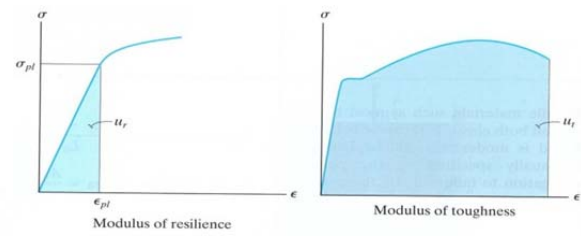
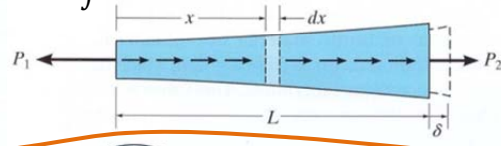


$$\sigma = E \cdot \epsilon \quad \tau = G \cdot \gamma$$

$$G = E/[2(1 + \nu)] \quad \nu = -\frac{\epsilon_{lat}}{\epsilon_{long}}$$

$$F = \int \sigma dA$$



$$\delta = \int_0^L \frac{P(x)dx}{A(x)E(x)}$$

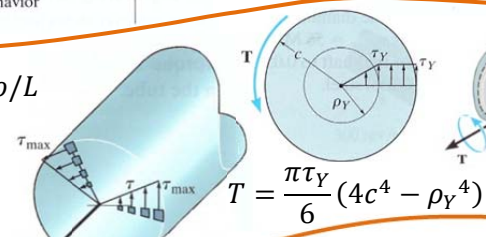
$$\delta = \alpha \Delta T L$$

$$\tau = T\rho/J \quad \gamma = \phi\rho/L$$

$$P = T\omega$$

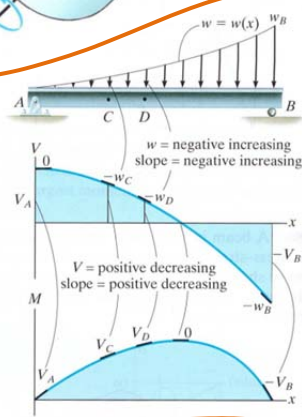
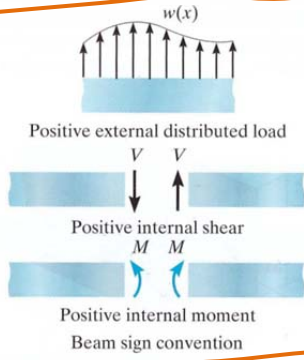
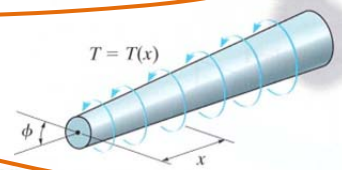
$$T = 2\pi \int_0^c \tau \rho^2 d\rho$$

$$\phi = \int_0^L \frac{T(x)dx}{J(x)G(x)}$$



$$\tau_{avg} = T/(2tA_m)$$

$$T_P = \frac{4}{3}T_Y$$

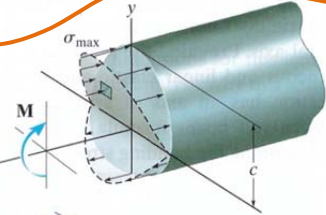
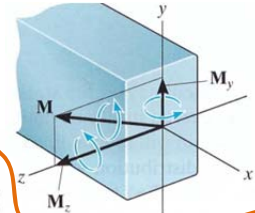


$$\sigma = -\frac{My}{I}$$

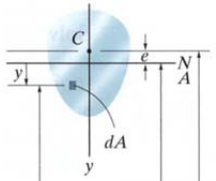
$$M = \int y\sigma dA$$

$$n = \frac{E_2}{E_1} \quad \sigma_2 = \sigma'_1 n$$

$$\sigma = -\frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

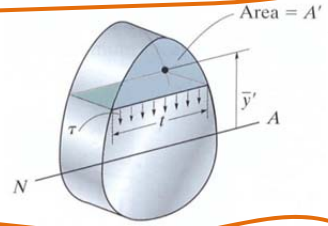


$$M = \frac{bh^2\sigma_Y}{4} \left(1 - \frac{y_Y^2}{h^2}\right)$$



$$\sigma = \frac{M(R-r)}{Ar(\bar{r}-R)}$$

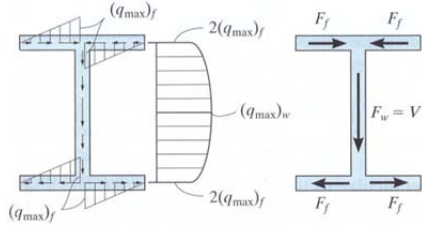
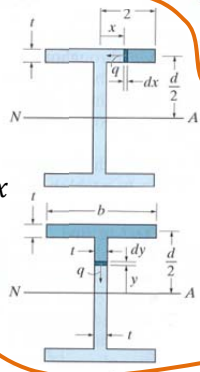
$$R = A/\int \frac{1}{r} dA$$



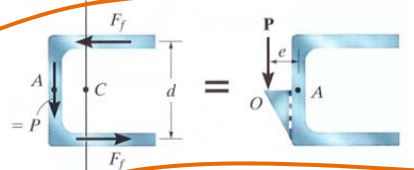
$$\tau = \frac{V\bar{y}'A'}{It}$$

$$q = \frac{V\bar{y}'A'}{I}$$

$$F = \int q dx$$



$$e = \frac{F_f d}{P}$$

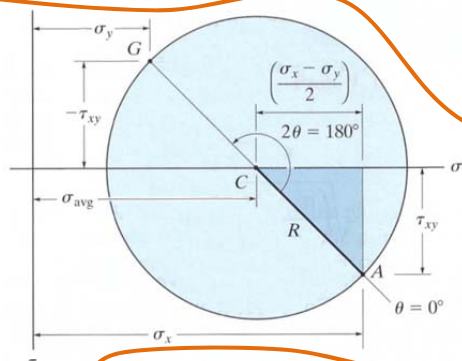
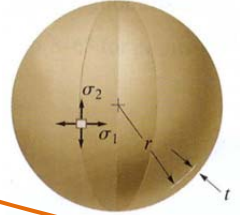


$$\sigma_1 = \frac{pr}{t}$$

$$\sigma_2 = \frac{pr}{2t}$$



$$\sigma_1 = \sigma_2 = \frac{pr}{2t}$$



$$C = \sigma_{avg} = \frac{\sigma_x + \sigma_y}{2}$$

$$R = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$\tan 2\theta_p = \frac{\tau_{xy}}{(\sigma_x - \sigma_y)/2} \quad \theta_{p2} = \theta_{p1} \pm 90^\circ$$

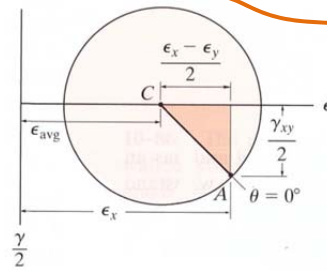
$$\theta_{s1,2} = \theta_p \pm 45^\circ$$

$$\sigma_{x',y'} = \frac{\sigma_x + \sigma_y}{2} \pm \frac{\sigma_x - \sigma_y}{2} \cos 2\theta \pm \tau_{xy} \sin 2\theta$$

$$\tau_{x'y'} = -\frac{\sigma_x - \sigma_y}{2} \sin 2\theta + \tau_{xy} \cos 2\theta$$

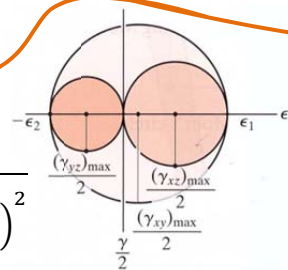
$$\epsilon_{x',y'} = \frac{\epsilon_x + \epsilon_y}{2} \pm \frac{\epsilon_x - \epsilon_y}{2} \cos 2\theta \pm \frac{\gamma_{xy}}{2} \sin 2\theta$$

$$\frac{\gamma_{x'y'}}{2} = -\frac{\epsilon_x - \epsilon_y}{2} \sin 2\theta + \frac{\gamma_{xy}}{2} \cos 2\theta$$



$$\epsilon_{avg} = \frac{\epsilon_x + \epsilon_y}{2}$$

$$R = \sqrt{\left(\frac{\epsilon_x - \epsilon_y}{2}\right)^2 + \left(\frac{\gamma_{xy}}{2}\right)^2}$$



$$\epsilon_x = 1/E \cdot (\sigma_x - \nu(\sigma_y + \sigma_z))$$

$$\epsilon_y = 1/E \cdot (\sigma_y - \nu(\sigma_x + \sigma_z))$$

$$\epsilon_z = 1/E \cdot (\sigma_z - \nu(\sigma_x + \sigma_y))$$

$$\gamma_{xy} = \frac{\tau_{xy}}{G} \quad \gamma_{yz} = \frac{\tau_{yz}}{G} \quad \gamma_{xz} = \frac{\tau_{xz}}{G}$$

$$|\sigma_1| = \sigma_Y \quad \text{same sign}$$

$$|\sigma_2| = \sigma_Y$$

$$|\sigma_1 - \sigma_2| = \sigma_Y$$

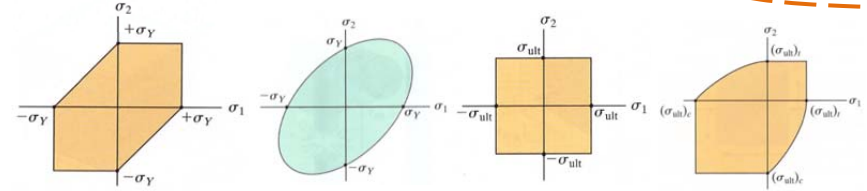
$$\sigma_1^2 - \sigma_1\sigma_2 + \sigma_2^2 = \sigma_Y^2$$

$$|\sigma_1| = \sigma_{ult}$$

$$|\sigma_2| = \sigma_{ult}$$

$$e = \frac{1-2\nu}{E} (\sigma_x + \sigma_y + \sigma_z)$$

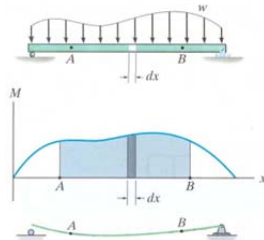
$$k = \frac{E}{3(1-2\nu)}$$



$$w(x) = EI \cdot \frac{d^4 v}{dx^4}$$

$$V(x) = EI \cdot \frac{d^3 v}{dx^3}$$

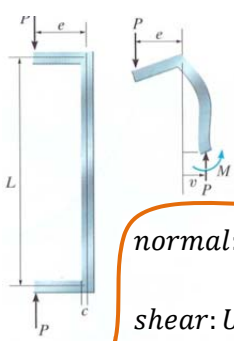
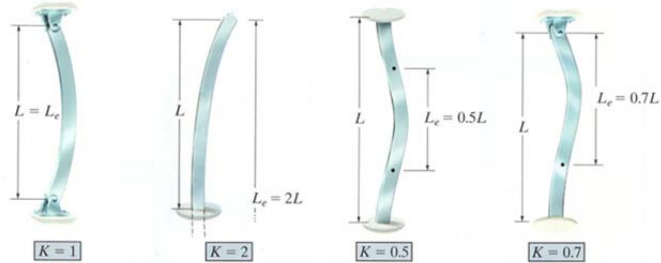
$$M(x) = EI \cdot \frac{d^2 v}{dx^2}$$



$$P_{cr} = \frac{\pi^2 EI}{(KL)^2}$$

$$\sigma_{cr} = \frac{\pi^2 E}{(KL/r)^2}$$

$$r = \sqrt{I/A}$$



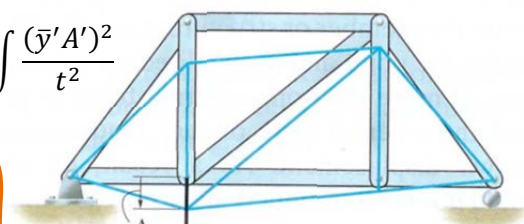
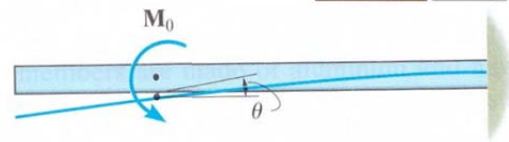
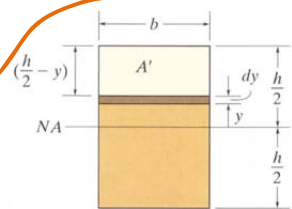
$$v_{max} = e \left[\sec \left(\sqrt{\frac{P}{EI}} \frac{KL}{2} \right) - 1 \right] \quad \sigma_{max} = \frac{P}{A} \left[1 + \frac{ec}{r^2} \sec \left(\frac{KL}{2r} \sqrt{\frac{P}{EA}} \right) \right]$$

$$\text{normal: } U_i = \int \frac{\sigma^2}{2E} dV \quad U_i = \int \left[\frac{1}{2E} (\sigma_x^2 + \sigma_y^2 + \sigma_z^2) - \frac{\nu}{E} (\sigma_x \sigma_y + \sigma_y \sigma_z + \sigma_x \sigma_z) \right. \\ \left. + \frac{1}{2G} (\tau_{xy}^2 + \tau_{yz}^2 + \tau_{xz}^2) \right] dV$$

$$\text{shear: } U_i = \int \frac{\tau^2}{2G} dV$$

$$\text{axial: } U_i = \int_0^L \frac{F^2}{2AE} dx \quad \text{torsion: } U_i = \int_0^L \frac{T^2}{2GJ} dx$$

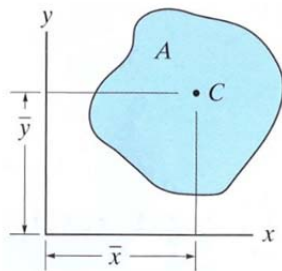
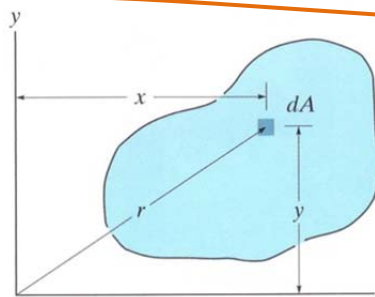
$$\text{bending: } U_i = \int_0^L \frac{M^2}{2EI} dx \quad \text{t. shear: } U_i = \int_0^L \frac{f_s V^2}{2GA} dx \quad f_s = \frac{A}{I^2} \int \frac{(\bar{y}' A')^2}{t^2}$$



$$U_e = U_i$$

$$U_e = \frac{1}{2} M_0 \theta$$

$$U_e = \frac{1}{2} P \Delta$$



$$\bar{x} = \int x dA / \int dA$$

$$\bar{y} = \int y dA / \int dA$$

$$I_x = \int y^2 dA \quad I_y = \int x^2 dA$$

$$J = \int r^2 dA = I_x + I_y$$

$$I_x = \bar{I}_x' + A \cdot \bar{y}^2$$

$$I_y = \bar{I}_y' + A \cdot \bar{x}^2$$

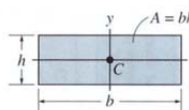
$$J = \bar{J} + A \cdot d^2$$

$$I_{xy} = \int xy dA$$

$$I_{xy} = \bar{I}_{x'y'} + A d_x d_y$$

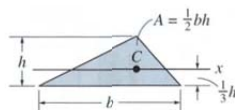
$$I_{min}^{max} = \frac{I_x + I_y}{2} \pm \sqrt{\left(\frac{I_x - I_y}{2} \right)^2 + I_{xy}^2}$$

$$\tan 2\theta = \frac{-I_{xy}}{(I_x - I_y)/2}$$

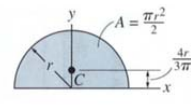


$$I_x = \frac{1}{12} b h^3$$

$$I_y = \frac{1}{12} h b^3$$

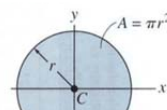


$$I_x = \frac{1}{36} b h^3$$



$$I_x = \frac{1}{8} \pi r^4$$

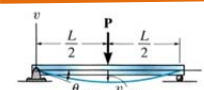
$$I_y = \frac{1}{8} \pi r^4$$



$$I_{x,y} = \frac{1}{4} \pi r^4$$

$$\Delta_{max} = \Delta_{st} \cdot \left(1 + \sqrt{1 + 2(h/\Delta_{st})} \right)$$

$$\Delta_{max} = \sqrt{\Delta_{st} v^2 / g}$$

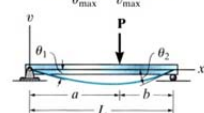


$$\theta_{max} = \frac{-PL^2}{16EI}$$

$$v_{max} = \frac{-PL^3}{48EI}$$

$$v = \frac{-Px}{48EI} (3L^2 - 4x^2)$$

$$0 \leq x \leq L/2$$

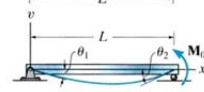


$$\theta_1 = \frac{-Pab(L+b)}{6EIL}$$

$$v|_{x=a} = \frac{-Pba}{6EIL} (L^2 - b^2 - a^2)$$

$$v = \frac{-Pbx}{6EIL} (L^2 - b^2 - x^2)$$

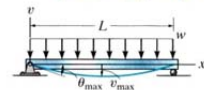
$$0 \leq x \leq a$$



$$\theta_1 = \frac{-M_0 L}{6EI}$$

$$v_{max} = \frac{-M_0 L^2}{9\sqrt{3}EI}$$

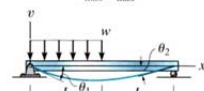
$$v = \frac{-M_0 x}{6EIL} (L^2 - x^2)$$



$$\theta_{max} = \frac{-wL^3}{24EI}$$

$$v_{max} = \frac{-5wL^4}{384EI}$$

$$v = \frac{-wx}{24EI} (x^3 - 2Lx^2 + L^3)$$

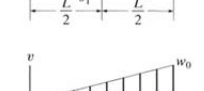


$$\theta_1 = \frac{-3wL^3}{128EI}$$

$$v|_{x=L/2} = \frac{-5wL^4}{768EI}$$

$$v = \frac{-wx}{384EI} (16x^3 - 24Lx^2 + 9L^3)$$

$$0 \leq x \leq L/2$$

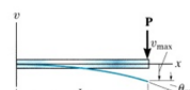


$$\theta_1 = \frac{-7w_0 L^3}{360EI}$$

$$v_{max} = \frac{-0.00652 w_0 L^4}{EI}$$

$$v = \frac{-w_0 x}{360EI} (3x^4 - 10L^2 x^2 + 7L^4)$$

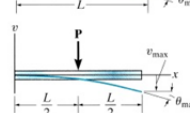
$$L/2 \leq x \leq L$$



$$\theta_{max} = \frac{-PL^2}{2EI}$$

$$v_{max} = \frac{-PL^3}{3EI}$$

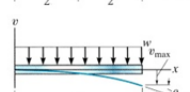
$$v = \frac{-Px^2}{6EI} (3L - x)$$



$$\theta_{max} = \frac{-PL^2}{8EI}$$

$$v_{max} = \frac{-5PL^3}{48EI}$$

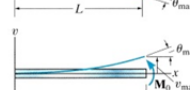
$$v = \frac{-Px^2}{12EI} (3L - 2x) \quad 0 \leq x \leq L/2$$



$$\theta_{max} = \frac{-wL^3}{6EI}$$

$$v_{max} = \frac{-wL^4}{8EI}$$

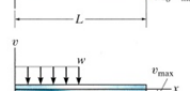
$$v = \frac{-wx^2}{24EI} (x^2 - 4Lx + 6L^2)$$



$$\theta_{max} = \frac{M_0 L}{EI}$$

$$v_{max} = \frac{M_0 L^2}{2EI}$$

$$v = \frac{M_0 x^2}{2EI}$$

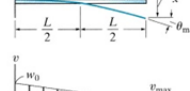


$$\theta_{max} = \frac{-wL^3}{48EI}$$

$$v_{max} = \frac{-7wL^4}{384EI}$$

$$v = \frac{-wx^2}{24EI} (x^2 - 2Lx + \frac{3}{2}L^2)$$

$$0 \leq x \leq L/2$$



$$\theta_{max} = \frac{-w_0 L^3}{24EI}$$

$$v_{max} = \frac{-w_0 L^4}{30EI}$$

$$v = \frac{-w_0 x^2}{120EI} (10L^3 - 10L^2 x + 5Lx^2 - x^3)$$

$$L/2 \leq x \leq L$$