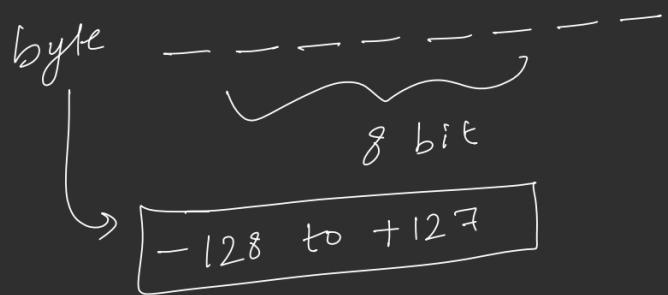


Negative No.

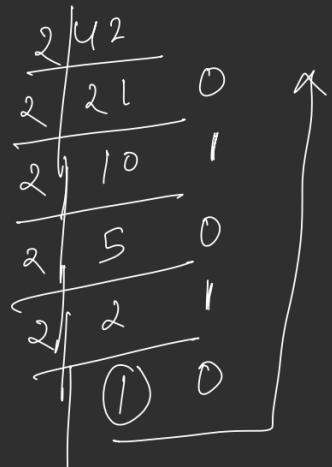
byte b = -42;



① +42 →

$\frac{0}{128} \frac{0}{64} \frac{1}{32} \frac{0}{16} \frac{1}{8} \frac{0}{4} \frac{1}{2} \frac{0}{1}$

$$\boxed{00101010} = 42$$



byte b = (42);

00101010

System.out.println(b);

= 42 ✓

$\boxed{00101010}$

b

byte b = -42; ↙

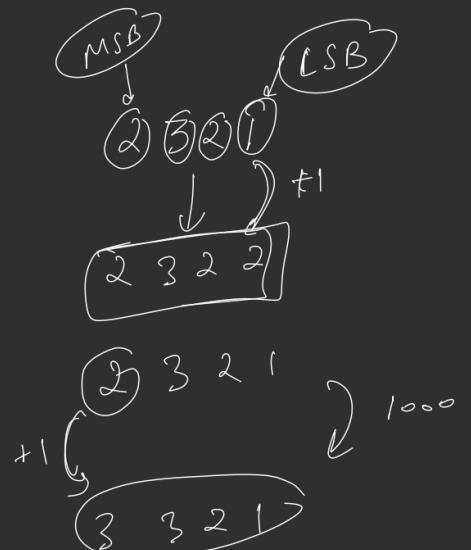
2's Complement

$$\begin{array}{rcl} ① \quad -42 & = & \begin{array}{ccccccc} 0 & 0 & 1 & 0 & 1 & 0 & 1 \\ | & | & | & | & | & | & | \end{array} \\ \text{1st Complement} & \rightarrow & \boxed{\begin{array}{cccccc} 1 & 1 & 0 & 1 & 0 & 1 \end{array}} \\ \downarrow & & \\ \text{2nd Complement} & = & \underline{\underline{1^t C + 1}} \\ & & \begin{array}{rcl} 1 & 1 & 0 & 1 & 0 & 1 & 0 \\ + & & & & & & | \\ \hline \boxed{1 & 1 & 0 & 1 & 0 & 1 & 0} \end{array} \end{array}$$

byte  $b = -42$   
 $\hookrightarrow 11010110$

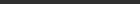
`System.out.println(b);`

$\xrightarrow{\text{MSB}}$   $11010110$   $\xrightarrow{\text{LSB}}$   
 $\text{MSB} = 1 \Rightarrow -\text{ve No.}$   
 $\text{MSB} = 0 \Rightarrow +\text{ve No.}$



$$\begin{array}{rcl} \text{byte} & = & \boxed{0} \frac{1}{128} \frac{1}{64} \frac{1}{32} \frac{1}{16} \frac{1}{8} \frac{1}{4} \frac{1}{2} \frac{1}{1} \\ & & \left( \begin{array}{l} -128 \text{ to } +127 \\ -127 \end{array} \right) \left( \begin{array}{l} 127 \end{array} \right) \end{array}$$

$\underbrace{-128 \text{ to } 127}_{\text{0 to } 1} \quad \underbrace{10000000}_{00000000}$

b  010110

System.out.println(b);

$$2^1 \lambda + C \Rightarrow$$

0	0	1	0	1	0	0	1	0
16	64	32	16	8	4	2	1	0

$$32 + 8 + 2 = \underline{-42} \quad \checkmark$$

byte b =   j;

$$= (0)$$

$$\begin{array}{r} + \\ \boxed{1} \quad 0 \quad 0 \quad 0 \quad 0 \\ \hline \end{array}$$

$$\begin{array}{r} & + & 1 \\ \boxed{1} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \downarrow & & & & & & & \\ \boxed{1} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array}$$

Floating No.

✓ Float  $b = 8 \cdot 125 f_j$  | float  $b = 0.7 f_j$

32 bit

1 bit	8 bits	23 bits
Sign bit	Exponent	Mantissa

$f_j = 8 \cdot 125$

①  $\underline{1000.001}$  (Find Binary of above No.)

$$0.125 \times 2 = 0.25 \rightarrow 0$$

$$0.25 \times 2 = 0.5 \rightarrow 0$$

$$0.5 \times 2 = 1.0 \rightarrow 1$$

② Make it in the form of —

$$(1.x) * 2^{\text{exp}}$$

$$\Rightarrow \underline{1.000001} * 2^{\text{③}}$$

③ Add Bias to the exponent.  
For float bias = 127

$$\Rightarrow 127 + 127 = \underline{130}$$

$$\text{exp} \Rightarrow \underline{10000010 + 0}$$

$$\begin{array}{r} 130 \\ 2 ) 65 \quad 0 \\ 2 ) 32 \quad 1 \\ 2 ) 16 \quad 0 \\ 2 ) 8 \quad 0 \\ 2 ) 4 \quad 0 \\ 2 ) 2 \quad 0 \\ 1 \quad 0 \end{array}$$

④ Place value in memory -

0	10000010	00000010000000000000000
1 bit	8 bit (Exp)	(Mantissa) 23 bit

System.out.println(f);

$$(-1)^{\text{sign}} * \left(1 + \text{Mantissa}\right) * 2^{\text{exp-Bias}}$$

$$\Rightarrow (-1)^0 * \left(1 + \frac{1}{2^3}\right) * 2^3$$

$$\Rightarrow \left(1 + \frac{1}{2^6}\right) * 8$$

$$= \left(1 + \frac{1}{2^6}\right) * 8$$

$$= \left(1 + \frac{1}{64}\right) * 8 \quad \Rightarrow$$

$$\Rightarrow \left(1 + \frac{1}{64}\right)$$

$$= \left(1 + 0.015625\right) * 8$$

$$= 8.125 \quad \checkmark$$

$$\begin{array}{r} 10000010 \\ \times 130 - 127 \\ \hline = 03 \end{array}$$

float  $f = \underline{\underline{0.7}}$

① Express to Binary

$0.7$   
↓  
 $0.1011001100110\dots$

②  $(1.xxx * 2^{\text{exp}})$

$(1.\underline{0110\ 0110\dots}) * 2^{-1}$

③ Add Bias  $\Rightarrow \underline{127}$

$$(-1 + 127) = \underline{\underline{126}}$$

$= \boxed{0111110}$

④ Express it in Memory:

$\boxed{0} \underline{0111110} \underline{0110} \underline{0110} \underline{0110} \underline{0110} \underline{0110} \underline{0110}$   
 $\underbrace{\hspace{1cm}}_{23 \text{ bit}} \underbrace{\hspace{1cm}}_{-22} \underbrace{\hspace{1cm}}_{-23}$

$$\begin{aligned} 0.7 \times 2 &= 1.4 \rightarrow 1 \\ 0.4 \times 2 &= 0.8 \rightarrow 0 \\ 0.8 \times 2 &= 1.6 \rightarrow 1 \\ 0.6 \times 2 &= 1.2 \rightarrow 1 \\ 0.2 \times 2 &= 0.4 \rightarrow 0 \\ 0.4 \times 2 &= 0.8 \rightarrow 0 \\ 0.8 \times 2 &= 1.6 \rightarrow 1 \\ 0.6 \times 2 &= 1.2 \rightarrow 1 \\ 0.2 & \end{aligned}$$

!

$2 | 126$   
 $2 | 63$   
 $2 | 31$   
 $2 | 15$   
 $2 | 7$   
 $2 | 3$   
 $2 | 1$

System.out.println(f);

$$\begin{aligned}
 & (-1)^8 * (1 + \textcolor{brown}{m}) * 2^{e-\beta} \\
 = & (-1)^0 * \left(1 + \frac{1}{2}\right) * 2^{12^6 - 12^7} \\
 = & \left(1 + \frac{1}{2}\right) * \frac{1}{2} \\
 = & \left(1 + \frac{1}{2^2} + \frac{1}{2^3} + \frac{1}{2^6} + \frac{1}{2^7} + \frac{1}{2^{10}} + \frac{1}{2^{11}} + \frac{1}{2^{14}} + \frac{1}{2^{15}} + \frac{1}{2^{18}} + \frac{1}{2^{19}}\right. \\
 & \quad \left. + \frac{1}{2^{22}} + \frac{1}{2^8}\right) * \frac{1}{2}
 \end{aligned}$$

$$\Rightarrow \frac{1.3999997615814208984375}{2}$$

$$\boxed{0.6999998807907104421875}$$

≠ 0.7      ×  $\boxed{0.7}$       √  $\boxed{\overline{0.76}}$

20 - - -

(1) Bias ?? Bias =  $127$

$$\begin{array}{c}
 \boxed{\text{S} \quad \text{exp} \quad \text{Mantissa}} \\
 | \quad | \quad | \\
 1 \text{ bit} \quad 8 \text{ bit} \quad 23 \text{ bit}
 \end{array}$$

$-127 + 127 = 0$   
 $\frac{0}{2} = 2^{56}$

$32 \text{ bit} \rightarrow \text{IEEE}$   
 $0.7f = \left(\frac{-1}{2}\right) = 0 \cancel{\times} 2^{55} + 127$

$\text{exp} = \underbrace{8 \text{ bits}}_{\text{exp}} = 2^{8-1} - 1$   
 $(2^{8-1} - 1) = (2^7 - 1) : (2^{8-1}) = \boxed{127}$

$(2^{\cancel{\text{exp}-1}} - 1) = \boxed{? ?}$

double d = 32.4186;

$$\begin{array}{c}
 \boxed{1 \text{ bit} \quad 11 \text{ bit} \quad 52 \text{ bit}} \\
 | \quad | \quad | \\
 \text{exp} \quad \text{mantissa} \\
 \underbrace{\quad}_{64 \text{ bit}}
 \end{array}$$

$(2^{11-1} - 1) = (2^{10} - 1) = \boxed{1023}$

Float  $\rightarrow$   $0.\boxed{7}_2$   
double

BigDecimal  
 $\boxed{0.7} \rightarrow \boxed{0.7}$