos(\theta) \frac{\partial^2}{\partial \theta \partial r} U(r, \theta, \phi)}{r^{11} \sin^6(\theta)} + \frac{(r^2 \sin^2(\theta))^{\frac{7}{2}} (r^2)^{\frac{3}{2}} \sin(\phi) \cos(\phi) \cos^2(\theta) \frac{\partial}{\partial r} U(r, \theta, \phi)}{r^{11} \sin^7(\theta)}
\end{aligned}$$

$$\omega^2 \cdot (12.0A^3 \sin^2(\theta) - 24.0A^3 - 24.0A^2 \sin^2(\theta) + 48.0A^2 + 12.0A \sin^2(\theta) - 22.4A - 1.6)$$

$$36A(A-1)^2 \cdot \left(7A\omega^2 \left(-0.8A^5 + 2.4A^4 - 2.0A^3 + 0.4A^2(A-1)^3 \sin^2(\theta) + 0.4 \right) - 1 \right) \sin(\theta)$$