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- MODULE CigaretteSmokers -
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A specification of the cigarette smokers problem, originally described in 1971 by $Suhas\ Patil.$ https://en.wikipedia.org/wiki/Cigarette_smokers_problem

EXTENDS Integers, FiniteSets

CONSTANT Ing, Offers VARIABLE smokers, dealer

'Ing' is a set of ingredients, originally $\{matches,\;paper,\;tobacco\}$

'Offers' is a subset of subsets of ingredients, each missing just one ingriedent

ASSUME
$$\land Offers \subseteq (SUBSET\ Ing)$$

 $\land \forall n \in Offers : Cardinality(n) = Cardinality(Ing) - 1$

'smokers' is a function from the ingredient the smoker has infinite supply of, to a BOOLEAN flag signifying smoker's state (smoking/not smoking) 'dealer' is an element of 'Offers', or an empty set

$$TypeOK \stackrel{\triangle}{=} \land smokers \in [Ing \rightarrow [smoking : \texttt{BOOLEAN} \]]$$
$$\land dealer \quad \in Offers \lor dealer = \{\}$$

 $vars \stackrel{\Delta}{=} \langle smokers, dealer \rangle$

$$\begin{array}{ll} \mathit{Init} \;\; \stackrel{\triangle}{=} \;\; \land \; smokers = [r \in \mathit{Ing} \mapsto [\mathit{smoking} \mapsto \mathit{false}]] \\ \;\; \land \; \mathit{dealer} \in \mathit{Offers} \end{array}$$

$$\begin{array}{ll} startSmoking & \triangleq & \land \ dealer \neq \{\} \\ & \land \ smokers' = [r \in \mathit{Ing} \mapsto [\mathit{smoking} \mapsto \{r\} \cup \mathit{dealer} = \mathit{Ing}]] \\ & \land \ \mathit{dealer'} = \{\} \end{array}$$

$$stopSmoking \triangleq \land dealer = \{\} \\ \land \exists \ r \in Ing : \land smokers[r].smoking \\ \land smokers' = [smokers \ \texttt{EXCEPT} \ ![r].smoking = \texttt{FALSE}] \\ \land \exists \ s \in Offers : dealer' = s$$

 $Next \triangleq startSmoking \lor stopSmoking$

$$\begin{array}{ll} \mathit{Spec} \; \stackrel{\triangle}{=} \; \mathit{Init} \wedge \Box [\mathit{Next}]_{\mathit{vars}} \\ \mathit{FairSpec} \; \stackrel{\triangle}{=} \; \mathit{Spec} \wedge \mathrm{WF}_{\mathit{vars}}(\mathit{Next}) \end{array}$$

An invariant checking that at most one smoker smokes at any particular moment

$$AtMostOne \ \stackrel{\triangle}{=} \ Cardinality(\{r \in Ing : smokers[r].smoking\}) \leq 1$$