### Parallelism

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OS Parallelish

Trivial Parallelien

An Intro to

Troop Counting

Line graph topology
Tree graph topology

Wrapping up

# Parallel Programing With MATLAB Examples

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## Parallelism in the OS

- A modern OS has a multitude of processes running, as shown by a system monitor
- OS creates an illusion of parallelism even if it runs on a single CPU not capable of multi-threading in hardware.

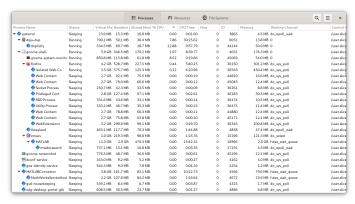


Figure: Explanations

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# How many CPUs/Hardware threads do I have?



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Forking in Bash (&) — a minimal variant

```
(sleep 1e-2; echo -n "Hello, ") & \
(sleep 1e-2; echo -n "World!")
```

## Forking in Bash (&) I

```
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```
#!/bin/sh
  # EXAMPLE: Print 'Hello, ' and 'World!'
  # in random order w/o a random number generator.
  # HINT: We deliberately create a race condition.
  if (($#)) ;then ntimes=$1 ;else ntimes=10; fi
  function hello {
      echo -n "Hello.
  function world {
      echo -n "World!"
  dlay=1e-2 # Change to 5 to see processes
  for ((i=0; $i<$ntimes; i=$i+1))
  do
14
      # Fork with '&'
      (sleep $dlay; hello) & (sleep $dlay; world)
      echo " -- Done with iteration: $i"
  done
```

## Forking in Bash (&) II

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```
[marek@cannonball]$ ./forkme.sh
Hello, World! --Done with iteration: 1
Hello, World! --Done with iteration: 2
World!Hello, --Done with iteration: 3
World!Hello, --Done with iteration: 4
Hello, World! --Done with iteration: 5
World!Hello, --Done with iteration: 6
Hello, World! --Done with iteration: 7
Hello, World! --Done with iteration: 8
Hello, World! --Done with iteration: 9
```

## A remarkable, more rare output

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```
[marek@cannonball matlabmpi]$ ./forkme.sh
Hello, World! --Done with iteration: 1
Hello, World! --Done with iteration: 2
Hello, World! --Done with iteration: 3
Hello, World! --Done with iteration: 4
Hello, World! --Done with iteration: 5
Hello, World! --Done with iteration: 6
World! --Done with iteration: 7
Hello, World!Hello, --Done with iteration: 8
Hello, World! --Done with iteration: 9
```

## A Glossary of Terms I

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program counter The location (address) of the instruction currently being executed; a place in a program

process A running program with all necessary resources (program counter, open file descriptors, memory state)

fork, forking, clone The UNIX/Linux system call which allows one process to create another one

IPC, inter-process communication The protocol by which two distinct processes can exchange information

thread (of execution) Formerly known as a light-weight process directly shares the state of memory (variables) with other threads; threads have separate program counters; a modern process is a collection of threads

## A Glossary of Terms II

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process/thread synchronization Mechanisms by which one process tells another not to mess with some sensitive parts of its state; IPC can be used for proces synchronization; threads are synchronized by mutexes

mutex, futex A mutually exclusive lock, which a simple integer (logical) variable which is set/unset (=acquired/released) by a thread. What is important is the interpretation by another thread. A thread agrees not to do certain things when mutex is acquired by another, until it is released. Semaphores generalize mutexes to arbitrary integer values. Futex is a fast mutex, introduced by the Linux OS.

## A Glossary of Terms III

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atomicity Some operations need to be atomic, such as changing the value of a mutex/semaphore. Atomicity means that a thread that reads the value of a mutex does not get an inconsistent value while another thread is in the process of changing it. Normal variables cannot be used as mutexes because reading and writing to them is not atomic. Atomicity is implemented using hardware (special instructions) and compiler (awarness that some variables must be changed atomically).

## MATLAB 'parfor' (parallel for) I

```
Parallelisn
```

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```
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```

```
1 % FILE: parforEx.m
2 %p=gcp();
3 %mpilnit;
 n=10;
5 % Evaluate x^2 for 1:n asynchronously and print
     results
  parfor i=1:n
      x=i^2
      %pause(1);
      disp([i,x]);
  end
  disp('All done');
```

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# MATLAB 'parfor' (parallel for) II

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```
parforEx
              1
            25
      9
            81
              4
     10
      3
              9
            16
            36
      7
            49
      8
            64
```

All done

## Question

Why does 'All done' print only once? Only at the end?

#### Trivial **Parallelism**

## Parallel pools, workers, clusters

- TIP: first install Parallel Computing Toolbox and try its GUI to configure a cluster
- Workers are a MATLAB abstraction of threads, and they should directly map to hardware (CPU, hardware threads)
- A paralel pool is a collection of workers under the management of the main thread
- A parallel pool can live on one or more CPUs, and can be distributed across many computers; these details are abstracted away
- A cluster is defined by a configuration file (a profile, eg., 'local.settings') and it specifies computers and the number of CPU used on each machine. The configuration file must be placed in one of several standard places (see 'help parcluster').

## Accumulating values, reduction variables I

#### Trivial **Parallelism**

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```
% FILE: reductionVar.m
2 % This file demonstrates a useful notion of a '
     Reduction Variable'
3 % Makes it possible to accumulate values in a
     parfor without using
 % spmd/gop.
  p=gcp('nocreate');
  if isempty(p)
      p = parpool('local', 8)
  end
  disp(sprintf('Number of workers: %d', p.
     NumWorkers));
 x = []:
```

```
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```

# Accumulating values, reduction variables II

```
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```

```
parfor i = 1:10
    pause(rand());
    disp(i);
    x = [x, i];
end

X
>> reduction_var
Number of workers: 8
x =
    1    2    3    4    5    6    7    8    9    10
```

### Fact

Deterministic: the answer is always the same.

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# Accumulating values, reduction variables III

Reduction Variables R2018b

MATLAS® supports an important exception, called reduction, to the rule that loop iterations must be independent. A reduction variable accumulates a value that depends on all the iterations together, but is independent of the iteration order. MATLAB allows reduction variables in parfor-loops.

Reduction variables appear on both sides of an assignment statement, such as any of the following, where expr is a MATLAB expression.

x = x + expr	X = expr + X
x = x - expr	See Associativity in Reduction Assignments in Requirements for Reduction Assignments
X = X .* expr	x = expr .* x
X = X * expr	X = expr * X
x = x & expr	X = expr & X
X = X   expr	x = expr   x
x = [x, expr]	x = [expr, x]
<pre>x = [x; expr]</pre>	X = [expr; X]
X = min(X, expr)	X = min(expr, X)
X = max(X, expr)	X = max(expr, X)
X = union(X, expr)	X = union(expr, X)
X = intersect(X, expr)	X = intersect(expr, X)

## SPMD and SIMD

SPMD Stands for "Single program, multiple data".

Multiple autonomous processors

simultaneously execute the same program at independent points (program counters). Can be implemented on general purpose CPUs (Intel, AMD)

SIMD Stands for "Single-instruction, multiple data". A vector processor processes the same instruction on different data (example: coordinatewise addition or multiplication of two vectors).

## Modern CPU(s) implements both paradigms:

- SIMD uses Intel/AMD SSE instructions and vector registers;
- SPMD uses multiple threads, cores and CPUs.

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# The MPI (Message Passing Interface)

- The most successful realization of SPMD; used in MATLAB; 40 years of history
- Implementations in C, C++, Fortran exist, with high-level language interfaces (e.g., Python).
- Worker becomes a lab
- Worker knows its identity, or labindex
- The main thread is now a lab with labindex==1 (recall: MATLAB has 1-based arrays)
- Labs communicate by using collective communications: labSend, labReceive, labeSendReceive;
- synchronization: labBarrier, labBroadcast
- Labs can be organized as a graph with variable topology, e.g. edges of a hypercube, for the purpose of communicating with some neighbors

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# Unintended blocking — a show stopper

- A blocking operation is one that stops the execution of the program (thread, process) until some condition is met
- Example: reading from a file. We wait for the data to be available (e.g., read from disk or network)
- Example: waiting for a mutex to be released
- labReceive, labBarrier are blocking operations
- A non-blocking operation does not wait for the condition to be met but immediately continues with the execution, reporting status to the caller
- Example: reading from a file in non-blockin mode reports the number of bytes successfully read. One repeatedly reads from the file, getting the file in chunks, until the end-of-file marker is found

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## **Definition (Deadlock)**

Deadlock (which is sometimes called the deadly embrace) occurs when two or more programs (threads, workers, labs) are each waiting for the others to complete a task before proceeding.

The programs act like the overly congenial gophers in some Looney Tunes cartoons:

"Oh please, you first," says one. "No no, I insist, you first," says the other. And nothing goes anywhere.

## An 'spmd' example (WRONG!) I

```
1 % FILE: race1.m
         % This file demonstrates a simple race condition
       3 % when trying to share a value between all
An Intro to
             workers
MPI
       4 p=gcp('nocreate');
         if isempty(p)
              p = parpool('local', 8)
         end
          disp(sprintf('Number of workers: %d', p.
             NumWorkers));
         value = Composite();
       13 % An incorrect way to broadcast a value and
         % receive it in all workers
         spmd
```

```
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```

```
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```

end

## An 'spmd' example (WRONG!) II

```
pause (rand () ./10);
       labindex == 1
        for w=1:numlabs
             display(sprintf('%d sending 7 to %d'
                , labindex ,w));
            labSend(7,w);
        end
    end
    value = labReceive;
    display(sprintf('%d received %d from 1',
        labindex, value));
for w=1:p.NumWorkers
```

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# An 'spmd' example (WRONG!)

## disp(value{w});

### end

```
>> race1
Number of workers: 8
Worker 1:
   1 sending 7 to 1
Error using race1
Error detected on worker 1.

Caused by:
        Error using race1
        Destination (1) is same as source, would cause deadlock.
>>
```

```
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```

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# An 'spmd' example (CORRECT!) I

```
1 % FILE: race1Fixed.m
 % This file demonstrates a simple race condition
3 % when trying to share a value between all
     workers.
4 % NOTE: We avoid sending to ourselves. This
 % avoids the race condition.
  p=gcp('nocreate');
  if isempty(p)
      p = parpool('local', 8)
  end
  disp(sprintf('Number of workers: %d', p.
     NumWorkers));
 value = Composite();
```

```
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```

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```
An 'spmd' example (CORRECT!) II
```

```
% An incorrect way to broadcast a value and
% receive it in all workers
spmd
     pause (rand () ./10);
        labindex == 1
         for w=2:numlabs
             display(sprintf('%d sending 7 to %d'
                 , labindex ,w));
             labSend(7,w)
         end
         value = 7:
     else
         value = labReceive:
```

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end

for w=1:p.NumWorkers

end

disp([w, value{w}]):

end

## An 'spmd' example (CORRECT!) III

```
display(sprintf('%d received %d from 1',
   labindex, value));
```

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# An 'spmd' example (CORRECT!) IV

```
>>
Number of workers: 8
Worker 1:
  1 sending 7 to 2
 1 sending 7 to 3
 1 sending 7 to 4
 1 sending 7 to 5
 1 sending 7 to 6
 1 sending 7 to 7
 1 sending 7 to 8
Worker 2.
  2 received 7 from 1
Worker 3.
  3 received 7 from 1
Worker 4:
  4 received 7 from 1
Worker 5.
  5 received 7 from 1
Worker 6:
  6 received 7 from 1
Worker 7:
  7 received 7 from 1
Worker 8.
  8 received 7 from 1
```

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# An 'spmd' example (CORRECT!) V

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8

>>

7

7 7 7

```
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```

## Broadcasting (another fix) I

```
% FILE: race1FixedBroadcast.m
       2 % This file demonstrates a simple race condition
       3 % when trying to share a value between all
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             workers
MPI
       4 % NOTE: In this version, we avoid the race
             condition
       5 % by using labBroadcast.
         p=gcp('nocreate');
          if isempty(p)
              p = parpool('local', 8)
         end
          disp(sprintf('Number of workers: %d', p.
             NumWorkers));
         value = Composite();
```

## Broadcasting (another fix) II

```
16 % An incorrect way to broadcast a value and
       17 % receive it in all workers
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          root=1;
MPI
          spmd
              pause (rand () ./10);
              if labindex == root
                   value = 7:
                   value = labBroadcast(root, value);
                   display(sprintf('Root==%d broadcast %d',
                      labindex, value));
              else
                   value = labBroadcast(root, 666); %
                      Second inut ignored on root
                   display(sprintf('%d received %d from
                      root==%d', labindex, value, root));
              end
          end
```

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# Broadcasting (another fix) III

```
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```

end

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```
>>
Number of workers: 8
Worker 1:
 Root == 1 broadcast 7
Worker 2:
  2 received 7 from root == 1
Worker 3.
  3 received 7 from root == 1
Worker 4:
  4 received 7 from root==1
Worker 5.
  5 received 7 from root == 1
Worker 6:
  6 received 7 from root==1
Worker 7:
  7 received 7 from root == 1
Worker 8.
  8 received 7 from root==1
            7
     3
            7
```

for w=1:p.NumWorkers

disp([w, value {w}]);

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11 0 1

# Broadcasting (another fix) IV

4 7 5 7

5 7 6 7

7

7

7

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7

>>

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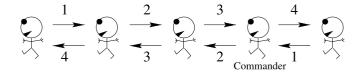


Figure: A line of soldiers counting themselves using message-passing rule-set A. The commander can add "3" from the soldier in front, "1" from the soldier behind, and "1" for himself, and deduce that there are 5 soldiers in total.

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# Message-passing rule-set A (parallel pseudo-code).

- 1 If you are the front soldier in the line, say the number one to the soldier behind you.
- If you are the rearmost soldier in the line, say the number one to the soldier in front of you.
- 3 If a soldier ahead of or behind you says a number to you, add one to it, and say the new number to the soldier on the other side.

```
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```

## Implementation I

```
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```
3 % marching in line
4 %
5 % NOTE: If you are running the program on a
6 % processor with n=4 cores and 2*n
7 % hyperthreads, the setting for the 'local'
8 % cluster is used, and the number of workers
9 % in a parpool is set automatically to n,
10 % ignoring hyperthreading. You can modify
11 % the number of worker threads using Matlab
12 % GUI, using Home > Parallel > Manage Cluster
13 % Profiles > Edit. So, if you request 8
14 % workers, make sure to first edit the local
15 % profile and increate the number of allowed
16 % workers to >=8. I changed it to 64.
17 %
p = gcp('nocreate');
```

2 % Mackay, algorithm 16.1: to count soldiers

1 % FILE: soldiers.m

```
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```

## Implementation II

```
numSoldiers=5:
      20 % Must have at least numSoldiers workers
         if ~isempty(p) && p.NumWorkers < numSoldiers
              delete(p);
              p = [];
         end
         if isempty(p)
Line graph topology
             % Create a local parpool with num. workers
                 == num. soldiers
              p = parpool('local', numSoldiers);
         end
          mpilnit;
         commander=2:
         % Must have at least commander+1 workers
          assert(p.NumWorkers > commander);
         spmd
              me=labindex;
      34
              value = 0;
```

#### Implementation III

```
if me==commander
                    [value1, source1, tag1]=labReceive;
                    fprintf('%d=commander got %d from %d\n',
                       me, value1, source1);
                    [value2, source2, tag2]=labReceive;
                    fprintf('%d=commander got %d from %d\n',
                       me, value2, source2);
Line graph topology
                    value=value1+value2+1;
Tree graph topology 41
                    fprintf('%d=commander says: count is %d\
                       n', me, value);
               elseif me==1
       43
                    value=1:
                    dest=2:
       45
                    fprintf ('%d sending %d to %d\n', me, value
       46
                        .dest):
                    labSend(value, dest);
       47
               elseif me==numlabs
       48
                    value = 1:
```

#### Implementation IV

```
dest=me-1:
                    fprintf('%d sending %d to %d\n',me, value
       51
                       , dest);
                   labSend(value, dest);
               else
                    [value, source, ~]=labReceive;
                   value=value+1;
Line graph topology
                    if source==me-1
                        dest=me+1:
                    elseif source==me+1
                        dest=me-1:
                   end
       60
                    fprintf('%d sending %d to %d\n',me,value
       61
                       .dest):
                   labSend(value, dest);
       62
               end
         end
```

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#### General topology of the troop

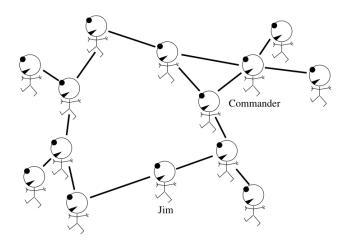


Figure: A swarm of guerillas.

# Arranging workers/labs into a graph I

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```
% Efficient graph encoding (often used in MPI programs)
4 % Adjacency matrix; passed as 1-d aray, in which each vertex is followed
5 % Row format: node followed by neighbors, sentinel 0.
6 % A final zero is added to terminate the structure.
7 adj=[1,2,0,...
2,1,3,11,0,...
3,2,4,5,0,...
```

1 % FILE: buildTroop.m

4,3,0,... 5,3,0,... 6.8,0,...

```
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```

# Arranging workers/labs into a graph II

```
7,8,0,...
                 8,6,7,9,0,...
                 9,8,10,12,0,...
                 10,9,11,0,...
                 11,2,10,0,...
                12.9,13,14,0,...
Tree graph topology
                13,12,0,...
                 14,12,0,...
                 0];
               (nodes)
```

# Arranging workers/labs into a graph III

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```
p = gcp('nocreate');
if ~isempty(p) && p.NumWorkers < numSoldiers</pre>
     delete(p):
    p = [];
end
if isempty(p)
    p = parpool('local', numSoldiers);
end
mpilnit;
% Convert nb to cell array
nb=Composite();
start=1;
for s=1:numSoldiers:
    me=adi(start);
```

```
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```

# Arranging workers/labs into a graph IV

```
neighbors = [];
    n=start+1:
    % Make a list of neigbors
     while adj(n)~=0
         neighbors = [neighbors, adj(n)];
         n=n+1;
    end
    nb{me}=neighbors;
     start=n+1;
end
assert(adj(start)==0);
% A normal function call to let soldiers report
    the neighbors
report(nb);
% A consistency check for graph data
```

# Arranging workers/labs into a graph V

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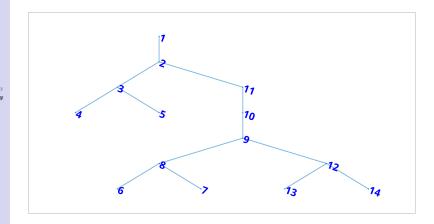
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```
61 l=adjacency matrix(nb);
62 % Check symmetry of the adjacency relation
63 assert(all(all(l==l')));
64 % Check for 'no loops' (loop=connection of edge
      to itself)
assert(all(diag(I)==0));
66 % Check for 'no cycles'; upper triangular
      portion of I should be nilpotent
  assert(all(all(triu(I)^numSoldiers==0)));
68
69 \%g = graph(I);
%plot(g,'LineWidth',4,'NodeFontSize'.44.'
      MarkerSize', 5, 'NodeLabelColor', 'blue', '
      NodeFontWeight', 'bold');
```

Tree graph topology

#### A tree topology of the troop



Wrapping up

## Message-passing rule-set B. I

- 1: **procedure** MessagePassing(*Graph*)
- 2:  $N \leftarrow$  the count your neighbours in *Graph*
- 3:  $m \leftarrow 0$   $\triangleright$  count of messages received from neighbours
- 4: **for** j from 1 to N **do**
- 5:  $v_j \leftarrow -1$   $\triangleright$  initial value of message is invalid
  - 6: end for
- 7:  $V \leftarrow 0$  > running total of messages you have received
- 8: **if** m == N 1 **then**
- 9: Find neighbor j such that  $v_j == -1$   $\triangleright$  the only one who has not sent you a message
- 10: Tell them the number V + 1
- 11: end if

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```
if V == N then
the number V + 1 is the required total.
for each neighbour n do
say to neighbour n the number V + 1 - v<sub>n</sub>
end for
end if
end procedure
```

```
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```

#### Implementation I

```
% FILE: soldiers2.m
          % NOTE: Make sure to modify the parpool to allow
               14 workers.
          buildTroop;
        5
          % Main course: count the soldiers by message
Tree graph topology
              passing
Implementation
          spmd
              me=labindex:
       8
              N=length(nb);
                                                   % Neighbor
                   count
              m=0:
                                                   % Message
                   count
              v=-ones(N,1):
                                                   % Message
                  values
              V=0;
                                                   % Running
                   total
                         of messages
```

#### Implementation II

```
labBarrier;
                                                % Not needed
                    harmless, for demo purposes
             % Receive first N-2 messages
              while m < N-1
                  [isDataAvail, source]=labProbe;
                  if isDataAvail
                                                % If
Tree graph topology
Implementation
                      available, get the data
                      n=find(source==nb,1); % Find which
                           neighbor sent the msssage
                       assert(~isempty(n)); % Otherwise
                          it is not a neighbor
                       fprintf('%d sees data available from
                           %d...\n ',me,source);
                       value=labReceive(source);
                       fprintf('%d received value %d from %
      24
                          d.\n',me, value, source);
```

# Implementation III

```
m=m+1:
                       v(n)=value;
                       V=V+value:
                   end
              end
              %labBarrier;
                                                   % Will
                  break the code!!!
Implementation
                                                  % Check
              assert (m==N-1);
                  number of messages
       34
              % Send the message to who has not send us a
                  message
              n = find(v = -1, 1);
                                        % Identify who has
                  not send us a message
              dest=nb(n);
              value to send=V+1;
```

#### Implementation IV

```
fprintf('%d sending %d to %d...\n'.me,
                   value to send.dest);
               labSend(value to send, dest);
       40
               % labSendReceive(value to send, dest);
                fprintf('%d completed sending %d to %d.\n',
       42
                   me, value to send, dest);
                fprintf('%d waiting for message from %d...\n
Line graph topology 12
Tree graph topology
                   '.me.dest):
Implementation
                [value, last source]=labReceive(dest);
Wrapping up 44
                fprintf('%d received %d from %d.\n',me,value
       45
                   , last source);
               assert(last source==dest);
                                                     % Last
       46
                   message source
               v(n)=value:
       47
               V=V+value:
       48
               m=m+1;
       49
```

# Implementation V

```
%labBarrier:
                                                  % Will
                  break the code!!!
       52
                                                 % Check
              assert (m==N);
                  message count
              % Send message to everyone except the one
                  who was the last to send us
Implementation
              % a message.
              for I=1:N
                   if l==n
                       continue:
                                                 % Do not
                           send again
                  end
                   value to send=V+1-v(1);
       61
                   fprintf('%d sending %d to %d...\n',me,
       62
                      value to send, nb(l));
                   labSend(value to send, nb(1));
```

```
Marek Rychlik
```

#### Implementation VI

```
fprintf('%d completed sending %d to %d.\
                      n', me, value to send, nb(1));
              end
       65
              if me==commander
                   fprintf('COMMANDER %d reporting count of
                       %d.\n', me, V+1);
              end
Tree graph topology
              fprintf('%d is done.\n',me);
Implementation
         end
         % A demonstration that a Composite is a kind of
             cell array
         % Print the totals of all soldiers.
       74 for n=1:numSoldiers
              fprintf('Running total of %d is %d.\n', n, V
                  {n});
        end
```

```
Marek Rychlik
```

## A modified implementation I

```
1 % FILE: soldiers3.m
       2 % This is like soldiers2, but uses
             labSendReceive instead
       3 % of 2 calls labSend/labReceive. It is preferred
              to do it this way,
       4 % as there is a smaller chance of programming
             error causing a race
Tree graph topology
       5 % condition (labReceive when there is noone
Implementation
             sending, or labSend when
       6 % there is noone waiting to labReceive).
         buildTroop;
         % Main course: count the soldiers by message
             passing
         spmd
             me=labindex:
       12
```

# A modified implementation II

```
Parallelism 13
Trivial
Parallelism 14
An Intro to MPI
Troop 15
Counting
Example
Line graph topology Implementation
Wrapping up 17
```

```
N=length(nb);
                                 % Neighbor
   count
m=0:
                                 % Message
   count
v=-ones(N,1);
                                 % Message
   values
V=0:
                                 % Running
   total of messages
fprintf('%d reached barrier.\n', me);
labBarrier:
                                 % Not needed
   , harmless, for demo purposes
fprintf('%d crossed barrier.\n', me);
% Receive first N-2 messages
while m < N-1
    [isDataAvail, source]=labProbe;
```

Implementation

end

#### A modified implementation III

```
isDataAvail% If available, get the
   data
    n=find (source==nb,1); % Find which
        neighbor sent the msssage
    assert(~isempty(n)); % Otherwise
       it is not a neighbor
    fprintf('%d sees data available from
        %d...\n',me,source);
    value=labReceive(source);
    fprintf('%d received value %d from %
       d.\n',me, value, source);
   m=m+1;
    v(n)=value:
    V=V+value:
end
```

# A modified implementation IV

```
%labBarrier:
                                                 % Will
                 break the code!!!
                                                % Check
              assert (m==N-1);
                 number of messages
             % Send the message to who has not send us a
                 message
Implementation
              n=find(v==-1,1); % Identify who has
                 not send us a message
              dest=nb(n):
       43
              fprintf('%d noticed not receiving from %d',
      44
                 dest):
              value to send=V+1;
      45
              fprintf('%d sending %d to %d...\n',me,
      46
                 value to send, dest);
              value = labSendReceive(dest, dest,
      47
                 value to send);
```

# OS Parallelism 48 Parallelism 49 An Intro to MPI 50 Counting Example 52 Line graph topology Implementation Wrapping up 54

57

60

## A modified implementation V

```
fprintf('%d received %d from %d.\n',me,value
   .dest):
v(n)=value;
V=V+value:
m=m+1;
%labBarrier:
                                  % Will
   break the code!!!
assert (m==N);
                                 % Check
   message count
% Send message to everyone except the one
   who was the last to send us
% a message.
for I=1:N
    if l==n
```

```
Marek Rychlik
```

# A modified implementation VI

```
Parallelism 61
Trivial Parallelism 62
An Intro to 63
MPI 64
Troop Counting Example Line graph topology Implementation
Wrapping up 67
```

end

```
continue:
                                 % Do not
            send again
    end
    value to send=V+1-v(1);
    fprintf('%d sending %d to %d...\n',me,
       value to send.nb(1));
    labSend(value to send, nb(1));
    fprintf('%d completed sending %d to %d.\
       n', me, value to send, nb(1));
end
  me==commander
    fprintf('COMMANDER %d reporting count of
        %d.\n', me, V+1);
end
fprintf('%d is done.\n',me);
```

#### IVIAIEK NYCIIIIR

OS Parallelism

Trivial Parallelism

An Intro to

Troop Counting

Counting Example

Tree graph topology

Implementation

Wranningun

Wrapping up

# A modified implementation VII

```
75 % A demonstration that a Composite is a kind of cell array
76 % Print the totals of all soldiers.
77 for n=1:numSoldiers
78 fprintf('Running total of %d is %d.\n', n, V
{n});
79 end
```

## Sample output I

Tree graph topology Implementation

```
>> soldiers3
Worker 1.
  Soldier 1 reporting, sir! My neighbors are 2, sir!
Worker 2.
  Soldier 2 reporting, sir! My neighbors are 1, 3, 11, sir!
Worker 3:
  Soldier 3 reporting, sir! My neighbors are 2, 4, 5, sir!
Worker 4.
 Soldier 4 reporting, sir! My neighbors are 3, sir!
Worker 5:
  Soldier 5 reporting, sir! My neighbors are 3, sir!
Worker 6.
  Soldier 6 reporting, sir! My neighbors are 8, sir!
Worker 7.
  Soldier 7 reporting, sir! My neighbors are 8, sir!
Worker 8:
  Soldier 8 reporting, sir! My neighbors are 6, 7, 9, sir!
Worker 9:
  Soldier 9 reporting, sir! My neighbors are 8, 10, 12, sir!
Worker 10:
  Soldier 10 reporting, sir! My neighbors are 9, 11, sir!
Worker 11.
  Soldier 11 reporting, sir! My neighbors are 2, 10, sir!
Worker 12.
  Soldier 12 reporting, sir! My neighbors are 9, 13, 14, sir!
Worker 13:
  Soldier 13 reporting, sir! My neighbors are 12, sir!
Worker 14.
  Soldier 14 reporting, sir! My neighbors are 12, sir!
Worker 1:
  1 reached harrier
```

#### Sample output II

```
1 crossed harrier
                  2 noticed not receiving from 1 sending 1 to 2...
                  1 received 13 from 2.
                  1 is done
                Worker 2:
                  2 reached barrier.
                  2 crossed barrier
                  2 sees data available from 3...
                   2 received value 3 from 3.
                  2 sees data available from 1
                   2 received value 1 from 1.
Line graph topology
                  11 noticed not receiving from 2 sending 5 to 11...
Tree graph topology
                  2 received 9 from 11
Implementation
                  2 sending 13 to 1...
                  2 completed sending 13 to 1.
                  2 sending 11 to 3...
                  2 completed sending 11 to 3.
                  2 is done.
                Worker 3:
                  3 reached harrier
                  3 crossed barrier
                  3 sees data available from 4...
                   3 received value 1 from 4
                  3 sees data available from 5...
                   3 received value 1 from 5.
                  2 noticed not receiving from 3 sending 3 to 2...
                  3 received 11 from 2
                  3 sending 13 to 4...
                  3 completed sending 13 to 4.
                  3 sending 13 to 5...
```

3 completed sending 13 to 5.

# Sample output III

Line graph topology

Tree graph topology Implementation

```
3 is done.
Worker 4.
  4 reached harrier
  4 crossed barrier.
  3 noticed not receiving from 4 sending 1 to 3...
  4 received 13 from 3.
  4 is done.
Worker 5:
  5 reached harrier
  5 crossed barrier.
  3 noticed not receiving from 5 sending 1 to 3...
  5 received 13 from 3
  5 is done
Worker 6:
  6 reached harrier
  6 crossed barrier.
  8 noticed not receiving from 6 sending 1 to 8...
  6 received 13 from 8
  6 is done
Worker 7:
  7 reached barrier.
  7 crossed barrier
  8 noticed not receiving from 7 sending 1 to 8...
  7 received 13 from 8.
  7 is done
Worker 8:
  8 reached barrier.
  8 crossed barrier
  8 sees data available from 7...
   8 received value 1 from 7.
  8 sees data available from 6...
```

## Sample output IV

```
Parallelism
Trivial
```

Parallelism

MPI

Troop
Counting
Example
Line graph topology

Tree graph topology Implementation

Wrapping up

```
8 received value 1 from 6
 9 noticed not receiving from 8 sending 3 to 9...
 8 received 11 from 9.
 8 sending 13 to 6...
 8 completed sending 13 to 6.
 8 sending 13 to 7...
 8 completed sending 13 to 7.
 8 is done.
Worker 9:
  9 reached harrier
 9 crossed barrier.
 9 sees data available from 12...
  9 received value 3 from 12.
 9 sees data available from 8
  9 received value 3 from 8.
 10 noticed not receiving from 9 sending 7 to 10...
 9 received 7 from 10
 9 sending 11 to 8...
 9 completed sending 11 to 8.
 9 sending 11 to 12...
 9 completed sending 11 to 12.
 COMMANDER 9 reporting count of 14.
  9 is done
Worker 10.
 10 reached barrier.
 10 crossed barrier.
 10 sees data available from 9
  10 received value 7 from 9.
 11 noticed not receiving from 10 sending 8 to 11...
 10 received 6 from 11.
 10 sending 7 to 9...
```

## Sample output V

```
10 completed sending 7 to 9.
                 10 is done
               Worker 11:
                 11 reached barrier.
                 11 crossed barrier
                 11 sees data available from 2...
                  11 received value 5 from 2.
                 10 noticed not receiving from 11 sending 6 to 10...
                 11 received 8 from 10
                 11 sending 9 to 2...
                 11 completed sending 9 to 2.
                 11 is done
Tree graph topology
               Worker 12:
Implementation
                 12 reached barrier.
                 12 crossed barrier
                 12 sees data available from 14...
                  12 received value 1 from 14.
                 12 sees data available from 13
                  12 received value 1 from 13
                 9 noticed not receiving from 12 sending 3 to 9...
                 12 received 11 from 9.
                 12 sending 13 to 13...
                 12 completed sending 13 to 13.
                 12 sending 13 to 14...
                 12 completed sending 13 to 14.
                 12 is done
               Worker 13:
                 13 reached harrier
                 13 crossed barrier.
```

13 received 13 from 12.

12 noticed not receiving from 13 sending 1 to 12...

OS Parallelism

Trivial Parallelism

MPI

Troop Counting Example

Tree graph topology

Implementation

Wrapping up

#### Sample output VI

```
13 is done.
Worker 14:
  14 reached harrier
 14 crossed barrier.
 12 noticed not receiving from 14 sending 1 to 12...
 14 received 13 from 12.
 14 is done
Running total of 1 is 13.
Running total of 2 is 13.
Running total of 3 is 13.
Running total of 4 is 13.
Running total of 5 is 13.
Running total of 6 is 13.
Running total of 7 is 13.
Running total of 8 is 13.
Running total of 9 is 13.
Running total of 10 is 13.
Running total of 11 is 13.
Running total of 12 is 13.
Running total of 13 is 13.
Running total of 14 is 13.
>>
```

#### What has been left out?

Parallelism

Trivial Parallelism

MPI Troop

Example
Line graph topology
Tree graph topology

Tree graph topology Implementation

Wrapping up

- OpenMP (e.g., GOMP=GNU OpenMP); a high level interface to threads (SPMD) and vectorization (SIMD); realized as C/Fortran compiler pragmas (annotations)
- POSIX threads ("pthreads"); a C library available on most OS which allows direct access to multi-threading and thread synchronization
- Extensive C++ language constructs supporting parallelism
- Building hardware; hardware is inherently parallel; the most straightforward hardware to build is FPGA (Field-Programmable Gate Arrays); programming languages Verilog and VHDL
- University of Arizona HPC facilities