

Embedding Programming Languages: PROLOG in HASKELL

by

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Abstract

This document looks at the problem of combining programming languages with contrasting and conflicting characteristics which mostly belong to different programming paradigms. The purpose to be fulfilled here is that rather than moulding a problem to fit in the chosen language it must be the other way around that the language adapts to the problem at hand. Moreover, it reduces the need for jumping between different languages. The aim is achieved either by embedding a target language whose features are desirable or to be captured into the host language which is the base on to which the mapping takes place which can be carried out by creating a module or library as an extension to the host language or developing a hybrid programming language that accommodates the best of both worlds.

This research focuses on combining the two most important and wide spread declarative programming paradigms, functional and logical programming. This will include playing with languages from each paradigm, HASKELL from the functional side and PROLOG from the logical side. The proposed approach aims at adding logic programming features which are native to PROLOG onto HASKELL by developing an extension which replicates the target language and utilises the advanced features of the host for an efficient implementation.

0.1 Thesis Statement

The thesis aims to provide insights into merging two declarative languages namely, HASKELL and PROLOG by embedding the latter into the former and analysing the result of doing so as they have conflicting characteristics. The finished product will be something like a *haskel-lised* PROLOG which has logical programming like capabilities.

We explore embedding domain specific languages in HASKELL

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Chapter 1

Introduction

1.1 What is this chapter about

This chapter introduces the scope of the thesis along with the preliminary arguments

1.2 Beginnings

Programming has become an integral part of working and interacting with computers and day by day more and more complex problems are being tackled using the power of programming technologies. It is possibly the only way to talk to computers and hence the need for a robust and multi purpose programming language has never been more urgent. The desirability of a programming language depends on a lot of factors such as the ease of use, the features and functionalities that it provides, adaptability and what sort of problems can it solve. One is spoilt for choice with a number of options for a wide variety of programming paradigms, for example Object Oriented Languages.

Over the last decade the declarative style of programming has gained popularity. The methodologies that have stood out are the Functional and Logical Approaches. The former is based on Functions and Lambda Calculus, while the latter is based on Horn Clause

18 Logic. Each of them has its own advantages and aw's. How does one choose which ap-
19 proach to adopt? Perhaps one does not need to choose! This document looks at the at-
20 tempts, improvements and future possibilities of uniting HASKELL, a Purely Functional
21 Programming Language and PROLOG, a Logical Programming Language so that one is not
22 forced to choose.

23 **1.3 Thesis Statement**

24 The thesis aims to provide insights into merging two declarative languages namely, HASKELL
25 and PROLOG by embedding the latter into the former and analysing the result of doing so as
26 they have conflicting characteristics. The finished product will be something like a *haskel-*
27 *lised* PROLOG which has logical programming like capabilities.

28 **1.4 Problem Statement**

29 Over the years the development of programming languages has become more and more
30 rapid. Today the number of is in the thousands and counting. The successors attempt to
31 introduce new concepts and features to simplify the process of coding a solution and assist
32 the programmer by lessening the burden of carrying out standard tasks and procedures. A
33 new one tries to capture the best of the old; learn from the mistakes, add new concepts
34 and move on; which seems to be good enough from an evolutionary perspective. But all
35 is not that straight forward when shifting from one language to another. There are costs
36 and incompatibilities to look at. A language might be simple to use and provide better
37 performance than its predecessor but not always be worth the switch.

38 PROLOG is a language that has a hard time being adopted. Born in an era where proce-
39 dural languages were receiving a lot of attention, it suered from competing against another
40 new kid on the block: C. Some of the problems were of its own making. Basic features
41 like modules were not provided by all compilers. Practical features for real world problems

42 were added in an ad hoc way resulting in the loss of its purely declarative charm. Some say
43 that PROLOG is fading away, [?, ?, ?]. It is apparently not used for building large programs
44 [?, ?, ?]. However there are a lot of good things about Prolog: it is ideal for search prob-
45 lems; it has a simple syntax, and a strong underlying theory. It is a language that should
46 not die away.

47 So the question is how to have all the good qualities of PROLOG without actually using
48 PROLOG?

49 Well one idea is to make PROLOG an add-on to another language which is widely used
50 and in demand. Here the choice is HASKELL; as both the languages are declarative they
51 share a common background which can help to blend the two.

52 Generally speaking, programming languages with a wide scope over problem domains
53 do not provide bespoke support for accomplishing even mundane tasks. Approaching to-
54 wards the solution can be complicated and tiresome, but the programming language in
55 question acts as the master key.

56 Flipping the coin to the other side we see, the more specific the language is to the
57 problem domain the easier it is to solve the problem. The simple reason being that, the
58 problem need not be moulded according to the capability of the language. For example a
59 problem with a naturally recursive solution cannot take advantage of tail recursion in many
60 imperative languages. Many problems require the system to be mutation free, but have to
61 deal with uncontrolled side-effects and so on.

62 Putting all of the above together, Domain Specific Languages are pretty good in doing
63 what they are designed to do, but nothing else, resulting in choosing a different language
64 every time. On the other hand, a general purpose language can be used for solving a wide
65 variety of problems but many a times, the programmer ends up writing some code dictated
66 by the language rather than the problem.

67 The solution, a programming language with a split personality, in our case, sometimes
68 functional, sometimes logical and sometimes both. Depending upon the problem, the lan-

69 guage shapes itself accordingly and exhibits the desired characteristics. The ideal situation
70 is a language with a rich feature set and the ability to mould itself according to the problem.
71 A language with ability to take the appropriate skill set and present it to the programmer,
72 which will reduce the hassle of jumping between languages or forcibly trying to solve a
73 problem according to a paradigm.

74 The subject in question here is HASKELL and the split personality being PROLOG. How
75 far can HASKELL be pushed to dawn the avatar of PROLOG ? is the million dollar question.

76 The above will result in a set of characteristics which are from both the declarative
77 paradigms.

78 This can be achieved in two ways,

79 **Embedding ([Chapter 4](#)):** This approach involves, translating a complete language into
80 the host language as an extension such as a library and/ or module . The result is
81 very shallow as all the positives as well as the negatives are brought into the host
82 language. The negatives mentioned being, that languages from different paradigms
83 usually have conflicting characteristics and result in inconsistent properties of the
84 resulting embedding. Examples and further discussion on the same is provided in the
85 chapters to come.

86 **Paradigm Integration ([Chapter 5](#)):** This approach goes much deeper as it does not in-
87 involve a direct translation. An attempt is made by taking a particular characteristic
88 of a language and merging it with the characteristic of the host language in order to
89 eliminate conflicts resulting in a multi paradigm language. It is more of weaving the
90 two languages into one tight package with the best of both and maybe even the worst
91 of both.

92 **1.5 Thesis Organization**

93 The next chapter, [Chapter 2](#) provides details about the short comings of the previous works
94 and the road to a better future. [Chapter 3](#), the background talks about the programming
95 paradigms and languages in general and the ones in question. Then we look at the ques-
96 tion from different angles namely, [Chapter 4](#), Embedding a Programming Language into
97 another Programming Language and [Chapter 5](#), Multi Paradigm Languages (Functional
98 Logic Languages). Some of the indirectly related content [Chapter 6](#) and finishing off with
99 the [Chapter 7](#), the expected outcomes.

100 **1.6 Chapter Recap**

Chapter 2

Background

2.1 What is this chapter about

Programming Languages fall into different categories also known as "paradigms". They exhibit different characteristics according to the paradigm they fall into. It has been argued [?] that rather than classifying a language into a particular paradigm, it is more accurate that a language exhibits a set of characteristics from a number of paradigms. Either way, the broader the scope of a language the more the expressibility or use it has.

Programming Languages that fall into the same family, in our case declarative programming languages, can be of different paradigms and can have very contrasting, conflicting characteristics and behaviours. The two most important ones in the family of declarative languages are the Functional and Logical style of programming.

Functional Programming, [?] gets its name as the fundamental concept is to apply mathematical functions to arguments to get results. A program itself consists of functions and functions only which when applied to arguments produce results without changing the state that is values on variables and so on. Higher order functions allow functions to be passed as arguments to other functions. The roots lie in λ -calculus [?], a formal system in mathemat-

119 ical logic and computer science for expressing computation based on function abstraction
120 and application using variable binding and substitution. It can be thought as the smallest
121 programming language [?], a single rule and a single function definition scheme. In par-
122 ticular there are typed and untyped λ calculi. In the untyped λ calculus functions have no
123 predetermined type whereas typed lambda calculus puts restriction on what sort(type) of
124 data can a function work with. SCHEME is based on the untyped variant while ML and
125 HASKELL are based on typed λ calculus. Most typed λ calculus languages are based on
126 Hindley-Milner or Damas-Milner or Damas- Hindley-Milner [?] type system. The ability
127 of the type system to give the most general type of a program without any help (annotation).
128 The algorithm [?] works by initially assigning undefined types to all inputs, next check the
129 body of the function for operations that impose type constraints and go on mapping the
130 types of each of the variables, lastly unifying all of the constraints giving the type of the
131 result.

132 Logical Programming, [?] on the other hand is based on formal logic. A program is a
133 set of rules and formulæ in symbolic logic that are used to derive new formulas from the
134 old ones. This is done until the one which gives the solution is not derived.

135 The languages to be worked with being HASKELL and PROLOG respectively. Some
136 differences include things like, HASKELL uses Pattern Matching while PROLOG uses Uni-
137 fication, HASKELL is all about functions while PROLOG is on Horn Clause Logic and so
138 on.

139 PROLOG [?] being one of the most dominant Logic Programming Languages has spawned
140 a number of distributions and is present from academia to industry.

141 HASKELL is one the most popular [?] functional languages around and is the first lan-
142 guage to incorporate Monads [?] for safe *IO*. Monads can be described as composable
143 computation descriptions [?] . Each monad consists of a description of what has action
144 has to be executed, how the action has to be run and how to combine such computations.
145 An action can describe an impure or side-effecting computation, for example, *IO* can be

146 performed outside the language but can be brought together with pure functions inside in
147 a program resulting in a separation and maintaining safety with practicality. HASKELL
148 computes results lazily and is strongly typed.

149 The languages taken up are contrasting in nature and bringing them onto the same plate
150 is tricky. The differences in typing, execution, working among others lead to an altogether
151 mixed bag of properties.

152 The selection of languages is not uncommon and this not only the case with HASKELL,
153 PROLOG seems to be the all time favourite for "let's implement PROLOG in the language X
154 for proving it's power and expressibility". The PROLOG language has been partially imple-
155 mented [?] in other languages like SCHEME [?], LISP [?, ?, ?], JAVA [?, ?], JAVASCRIPT
156 [?] and the list [?] goes on and on.

157 The technique of embedding is a shallow one, it is as if the embedded language floats
158 over the host. Over time there has been an approach that branches out, which is Paradigm
159 Integration. A lot of work has been done on Unifying the Theories of Programming [?, ?,
160 ?, ?, ?, ?]. All sorts of hybrid languages which have characteristics from more than one
161 paradigm are coming into the mainstream.

162 Before moving on, let us take a look at some terms related to the content above. To
163 begin with Foreign Function Interfaces (FFI) [?], a mechanism by which a program written
164 in one programming language can make use of services written in another. For example, a
165 function written in C can be called within a program written in HASKELL and vice versa
166 through the FFI mechanism. Currently the HASKELL foreign function interface works only
167 for one language. Another notable example is the Common Foreign Function Interface
168 (CFFI) [?] for LISP which provides fairly complete support for C functions and data. JAVA
169 provides the Java Native Interface(JNI) for the working with other languages. Moreover
170 there are services that provide a common platform for multiple languages to work with
171 each other and run their programs. They can be termed as multi lingual run times which
172 lay down a common layer for languages to use each others functions. An example for this

173 is the Microsoft Common Language Runtime (CLR) [?] which is an implementation of the
174 Common Language Infrastructure (CLI) standard [?].

175 Another important concept is meta programming [?], which involves writing computer
176 programs that write or manipulate other programs. The language used to write meta pro-
177 grams is known as the meta language while the the language in which the program to be
178 modified is written is the object language. If both of them are the same then the language
179 is said to be reflective. HASKELL programs can be modified using Template HASKELL
180 [?] an extension to the language which provides services to jump between the two types of
181 programs. The abstract syntax trees in the form of HASKELL data types can be modified at
182 compile time which playing with the code and going back and forth.

183 A specific tool used in meta programming is quasi quotation [?, ?, ?], permits HASKELL
184 expressions and patterns to be constructed using domain specific, programmer-defined con-
185 crete syntax. For example, consider a particular application that requires a complex data
186 type. To accommodate the same it has to be represented using HASKELL syntax and preform-
187 ing pattern matching may turn into a tedious task. So having the option of using specific
188 syntax reduces the programmer from this burden and this is where a quasi-quoter comes
189 into the picture. Template HASKELL provides the facilities mentioned above. For example,
190 consider the following code in PROLOG to append two lists, going through the code, the
191 first rule says that an empty list appended with any list results in the list itself. The second
192 predicate matches the head of the first and the resulting lists and then recurs on the tails.
193 The same in HASKELL,

```
1 append(Ps, Qs, Rs) = (Ps = [] & Qs = Rs) ||  
2   ( X, Xs, Ys -> Ps = [X|Xs] &  
3     Rs = [X|Ys] &  
4     append(Xs, Qs, Ys))
```

194 Consider the Object Functional Programming Language, SCALA [?], it is purely func-
195 tional but with objects and classes. With the above in mind, coming back to the problem

196 of implementing PROLOG in HASKELL. There have been quite a few attempts to "merge"
197 the two programming languages from different programming paradigms. The attempts fall
198 into two categories as follows,

- 199 1. Embedding, where PROLOG is merely translated to the host language HASKELL or
200 a Foreign Function Interface.
- 201 2. Paradigm Integration, developing a hybrid programming language that is a Func-
202 tional Logic Programming Language with a set of characteristics derived from both
203 the participating languages.

204 The approaches listed above are next in line for discussions.

205 **2.2 Chapter Recap**

206 Chapter 3

207 Accomplished Work

208 3.1 What is this chapter about

210 3.2 Current Work

211 There have been several attempts at embedding PROLOG into HASKELL which are dis-
212 cussed below along with the shortcomings.

213 1. Very few embedded implementations exist which offer a perspective into the job
214 at hand. One of the earliest implementations [?] is for an older specification of
215 HASKELL called HASKELL 98 hugs. It is more of a proof of concept providing a
216 mechanism to include variable search strategies in order to produce a result. Another
217 implementation [?] based of it simplifies the notation to a list format. Nonetheless,
218 both implementations lack simplicity and support for basic PROLOG features such as
219 *cuts*, *fails*, *assert* among others.

220 2. The papers that try to take the above further are also few in number and do not
221 have any implementations with the proposed concepts. Moreover, none of them are

222 complete and most lack many practical parts of PROLOG.

- 223 3. In the case of libraries, a few exist, most are old and are not currently maintained or
224 updated. Many provide only a shell through which one has to do all the work, which
225 is synonymous with the embeddings mentioned above. Some are far more feature
226 rich than others that is with some practical PROLOG concepts, but are not complete.
- 227 4. Moreover, none of the above have full list support that exist in PROLOG.

228 And as far as the idea of merging paradigms goes, it is not the main focus of this
229 thesis and can be more of an "add-on". A handful of crossover hybrid languages based
230 on HASKELL exist, CURRY [?] being the prominent one. Moving away from HASKELL
231 and exploring other languages from different paradigms, a respectable number of crossover
232 implementations exist but again most of them have faded out.

233 As discussed in the sections above, either an embedding or an integration approach is
234 taken up for programming languages to work together. So, there is either a very shallow
235 approach that does not utilize the constructs available in the host language and results in a
236 mere translation of the characteristics, or the other is a fairly complex process which results
237 in tackling the conflicting nature of different programming paradigms and languages, re-
238 sulting in a toned-down compromised language that takes advantages of neither paradigms.
239 Mostly the trend is to build a library for extension to replicate the features as an add on.

240 3.3 Contributions

241 Taking into consideration above, there is quite some room for improvement and additions.
242 Moving onto what this thesis shall explore, first thing's first a complete, fully functional
243 library which comes close to a PROLOG like language and has practical abilities to carry
244 out real-world tasks. They include predicates like *cut*, *assert*, *fail*, *setOf*, *bagOf* among
245 others. This would form the first stage of the implementation. Secondly, exploring aspects

246 such as *assert* and database capabilities. A third question to address is the accommodation
247 of input and output, specifically dealing with the *IO Monad* in HASKELL with PROLOG *IO*.
248 Moreover, PROLOG is an untyped language which allows lists with elements of different
249 types to be created. Something like this is not by default in HASKELL. Hence syntactic
250 support for the same is the next question to address. Furthermore, experimenting with how
251 programs expressed with same declarative meaning differ operationally. Lastly, how would
252 characteristics of hybrid languages fit into and play a role in an embedded setting.

253 3.4 Improved Contributions

254 1. Most languages have a recursive abstract syntax which restricts the eDSL in terms of
255 its capability to *open up* the language i.e. to include meta syntactic variables, adding
256 custom quantifiers and logic. ([Prototype 1](#)) provides a methodology to convert a
257 language whose recursive abstract syntax is represented by a tree into a non-recursive
258 version whose fixed point is isomorphically equivalent to the original type. One of
259 the outcomes is a polymorphically typed embedded language within HASKELL

260 To test it out we adopt the closed PROLOG like language defined in [?] and open
261 it up. And for the unification part we use [?], which provides a generic unification
262 algorithm implementation encapsulated into a monad.

263 2. ([Prototype 2](#)) does the what a PROLOG query resolver would do given a query and a
264 knowledge base. The mechanism for the same is adopted from [?]. The embedded
265 language is modified as per the procedure in ([Prototype 1](#)) and the monadic unifica-
266 tion part is plugged into the existing architecture to demonstrate that it is independent
267 of the other components. Lastly the result is converted into the original language via
268 a translate function.

269 3. ([Prototype 3](#)) demonstrates the modularity of the unification process of the query

270 resolver with multiple search strategies.

271 4. [\(Prototype 4\)](#) throws light on how IO operations can be embedded into the abstract
272 syntax of a DSL which when interpreted would produce output consisting of a pure
273 set of instructions irrespective of the nature of the construct. The effects are only
274 produced only when the actions are executed.

275 **3.5 Thesis Contributions**

276 1. Prototype 1 does flattening language opening up the language (binding monad) adding
277 custom variables monadic unification (stuff happens in a bubble) $\text{rec type} \rightarrow \text{non rec}$
278 $\text{type} \rightarrow \text{fix non rec type isomorphically} == \text{rec type}$

279 You can make an Flatterm int

280 but you cannot make term int

281 adding quantifiers

282 2. Prototype 2 does extends current prolog-0.2.0.1 this is to show that we can plug out
283 approach into existing implementation and things work

284 3. Prototype 3 does variable search strategy what ever method you do for searching at
285 the point of unification you can do it with our approach

286 4. Prototype 4 does how can io be squeezed into this model where whenever the resolver
287 encounters an io operation it generates a thunk (sort of unsolved statement) which
288 when executed would result in a side effect but till that point every thing is pure

289 **3.6 What work was done in terms of points**

290 1. Literature review on eDSL's.

- 291 2. Short survey on multi paradigm declarative languages.
- 292 3. Accumulated and evaluated PROLOG in HASKELL.
- 293 4. Defined a procedure to open up a language starting from a generic recursive abstract
294 syntax.
- 295 5. Made a few libraries to work together.
- 296 6. Some stuff for monadic unification.
- 297 7. Something to show it was modular and independent of the original grammar.
- 298 8. Something to show that the unification part is independent of the search strategy and
299 hence multiple ones can be used, possibly simultaneously to find a solution.
- 300 9. Creating a micro language to represent and encapsulate IO operation in an eDSL so
301 that the it remains pure even after interpretation and only produces side effects when
302 the action is actually executed and hence in some way it can be controlled.

303 **3.7 Chapter Recap**

304 **3.8 What is this chapter about**

305

306 **Chapter 4**

307 **Embedding a Programming Language** 308 **into another Programming Language**

309 The art of embedding a programming language into another one has been explored a num-
310 ber of times in the form of building libraries or developing Foreign Function Interfaces and
311 so on. This area mainly aims at an environment and setting where two or more languages
312 can work with each other harmoniously with each one able to play a part in solving the
313 problem at hand. This chapter mainly reviews the content related to embedding PROLOG
314 in HASKELL but also includes information on some other implementations and embedding
315 languages in general.

316 **4.1 The Informal Content from Blogs, Articles and Inter-** 317 **net Discussions**

318 Before moving on to the formal content such as publications, modules and libraries let's
319 take a look at some of the unofficially published content. This subsection takes a look at
320 the information, thoughts and discussions that are currently taking place from time to time
321 on the internet. A lot of interesting content is generated which has often led to some formal

322 content.

323 A lot has been talked about embedding languages and also the techniques and methods
324 to do so. It might not seem such a hot topic as such but it has always been a part of any pro-
325 gramming language to work and integrate their code with other programming languages.
326 One of the top discussions are in, Lambda the Ultimate, The Programming Languages
327 Weblog [?], which lists a number of PROLOG implementations in a variety of languages
328 like LISP, SCHEME, SCALA, JAVA, JAVASCRIPT, RACKET [?] and so on. Moreover the
329 discussion focusses on a lot of critical points that should be considered in a translation of
330 PROLOG to the host language regarding types and modules among others.

331 One of the implementations discussed redirects us to one of the most earliest imple-
332 mentations of PROLOG in HASKELL for Hugs 98, called Mini PROLOG [?]. Although this
333 implementation takes as reference the working of the PROLOG Engine and other details,
334 it still is an unofficial implementation with almost no documentation, support or ongoing
335 development. Moreover, it comes with an option of three engines to play with but still lacks
336 complete list support and a lot of practical features that PROLOG has and this seems to be
337 a common problem with the only other implementation that exists, [?].

338 Adding fuel to fire, is the question on PROLOG's existence and survival [?, ?, ?, ?]
339 since its use in industry is far scarce than the leading languages of other paradigms. The
340 purely declarative nature lacks basic requirements such as support for modules. And then
341 there is the ongoing comparison between the siblings [?] of the same family, the family
342 of Declarative Languages. Not to forget HASKELL also has some tricks [?] up its sleeve
343 which enables encoding of search problems.

344 4.2 Related Books

345 As HASKELL is relatively new in terms of being popular, its predecessors like SCHEME
346 have explored the territory of embedding quite profoundly [?], which aims at adding a few

constructs to the language to bring together both styles of Declarative Programming and capture the essence of PROLOG. Moreover, HASKELL also claims for it to be suitable for basic Logic Programming naturally using the List Monad [?]. A general outlook towards implementing PROLOG has also been discussed by [?] to push the ideas forward.

4.3 Related Papers

There is quite some literature that can be found and which consist of embedding detailed parts of Prolog features like basic constructs, search strategies and data types. One of the major works is covered by the subsection below consisting of a series of papers from Mike Spivey and Silvija Seres aimed at bring Haskell and Prolog closer to each other. The next subsection covers the literature based on the above with improvements and further additions.

- Papers from Mike Spivey and Silvija Seres

The work presented in the series [?, ?, ?, ?, ?] attempts to encapsulate various aspects of an embedding of PROLOG in HASKELL. Being the very first documented formal attempt, the work is influenced by similar embeddings of PROLOG in other languages like SCHEME and LISP. Although the host language has distinct characteristics such as lazy evaluation and strong type system the proposed scheme tends to be general as the aim here is to achieve PROLOG like working not a multi paradigm declarative language. PROLOG predicates are translated to HASKELL functions which produce a stream of results lazily depicting depth first search with support for different strategies and practical operators such as *cut* and *fail* with higher order functions. The papers provide a minimalistic extension to HASKELL with only four new constructs. Though no implementation exists, the synthesis and transformation techniques for functional programs have been *logicalised* and applied to PROLOG programs. Another related work [?] looks through conventional data types so as to adapt to the

372 problems at hand so as to accommodate and jump between search strategies.

373 • Other works related or based on the above

374 Continuing from above, [?] taps into the advantages of the host language to em-
375 bed a typed functional logic programming language. This results in typed logical
376 predicates and a backtracking monad with support for various data types and search
377 strategies. Though not very efficient nor practical the method aims at a more ele-
378 gant translation of programs from one language to the other. While other papers [?]
379 attempt at exercising HASKELL features without adding anything new rather doing
380 something new with what is available. Specifically speaking, using HASKELL type
381 classes to express general structure of a problem while the solutions are instances.
382 [?] replicates PROLOG's control operations in HASKELL suggesting the use of the
383 HASKELL *State Monad* to capture and maintain a global state. The main contribu-
384 tions are a Backtracking Monad Transformer that can enrich any monad with back-
385 tracking abilities and a monadic encapsulation to turn a PROLOG predicate into a
386 HASKELL function.

387 4.4 Related Libraries in Haskell

388 • Prolog Libraries

389 To replicate Prolog like capabilities Haskell seems to be already in the race with a
390 host of related libraries. First we begin with the libraries about Prolog itself, a few
391 exist [?] being a preliminary or "mini Prolog" as such with not much in it to be able
392 to be useful, [?] is all powerful but is an Foreign Function Interface so it is "Prolog in
393 Haskell" but we need Prolog for it, [?] which is the only implementation that comes
394 the closest to something like an actual practical Prolog. But all they give is a small
395 interpreter, none or a few practical features, incomplete support for lists, minor or no
396 monadic support and an REPL without the ability to "write a Prolog Program File".

397 • Logic Libraries

398 The next category is about the logical aspects of Prolog, again a handful of libraries
399 do exist and provide a part of the functionality which is related propositional logic
400 and backtracking. [?] is a continuation-based, backtracking, logic programming
401 monad which sort of depicts Prolog's backtracking behaviour. Prolog is heavily
402 based on formal logic, [?] provides a powerful system for Propositional Logic. Oth-
403 ers include small hybrid languages [?] and Parallelising Logic Programming and Tree
404 Exploration [?].

405 • Unification Libraries

406 The more specific the feature the lesser the support in Haskell. Moving on to the
407 other distinct feature of Prolog is Unification, two libraries exist [?], [?] that unify
408 two Prolog Terms and return the resulting substitution.

409 • Backtracking

410 Another important aspect of PROLOG is backtracking. To simulate it in HASKELL,
411 the libraries [?, ?] use monads. Moreover, there is a package for the EGISON pro-
412 gramming language [?] which supports non-linear pattern-matching with backtrack-
413 ing.

414 4.5 From chap 7

415 Embedding a language into another language has been explored with a variety of languages.
416 Attempts have been made to build Domain Specific Languages from the host languages [?],
417 Foreign Function Interfaces [?]

418 Creating a programming language from scratch is a tedious task requiring ample amount
419 of programming, not to mention the effort required in designing. A typical procedure would
420 consist of formulating characteristics and properties based on the following points,

- 421 1. Syntax
- 422 2. Semantics
- 423 3. Standard Library
- 424 4. Runtime System
- 425 5. Parsers
- 426 6. Code Generators
- 427 7. Interpreters
- 428 8. Debuggers

429 A lot of the above can be skipped or taken from the base language if an embedding ap-
430 proach is chosen. For an embedded domain specific language the functionality is translated
431 and written as an add on. The result can be thought of as a library. But the difference be-
432 tween an ordinary library and an eDSL is the feature set provided and the degree of embed-
433 ding [?]. For example, reading a file and parsing its contents to perform certain operations
434 to return *string* results is a shallow form of embedding as the generation of code, results is
435 not native nor are the functions processing them dealing with embedded data types as such.
436 On the other hand, building data structures in the base language which represent the target
437 language expression would be called a deep embedding approach.

438 The snippet of HASKELL code below describes PROLOG entities,

```
1 data Term = Struct Atom [Term]
2           | Var VariableName
3           | Wildcard
4           | PString    !String
5           | PInteger   !Integer
6           | PFloat     !Double
7           | Flat [FlatItem]
8           | Cut Int
9 deriving (Eq, Data, Typeable)
```

439 The above can be described as concrete syntax for the "new" language and can be used
440 to write a program.

441 As discussed in the

442 **4.6 Theory**

443 1. Papers

- 444 (a) Embedding an interpreted language using higher-order functions, [?]
- 445 (b) Building domain-specific embedded languages, [?]
- 446 (c) Embedded interpreters, [?]
- 447 (d) Cayenne – a Language With Dependent Types, [?]
- 448 (e) Foreign interface for PLT Scheme, [?]
- 449 (f) Dot-Scheme: A PLT Scheme FFI for the .NET framework, [?]
- 450 (g) Application-specific foreign-interface generation, [?]
- 451 (h) Embedding S in other languages and environments, [?]

452 2. Books

- 453 (a) ?????????

454 3. Articles / Blogs / Discussions

- 455 (a) Embedding one language into another, [?]
- 456 (b) Application-specific foreign-interface generation, [?]
- 457 (c) Linguistic Abstraction, [?]
- 458 (d) LISP, Unification and Embedded Languages, [?]

459 4. Websites

- 460 (a) Embedding SWI-Prolog in other applications, [?]

461 **4.7 Implementations**

- 462 1. Lots of them I guess

463 **4.8 Important People**

- 464 1. ????

465 **4.9 Miscellaneous / Possibly Related Content**

- 466 1. ????

467 **4.10 Chapter Recap**

468 **Chapter 5**

469 **Multi Paradigm Languages (Functional** 470 **Logic Languages)**

471 **5.1 What is this chapter about**

472

473 Over the years another approach has branched off from embedding languages, to merge
474 and/or integrate programming languages from different paradigms. Let us take an exam-
475 ple of the SCALA Programming Language [?], a hybrid Object-Functional Programming
476 Language which takes a leaf from each of the two books. In this thesis, the languages in
477 question are HASKELL and PROLOG. This section takes a look at the literature on Multi
478 Paradigm Languages, mainly Functional Logic Programming Languages that combine two
479 of the most widespread Declarative Programming Styles.

480 A peak into language classification reveals that it is not always a straight forward task to
481 segregate languages according to their features and/or characteristics. Turns out that there
482 are a number of notions which play a role in deciding where the language belongs. Many
483 a times a language ends up being a part of almost all paradigms due extensive libraries.
484 Simply speaking, a multi-paradigm programming language is a programming language that

485 supports more than one programming paradigm [?], more over as Timothy Budd puts it [?]
486 ”The idea of a multi paradigm language is to provide a framework in which programmers
487 can work in a variety of styles, freely intermixing constructs from different paradigms.”

488 **5.2 The Informal Content from Blogs, Articles and Inter-** 489 **net Discussions**

490 • Multi Paradigm Languages

491 A lot has been talked and discussed on coming to clear grounds about the classifica-
492 tion of programming languages. If the conventional ideology is considered then the
493 scope of each language is pretty much infinite as small extension modules replicate
494 different feature sets which are not naturally native to the language itself. The defi-
495 nitions of multi paradigm languages across the web [?, ?, ?] converge to roughly the
496 same thing that of providing a framework to work with different styles with a list of
497 languages [?, ?] that ticks the boxes. Generally speaking, it does not feel all that hot
498 or popular in programming circles; one reason could be that it is a very broad topic
499 and specifying details can clear the fog.

500 • Functional Logic Programming Languages

501 Continuing from the previous section, narrowing down the search by considering
502 only multi paradigm declarative languages namely, Functional Logical programming
503 languages. By doing so a large amount of information pops up, from articles that
504 give brief description and mentions [?, ?] to the implementing techniques [?] which
505 give a brief overview of the aim and also the backdrop of publications.

506 The jackpot however is the fact that there is a dedicated website [?] for the history,
507 research and development, existing languages, the literature, the contacts and every-
508 thing else that one can think of for functional logic languages. As a matter of fact the

509 holy grail of information is maintained by two of the most important people in the
510 field Michael Hanus [?] and Sergio Antoy [?].

511 **5.3 Literature and Publications**

512 • Multi Paradigm Languages

513 Possibly one of the most important works towards bringing programming styles to-
514 gether is the book by C.A.R. Hoare [?] which points out that among the large number
515 of programming paradigms and/or theories the unification theory serves as a comple-
516 mentary rather than a replacement to relate the universe. As as always since we
517 are talking about HASKELL we have to include monads and unifying theories using
518 monads [?].

519 • Functional Logic Programming Languages

520 A recent survey [?] throws light on these hybrid languages.

521 One of the most prominent multi paradigm languages in HASKELL is CURRY [?].
522 Th syntax is borrowed from the parent language and so are a lot of the features.
523 Taking a recap, a functional programming language works on the notion of mathe-
524 matical functions while a logic programming language is based on predicate logic.
525 The strong points of CURRY are that the features or basis of the language are general
526 and are visible in a number of languages like [?]. The language can play with prob-
527 lems from both worlds. In a problem where there are no unknowns and/or variables
528 the language behaves like a functional language which is pattern matching the rules
529 and execute the respective bodies. In the case of missing information, it behaves
530 like PROLOG; a sub-expression e is evaluated on the conditions that it should satisfy
531 which constraint the possible values of e . This brings us to the first important fea-
532 ture of functional logic languages *narrowing*. The expressions contain *free variables*;

533 simply speaking incomplete information that needs to be *unified* to a value depending
534 on the constraints of the problem. The language introduces only a few new constructs
535 to support non determinism and choice. Firstly, *narrowing* ($=:=$), which deals with
536 the expressions and unknown values and binds them with appropriate values. The
537 next one is the *choice* operator (?) for non-deterministic operations. Lastly, for uni-
538 fying variables and values under some conditions, (&) operator has been provided to
539 add constraints to the equation. Putting it all together, it gives us the feel of a logic
540 language for something that looks very much like HASKELL. Unification is like two
541 way pattern matching and with a similar analogy CURRY is a HASKELL that works
542 both ways and hence variables can be on either sides. Although the language can do
543 a lot but gaps do exist such as the improvement of narrowing techniques.

544 **5.4 Some Multi Paradigm Languages**

545 The list of multi paradigm languages is huge, but in this thesis we will mostly stick to Func-
546 tional Logical programming languages. Beginning with functional hybrids, a small project
547 language called VIRGIL [?], combining objects to work with functions and procedures. On
548 similar lines is COMMON OBJECT LISP SYSTEM (CLOS) [?]. This can be justified as
549 object oriented programming has been one of the most dominant styles of programming
550 and hence even HASKELL has one called O'HASKELL [?] though it last saw a release back
551 in 2001. Another prominent implementation is OCAML [?, ?] which adds object oriented
552 capabilities with a powerful type system and module support. This is the case with most of
553 the languages in this section hardly a few have survived as the new ones incorporated the
554 positives of the old. As mentioned before one of the most popular [?] and widely usage both
555 in academia and industry is the SCALA [?] programming language stands out.

5.5 Functional Logic Programming Languages

Knowing that there is quite some amount of literature out there on these type of languages, it is fairly easy to say that there have been numerous attempts at specifications and/or implementations. Sadly though not many have survived leave alone being successful as a result of the competition. Only the ones that are easily available or have an implementation or have been cited or referred by other attempts have been included as the list is long and does not reflect the main intention of the document. Beginning with the ones from Australia, which seems to be a popular destination for fiddling with PROLOG and merging paradigms. As of now there have been three popular ones, beginning with NEU PROLOG, [?], OZ (MOZART PROGRAMMING SYSTEM) [?] and MERCURY [?]. Delving deeper the languages feel more like extensions of PROLOG rather than hybrids. Starting with MERCURY which a boundary between deterministic and non-deterministic programs, similarly NUE PROLOG has special support for functions while OZ gives concurrent constraint programming plus distributed support, with different function types for goal solving and expression rewriting. ESCHER [?] comes very close to HASKELL with monads, higher order functions and lazy evaluation. Taking a look at PROLOG variants, CIAO [?]; a preprocessor to PROLOG for functional syntax support, λ PROLOG [?] aims at modular higher order programming with abstract data types in a logical setting, BABEL [?, ?, ?] combines pure PROLOG with a first order functional notation, LIFE [?] is for Logic, Inheritance, Functions and Equations in PROLOG syntax with currying and other features like functional languages and others [?, ?].

The functional language SCHEME is a very popular choice for this sort of a thing. With a book [?] and an implementation to accompany [?, ?] which seems to have translated into HASKELL, [?, ?, ?].

Finally talking about CURRY, one of the most popular HASKELL based multi paradigm languages with support for deterministic and non-deterministic computations. Contributing to the same there have been some predecessors [?, ?].

583 **5.6 From chap 9**

584 Unifying / Marrying / Merging / Combining Programming Paradigms / Theories

585 **5.7 Theory**

586 • Papers

- 587 1. Unifying Theories of Programming with Monads, [?]
- 588 2. Symposium on Unifying Theories of Programming, 2006, [?].
- 589 3. Symposium on Unifying Theories of Programming, 2008, [?].
- 590 4. Symposium on Unifying Theories of Programming, 2010, [?].
- 591 5. Symposium on Unifying Theories of Programming, 2012, [?].

592 • Books

- 593 1. Unifying Theories of Programming, [?]

594 • Articles / Blogs / Discussions

- 595 1. ???

596 • Websites

- 597 1. ???

598 **5.8 Implementations**

- 599 1. Scala
- 600 2. Virgil
- 601 3. CLOS, Common Lisp Object System

602 4. Visual Prolog

603 5. ???

604 **5.9 Miscellaneous / Possibly Related Content**

605 1. ???

606 **5.10 Chapter Recap**

Chapter 6

Related Concepts

6.1 What is this chapter about

There are some technicalities which are indirectly related to the problem but do not bare a point of contact. The underpinnings of the languages throw some more light on the how different languages work to solve a problem. Different programming paradigms incorporate different operational mechanisms. For example, PROLOG programs execute on the Warren Abstract Machine [?] which has three different storage usages; a global stack for compound terms, for environment frames and choice points and lastly the trail to record which variables bindings ought to be undone on backtracking.

Constraint programming [?] is closely related to the declarative programming paradigm in the sense that the relations between variables is specified in the form of constraints. For example, consider a program to solve a simultaneous equation, now adding on to that restricting the range of the values that the variables can possible take, thus adding constraints to the possible solutions. Related to the same are Constraint Handling Rules [?], which are extensions to a language, simply speaking adding constraints to a language like PROLOG.

Lastly some details on the working of functional logic programming languages, resid-

625 uation and narrowing [?, ?]. Residuation involves delaying of functions calls until they are
626 deterministic, that is, deterministic reduction of functions with partial data. This principle
627 is used in languages like ESCHER [?], LIFE [?], NUE-PROLOG [?] and OZ [?]. Narrowing
628 on the other hand is a mixture of reduction in functional languages and unification in logic
629 languages. In narrowing, a variable is bound a value within the specified constraints and
630 try to find a solution, values are generated while searching rather than just for testing. The
631 languages based on this approach are ALF [?], BABEL [?], LPG [?] and CURRY [?].

632 F-Algebras

633 We are now ready to define F-algebras in the most general terms. First I'll use the
634 language of category theory and then quickly translate it to HASKELL.

635 An F-algebra consists of:

- 636 1. an endofunctor F in a category C,
- 637 2. an object A in that category, and
- 638 3. a morphism from F(A) to A.

639 An F-algebra in HASKELL is defined by a functor f, a carrier type a, and a function
640 from (f a) to a. (The underlying category is Hask.)

641 Right about now the definition with which I started this post should start making sense:

```
type Algebra f a = f a -> a
```

642 For a given functor f and a carrier type a the algebra is defined by specifying just one
643 function. Often this function itself is called the algebra, hence my use of the name alg in
644 previous examples.

645 6.2 Chapter Recap

646 **Chapter 7**

647 **Prolog in _____ other languages**

648 Prolog in _____

649 **7.1 Theory**

650 • Papers

651 1. QLog, [?]

652 2. LogLisp Motivation, design, and implementation, [?]

653 • Books

654 1. Warrens Abstract Machine A TUTORIAL RECONSTRUCTION, [?]

655 2. LOGLISP: an alternative to PROLOG, [?]

656 • Articles / Blogs / Discussions

657 1. Hello

658 • Websites

659 1. Hello

660 **7.2 Implementations**

- 661 1. Castor : Logic paradigm for C++, [?]
- 662 2. GNU Prolog for Java, [?]
- 663 3. JLog - Prolog in Java, [?]
- 664 4. JScriptLog - Prolog in Java, [?]
- 665 5. Quintus Prolog, [?]
- 666 6. Yield Prolog, [?]
- 667 7. Racklog, [?]

668 **7.3 Important People**

- 669 1. ???

670 **7.4 Miscellaneous / Possibly Related Content**

- 671 1. ???

672 Chapter 8

673 Prolog in Haskell

674 Prolog in Haskell

675 8.1 Theory

676 • Papers

677 1. Embedding Prolog in Haskell / Functional Reading of Logic Programs, [?]

678 2. Algebra of Logic Programming, [?]

679 3. The Algebra of Logic Programming, [?]

680 4. Optimisation Problems in Logic Programming : An Algebraic Approach, [?]

681 5. Higher Order Transformation of Logic Programs, [?]

682 6. The Algebra of Searching, [?]

683 7. FUNCTIONAL PEARL Combinators for breadth-first search, [?]

684 8. Type Logic Variables, K Classen, [?]

685 9. A Type-Safe Embedding of Constraint Handling Rules into Haskell Wei-Ngan
686 Chin, Mar-tin Sulzmann and Meng Wang, [?]

687 10. Prological Features in a Functional Setting Axioms and Implementation, R
688 Hinze, [?]

689 11. Escape from Zurg: An Exercise in Logic Programming, [?]

690 • Books

691 1. The Reasoned Schemer, Daniel P. Friedman, William E. Byrd, Oleg Kiselyov,
692 [?]

693 2. Programming Languages: Application and Interpretation, Shriram Krishna-
694 murthi, Chapters 33-34 of PLAI discuss Prolog and implementing Prolog, [?]

695 • Articles / Blogs / Discussions

696 1. Lambda the Ultimate, Programming Languages, [?]

697 2. Takashi's Workplace (Implementation), [?]

698 3. Haskell vs. Prolog Comparison, [?]

699 • Websites

700 1. Logic Programming in Haskell, [?]

701 8.2 Implementations

702 1. A Prolog in Haskell, Takashi's Workplace, [?]

703 2. Mini Prolog for Hugs 98, [?]

704 3. Nano Prolog, [?]

705 4. Prolog, [?]

706 5. cspm-To-Prolog, [?]

- 707 6. prolog-graph, [?]
- 708 7. prolog-graph-lib, [?]
- 709 8. hswip, [?]

710 **8.3 Important People**

- 711 1. Mike Spivey
- 712 2. Silvija Seres

713 **8.4 Miscellaneous / Possibly Related Content**

- 714 1. Unification Libraries
 - 715 (a) unification-fd, [?]
 - 716 (b) cmu, [?]
- 717 2. Logic Libraries
 - 718 (a) logicct, [?], [?]
 - 719 (b) logic-classes, [?]
 - 720 (c) proplogic, [?]
 - 721 (d) cflp, [?]
 - 722 (e) logic-grows-on-trees, [?]
- 723 3. Concatenative Programming
 - 724 (a) peg, [?]
- 725 4. Constraint Programming and Constraint Handling Rules

- 726 (a) monadiccp, [?]
- 727 (b) monadicccp-gecode, [?]
- 728 (c) csp, [?]
- 729 (d) liquid fix point, [?]

730 **Chapter 9**

731 **Quasiquotation**

732 **9.1 Theory**

733 1. Papers

734 (a)

735 2. Books

736 (a)

737 3. Articles / Blogs / Discussions

738 (a)

739 4. Websites

740 (a) Quasiquotation Wikipedia, [?]

741 (b) Quasiquotation in Haskell, [?]

742 **9.2 Implementations**

743 1.

744 **9.3 Miscellaneous / Possibly Related Content**

745 1.

746 **9.4 What is Quasiquotation ?**

747 1. [?]

748 When language is used to attribute properties to language or otherwise theorize about
749 it, a linguistic device is needed that turns language on itself. Quotation is one such
750 device. It is our primary meta-linguistic tool.

751 2. [?]

752 a metalinguistic device for referring to the form of an expression containing variables
753 without referring to the symbols for those variables. Thus while "not p" refers to the
754 expression consisting of the word not followed by the letter p, the quasi-quotation
755 \ulcorner not p \urcorner refers to the form of any expression consisting of the word not followed by
756 any value of the variable p.

757 3. Quasiquotation Wikipedia, [?]

758 Quasi-quotation or Quine quotation is a linguistic device in formal languages that
759 facilitates rigorous and terse formulation of general rules about linguistic expressions
760 while properly observing the usemention distinction.

761 [?] The usemention distinction is a foundational concept of analytic philosophy,[1]
762 according to which it is necessary to make a distinction between using a word (or
763 phrase) and mentioning it

764 **9.5 Quasiquotaion in HASKELL**

765 [?, ?]

766 Quasiquoting allows programmers to use custom, domain-specific syntax to construct
767 fragments of their program. Along with HASKELL's existing support for domain specific
768 languages, you are now free to use new syntactic forms for your EDSLs.

769 Working with complex data types can impose a significant syntactic burden; extensive
770 applications of nested data constructors are often required to build values of a given data
771 type, or, worse yet, to pattern match against values.

772 Allow HASKELL expressions and patterns to be constructed using domain specific,
773 programmer-defined concrete syntax.

774 **9.6 Chapter Recap**

775 **9.7 What is this chapter about**

776

777 Chapter 10

778 Meta Syntactic Variables

779 Some sources for the topic

780 [?] A metasyntactic variable is a placeholder name used in computer science, a word
781 without meaning intended to be substituted by some objects pertaining to the context where
782 it is used. The word foo as used in IETF Requests for Comments is a good example. By
783 mathematical analogy, a metasyntactic variable is a word that is a variable for other words,
784 just as in algebra letters are used as variables for numbers. Any symbol or word which does
785 not violate the syntactic rules of the language can be used as a metasyntactic variable.

786 [?] A name used in examples and understood to stand for whatever thing is under dis-
787 cussion, or any random member of a class of things under discussion. The word foo is the
788 canonical example. To avoid confusion, hackers never (well, hardly ever) use foo or other
789 words like it as permanent names for anything. In filenames, a common convention is that
790 any filename beginning with a metasyntactic-variable name is a scratch file that may be
791 deleted at any time.

792 Metasyntactic variables are so called because they are variables in the metalanguage
793 used to talk about programs etc; they are variables whose values are often variables (as in
794 usages like the value of $f(\text{foo}, \text{bar})$ is the sum of foo and bar). However, it has been plausibly
795 suggested that the real reason for the term metasyntactic variable is that it sounds good. To

796 some extent, the list of one's preferred metasyntactic variables is a cultural signature. They
797 occur both in series (used for related groups of variables or objects) and as singletons. Here
798 are a few common signatures:

799 [?] In programming, a metasyntactic (which derives from meta and syntax) variable is
800 a variable (a changeable value) that is used to temporarily represent a function . Examples
801 of metasyntactic variables include (but are by no means limited to) ack, bar , baz, blarg,
802 wibble, foo , fum, and qux. Metasyntactic variables are sometimes used in developing a
803 conceptual version of a program or examples of programming code written for illustrative
804 purposes.

805 Any filename beginning with a metasyntactic variable denotes a scratch file. This means
806 the file can be deleted at any time without affecting the program.

807 [?]

808 A word, used in conversation or text that is meant as a variable. There is a fairly
809 standard set in the ComputerScience culture. People tend to create their own if they are not
810 exposed to others, which can be confusing. Of course, if you haven't seen them before they
811 can be quite confusing. They are, however, useful enough that this is not enough reason to
812 give them up. Standard set: foo, bar, baz, foobar/quux, quuux, quuuux,

813 example: "Suppose I have a list, foo, with a node, bar, ..."

814 **10.1 Chapter Recap**

Chapter 11

Haskell or Why Haskell ?

11.1 What is this chapter about

In this chapter we discuss the properties of HASKELL

This chapter discusses the properties of the host language HASKELL and mainly the feature set it provides for embedding domain specific languages(EDSLs).

1. Why a Functional Language?

2. HASKELL as a functional programming language Haskell is an advanced purely-functional programming language. In particular, it is a polymorphically statically typed, lazy, purely functional language [?]. It is one of the popular functional programming languages [?]. HASKELL is widely used in the industry [?].

Shifting a bit to Embedded Domain Specific Languages (EDSLs) such as Emacs LISP. Opting for embedding provides a "shortcut" to create a language which may be designed to provide specific functionality. Designing a language from scratch would require writing a parser, code generator / interpreter and possibly a debugger, not to mention all the routine stuff that every language needs like variables, control structures and arithmetic types. All of the aforementioned are provided by the host

833 language; in this case HASKELL. Examples for the same can be found here [?, ?]
834 which talk about introducing combinator libraries for custom functionality.

835 The flip side of the coin is that the host language enforces certain aspects and proper-
836 ties of the eDSL and hence might not be exact to specification, all required constructs
837 cannot be implemented due to constraints, programs could be difficult to debug since
838 it happens at the host level and so on.

839 3. Looking at HASKELL as a tool for embedding domain specific languages[?]

840 (a) Monads

841 Control flow defines the order/ manner of execution of statements in a pro-
842 gram[?]. The specification is set by the programming language. Generally, in
843 the case of imperative languages the control flow is sequential while for a func-
844 tional language is recursion [?]. For example, JAVA has a top down sequential
845 execution approach. The declarative style consists of defining components of
846 programs i.e. computations not a control flow[?].

847 This is where HASKELL shines by providing something called a *monad*. Func-
848 tional Programming Languages define computations which then need to be or-
849 dered in some way to form a combination[?]. A monad gives a bubble within
850 the language to allow modification of control flow without affecting the rest of
851 the universe. This is especially useful while handling side effects.

852 A related topic would be of persistence languages, architectures and data struc-
853 tures. Persistent programming is concerned with creating and manipulating data
854 in a manner that is independent of its lifetime [?]. A persistent data structure
855 supports access to multiple versions which may arise after modifications [?, ?].
856 A structure is partially persistent if all versions can be accessed but only the
857 current can be modified and fully persistent if all of them can be modified.

858 Coming back to control flow; for example, implementing backtracking in an

859 imperative language would mean undoing side effects which even PROLOG is
860 not able to do since the asserts and retracts cannot be undone. In HASKELL, a
861 monad defines a model for control flow and how side effects would propagate
862 through a computation from step to step or modification to modification. And
863 HASKELL allows creation of custom monads relieving the burden of dealing
864 with a fixed model of the host language.

865 (b) Lazy Evaluation

866 Another property of HASKELL is laziness or lazy evaluation which means that
867 nothing is evaluated until it is necessary. This results in the ability to define
868 infinite data structures because at execution only a fragment is used [?].

869 **11.2 Chapter Recap**

Chapter 12

Prolog or Why Prolog ?

12.1 What is this chapter about

This chapter discusses the properties of the target language PROLOG and the feature set that will be translated to the host language to extend its capabilities.

1. Why a Logic Programming Language ?
2. PROLOG as a logic programming language.

PROLOG is a general purpose logic programming language mainly used in artificial intelligence and computational linguistics. It is a Declarative language i.e. a program is a set of facts and rules running a query on which will return a result. The relation between them is defined by clauses using *Horn Clauses*[?]. PROLOG is very popular and has a number of implementations [?] for different purposes.

3. Why embed PROLOG ?

(a) Existing Implementations

As a starting point a few publications and implementations helped in exploring

886 the topic. The shortcomings were clearly visible to work and improve upon
887 giving a starting point.

888 (b) Simple Syntax [?]

889 Prolog is dynamically typed. It has a single data type, the term, which has
890 several subtypes: atoms, numbers, variables and compound terms.

891 An atom is a general-purpose name with no inherent meaning. It is composed
892 of a sequence of characters that is parsed by the Prolog reader as a single unit.

893 Numbers can be floats or integers. Many Prolog implementations also provide
894 unbounded integers and rational numbers.

895 Variables are denoted by a string consisting of letters, numbers and underscore
896 characters, and beginning with an upper-case letter or underscore. Variables
897 closely resemble variables in logic in that they are placeholders for arbitrary
898 terms. A variable can become instantiated (bound to equal a specific term) via
899 unification.

900 A compound term is composed of an atom called a "functor" and a number of
901 "arguments", which are again terms. Compound terms are ordinarily written
902 as a functor followed by a comma-separated list of argument terms, which is
903 contained in parentheses. The number of arguments is called the term's arity.
904 An atom can be regarded as a compound term with arity zero.

905 Prolog programs describe relations, defined by means of clauses. Pure Prolog
906 is restricted to Horn clauses, a Turing-complete subset of first-order predicate
907 logic. There are two types of clauses: Facts and rules.

908 [?] In Prolog all data objects are called terms Atomic terms

909 Come in two forms, atoms and integers. Atoms (this is a misnomer as in logic
910 predicates are called atoms and atoms are called constants. However, we'll
911 stick to the Prolog convention.) Strings of alphanumerics and `_`, starting with a
912 lower case alphabetic. Strings enclosed in 'single quotes' Integers are numeric
913 Example

```

1 geoff
2 'the cat and the rat'
3 'ABCD'
4 123

```

914 Function terms

915 Functions have the form $f(\text{term}_1, \text{term}_2)$ Functor starts with a lower
 916 case alphabetic. Example

```

1 prerequisite_to(adv_ai)
2 grade_attained_in(prerequisite_to(adv_ai), pass)

```

917 The number of arguments is the arity of the function. When referring to a
 918 functor, it is written with its arity in the format f/arity . This is also
 919 true for atoms, whose arity is 0. Note that this is a recursive definition. The view
 920 of functions as trees Operators Some functors are used in infix notation, e.g.
 921 $5+4$ Operators do not cause the associated function to be carried out. Variables
 922 Uppercase or `_` for start of variables Example

```

1 Who
2 What
3 _special
4 _

```

923 Variables in Prolog are rather different to those in most other languages. Further
 924 discussion and use is deferred until later.

925 (c) Simple Semantics

926 Under a declarative reading, the order of rules, and of goals within rules, is irrel-
 927 evant since logical disjunction and conjunction are commutative. Procedurally,
 928 however, it is often important to take into account Prolog's execution strategy,
 929 either for efficiency reasons, or due to the semantics of impure built-in predi-
 930 cates for which the order of evaluation matters. Also, as Prolog interpreters try
 931 to unify clauses in the order they're provided, failing to give a correct ordering
 932 can lead to infinite recursion.

933 In this subsection the operational semantics of CHR in Prolog are presented

informally. They do not differ essentially from other CHR systems. When a constraint is called, it is considered an active constraint and the system will try to apply the rules to it. Rules are tried and executed sequentially in the order they are written.

[?]

A rule is conceptually tried for an active constraint in the following way. The active constraint is matched with a constraint in the head of the rule. If more constraints appear in the head, they are looked for among the suspended constraints, which are called passive constraints in this context. If the necessary passive constraints can be found and all match with the head of the rule and the guard of the rule succeeds, then the rule is committed and the body of the rule executed. If not all the necessary passive constraints can be found, or the matching or the guard fails, then the body is not executed and the process of trying and executing simply continues with the following rules. If for a rule there are multiple constraints in the head, the active constraint will try the rule sequentially multiple times, each time trying to match with another constraint. This process ends either when the active constraint disappears, i.e. it is removed by some rule, or after the last rule has been processed. In the latter case the active constraint becomes suspended.

A suspended constraint is eligible as a passive constraint for an active constraint. The other way it may interact again with the rules is when a variable appearing in the constraint becomes bound to either a non-variable or another variable involved in one or more constraints. In that case the constraint is triggered, i.e. it becomes an active constraint and all the rules are tried.

i. Rule Types There are three different kinds of rules, each with its specific semantics:

A. simplification The simplification rule removes the constraints in its

961 head and calls its body.

962 B. propagation The propagation rule calls its body exactly once for the

963 constraints in its head.

964 C. simpagation The simpagation rule removes the constraints in its head

965 after the and then calls its body. It is an optimization of simplification

966 rules of the form: $[constraints_1, constraints_2 \Leftrightarrow constraints_1,$

967 $body]$ Namely, in the simpagation form: $[constraints_1 \setminus constraints_2$

968 $\Leftrightarrow body]$ The constraints_1 constraints are not called in the body.

969 ii. Rule Names Naming a rule is optional and has no semantic meaning. It

970 only functions as documentation for the programmer.

971 iii. Pragmas The semantics of the pragmas are:

972 iv. passive(Identifier) The constraint in the head of a rule Identifier can only

973 match a passive constraint in that rule.

974 (d) Universal Horn Clauses

975 (e) Unification

976 (f) Definite Clause Grammar

977 12.2 Chapter Recap

Chapter 13

Prototype 1

13.1 About this chapter

This chapter throws light on what PROLOG does to resolve a given query via *unification* and this can be replicated in the host language along with the challenges.

This chapter discusses the aspects of opening a language while preserving the original structure of a closed recursive structure in HASKELL. Also discussed are the issues related to customizing certain aspects such as meta-syntactic variables.

13.2 How Prolog works ?

Looking at how PROLOG works [?].

Most PROLOG distributions have three types of terms:

1. Constants.

2. Variables.

3. Complex terms.

Two terms can be unified if they are the same or the variables can be assigned to terms such that the resulting terms are equal.

994 The possibilities could be,

995 1. If term1 and term2 are constants, then term1 and term2 unify if and only if they are
996 the same atom, or the same number.

```
1  ?- =(mia,mia).  
2  yes
```

997 2. If term1 is a variable and term2 is any type of term, then term1 and term2 unify, and
998 term1 is instantiated to term2 . Similarly, if term2 is a variable and term1 is any type
999 of term, then term1 and term2 unify, and term2 is instantiated to term1 . (So if they
1000 are both variables, theyre both instantiated to each other, and we say that they share
1001 values.)

```
1  ?- mia = X.  
2  X = mia  
3  yes
```

```
1  ?- X = Y.  
2  yes
```

1002 3. If term1 and term2 are complex terms, then they unify if and only if:

1003 (a) They have the same functor and arity, and

1004 (b) all their corresponding arguments unify, and

1005 (c) the variable instantiations are compatible.

```
1  ?- k(s(g),Y) = k(X,t(k)).  
2  X = s(g)  
3  Y = t(k)  
4  yes
```

1006 4. Two terms unify if and only if it follows from the previous three clauses that they
1007 unify.

1008 For example, consider the append function

```
1 append([],L,L).  
2 append([H|T],L2,[H|L3]) :- append(T,L2,L3).
```

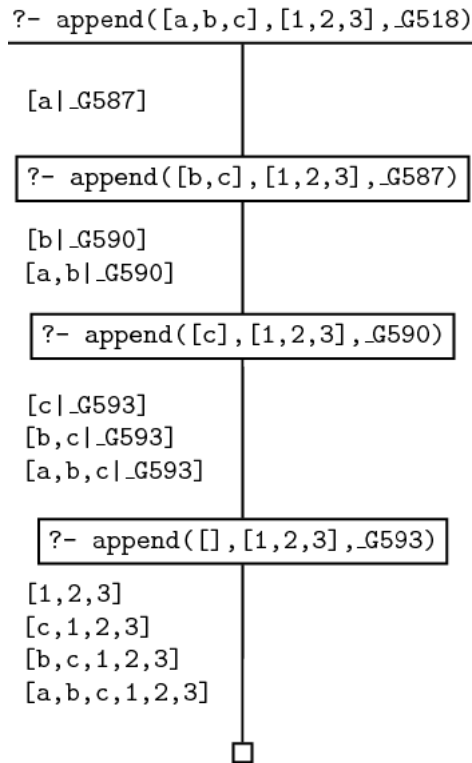


Figure 13.1: Trace for append [?]

1009 13.3 What we do in this Prototype

1010 This prototype throws light on the process of tackling the issues involved in creating a data
1011 type to replicate the target language type system while conforming to the host language
1012 restrictions and also utilizing the benefits.

1013 We have a PROLOG like language in HASKELL defined via *data*.

1014 The language defined is recursive in nature.

1015 We convert it into a non recursive data type.

1016 Basically we do Unification monadically.

1017 **13.4 Creating a data type**

1018 A type system consists of a set of rules to define a "type" to different constructs in a pro-
1019 gramming language such as variables, functions and so on. A static type system requires
1020 types to be attached to the programming constructs before hand which results in finding
1021 errors at compile time and thus increase the reliability of the program. The other end is the
1022 dynamic type system which passes through code which would not have worked in former
1023 environment, it comes of as less rigid.

1024 The advantages of static typing [?]

- 1025 1. Earlier detection of errors
- 1026 2. Better documentation in terms of type signatures
- 1027 3. More opportunities for compiler optimizations
- 1028 4. Increased run-time efficiency
- 1029 5. Better developer tools

1030 For dynamic typing

- 1031 1. Less rigid
- 1032 2. Ideal for prototyping / unknown / changing requirements or unpredictable behaviour
- 1033 3. Re-usability

1034 **Transitional paragraph** An ideal case would would be something that is dont
1035 know what to write

1036 To start with, replicating the single type "term" in PROLOG one must consider the dis-
 1037 tinct constructs it can be associated to such as complex structures (for example predicates,
 1038 clauses etc.), don't cares, cuts, variables and so on.

1039 Consider the language below,

```

1  data VariableName = VariableName Int String
2      deriving (Eq, Data, Typeable, Ord)
3  data Atom         = Atom         !String
4                      | Operator   !String
5      deriving (Eq, Ord, Data, Typeable)
6  data Term = Struct Atom [Term]
7              | Var VariableName
8              | Wildcard
9              | PString   !String
10             | PInteger  !Integer
11             | PFloat    !Double
12             | Flat [FlatItem]
13             | Cut Int
14      deriving (Eq, Data, Typeable)
15  data Clause = Clause { lhs :: Term, rhs_ :: [Goal] }
16                | ClauseFn { lhs :: Term, fn :: [Term] -> [Goal] }
17      deriving (Data, Typeable)
18  type Program = [Sentence]
19  type Body    = [Goal]
20  data Sentence = Query    Body
21                | Command Body
22                | C Clause
23      deriving (Data, Typeable)

```

1040 Even though *Term* has a number of constructors the resulting construct has a single
 1041 type. Hence, a function would still be untyped / singly typed,

```
append :: [Term] -> [Term] -> [Term]
```

1042 The above data type is recursive as seen in the constructor,

```
Struct Atom [Term]
```

1043 One of the issues with the above is that it is not possible to distinguish the structure
 1044 of the data from the data type itself [?]. Consider the following, a reduced version of the
 1045 above data type,

```

1  type Atom          = String
2  data VariableName = VariableName Int String
3      deriving (Eq, Data, Typeable, Ord)
4  data Term = Struct Atom [Term]
5      | Var VariableName
6      | Wildcard -- Don't cares
7      | Cut Int
8      deriving (Eq, Data, Typeable)

```

1046 Also one cannot create Quantifiers plus logic

1047 To split a data type into two levels, a single recursive data type is replaced by two related
 1048 data types. Consider the following,

```

1  data FlatTerm a =
2      Struct Atom [a]
3      | Var VariableName
4      | Wildcard
5      | Cut Int deriving (Show, Eq, Ord)

```

1049 One result of the approach is that the non-recursive type *FlatTerm* is modular and
 1050 generic as the structure "FlatTerm" is separate from it's type which is "a". Simply speaking
 1051 we can have something like

```
FlatTerm Bool
```

1052 and a generic fuinction like,

```
map :: (a -> b) -> FlatTerm a -> FlatTerm b
```

1053 13.5 Working with the language

1054 Creating instances,

```

1  instance Functor (FlatTerm) where
2      fmap = T.fmapDefault
3  instance Foldable (FlatTerm) where
4      foldMap = T.foldMapDefault
5  instance Traversable (FlatTerm) where
6      traverse f (Struct atom x) = Struct atom <$>
7      sequenceA (Prelude.map f x)

```

```

8         traverse _ (Var v)           = pure (Var v)
9         traverse _ Wildcard          = pure (Wildcard)
10        traverse _ (Cut i)            = pure (Cut i)
11 instance Unifiable (FlatTerm) where
12     zipMatch (Struct al ls) (Struct ar rs) =
13         if (al == ar) && (length ls == length rs)
14         then Struct al <$>
15             pairWith (\l r -> Right (l,r)) ls rs
16         else Nothing
17     zipMatch Wildcard _ = Just Wildcard
18     zipMatch _ Wildcard = Just Wildcard
19     zipMatch (Cut i1) (Cut i2) = if (i1 == i2)
20     then Just (Cut i1)
21     else Nothing
22 instance Applicative (FlatTerm) where
23     pure x = Struct "" [x]
24     _ <*> Wildcard          = Wildcard
25     _ <*> (Cut i)           = Cut i
26     _ <*> (Var v)           = (Var v)
27     (Struct a fs) <*> (Struct b xs) = Struct (a ++ b) [f x | f <- fs, x <- xs]

```

1055 After flattening do fixing,

1056 Opening up the language somehow so as to accommodate your own variables.

1057 13.6 Black box

1058 13.7 Something about unification-fd and Monadic Unifi- 1059 cation

1060 Library [?]

1061 Tutorial 1 [?]

1062 Tutorial 2 [?]

1063 1. What library provides ?

1064 This module provides first-order structural unification over general structure types.

1065 It also provides the standard suite of functions accompanying unification (applying
1066 bindings, getting free variables, etc.).

1067 The implementation makes use of numerous optimization techniques. First, we use
1068 path compression everywhere (for weighted path compression see `Control.Unification.Ranked`).
1069 Second, we replace the occurs-check with visited-sets. Third, we use a technique for
1070 aggressive opportunistic observable sharing; that is, we track as much sharing as
1071 possible in the bindings (without introducing new variables), so that we can compare
1072 bound variables directly and therefore eliminate redundant unifications.

1073 2. Unifiable stuff

1074 The basic class for generating, reading, and writing to bindings stored in a monad.
1075 These three functionalities could be split apart, but are combined in order to simplify
1076 contexts. Also, because most functions reading bindings will also perform path com-
1077 pression, there's no way to distinguish "true" mutation from mere path compression.
1078 The superclass constraints are there to simplify contexts, since we make the same
1079 assumptions everywhere we use `BindingMonad`.

1080 In order to use our `T` data type with the rest of the API, we'll need to give a Unifi-
1081 able instance for it. Before we do that we'll have to give `Functor`, `Foldable`, and
1082 `Traversable` instances. These are straightforward and can be automatically derived
1083 with the appropriate language pragmas.

1084 The `Unifiable` class gives one step of the unification process. Just as we only need
1085 to specify one level of the ADT (i.e., `T`) and then we can use the library's `UTerm` to
1086 generate the recursive ADT, so too we only need to specify one level of the unification
1087 (i.e., `zipMatch`) and then we can use the library's operators to perform the recursive
1088 unification, subsumption, etc.

1089 The `zipMatch` function takes two arguments of type `t a`. The abstract `t` will be our
1090 concrete `T` type. The abstract `a` is polymorphic, which ensures that we can't mess

1091 around with more than one level of the term at once. If we abandon that guarantee,
1092 then you can think of it as if a is $\text{UTerm } T \ v$. Thus, $t \ a$ means $T \ (\text{UTerm } T \ v)$; and
1093 $T \ (\text{UTerm } T \ v)$ is essentially the type $\text{UTerm } T \ v$ with the added guarantee that the
1094 values aren't in fact variables. Thus, the arguments to `zipMatch` are non-variable
1095 terms.

1096 The `zipMatch` method has the rather complicated return type: `Maybe (t (Either a`
1097 `(a,a)))`. Let's unpack this a bit by thinking about how unification works. When we
1098 try to unify two terms, first we look at their head constructors. If the constructors
1099 are different, then the terms aren't unifiable, so we return `Nothing` to indicate that
1100 unification has failed. Otherwise, the constructors match, so we have to recursively
1101 unify their subterms. Since the T structures of the two terms match, we can return
1102 `Just t0` where $t0$ has the same T structure as both input terms. Where we still have to
1103 recursively unify subterms, we fill $t0$ with `Right(l,r)` values where l is a subterm of the
1104 left argument to `zipMatch` and r is the corresponding subterm of the right argument.
1105 Thus, `zipMatch` is a generalized zipping function for combining the shared structure
1106 and pairing up substructures. And now, the implementation:

```
1  instance Unifiable T where
2      zipMatch (T m ls) (T n rs)
3          | m /= n      = Nothing
4          | otherwise =
5              T n <$> pairWith (\l r -> Right(l,r)) ls rs
```

1107 Where `list-extras>Data.List.Extras.Pair.pairWith` is a version of `zip` which returns
1108 `Nothing` if the lists have different lengths. So, if the names m and n match, and
1109 if the two arguments have the same number of subterms, then we pair those subterms
1110 off in order; otherwise, either the names or the lengths don't match, so we return
1111 `Nothing`.

1112 3. UTerm stuff

1113 The type of terms generated by structures `t` over variables `v`. The structure type should
1114 implement `Unifiable` and the variable type should implement `Variable`.

1115 The `Show` instance doesn't show the constructors, in order to improve legibility for
1116 large terms.

1117 All the category theoretic instances (`Functor`, `Foldable`, `Traversable`,...) are provided
1118 because they are often useful; however, beware that since the implementations must
1119 be pure, they cannot read variables bound in the current context and therefore can
1120 create incoherent results. Therefore, you should apply the current bindings before
1121 using any of the functions provided by those classes.

1122 4. `STVar` stuff

1123 This module defines an implementation of unification variables using the `ST` monad.

1124 5. `IntVar` stuff

1125 This module defines a state monad for functional pointers represented by integers as
1126 keys into an `IntMap`. This technique was independently discovered by Dijkstra et al.
1127 This module extends the approach by using a state monad transformer, which can
1128 be made into a backtracking state monad by setting the underlying monad to some
1129 `MonadLogic` (part of the `logict` library, described by Kiselyov et al.).

1130 Atze Dijkstra, Arie Middelkoop, S. Doaitse Swierstra (2008) Efficient Functional
1131 Unification and Substitution, Technical Report UU-CS-2008-027, Utrecht Univer-
1132 sity.

1133 Oleg Kiselyov, Chung-chieh Shan, Daniel P. Friedman, and Amr Sabry (2005) Back-
1134 tracking, Interleaving, and Terminating Monad Transformers, ICFP

1135 A "mutable" unification variable implemented by an integer. This provides an en-
1136 tirely pure alternative to truly mutable alternatives (like `STVar`), which can make
1137 backtracking easier.

1138 N.B., because this implementation is pure, we can use it for both ranked and unranked
1139 monads.

1140 6. Binding Monad Stuff

1141 A monad for handling STVar bindings.

1142 Run the ST ranked binding monad. N.B., because STVar are rank-2 quantified, this
1143 guarantees that the return value has no such references. However, in order to remove
1144 the references from terms, you'll need to explicitly apply the bindings and ground
1145 the term.

1146 7. U.unify stuff

1147 Unify two terms, or throw an error with an explanation of why unification failed.
1148 Since bindings are stored in the monad, the two input terms and the output term
1149 are all equivalent if unification succeeds. However, the returned value makes use of
1150 aggressive opportunistic observable sharing, so it will be more efficient to use it in
1151 future calculations than either argument.

1152 8. U.unifyOccurs

1153 A variant of unify which uses occursIn instead of visited-sets. This should only
1154 be used when eager throwing of occursFailure errors is absolutely essential (or for
1155 testing the correctness of unify). Performing the occurs-check is expensive. Not only
1156 is it slow, it's asymptotically slow since it can cause the same subterm to be traversed
1157 multiple times.

1158

9. Translation stuff

1159

13.8 Chapter Recap

```

1  monadicUnification :: (BindingMonad FlatTerm (STVar s FlatTerm) (ST.STBinding s))
2      ErrorT (UT.UFailure (FlatTerm) (ST.STVar s (FlatTerm)))
3          (ST.STBinding s) (UT.UTerm (FlatTerm) (ST.STVar s (FlatTerm))),
4          Map VariableName (ST.STVar s (FlatTerm))))
5  monadicUnification t1 t2 = do
6      -- let
7      --     t1f = termFlattener t1
8      --     t2f = termFlattener t2
9      (x1,d1) <- lift . translateToUTerm $ t1
10     (x2,d2) <- lift . translateToUTerm $ t2
11     x3 <- U.unify x1 x2
12     --get state from somewhere, state -> dict
13     return $! (x3, d1 'Map.union' d2)
14
15
16  goUnify ::
17      (forall s. (BindingMonad FlatTerm (STVar s FlatTerm) (ST.STBinding s))
18      =>
19          (ErrorT
20              (UT.UFailure FlatTerm (ST.STVar s FlatTerm))
21              (ST.STBinding s)
22              (UT.UTerm FlatTerm (ST.STVar s FlatTerm),
23              Map VariableName (ST.STVar s FlatTerm)))
24          )
25      -> [(VariableName, Prolog)]
26  goUnify test = ST.runSTBinding $ do
27      answer <- runErrorT $ test --ERROR
28      case answer of
29          (Left _)          -> return []
30          (Right (_, dict)) -> f1 dict
31
32
33  f1 ::
34      (BindingMonad FlatTerm (STVar s FlatTerm) (ST.STBinding s))
35      => (forall s. Map VariableName (STVar s FlatTerm)
36          -> (ST.STBinding s [(VariableName, Prolog)]))
37      )
38  f1 dict = do
39      let ld1 = Map.toList dict
40      ld2 <- Control.Monad.Error.sequence [ v1 | (k,v) <- ld1, let v1 = UT.lookupVar v
41      let ld3 = [ (k,v) | ((k,_),Just v) <- ld1 'zip' ld2]
42          ld4 = [ (k,v) | (k,v2) <- ld3, let v = translateFromUTerm dict v2 ]
43      return ld4

```

Figure 13.2: A sample Minted figure

Chapter 14

Prototype 2.1

14.1 About this chapter

This chapter attempts to infuse the generic methodology from 13 in a current PROLOG implementation [?] and make the unification "monadic".

14.2 How prolog-0.2.0.1 works

As described in the previous chapter about extending languages to incorporate functionality, this prototype applies the procedure to the eDSL in [?].

The original abstract syntax used by the library,

```
1 data VariableName = VariableName Int String
2     deriving (Eq, Data, Typeable, Ord)
3
4 type Atom          = String
5
6 data Term = Struct Atom [Term]
7     | Var VariableName
8     | Wildcard -- Don't cares
9     | Cut Int
10     deriving (Eq, Data, Typeable)
11
12 data Clause = Clause { lhs :: Term, rhs_ :: [Goal] }
```

```

13         | ClauseFn { lhs :: Term, fn :: [Term] -> [Goal] }
14     deriving (Data, Typeable)
15
16 type Goal      = Term
17 type Program   = [Clause]

```

1169 From the above we will focus on the *Term* since the others just add wrappers around
 1170 expressions which can be created by it. The above language suffers from most of the prob-
 1171 lems discussed in the previous chapter. The above is used to construct PROLOG "terms"
 1172 which are of a "single type".

1173 The implementation consists of components that one would find in a Language Pro-
 1174 cessing System 14.1,

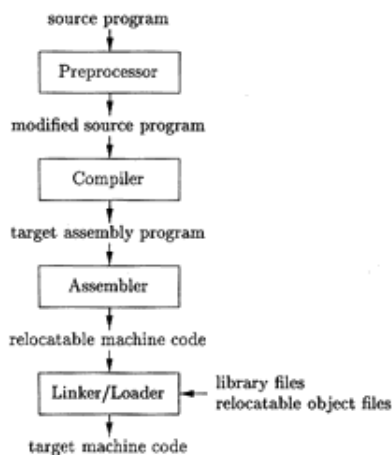


Figure 1.5: A language-processing system

Figure 14.1: A language-processing system [?]

1175 specifically speaking, parts of a compiler 14.2,

1176 The architecture for a compiler as described in 14.2 would not be needed since HASKELL
 1177 provides most of them. Nonetheless, the library has the following major components,

- 1178 1. Syntax, defining the language.
- 1179 2. Database, to create a storage for the expressions.

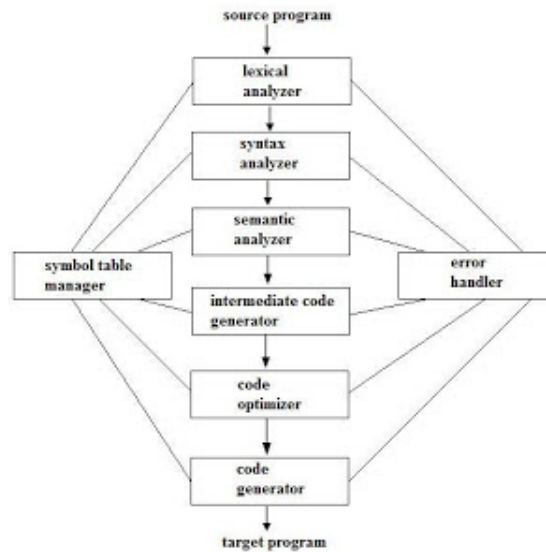


Fig 1.5 Phases of a compiler

Figure 14.2: Phases of Compiler [?]

1180 3. Parser.

1181 4. Interpreter.

1182 5. Unifier.

1183 6. REPL.

1184 To prove the modularity of the approach for language modification and monadic unifi-
 1185 cation only the abstract syntax and unifier will be customized.

1186 14.3 What we do in this prototype?

1187 In the first prototype we just did unification of two terms not query resolution.

1188 We do complete PROLOG query resolution like stuff.

1189 13 provides a generic procedure / methodology to convert a language into monadic
 1190 unifiable form

1191 14.4 Current implementation (prolog-0.2.0.1)

1192 The current unification uses basic pattern matching to unify the terms

```
1  unify, unify_with_occurs_check :: MonadPlus m => Term -> Term
2  -> m Unifier
3
4  unify = fix unify'
5
6  unify_with_occurs_check =
7      fix $ \self t1 t2 -> if (t1 'occursIn' t2 || t2 'occursIn' t1)
8                          then fail "occurs check"
9                          else unify' self t1 t2
10     where
11         occursIn t = everything (||) (mkQ False (==t))
12
13 unify' :: MonadPlus m => (Term -> Term -> m Unifier) -> Term ->
14 Term -> m [(VariableName, Term)]
15
16 -- If either of the terms are don't cares then no unifiers exist
17 unify' _ Wildcard _ = return []
18 unify' _ _ Wildcard = return []
19
20 -- If one is a variable then equate the term to its value which
21 -- forms the unifier
22 unify' _ (Var v) t = return [(v,t)]
23 unify' _ t (Var v) = return [(v,t)]
24
25 -- Match the names and the length of their parameter list and
26 -- then match the elements of list one by one.
27 unify' self (Struct a1 ts1) (Struct a2 ts2)
28     | a1 == a2 && same length ts1 ts2 =
29     unifyList self (zip ts1 ts2)
30
31 unify' _ _ _ = mzero
32
33 same :: Eq b => (a -> b) -> a -> a -> Bool
34 same f x y = f x == f y
35
36 -- Match the elements of each of the tuples in the list.
37 unifyList :: Monad m => (Term -> Term -> m Unifier) ->
38 [(Term, Term)] -> m Unifier
39 unifyList _ [] = return []
40 unifyList unify ((x,y):xys) = do
```

```

41     u <- unify x y
42     u' <- unifyList unify (Prelude.map (both (apply u)) xys)
43     return (u++u')

```

1193 14.5 Modifications

1194 The resulting language is not far from what we did in 13 apart from the fact that the *Term*
1195 expressions are encapsulated to form *Clauses* which in turn form a *Program*.

1196 Moreover, the required instances make the language compatible with the unification
1197 procedure.

```

1  data FTS a = FS Atom [a] | FV VariableName | FW | FC Int
2              deriving (Show, Eq, Typeable, Ord)
3
4  newtype Prolog = P (Fix FTS) deriving (Eq, Show, Ord, Typeable)
5
6  unP :: Prolog -> Fix FTS
7  unP (P x) = x
8
9  instance Functor (FTS) where
10     fmap          = T.fmapDefault
11
12  instance Foldable (FTS) where
13     foldMap        = T.foldMapDefault
14
15  instance Traversable (FTS) where
16     traverse f (FS atom xs)      = FS atom <$>
17     sequenceA (Prelude.map f xs)
18     traverse _ (FV v)            = pure (FV v)
19     traverse _ FW                = pure (FW)
20     traverse _ (FC i)            = pure (FC i)
21
22  instance Unifiable (FTS) where
23     zipMatch (FS al ls) (FS ar rs) =
24         if (al == ar) && (length ls == length rs)
25         then FS al <$> pairWith (\l r -> Right (l,r)) ls rs
26         else Nothing
27     zipMatch FW _ = Just FW
28     zipMatch _ FW = Just FW
29     zipMatch (FC i1) (FC i2) = if (i1 == i2)

```

```

30     then Just (FC i1)
31     else Nothing
32
33 instance Applicative (FTS) where
34     pure x                = FS "" [x]
35     _      <*>    FW      = FW
36     _      <*>    (FC i)   = FC i
37     _      <*>    (FV v)   = (FV v)
38     (FS a fs) <*> (FS b xs) = FS (a ++ b) [f x | f <- fs, x <- xs]

```

1198 Additionally helper functions for converting expressions between the two domains and
1199 translation to *UTerm*.

```

1  termFlattener :: Term -> Fix FTS
2  termFlattener (Var v)           = DFF.Fix $ FV v
3  termFlattener (Wildcard)        = DFF.Fix FW
4  termFlattener (Cut i)           = DFF.Fix $ FC i
5  termFlattener (Struct a xs)     = DFF.Fix $ FS a (Prelude.map termFlattener xs)
6
7  unFlatten :: Fix FTS -> Term
8  unFlatten (DFF.Fix (FV v))      = Var v
9  unFlatten (DFF.Fix FW)          = Wildcard
10 unFlatten (DFF.Fix (FC i))       = Cut i
11 unFlatten (DFF.Fix (FS a xs))    = Struct a (Prelude.map unFlatten xs)
12
13
14 variableExtractor :: Fix FTS -> [Fix FTS]
15 variableExtractor (Fix x) = case x of
16     (FS _ xs)  -> Prelude.concat $ Prelude.map variableExtractor xs
17     (FV v)     -> [Fix $ FV v]
18     _         -> []
19
20 variableNameExtractor :: Fix FTS -> [VariableName]
21 variableNameExtractor (Fix x) = case x of
22     (FS _ xs) -> Prelude.concat $ Prelude.map variableNameExtractor xs
23     (FV v)    -> [v]
24     _        -> []
25
26 variableSet :: [Fix FTS] -> S.Set (Fix FTS)
27 variableSet a = S.fromList a
28
29 variableNameSet :: [VariableName] -> S.Set (VariableName)
30 variableNameSet a = S.fromList a
31
32 varsToDictM :: (Ord a, Unifiable t) =>

```



```

33     S.Set a -> ST.STBinding s (Map a (ST.STVar s t))
34 varsToDictM set = foldrM addElt Map.empty set where
35   addElt sv dict = do
36     iv <- freeVar
37     return $! Map.insert sv iv dict
38
39
40 uTermify
41   :: Map VariableName (ST.STVar s (FTS))
42   -> UTerm FTS (ST.STVar s (FTS))
43   -> UTerm FTS (ST.STVar s (FTS))
44 uTermify varMap ux = case ux of
45   UT.UVar _          -> ux
46   UT.UTerm (FV v)    -> maybe (error "bad map") UT.UVar $ Map.lookup v varMap
47   -- UT.UTerm t      -> UT.UTerm $! fmap (uTermify varMap) t
48   UT.UTerm (FS a xs) -> UT.UTerm $ FS a $! fmap (uTermify varMap) xs
49   UT.UTerm (FW)      -> UT.UTerm FW
50   UT.UTerm (FC i)    -> UT.UTerm (FC i)
51
52 translateToUTerm ::
53   Fix FTS -> ST.STBinding s
54   (UT.UTerm (FTS) (ST.STVar s (FTS)),
55    Map VariableName (ST.STVar s (FTS)))
56 translateToUTerm e1Term = do
57   let vs = variableNameSet $ variableNameExtractor e1Term
58   varMap <- varsToDictM vs
59   let t2 = uTermify varMap . unfreeze $ e1Term
60   return (t2, varMap)
61
62
63 -- | vTermify recursively converts @UVar x@ into @UTerm (VarA x).
64 -- This is a subroutine of @translateFromUTerm @. The resulting
65 -- term has no (UVar x) subterms.
66
67 vTermify :: Map Int VariableName ->
68   UT.UTerm (FTS) (ST.STVar s (FTS)) ->
69   UT.UTerm (FTS) (ST.STVar s (FTS))
70 vTermify dict t1 = case t1 of
71   UT.UVar x -> maybe (error "logic") (UT.UTerm . FV) $ Map.lookup (UT.getVarID x)
72   UT.UTerm r ->
73     case r of
74       FV iv -> t1
75       _     -> UT.UTerm . fmap (vTermify dict) $ r
76
77 translateFromUTerm ::

```

```

78     Map VariableName (ST.STVar s (FTS)) ->
79     UT.UTerm (FTS) (ST.STVar s (FTS)) -> Prolog
80 translateFromUTerm dict uTerm =
81     P . maybe (error "Logic") id . freeze . vTermify varIdDict $ uTerm where
82     forKV dict initial fn = Map.foldlWithKey' (\a k v -> fn k v a) initial dict
83     varIdDict = forKV dict Map.empty $ \ k v -> Map.insert (UT.getVarID v) k
84
85
86 -- / Unify two (E1 a) terms resulting in maybe a dictionary
87 -- of variable bindings (to terms).
88 --
89 -- NB !!!!
90 -- The current interface assumes that the variables in t1 and t2 are
91 -- disjoint. This is likely a mistake that needs fixing
92
93 unifyTerms :: Fix FTS -> Fix FTS -> Maybe (Map VariableName (Prolog))
94 unifyTerms t1 t2 = ST.runSTBinding $ do
95     answer <- runExceptT $ unifyTermsX t1 t2
96     return $! either (const Nothing) Just answer
97
98 -- / Unify two (E1 a) terms resulting in maybe a dictionary
99 -- of variable bindings (to terms).
100 --
101 -- This routine works in the unification monad
102
103 unifyTermsX ::
104     (Fix FTS) -> (Fix FTS) ->
105     ExceptT (UT.UFailure (FTS) (ST.STVar s (FTS)))
106     (ST.STBinding s)
107     (Map VariableName (Prolog))
108 unifyTermsX t1 t2 = do
109     (x1,d1) <- lift . translateToUTerm $ t1
110     (x2,d2) <- lift . translateToUTerm $ t2
111     _ <- U.unify x1 x2
112     makeDicts $ (d1,d2)
113
114 mapWithKeyM :: (Ord k,Applicative m,Monad m)
115     => (k -> a -> m b) -> Map k a -> m (Map k b)
116 mapWithKeyM = Map.traverseWithKey
117
118
119 makeDict ::
120     Map VariableName (ST.STVar s (FTS)) -> ST.STBinding s (Map VariableName
121 makeDict sVarDict =
122     flip mapWithKeyM sVarDict $ \ _ -> \ iKey -> do

```

```

123         Just xx <- UT.lookupVar $ iKey
124         return $! (translateFromUTerm sVarDict) xx
125
126
127     -- / recover the bindings for the variables of the two terms
128     -- unified from the monad.
129
130 makeDicts ::
131     (Map VariableName (ST.STVar s (FTS)), Map VariableName (ST.STVar s (FTS))) ->
132     ExceptT (UT.UFailure (FTS) (ST.STVar s (FTS)))
133     (ST.STBinding s) (Map VariableName (Prolog))
134 makeDicts (svDict1, svDict2) = do
135     let svDict3 = (svDict1 `Map.union` svDict2)
136     let ivs = Prelude.map UT.UVar . Map.elems $ svDict3
137     applyBindingsAll ivs
138     -- the interface below is dangerous because Map.union is left-biased.
139     -- variables that are duplicated across terms may have different
140     -- bindings because 'translateToUTerm' is run separately on each
141     -- term.
142     lift . makeDict $ svDict3

```

1200 Take original expressions flatten fix convert unify run it STBinding monad to extract
1201 substitutions.

```

1  monadicUnification :: (BindingMonad FTS (STVar s FTS)
2  (ST.STBinding s))
3  => (forall s. ((Fix FTS) -> (Fix FTS) ->
4  ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
5  (ST.STBinding s) (UT.UTerm (FTS) (ST.STVar s (FTS)),
6  Map VariableName (ST.STVar s (FTS)))))
7  monadicUnification t1 t2 = do
8  -- let
9  --     t1f = termFlattener t1
10 --     t2f = termFlattener t2
11  (x1,d1) <- lift . translateToUTerm $ t1
12  (x2,d2) <- lift . translateToUTerm $ t2
13  x3 <- U.unify x1 x2
14  --get state from somewhere, state -> dict
15  return $! (x3, d1 `Map.union` d2)
16
17
18 goUnify ::
19     (forall s. (BindingMonad FTS (STVar s FTS) (ST.STBinding s))
20     =>

```

```

21         (ErrorT
22           (UT.UFailure FTS (ST.STVar s FTS))
23           (ST.STBinding s)
24           (UT.UTerm FTS (ST.STVar s FTS),
25            Map VariableName (ST.STVar s FTS)))
26     )
27     -> [(VariableName, Prolog)]
28 goUnify test = ST.runSTBinding $ do
29   answer <- runErrorT $ test --ERROR
30   case answer of
31     (Left _)           -> return []
32     (Right (_, dict)) -> f1 dict
33
34
35 f1 ::
36   (BindingMonad FTS (STVar s FTS) (ST.STBinding s))
37   => (forall s. Map VariableName (STVar s FTS)
38      -> (ST.STBinding s [(VariableName, Prolog)]))
39   )
40 f1 dict = do
41   let ld1 = Map.toList dict
42   ld2 <- Control.Monad.Error.sequence
43   [ v1 | (k,v) <- ld1, let v1 = UT.lookupVar v]
44   let ld3 = [ (k,v) | ((k,_),Just v) <- ld1 'zip' ld2]
45       ld4 = [ (k,v) | (k,v2) <- ld3,
46                  let v = translateFromUTerm dict v2 ]
47   return ld4
48 unifierConvertor :: [(VariableName, Prolog)] -> Unifier
49 unifierConvertor xs = Prelude.map (\(v, p) -> (v, (unFlatten $ unP $ p))) xs
50
51 unify :: MonadPlus m => Term -> Term -> m Unifier
52 unify t1 t2 = unifierConvertor (goUnify (monadicUnification (termFlattener t1) (te

```

1202 14.6 Results

1203 It works,

1204 14.7 Chapter Recap

Chapter 15

Prototype 3

15.1 What is this chapter about

When two terms are to be unified we can use 13 ,
term1 and term2 are matched and an assignment is the result
now this may be a part of a query resolution procedure
to reach the point where two terms need to unified will happen through some sort of
search strategy
and our approach is independent of that, and this prototype is a proof of concept to
implementing query resolution using unification with variable search strategy

15.2 Unification

The first, "unification," regards how terms are matched and variables assigned to make
terms match. [?]

1219 15.3 Resolution

1220 this where the complete procedure takes place after the query is passed along with the
1221 knowledge

1222 the resolver searches to create and a list of goals and then tries to achieve each one.

1223 [?]

1224 [?]

1225 15.4 Search strategies

1226 The base implementation used for this prototype is [?] and below are the search strategies

1227 15.5 Stack Engine

```
1  -- Stack based Prolog inference engine
2  -- Mark P. Jones November 1990, modified for Gofer 20th July 1991,
3  -- and for Hugs 1.3 June 1996.
4  --
5  -- Suitable for use with Hugs 98.
6  --
7
8  module StackEngine( version, prove ) where
9
10 import Prolog
11 import st
12 import Interact
13
14 version = "stack based"
15
16 --- Calculation of solutions:
17
18 -- the stack based engine maintains a stack of triples (s,goal,alts)
19 -- corresponding to backtrack points, where s is the stitution at that
20 -- point, goal is the outstanding goal and alts is a list of possible ways
21 -- of extending the current proof to find a solution. Each member of alts
22 -- is a pair (tp,u) where tp is a new goal that must be proved and u is
```

```

23  -- a unifying stitution that must be combined with the stitution s.
24  --
25  -- the list of relevant clauses at each step in the execution is produced
26  -- by attempting to unify the head of the current goal with a suitably
27  -- renamed clause from the database.
28
29  type Stack = [ (st, [Term], [Alt]) ]
30  type Alt   = ([Term], st)
31
32  alts      :: Database -> Int -> Term -> [Alt]
33  alts db n g = [ (tp,u) | (tm:-tp) <- renClauses db n g, u <- unify g tm ]
34
35  -- The use of a stack enables backtracking to be described explicitly,
36  -- in the following 'state-based' definition of prove:
37
38  prove     :: Database -> [Term] -> [st]
39  prove db gl = solve 1 nullst gl []
40  where
41    solve :: Int -> st -> [Term] -> Stack -> [st]
42    solve n s []      ow      = s : backtrack n ow
43    solve n s (g:gs) ow
44        | g==theCut = solve n s gs (cut ow)
45        | otherwise = choose n s gs (alts db n (app s g)) ow
46
47    choose :: Int -> st -> [Term] -> [Alt] -> Stack -> [st]
48    choose n s gs []      ow = backtrack n ow
49    choose n s gs ((tp,u):rs) ow = solve (n+1) (u@@s) (tp++gs) ((s,gs,rs):ow)
50
51    backtrack      :: Int -> Stack -> [st]
52    backtrack n [] = []
53    backtrack n ((s,gs,rs):ow) = choose (n-1) s gs rs ow
54
55
56  --- Special definitions for the cut predicate:
57
58  theCut      :: Term
59  theCut      = Struct "!" []
60
61  cut         :: Stack -> Stack
62  cut ss      = []
63
64  --- End of Engine.hs

```

15.6 Pure Engine

```

1  -- The Pure Prolog inference engine (using explicit prooftrees)
2  -- Mark P. Jones November 1990, modified for Gofer 20th July 1991,
3  -- and for Hugs 1.3 June 1996.
4  --
5  -- Suitable for use with Hugs 98.
6  --
7
8  module PureEngine( version, prove ) where
9
10 import Prolog
11 import st
12 import Interact
13 import Data.List(nub)
14
15 version = "tree based"
16
17 --- Calculation of solutions:
18
19 -- Each node in a prooftree corresponds to:
20 -- either: a solution to the current goal, represented by Done s, where s
21 --          is the required stitution
22 -- or:     a choice between a number of trees ts, each corresponding to a
23 --          proof of a goal of the current goal, represented by Choice ts.
24 --          The proof tree corresponding to an unsolvable goal is Choice []
25
26 data Prooftree = Done st | Choice [Prooftree]
27
28 -- prooftree uses the rules of Prolog to construct a suitable proof tree for
29 --          a specified goal
30 prooftree :: Database -> Int -> st -> [Term] -> Prooftree
31 prooftree db = pt
32   where pt :: Int -> st -> [Term] -> Prooftree
33         pt n s [] = Done s
34         pt n s (g:gs) = Choice [ pt (n+1) (u@@s) (map (app u) (tp++gs))
35                                | (tm:-tp)<-renClauses db n g, u<-unify g tm ]
36   {--
37   pt 1 nullst [] = Done (nullst)
38
39   pt n s (g:gs)
40
41   renClauses :- Rename variables in a clause, the parameters are the database, an
42                 (head of list) resulting in a clause.

```



```

43
44 unify :- take the head of the list and and match with head of clause from renCla
45
46 app :- function for applying (st) to (Terms)
47 the new list is formed by replacing the cluase head with its body and applying t
48
49 so the new parameters for pt are
50
51 (n+1) (the old stitution + the new one from unify) (the list formed after applyi
52
53
54 Working of a small example
55
56 The database,
57 (foldl addClause emptyDb [((:-) (Struct "hello" []) []), ((:-) (Struct "hello" [
58 hello.
59 hello(world).
60 hello:-world.
61 hello(X_1).
62
63 The other parameters are 1 nullst(as mentioned in the prove function).
64
65 For the list of goals, [(Struct "hello" []), (Struct "hello" [(Struct "world" [
66
67 1. [Struct "hello" []] :: [Term]
68
69 * Rule 1 does not apply
70
71 * Rule 2 does apply,
72
73 (tm:- tp) <- renClauses db 1 (Struct "hello" [])
74
75 tm ==> "hello , hello(world) , hello , hello(X_1) , "
76 tp ==> "[] , [] , [world] , [] , "
77
78
79
80
81
82
83
84
85
86 --}
87

```

```

88
89
90 -- DFS Function
91 -- search performs a depth-first search of a proof tree, producing the list
92 -- of solution substitutions as they are encountered.
93 search          :: ProofTree -> [st]
94 search (Done s)  = [s]
95 search (Choice pts) = [ s | pt <- pts, s <- search pt ]
96
97
98 prove          :: Database -> [Term] -> [st]
99 prove db       = search . proofTree db 1 nullst
100
101 --- End of PureEngine.hs

```

1229 15.7 Andorra Engine

```

1  {-
2  By Donald A. Smith, December 22, 1994, based on Mark Jones' PureEngine.
3
4  This inference engine implements a variation of the Andorra Principle for
5  logic programming. (See references at the end of this file.) The basic
6  idea is that instead of always selecting the first goal in the current
7  list of goals, select a relatively deterministic goal.
8
9  For each goal g in the list of goals, calculate the resolvents that would
10 result from selecting g. Then choose a g which results in the lowest
11 number of resolvents. If some g results in 0 resolvents then fail.
12 (This would occur for a goal like: ?- append(A,B,[1,2,3]),equals(1,2).)
13 Prolog would not perform this optimization and would instead search
14 and backtrack wastefully. If some g results in a single resolvent
15 (i.e., only a single clause matches) then that g will get selected;
16 by selecting and resolving g, bindings are propagated sooner, and useless
17 search can be avoided, since these bindings may prune away choices for
18 other clauses. For example: ?- append(A,B,[1,2,3]),B=[].
19 -}
20
21 module AndorraEngine( version, prove ) where
22
23 import Prolog
24 import st
25 import Interact

```

```

26
27 version = "Andorra Principle Interpreter (select deterministic goals first)"
28
29 solve    :: Database -> Int -> st -> [Term] -> [st]
30 solve db = slv where
31     slv      :: Int -> st -> [Term] -> [st]
32     slv n s [] = [s]
33     slv n s goals =
34         let allResolvents = resolve_selecting_each_goal goals db n in
35         let (gs,gres) = findMostDeterministic allResolvents in
36         concat [slv (n+1) (u@@s) (map (app u) (tp++gs)) | (u,tp) <- gres]
37
38 resolve_selecting_each_goal::
39     [Term] -> Database -> Int -> [[Term],[[st,[Term]]]]
40 -- For each pair in the list that we return, the first element of the
41 -- pair is the list of unresolved goals; the second element is the list
42 -- of resolvents of the selected goal, where a resolvent is a pair
43 -- consisting of a stitution and a list of new goals.
44 resolve_selecting_each_goal goals db n = [(gs, gResolvents) |
45     (g,gs) <- delete goals, let gResolvents = resolve db g n]
46
47 -- The unselected goals from above are not passed in.
48 resolve :: Database -> Term -> Int -> [(st,[Term])]
49 resolve db g n = [(u,tp) | (tm:-tp)<-renClauses db n g, u<-unify g tm]
50 -- u is not yet applied to tp, since it is possible that g won't be selected.
51 -- Note that unify could be nondeterministic.
52
53 findMostDeterministic:: [[Term],[[st,[Term]]]] -> ([Term],[[st,[Term]]])
54 findMostDeterministic allResolvents = minF comp allResolvents where
55     comp:: (a,[b]) -> (a,[b]) -> Bool
56     comp (_,gs1) (_,gs2) = (length gs1) < (length gs2)
57 -- It seems to me that there is an opportunity for a clever compiler to
58 -- optimize this code a lot. In particular, there should be no need to
59 -- determine the total length of a goal list if it is known that
60 -- there is a shorter goal list in allResolvents ... ?
61
62 delete :: [a] -> [(a,[a])]
63 delete l = d l [] where
64     d :: [a] -> [a] -> [(a,[a])]
65     d [g] sofar = [(g,sofar)]
66     d (g:gs) sofar = (g,sofar++gs) : (d gs (g:sofar))
67
68 minF      :: (a -> a -> Bool) -> [a] -> a
69 minF f (h:t) = m h t where
70 -- m :: a -> [a] -> a

```

```

71     m sofar [] = sofar
72     m sofar (h:t) = if (f h sofar) then m h t else m sofar t
73
74 prove    :: Database -> [Term] -> [st]
75 prove db = solve db 1 nullst
76
77 {- An optimized, incremental version of the above interpreter would use
78    a data representation in which for each goal in "goals" we carry around
79    the list of resolvents. After each resolution step we update the lists.
80 -}
81
82 {- References
83
84    Seif Haridi & Per Brand, "Andorra Prolog, an integration of Prolog
85    and committed choice languages" in Proceedings of FGCS 1988, ICOT,
86    Tokyo, 1988.
87
88    Vitor Santos Costa, David H. D. Warren, and Rong Yang, "Two papers on
89    the Andorra-I engine and preprocessor", in Proceedings of the 8th
90    ICLP. MIT Press, 1991.
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92    Steve Gregory and Rong Yang, "Parallel Constraint Solving in
93    Andorra-I", in Proceedings of FGCS'92. ICOT, Tokyo, 1992.
94
95    Sverker Janson and Seif Haridi, "Programming Paradigms of the Andorra
96    Kernel Language", in Proceedings of ILPS'91. MIT Press, 1991.
97
98    Torkel Franzen, Seif Haridi, and Sverker Janson, "An Overview of the
99    Andorra Kernel Language", In LNAI (LNCS) 596, Springer-Verlag, 1992.
100 -}

```

1230 15.8 Current Unification

```

1  {-# LANGUAGE DeriveDataTypeable,
2      ViewPatterns,
3      ScopedTypeVariables,
4      DefaultSignatures,
5      TypeOperators,
6      TypeFamilies,
7      DataKinds,
8      DataKinds,
9      PolyKinds,

```

```

10         OverlappingInstances,
11         TypeOperators,
12         LiberalTypeSynonyms,
13         TemplateHaskell,
14         AllowAmbiguousTypes,
15         ConstraintKinds,
16         Rank2Types,
17         MultiParamTypeClasses,
18         FunctionalDependencies,
19         FlexibleContexts,
20         FlexibleInstances,
21         UndecidableInstances
22     #-}
23
24 --stitutions and Unification of Prolog Terms
25 -- Mark P. Jones November 1990, modified for Gofer 20th July 1991,
26 -- and for Hugs 1.3 June 1996.
27 --
28 -- Suitable for use with Hugs 98.
29 --
30
31 module st where
32
33 import Prolog
34 import CustomSyntax
35 import Data.Map as Map
36 import Data.Maybe
37 import Data.Either
38
39 --Unification
40 import Control.Unification.IntVar
41 import Control.Unification.STVar as ST
42
43 import Control.Unification.Ranked.IntVar
44 import Control.Unification.Ranked.STVar
45
46 import Control.Unification.Types as UT
47
48 import Control.Monad.State.UnificationExtras
49 import Control.Unification as U
50
51 -- Monads
52 import Control.Monad.Error
53 import Control.Monad.Trans.Except
54

```

```

55 import Data.Functor.Fixedpoint as DFF
56
57 --State
58 import Control.Monad.State.Lazy
59 import Control.Monad.ST
60 import Control.Monad.Trans.State as Trans
61
62 infixr 3 @@
63 infix 4 ->-
64
65 --- stitutions:
66
67 type st = Id -> Term
68
69 newtype stP = stP { unstP :: st }
70
71 -- instance Show stP where
72 --   show (i) = show £ Var i
73 -- stitutions are represented by functions mapping identifiers to terms.
74 --
75 -- app s      extends the stitution s to a function mapping terms to terms
76 {--
77 Looks like an apply function that applies a stitution function tho the variables
78 --}
79
80
81 -- nullst is the empty stitution which maps every identifier to the same identifi
82
83
84
85 -- i ->- t    is the stitution which maps the identifier i to the term t, but oth
86
87
88 -- s1@@ s2    is the composition of stitutions s1 and s2
89 --           N.B. app is a monoid homomorphism from (st,nullst,(@@))
90 --           to (Term -> Term, id, (.) ) in the sense that:
91 --           app (s1 @@ s2) = app s1 . app s2
92 --           s @@ nullst = s = nullst @@ s
93
94 app :: st -> Term -> Term
95 app s (Var i)      = s i
96 app s (Struct a ts) = Struct a (Prelude.map (app s) ts)
97 {--
98 app (stFunction) (Struct "hello" [Var (0, "Var")])
99 hello(Var_2) :: Term

```

```

100
101  --}
102
103
104  nullst                :: st
105  nullst i              = Var i
106  {--
107    nullst (0, "Var")
108    Var :: Term
109  --}
110
111
112  --
113  (->-)                  :: Id -> Term -> st
114  (i ->- t) j | j==i     = t
115              | otherwise = Var j
116  {--
117    :t (->-) (1,"X") (Struct "hello" [])
118    (1,"X") ->- Struct "hello" [] :: (Int,[Char]) -> Term
119  --}
120
121
122  -- Function composition for applying two stitution functions.
123  (@@)                  :: st -> st -> st
124  s1 @@ s2               = app s1 . s2

```

1231 15.9 Syntax Modification

```

1  {-# LANGUAGE DeriveDataTypeable,
2      ViewPatterns,
3      ScopedTypeVariables,
4      FlexibleInstances,
5      DefaultSignatures,
6      TypeOperators,
7      FlexibleContexts,
8      TypeFamilies,
9      DataKinds,
10     OverlappingInstances,
11     DataKinds,
12     PolyKinds,
13     TypeOperators,
14     LiberalTypeSynonyms,

```

```

15         TemplateHaskell,
16         RankNTypes,
17         AllowAmbiguousTypes,
18         MultiParamTypeClasses,
19         FunctionalDependencies,
20         ConstraintKinds,
21         ExistentialQuantification
22     #-}
23
24 module CustomSyntax where
25
26 import Data.Generics (Data(..), Typeable(..))
27 import Data.List (intercalate)
28 import Data.Char (isLetter)
29
30 import Control.Monad.State.UnificationExtras
31 import Control.Unification as U
32
33
34 import Data.Functor.Fixedpoint as DFF
35
36
37 import Control.Unification.IntVar
38 import Control.Unification.STVar as ST
39
40 import Control.Unification.Ranked.IntVar
41 import Control.Unification.Ranked.STVar
42
43 import Control.Unification.Types as UT
44
45
46
47 import Data.Traversable as T
48 import Data.Functor
49 import Data.Foldable
50 import Control.Applicative
51
52
53 import Data.List.Extras.Pair
54 import Data.Map as Map
55 import Data.Set as S
56
57
58 import Control.Monad.Error
59 import Control.Monad.Trans.Except

```



```

60
61
62 import Prolog
63
64 data FTS a = forall a . FV Id | FS Atom [a] deriving (Eq, Show, Ord, Typeable)
65
66 newtype Prolog = P (Fix FTS) deriving (Eq, Show, Ord, Typeable)
67
68 unP :: Prolog -> Fix FTS
69 unP (P x) = x
70
71 instance Functor FTS where
72     fmap = T.fmapDefault
73
74 instance Foldable FTS where
75     foldMap = T.foldMapDefault
76
77 instance Traversable FTS where
78     traverse f (FS atom xs) = FS atom <$> sequenceA (Prelude.map f xs)
79     traverse _ (FV v) = pure (FV v)
80
81 instance Unifiable FTS where
82     zipMatch (FS al ls) (FS ar rs) = if (al == ar) && (length ls == length rs)
83                                     then FS al <$> pairWith (\l r -> Right (l,r))
84                                     else Nothing
85     zipMatch (FV v1) (FV v2) = if (v1 == v2) then Just (FV v1)
86                               else Nothing
87     zipMatch _ _ = Nothing
88
89 instance Applicative FTS where
90     pure x = FS "" [x]
91     (FS a fs) <*> (FS b xs) = FS (a ++ b) [f x | f <- fs, x <- xs]
92     --other cases
93     {--
94     instance Monad FTS where
95         func =
96     instance Variable FTS where
97         func =
98
99     instance BindingMonad FTS where
100         func =
101     --}
102
103 data VariableName = VariableName Int String
104

```

```

105 idToVariableName :: Id -> VariableName
106 idToVariableName (i, s) = VariableName i s
107
108 variablenameToId :: VariableName -> Id
109 variablenameToId (VariableName i s) = (i,s)
110
111 termFlattener :: Term -> Fix FTS
112 termFlattener (Var v)          = DFF.Fix $ FV v
113 termFlattener (Struct a xs)    = DFF.Fix $ FS a (Prelude.map termFlattener xs)
114
115 unFlatten :: Fix FTS -> Term
116 unFlatten (DFF.Fix (FV v))    = Var v
117 unFlatten (DFF.Fix (FS a xs)) = Struct a (Prelude.map unFlatten xs)
118
119
120 variableExtractor :: Fix FTS -> [Fix FTS]
121 variableExtractor (Fix x) = case x of
122   (FS _ xs)  -> Prelude.concat $ Prelude.map variableExtractor xs
123   (FV v)     -> [Fix $ FV v]
124   -- _       -> []
125
126 variableIdExtractor :: Fix FTS -> [Id]
127 variableIdExtractor (Fix x) = case x of
128   (FS _ xs) -> Prelude.concat $ Prelude.map variableIdExtractor xs
129   (FV v)    -> [v]
130
131 {--
132  variableNameExtractor :: Fix FTS -> [VariableName]
133  variableNameExtractor (Fix x) = case x of
134    (FS _ xs) -> Prelude.concat & Prelude.map variableNameExtractor xs
135    (FV v)    -> [v]
136    _         -> []
137  --}
138
139 variableSet :: [Fix FTS] -> S.Set (Fix FTS)
140 variableSet a = S.fromList a
141
142 variableNameSet :: [Id] -> S.Set (Id)
143 variableNameSet a = S.fromList a
144
145
146 varsToDictM :: (Ord a, Unifiable t) =>
147   S.Set a -> ST.STBinding s (Map a (ST.STVar s t))
148 varsToDictM set = foldrM addElt Map.empty set where
149   addElt sv dict = do

```

```

150     iv <- freeVar
151     return $! Map.insert sv iv dict
152
153
154 uTermify
155   :: Map Id (ST.STVar s (FTS))
156   -> UTerm FTS (ST.STVar s (FTS))
157   -> UTerm FTS (ST.STVar s (FTS))
158 uTermify varMap ux = case ux of
159   UT.UVar _          -> ux
160   UT.UTerm (FV v)    -> maybe (error "bad map") UT.UVar $ Map.lookup v varMap
161   -- UT.UTerm t      -> UT.UTerm £! fmap (uTermify varMap) t
162   UT.UTerm (FS a xs) -> UT.UTerm $ FS a $! fmap (uTermify varMap) xs
163
164
165 translateToUTerm ::
166   Fix FTS -> ST.STBinding s
167   (UT.UTerm (FTS) (ST.STVar s (FTS)),
168    Map Id (ST.STVar s (FTS)))
169 translateToUTerm e1Term = do
170   let vs = variableNameSet $ variableIdExtractor e1Term
171   varMap <- varsToDictM vs
172   let t2 = uTermify varMap . unfreeze $ e1Term
173   return (t2,varMap)
174
175
176 -- / vTermify recursively converts @UVar x@ into @UTerm (VarA x).
177 -- This is a routine of @ translateFromUTerm @. The resulting
178 -- term has no (UVar x) terms.
179
180 vTermify :: Map Int Id ->
181   UT.UTerm (FTS) (ST.STVar s (FTS)) ->
182   UT.UTerm (FTS) (ST.STVar s (FTS))
183 vTermify dict t1 = case t1 of
184   UT.UVar x -> maybe (error "logic") (UT.UTerm . FV) $ Map.lookup (UT.getVarID x)
185   UT.UTerm r ->
186     case r of
187       FV iv -> t1
188       _ -> UT.UTerm . fmap (vTermify dict) $ r
189
190 translateFromUTerm ::
191   Map Id (ST.STVar s (FTS)) ->
192   UT.UTerm (FTS) (ST.STVar s (FTS)) -> Prolog
193 translateFromUTerm dict uTerm =
194   P . maybe (error "Logic") id . freeze . vTermify varIdDict $ uTerm where

```

```

195     forKV dict initial fn = Map.foldlWithKey' (\a k v -> fn k v a) initial dict
196     varIdDict = forKV dict Map.empty $ \ k v -> Map.insert (UT.getVarID v) k
197
198
199     -- / Unify two (E1 a) terms resulting in maybe a dictionary
200     -- of variable bindings (to terms).
201     --
202     -- NB !!!!
203     -- The current interface assumes that the variables in t1 and t2 are
204     -- disjoint. This is likely a mistake that needs fixing
205
206     unifyTerms :: Fix FTS -> Fix FTS -> Maybe (Map Id (Prolog))
207     unifyTerms t1 t2 = ST.runSTBinding $ do
208       answer <- runExceptT $ unifyTermsX t1 t2
209       return $! either (const Nothing) Just answer
210
211     -- / Unify two (E1 a) terms resulting in maybe a dictionary
212     -- of variable bindings (to terms).
213     --
214     -- This routine works in the unification monad
215
216     unifyTermsX ::
217       Fix FTS -> Fix FTS ->
218       ExceptT (UT.UFailure (FTS) (ST.STVar s (FTS)))
219         (ST.STBinding s)
220         (Map Id (Prolog))
221     unifyTermsX t1 t2 = do
222       (x1,d1) <- lift . translateToUTerm $ t1
223       (x2,d2) <- lift . translateToUTerm $ t2
224       _ <- unify x1 x2
225       makeDicts $ (d1,d2)
226
227
228
229     mapWithKeyM :: (Ord k,Applicative m,Monad m)
230       => (k -> a -> m b) -> Map k a -> m (Map k b)
231     mapWithKeyM = Map.traverseWithKey
232
233
234     makeDict ::
235       Map Id (ST.STVar s (FTS)) -> ST.STBinding s (Map Id (Prolog))
236     makeDict sVarDict =
237       flip mapWithKeyM sVarDict $ \ _ -> \ iKey -> do
238         Just xx <- UT.lookupVar $ iKey
239         return $! (translateFromUTerm sVarDict) xx

```

```

240
241
242 -- / recover the bindings for the variables of the two terms
243 -- unified from the monad.
244
245 makeDicts ::
246   (Map Id (ST.STVar s (FTS)), Map Id (ST.STVar s (FTS))) ->
247   ExceptT (UT.UFailure (FTS) (ST.STVar s (FTS)))
248   (ST.STBinding s) (Map Id (Prolog))
249 makeDicts (svDict1, svDict2) = do
250   let svDict3 = (svDict1 'Map.union' svDict2)
251   let ivs = Prelude.map UT.UVar . Map.elems $ svDict3
252   applyBindingsAll ivs
253   -- the interface below is dangerous because Map.union is left-biased.
254   -- variables that are duplicated across terms may have different
255   -- bindings because 'translateToUTerm' is run separately on each
256   -- term.
257   lift . makeDict $ svDict3
258
259 instance (UT.Variable v, Functor t) => Error (UT.UFailure t v) where {}
260
261 test1 ::
262   ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
263   (ST.STBinding s)
264   (UT.UTerm (FTS) (ST.STVar s (FTS)),
265    Map Id (ST.STVar s (FTS)))
266 test1 = do
267   let
268     t1a = (Fix $ FV $ (0, "x"))
269     t2a = (Fix $ FV $ (1, "y"))
270     (x1,d1) <- lift . translateToUTerm $ t1a --error
271     (x2,d2) <- lift . translateToUTerm $ t2a
272     x3 <- U.unify x1 x2
273     return (x3, d1 'Map.union' d2)
274
275
276 test2 ::
277   ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
278   (ST.STBinding s)
279   (UT.UTerm (FTS) (ST.STVar s (FTS)),
280    Map Id (ST.STVar s (FTS)))
281 test2 = do
282   let
283     t1a = (Fix $ FS "a" [Fix $ FV $ (0, "x")])
284     t2a = (Fix $ FV $ (1, "y"))

```

```

285     (x1,d1) <- lift . translateToUTerm $ t1a --error
286     (x2,d2) <- lift . translateToUTerm $ t2a
287     x3 <- U.unify x1 x2
288     return (x3, d1 'Map.union' d2)
289
290
291 test3 ::
292     ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
293         (ST.STBinding s)
294         (UT.UTerm (FTS) (ST.STVar s (FTS)),
295          Map Id (ST.STVar s (FTS)))
296 test3 = do
297     let
298         t1a = (Fix $ FS "a" [Fix $ FV $ (0, "x")])
299         t2a = (Fix $ FV $ (0, "x"))
300     (x1,d1) <- lift . translateToUTerm $ t1a --error
301     (x2,d2) <- lift . translateToUTerm $ t2a
302     x3 <- U.unify x1 x2
303     return (x3, d1 'Map.union' d2)
304
305     {--
306     goTest test3
307     "ok:      STVar -9223372036854775807
308     [(VariableName 0 \"x\",STVar -9223372036854775808)]"
309     --}
310
311 test4 ::
312     ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
313         (ST.STBinding s)
314         (UT.UTerm (FTS) (ST.STVar s (FTS)),
315          Map Id (ST.STVar s (FTS)))
316 test4 = do
317     let
318         t1a = (Fix $ FS "a" [Fix $ FV $ (0, "x")])
319         t2a = (Fix $ FV $ (0, "x"))
320     (x1,d1) <- lift . translateToUTerm $ t1a --error
321     (x2,d2) <- lift . translateToUTerm $ t2a
322     x3 <- U.unifyOccurs x1 x2
323     return (x3, d1 'Map.union' d2)
324
325     {--
326     goTest test4
327     "ok:      STVar -9223372036854775807
328     [(VariableName 0 \"x\",STVar -9223372036854775808)]"
329     --}
330
331 test5 ::

```

```

330     ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
331         (ST.STBinding s)
332         (UT.UTerm (FTS) (ST.STVar s (FTS))),
333         Map Id (ST.STVar s (FTS)))
334 test5 = do
335     let
336         t1a = (Fix $ FS "a" [Fix $ FV $ (0, "x")])
337         t2a = (Fix $ FS "b" [Fix $ FV $ (0, "y")])
338         (x1,d1) <- lift . translateToUTerm $ t1a --error
339         (x2,d2) <- lift . translateToUTerm $ t2a
340         x3 <- U.unify x1 x2
341         return (x3, d1 'Map.union' d2)
342
343 goTest :: (Show b) => (forall s .
344     (ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
345         (ST.STBinding s)
346         (UT.UTerm (FTS) (ST.STVar s (FTS))),
347         Map Id (ST.STVar s (FTS)))) -> String
348 goTest test = ST.runSTBinding $ do
349     answer <- runErrorT $ test
350     return $! case answer of
351         (Left x)  -> "error: " ++ show x
352         (Right y) -> "ok:    " ++ show y
353
354
355 -----
356 -----
357 -----GLUE-CODE-----
358 {--
359 monadicUnify :: Term -> Term -> ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
360             (ST.STBinding s)
361             (UT.UTerm (FTS) (ST.STVar s (FTS))),
362             Map Id (ST.STVar s (FTS)))
363 monadicUnify t1 t2 = do
364     let
365         t1f = termFlattener t1
366         t2f = termFlattener t2
367         (x1,d1) <- lift . translateToUTerm $ t1f
368         (x2,d2) <- lift . translateToUTerm $ t2f
369         x3 <- U.unify x1 x2
370         return (x3, d1 'Map.union' d2)
371
372 --}
373
374 -- type st = Id -> Term

```

```

375
376 -- Convert result from monadicUnify to [st]
377 {--
378 goMonadicTest :: (Show b) => (forall s .
379   (ErrorT (UT.UFailure (FTS) (ST.STVar s (FTS)))
380     (ST.STBinding s)
381     (UT.UTerm (FTS) (ST.STVar s (FTS)),
382     Map Id (ST.STVar s (FTS)))))) -> [st]
383 goMonadicTest test = ST.runSTBinding £ do
384   answer <- runErrorT £ test
385   return £! case answer of
386     (Left x)  -> [nullst]
387     (Right y) -> convertTost y
388 --}
389
390 --(Id, STVar s FTS)
391 --convertTost :: Map Id (ST.STVar s FTS) -> [(Id, ST.STVar s FTS)]
392 {--
393 convertTost m = convertTost1 Map.toAscList m
394
395 convertTost1 (id, ST.STVar _ fts):xs = (id, (unFlatten fts)) : convertTost1 xs
396 --}

```

1232 15.10 Monadic Unification

```

1 monadicUnification :: (BindingMonad FTS (STVar s FTS) (ST.STBinding s)) => (forall
2   (ST.STBinding s) (UT.UTerm (FTS) (ST.STVar s (FTS)),
3   Map Id (ST.STVar s (FTS))))
4 monadicUnification t1 t2 = do
5   let
6     t1f = termFlattener t1
7     t2f = termFlattener t2
8     (x1,d1) <- lift . translateToUTerm $ t1f
9     (x2,d2) <- lift . translateToUTerm $ t2f
10    x3 <- U.unify x1 x2
11    --get state from somewhere, state -> dict
12    return $! (x3, d1 'Map.union' d2)
13
14
15 goUnify ::
16   (forall s. (BindingMonad FTS (STVar s FTS) (ST.STBinding s))
17   =>

```



```

18         (ErrorT
19           (UT.UFailure FTS (ST.STVar s FTS))
20           (ST.STBinding s)
21           (UT.UTerm FTS (ST.STVar s FTS),
22             Map Id (ST.STVar s FTS)))
23       )
24   -> [(Id, Prolog)]
25 goUnify test = ST.runSTBinding $ do
26   answer <- runErrorT $ test --ERROR
27   case answer of
28     (Left _)           -> return []
29     (Right (_, dict)) -> f1 dict
30
31
32 f1 ::
33   (BindingMonad FTS (STVar s FTS) (ST.STBinding s))
34   => (forall s. Map Id (STVar s FTS)
35     -> (ST.STBinding s [(Id, Prolog)]))
36   )
37 f1 dict = do
38   let ld1 = Map.toList dict
39   ld2 <- sequence [ v1 | (k,v) <- ld1, let v1 = UT.lookupVar v ]
40   let ld3 = [ (k,v) | ((k,_),Just v) <- ld1 'zip' ld2 ]
41   ld4 = [ (k,v) | (k,v2) <- ld3, let v = translateFromUTerm dict v2 ]
42   return ld4
43
44
45 --unify :: Term -> Term -> [st]
46 unify t1 t2 = stConvertor (goUnify (monadicUnification t1 t2))
47
48
49 varX :: Term
50 varX = Var (0,"x")
51
52 varY :: Term
53 varY = Var (1,"y")
54
55
56 stConvertor :: [(Id, Prolog)] -> [st]
57 stConvertor xs = Prelude.map (\(varId, p) -> (->-) varId (unFlatten $ unP $ p)) xs

```

1233 15.11 Chapter Recap

Chapter 16

Prototype 4

16.1 What is this chapter about

Our aim to embedd IO into the DSL

So something like a "data" declaration for IO operations

16.2 I/O is pure

[?]

A common question amongst people learning Haskell is whether I/O is pure or not. Haskell advertises itself as a purely functional programming language, but I/O looks like its inherently impure - for example, the function `getLine`, which gets a line from `stdin`, returns a different result depending on what the user types:

```
1 Prelude> x <- getLine
2 Hello
3 Prelude> x
4 "Hello"
```

How can this possibly be pure?

1247 In this post I want to explain exactly why I/O in Haskell is pure. Ill do it by building up
1248 data structures that represent blocks of code. These data structures can later be executed,
1249 and they cause effects to occur - but until that point well always work with pure functions,
1250 never with effects.

1251 Lets look at a simplified form of I/O, where we only care about reading from stdin,
1252 writing to stdout and returning a value. We can model this with the IOAction data type.

1253 That is, an IOAction is one of the following three things:

- 1254 1. A container for a value of type a,
- 1255 2. A container holding a String to be printed to stdout, followed by another IOAction a,
1256 or
- 1257 3. A container holding a function from String to IOAction a, which can be applied to
1258 whatever String is read from stdin.

1259 Notice that the only terminal constructor is Return that means that any IOAction must
1260 be a combination of Get and Put constructors, finally ending in a Return.

1261 Some simple actions include the one that prints to stdout before returning ():

```
put s = Put s (Return ())
```

1262 and the action that reads from stdin and returns the string unchanged:

```
get = Get (\s -> Return s)
```

1263 To build up a language for doing I/O we need to be able to combine and sequence
1264 actions. We want the ability to perform an IOAction a followed by an IOAction b, and
1265 return some result.

1266 In fact, we could have the second IOAction depend on the return value of the first one -
1267 that is, we need a sequencing combinator of the following type:

```
seqio :: IOAction a -> (a -> IOAction b) -> IOAction b
```

1268 We want to take the IOAction a supplied in the first argument, get its return value (which
1269 is of type a) and feed that to the function in the second argument, getting an IOAction b
1270 out, which can be sequenced with the first IOAction a.

1271 Thats a bit of a mouthful, but writing this combinator isnt too hard. When we reach the
1272 final Return, we apply the function f to get a new action. For the other constructors, we
1273 keep the form of the action the same, and just thread seqio through the seqio constructor.

1274 Using seqio we can define the action that gets input from stdin and immediately prints
1275 it to the screen:
1276 or even more complicated actions:

```
1 hello = put "What is your name?"      'seqio' \_ ->
2       get                             'seqio' \name ->
3       put "What is your age?"         'seqio' \_ ->
4       get                             'seqio' \age ->
5       put ("Hello " ++ name ++ "!") 'seqio' \_ ->
6       put ("You are " ++ age ++ " years old")
```

1277 Although this looks like imperative code (admittedly with pretty unpleasant syntax), its
1278 really a value of type IOAction (). In Haskell, code can be data and data can be code.

1279 In the gist Ive defined a function to convert an IOAction to a String, which allows them
1280 to be printed, so you can load the file into GHCi and verify that hello is in fact just data:

```
1 *Main> print hello
2 Put "What is your name?" (
3   Get ($0 ->
4     Put "What is your age?" (
5       Get ($1 ->
6         Put "Hello $0!" (
7           Put "You are $1 years old" (
8             Return ()
9           )
10        )
11      )
12    )
13  )
14 )
```

1281 It will surprise no one to learn that IOAction is a monad. In fact weve already defined the
1282 necessary bind operation in seqio, so getting the Monad instance is trivial:

```

1  instance Monad IOAction where
2      return = Return
3      (>>=) = seqio

```

1283 The main benefit of doing this is that we can now sequence actions using Haskell's `do`
 1284 notation, which desugars into calls to `(\do=)`, and hence to `seqio`. Our earlier `hello` example
 1285 can now be written as:

```

1  hello2 = do put "What is your name?"
2              name <- get
3              put "What is your age?"
4              age <- get
5              put ("Hello, " ++ name ++ "!")
6              put ("You are " ++ age ++ " years old!")

```

1286 Remember though, that this is still just defining a value of type `IOAction ()` - no code is
 1287 executed, and no effects occur! So far, this post is 100 % pure.

1288 To see the effects, we need to define a function that takes an `IOAction a` and converts
 1289 it into a value of type `IO a`, which can then be executed by the interpreter or the runtime
 1290 system. It's easy to write such a function just by turning it into the appropriate calls to
 1291 `putStrLn` and `getLine`.

```

1  run :: IOAction a -> IO a
2  run (Return a) = return a
3  run (Put s io) = putStrLn s >> run io
4  run (Get g)    = getLine >>= \s -> run (g s)

```

1292 You can now load up `GHCi` and apply `run` to any action - a value of type `IO a` will be
 1293 returned, and then immediately executed by the interpreter:

```

1  *Main> run hello
2  What is your name?
3  Chris
4  What is your age?
5  29
6  Hello Chris!
7  You are 29 years old

```

1294 Is there any practical use to this?

1295 Yes - an IOAction is a mini-language for doing I/O. In this mini language you are
1296 restricted to only reading from stdin and writing to stdout - there is no accessing files,
1297 spawning threads or network I/O.

1298 In effect we have a safe domain-specific language. If a user of your program or library
1299 supplies a value of type IOAction a, you know that you are free to convert it to an IO a using
1300 run and execute it, and it will never do anything except reading from stdin and writing to
1301 stdout (not that those things arent potentially dangerous in themselves, but)

```
1  -- http://chris-taylor.github.io/blog/2013/02/09/io-is-not-a-side-effect/
2
3  data IOAction a =
4    -- A container for a value of type a.
5      Return a
6    -- A container holding a String to be printed to stdout, followed by another IOAction
7      | Put String (IOAction a)
8    -- A container holding a function from String -> IOAction a, which can be applied
9      | Get (String -> IOAction a)
10 {--
11
12  Return 1
13
14  Put "hello" (Return ())
15  Put "hello" (
16    Return ()
17  )
18
19  Put "hello" (Return 1)
20  Put "hello" (
21    Return 1
22  )
23
24  Put "hello" (get)
25  Put "hello" (
26    Get (£0 ->
27      Return "£0"
28    )
29  )
30
31  Get put
```

```

32  Get (f0 ->
33      Put "f0" (
34          Return ()
35      )
36  )
37
38  --}
39
40  -- Read and return
41  get :: IOAction String
42  get  = Get Return
43  {--
44
45  Get (f0 ->
46      Return "f0"
47  )
48
49  --}
50
51  -- Print and return.
52  put :: String -> IOAction ()
53  put s = Put s (Return ())
54  {--
55
56  put "hello"
57  Put "hello" (
58      Return ()
59  )
60
61  --}
62
63  -- (>=) Action sequencer and combiner :- read -> write -> read -> write -> ....
64  seqio :: IOAction a -> (a -> IOAction b) -> IOAction b
65  --      (First action      (Take and perform
66  --      which generates next action)
67  --      value a)
68  seqio (Return a) f = f a
69  seqio (Put s io) f = Put s (seqio io f)
70  seqio (Get g)     f = Get (\s -> seqio (g s) f)
71
72  --Take input and print.
73  echo :: IOAction ()
74  echo = get 'seqio' put
75  {--
76

```

```

77  Get (£0 ->
78      Put "£0" (
79          Return ()
80      )
81  )
82
83  --}
84
85  hello :: IOAction ()
86  hello = put "What is your name?"      'seqio' \_ ->
87          get                          'seqio' \name ->
88          put "What is your age?"      'seqio' \_ ->
89          get                          'seqio' \age ->
90          put ("Hello " ++ name ++ "!") 'seqio' \_ ->
91          put ("You are " ++ age ++ " years old")
92  {--
93
94  Put "What is your name?" (
95      Get (£0 ->
96          Put "What is your age?" (
97              Get (£1 ->
98                  Put "Hello £0!" (
99                      Put "You are £1 years old" (
100                          Return ()
101                      )
102                  )
103              )
104          )
105      )
106  )
107
108  run hello
109  What is your name?
110  Mehul
111  What is your age?
112  25
113  Hello Mehul!
114  You are 25 years old
115
116  --}
117
118  -- hello in "do" block since IOAction is a Monad
119  hello2 :: IOAction ()
120  hello2 = do put "What is your name?"
121            name <- get

```



```

122         put "What is your age?"
123         age <- get
124         put ("Hello, " ++ name ++ "!")
125         put ("You are " ++ age ++ " years old!")
126     {--
127
128     Put "What is your name?" (
129         Get (l0 ->
130             Put "What is your age?" (
131                 Get (l1 ->
132                     Put "Hello, l0!" (
133                         Put "You are l1 years old!" (
134                             Return ()
135                         )
136                     )
137                 )
138             )
139         )
140     )
141
142     run hello2
143     What is your name?
144     Mehul
145     What is your age?
146     25
147     Hello, Mehul!
148     You are 25 years old!
149
150     --}
151
152     -- where the effects happen.
153     -- "Real" IO functions like return, putStrLn, getLine.
154     run :: IOAction a -> IO a
155     run (Return a) = return a
156     run (Put s io) = putStrLn s >> run io
157     run (Get f)    = getLine >>= run . f
158     {--
159
160     run (Return 1)
161     1
162
163     run (Put "hello" get)
164     hello
165     1
166     "1"

```

```

167
168 run (Get put)
169 1
170 1
171
172 --}
173
174
175 -- Glue code that makes everything play nice --
176
177 instance Monad IOAction where
178     return = Return
179     (>=) = seqio
180
181 instance Show a => Show (IOAction a) where
182     show io = go 0 0 io
183     where
184         go m n (Return a) = ind m "Return " ++ show a
185         go m n (Put s io) = ind m "Put " ++ show s ++ " (\n" ++ go (m+2) n io ++ "\n"
186         go m n (Get g)     = let i = "$" ++ show n
187                             in ind m "Get (" ++ i ++ " -> \n" ++ go (m+2) (n+1) (g i)
188
189         ind m s = replicate m ' ' ++ s
190
191 -- IOAction is also a Functor --
192
193 mapio :: (a -> b) -> IOAction a -> IOAction b
194 mapio f (Return a) = Return (f a)
195 mapio f (Put s io) = Put s (mapio f io)
196 mapio f (Get g)     = Get (\s -> mapio f (g s))
197 {--
198
199 mapio (+1) (Return 1)
200 Return 2
201
202 mapio (id) (Put "hello" get)
203 Put "hello" (
204     Get (£0 ->
205         Return "£0"
206     )
207 )
208
209 mapio (id) (Get put)
210 Get (£0 ->
211     Put "£0" (

```

```

212     Return ()
213   )
214 )
215
216 --}
217
218 instance Functor IOAction where
219     fmap = mapio

```

1302 16.3 Dr. Casperson Pure IO

```

1  -- Prolog IO
2
3  {--
4  FREE MONADS
5  In general, a structure is called free when it is left-adjoint to a forgetful functor.
6  In this specific instance, the Term data type is a higher-order functor that maps
7  a functor f to the monad Term f ; this is illustrated by the above two instance
8  definitions. This Term functor is left-adjoint to the forgetful functor from monads
9  to their underlying functors.
10 --}
11
12 data Term f a = Pure a
13                | Impure (f (Term f a))
14
15 main = undefined
16
17 instance Functor f => Functor (Term f) where
18     fmap f (Pure x )      = Pure (f x )
19     fmap f (Impure t)     = Impure (fmap (fmap f ) t)
20
21 instance Functor f => Monad (Term f) where
22     return x              = Pure x
23     (Pure x ) >>= f       = f x
24     (Impure t) >>= f      = Impure (fmap (>>= f ) t)

```

1303 16.4 Mehul Pure IO

1304 So when the program is getting interpreted the interpreter encounters an IO operation which
1305 then gets "interpreted" to the above and it continues normally.

1306 The interpreted program is still pure since the IO actions have not been executed

1307 if the running is done inside a monad then the IO still is pure.

```
1  import Data.Traversable
2  import Control.Monad
3  import Data.Functor
4  import Control.Applicative
5  import System.IO
6
7  data PrologResult
8      = NoResult
9      | Cons OneBinding PrologResult
10     | IOIn (IO String) (String -> PrologResult)
11     | IOOut (IO ()) PrologResult
12
13
14
15  data OneBinding = Pair VariableName VariableName
16
17
18  --data MiniLang a = MyData a | Empty | Input
19
20  --runInIO :: PrologResult -> IO [OneBinding]
21
22
23  data PrologIO a = Input (IO a) | Output (a -> IO ()) | PrologData a | Empty
24  --
25  {--
26  instance Functor (PrologIO) where
27      fmap f Empty = Empty
28      fmap f (Input (IO a)) = Input (IO (f a))
29      -- fmap f (Output (a -> IO ())) = Output (a -> IO (f a))
30      -- fmap f (PrologData a) = PrologData (f a)
31  --}
32
33  instance Monad PrologIO where
34      return a = PrologData a
35      -- (Input i) >>= (Output o) = i >>= (\a -> (o a))
```

```

36
37 instance (Show a) => Show (PrologIO a) where
38     show (Empty)                = show "No result"
39     show (PrologData a) = show a
40     --      show (Input f)                = show (f ++ "")
41     --      show (Output )
42
43
44 -- (>=) Action sequencer and combiner :- read -> write -> read -> write -> ....
45 seqio :: PrologIO a -> (a -> PrologIO b) -> PrologIO b
46 --      (First action      (Take and perform
47 --      which generates next action)
48 --      value a)
49 seqio (PrologData a)          f          = f a
50 --seqio (Output o)              f          = \a -> o a
51 --seqio (Input i)              f          = \s -> (seqio (i s) f) --
52
53
54
55 {--
56 instance Applicative PrologIO where
57     func =
58
59 instance Traversable PrologIO where
60     traverse f Empty                                = Empty
61     traverse f (Input (IO a))                        = Input (IO (f a))
62     traverse f (Output (a -> IO ()))                = Output ((a) -> IO (f a))
63     traverse f (PrologData a)                        = PrologData (f a)
64 --}
65
66
67 concat :: PrologIO t -> PrologIO t -> IO ()
68 concat (Input f1) (Output f2) = do
69     x <- f1
70     f2 x
71 {--
72 concat (Input getLine) (Output putStrLn)
73 Loading package list-extras-0.4.1.4 ... linking ... done.
74 Loading package syb-0.5.1 ... linking ... done.
75 Loading package array-0.5.0.0 ... linking ... done.
76 Loading package deepseq-1.3.0.2 ... linking ... done.
77 Loading package containers-0.5.5.1 ... linking ... done.
78 Loading package transformers-0.4.3.0 ... linking ... done.
79 Loading package mtl-2.2.1 ... linking ... done.
80 Loading package logict-0.6.0.2 ... linking ... done.

```

```
81  Loading package unification-fd-0.10.0.1 ... linking ... done.
82  1
83  1
84  --}
```

1308 **16.5 Chapter Recap**

Chapter 17

Work Completed

17.1 What is this chapter about

17.2 What we are doing

A partial implementation of the logic programming language PROLOG is provided by the library `prolog-0.2.0.1`. One of the objectives is to implement monadic unification using the library [?].

17.3 Unifiable Data Structures

For a data type to be Unifiable, it must have instances of Functor, Foldable and Traversable. The interaction between different classes is depicted in figure 1.1.

The Functor class provides the `fmap` function which applies a particular operation to each element in the given data structure. The Foldable class *folds* the data structure by recursively applying the operation to each element and

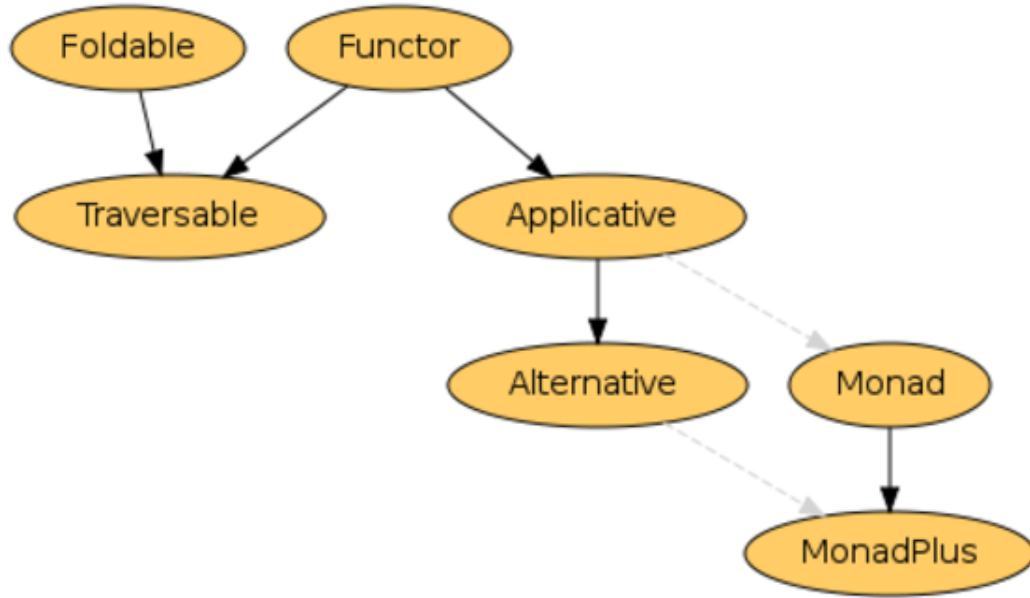


Figure 17.1: Functor Hierarchy [?]

1323 17.4 Why Fix is necessary?

1324 Since HASKELL is a lazy language it can work with infinite data structures. *Type Synonyms*
 1325 in HASKELL cannot be self referential.

1326 In our case consider the following example,

```

-- The Prolog Syntax
type Atom = String
data VariableName = VariableName Int String deriving (Show,Eq,Ord)
data FlatTerm a =
    | Struct Atom [a]
    | Var VariableName
    | Wildcard
    | Cut Int deriving (Show,Eq,Ord)
  
```

1327 A FlatTerm can be of infinite depth which due to the reason stated above cannot be
 1328 accounted for during application function. The resulting type signature would be of the
 1329 form,

```
FlatTerm (FlatTerm (FlatTerm (FlatTerm (.....))))
```


1330 Enter the Fix same as the function as a data type. The above would be simply reduced
1331 to,

```
Fix FlatTerm
```

1332 resulting in the PROLOG Data Type

```
data Prolog = P (Fix FlatTerm) deriving (Show,Eq,Ord)
```

1333 17.5 Dr. Casperson's Explanation

1334 A recursive data type in HASKELL is where one value of some type contains values of that
1335 type, which in turn contain more values of the same type and so on. Consider the following
1336 example.

```
data Tree = Leaf Int | Node Int (Tree) (Tree)
```

1337 A sample Tree would be,

```
(Node 0 (Leaf 1) (Node 2 (Leaf 3) (Leaf 4)))
```

1338 The above structure can be infinitely deep since HASKELL is a *lazy* programming lan-
1339 guage. But working with an infinitely deep / nested structure is not possible and will result
1340 in a *occurs check* error. This is because writing a type signature for a function to deal
1341 with such a parameter is not possible. One option would be to *flatten* the data type by the
1342 introduction of a type variable. Consider the following,

```
data FlatTree a = Leaf Int | Node Int a a
```

1343 A sample FlatTerm would be similar to Tree.

1344 The FlatTree is recursive but does not reference itself. But it too can be infinitely deep
1345 and hence writing a function to work on the structure is not possible.

1346 17.6 The other fix

1347 The `fix` function in the `Control.Monad.Fix` module allows for the definition of recursive
1348 functions in HASKELL. Consider the following scenario,

```
fix :: (a -> a) -> a
```

1349 The above function results in an infinite application stream,

```
f s : f (f (f (...)))
```

1350 A fixed point of a function `f` is a value `a` such that `f a == a`. This is where the name of
1351 `fix` comes from: it finds the least-defined fixed point of a function.

1352 17.7 The Fix we use

1353 Fix-point type allows to define generic recursion schemes [?]. [?]

1354 **What is Algebra** Naively speaking algebra gives us the ability to perform calculations
1355 with numbers and symbols.

1356 **What can algebra do** The ability to form and evaluate expressions.

1357 **How to generate expressions** Using grammars, for example

```
1 data Expr = Const Int
2           | Add Expr Expr
3           | Mul Expr Expr
```

1358 **How to uncover primitives from a recursive type** Make it non-recursive by defining a
1359 type function, otherwise known as type constructor,

```
1 ExprF a = Const Int
2         | Add a a
3         | Mul a a
```

1360 **How to create a nested structure from the above** The fractally recursive structure of `Expr`
1361 can be generated by repeatedly applying `ExprF` to itself.

```
1  (ExprF (ExprF (ExprF a)))
```

1362 **How to generate really deep expressions** Keep on applying

```
ExprF
```

1363 **Is there a better way** After infinitely many iterations we should get to a fix point where
1364 further iterations make no difference. It means that applying one more ExprF would
1365 not change anything – a fix point does not move under ExprF. It's like adding one to
1366 infinity: you get back infinity.

1367 **How do that in HASKELL** In HASKELL, we can express the fix point of a type construc-
1368 tor f as a type:

```
1  newtype Fix f = f (Fix f)
```

1369 With that, we can redefine Expr as a fixed point of ExprF:

```
1  type Expr = Fix ExprF
```

1370 **Any other benefits** Writing functions is simpler. You can have the terms of all depths
1371 encapsulated under the same type, i.e.

```
Fix ExprF
```

1372 So rather than writing separate functions for,

```
1  (ExprF a)
2
3  (ExprF (ExprF a))
4
5  (ExprF (ExprF (ExprF a)))
6
7  (ExprF (ExprF (ExprF ...)))
```

1373 We write a function from,

```
func :: Fix ExprF -> Fix ExprF
```

17.8 Opening up or Extending language Explanation using Box Analogy

This section will describe what it means to “open up or extend a language”.

1. Let us start with a sample language with a recursive abstract syntax,

```
1  type Atom                = String
2
3  data VariableName        = VariableName Int String
4      deriving (Eq, Data, Typeable, Ord)
5
6  data Term                = Struct Atom [Term]
7                          | Var VariableName
8                          | Wildcard
9                          | Cut Int
10     deriving (Eq, Data, Typeable)
```

The above language represent a stripped down version of PROLOG from [?]. The pool of the expressions that can be generated from *Term* are restricted to the constructors,

```
1  Struct "hello" [Struct "a" []]      -- hello(a).
2  Var (VariableName 125 "X")          -- X = 125.
3  Wildcard                          -- _ .
4  Cut 0                               -- !.
```

It does not allow the ability to have a “typed” *Term*, for example a *Term* of type *int* or *string* and so on.

2. So we **flatten** the language by introducing a type variable,

```
1  type Atom = String
2
3  data VariableName = VariableName Int String deriving (Show, Eq, Ord)
4
5  data FlatTerm a =
6      Struct Atom [a]
7      | Var VariableName
8      | Wildcard
9      | Cut Int deriving (Show, Eq, Ord)
```

1383 The above language can be of any type a . A more accurate way of saying it would
1384 be that a can be a *kind* in HASKELL.

1385 In type theory, a kind is the type of a type constructor or, less commonly, the type
1386 of a higher-order type operator. A kind system is essentially a simply typed lambda
1387 calculus 'one level up,' endowed with a primitive type, denoted $*$ and called 'type,'
1388 which is the kind of any (monomorphic) data type for example [?],

```
1 Int :: *
2 Maybe :: * -> *
3 Maybe Bool :: *
4 a -> a :: *
5 [] :: * -> *
6 (->) :: * -> * -> *
```

1389 Simply speaking the a can be changed.

1390 3. It gives the language the capability to be expanded. Adding some functionality to the
1391 original language could be done in a no. of ways

1392 (a) Manually modifying the structure of the language,

```
1 type Atom = String
2
3 data VariableName = VariableName Int String
4   deriving (Eq, Data, Typeable, Ord)
5
6 data Term = Struct Atom [Term]
7           | Var VariableName
8           | Wildcard
9           | Cut Int
10          | New_Constructor_1 .....
11          | New_Constructor_2 .....
12   deriving (Eq, Data, Typeable)
```

1393 This would then trigger a ripple effect throughout the architecture because ac-
1394 comodations need to be made for the new functionality.

1395 (b) The other option would be to *functorize* language like we did by adding a type
1396 variable which can be used to plug something that provides the functionality

1397 into the language. Consider the following example,

```
1 data Box f = Abox | T f (Box f) deriving (.....)
```

1398 then something like,

```
1 T (Struct 'atom' [Abox, T (Cut 0)])
```

1399 is possible. Since we needed the fixed point of the language we used *Fix* but
1400 generically one could add multiple custom functionality.

1401 4. If we have a grammar that support an expressions like,

1402 $x \cdot y + x \cdot z$

1403 Once the language is 'functorized' one can add quantifiers and logic to the language
1404 to do something like,

1405 $\forall x \forall y \forall z \quad x \cdot y + x \cdot z$

1406 $= x \cdot (y + z)$

1407 5. Multiple modifications

1408 6. As is with the original language it can be wrapped with multiple other data structures,

```
1 Just (Strcut ..... ) -- A Maybe Term
2 [Cut 0]                -- A List of Terms
```

1409 and so on. But the core expression can only be of type *Term*.

1410 Whereas a *FlatTerm* expression can not only have an outer wrapper but also its type
1411 is 'open'.

1412 17.9 Chapter Recap

Chapter 18

Results

18.1 What is this chapter about

18.2 Types

One of the major differences between PROLOG and HASKELL is how each language handles types. PROLOG is an untyped language meaning any operation can be performed on the data irrespective of its type. HASKELL on the other hand is strongly typed i.e. each operation requires a signature stating what types of data it can work with. Moreover, the HASKELL type system is static.

PROLOG like any other language can work with some basic data types like numbers, characters, strings among others. Using these one can make terms like *Atoms*, *Clauses*, *Constants*, *Strings*, *Characters*, *Predicates*, *Structures*, *Special Characters* and so on. These need to be incorporated into the implementation so as to give a palette for writing programs.

Our preliminary implementation is as follows,

```
type Atom = String
```

```
data VariableName = VariableName Int String deriving (Show,Eq,Ord)
```

```

data FlatTerm a =
    Struct Atom [a]
    | Var VariableName
    | Wildcard
    | Cut Int deriving (Show,Eq,Ord)

{--
Output :-

Struct "a" [Var (VariableName 0 "x"),Cut 0,Wildcard,Struct "b" []]

--}

```

1428 which in PROLOG would look like,

```
a(X, !, b).
```

1429 18.3 Lazy Evaluation

1430 18.4 Opening up the Language

1431 **Flattening**

1432 **Fixing**

1433 **MetaSyntactic Variables**

1434 18.5 Quasi Quotation

1435 18.6 Template Haskell

1436 18.7 Higher Order Functions

```
% Mehul Solanki.

% Higher Order Functions.

% The following library contains the maplist function.
:- use_module(library(apply)).

% The maplist function takes a function and a list to apply the
% function.
% The function write is passes which will print out the elements
% of the list.
higherOrder(X) :- maplist(write,X).

/*
higherOrder([1,2,3,4]).
1234
true
*/
```

1437 18.8 I/O

```
data Result = Ordinary _____ --No I/O required
| SideEffect (IO _____)      -- Requiring Output
| ReadEffect (IO _____ -> Result) -- Requiring Input
```

1438 **18.9 Mutability**

1439 **18.10 Unification**

1440 **18.11 Monads**

1441 **18.12 Chapter Recap**

Chapter 19

Future Scope

19.1 What is this chapter about

1. Quasi quoter to get something like,

```
1 [prolog|a(X) :- b(y)|]
```

where X is a PROLOG variable and y is a HASKELL variable injected into the expression

2. We already have variable search strategies, what if the query resolver could be instructed to use a particular search strategy to get the result.

```
1 queryResolver searchStrategy query knowledgeBase
```

3. Add database operations

4. Multi type variable Language

5. Pure + IO Combined Language

```
1 data ResultWithIO typevariableforpureexpressions typevariableforioexpressions
2     = PureConstructor_1 ....
3     | PureConstructor_2 ....
```

```

4      | IOContrcutor_1 .....
5      | IOConstructor_2 ...
6      | ConstructorWithBoth_1 .....
7      | ConstructorWithBoth_2 .....
8      deriving(.....)

```

1454 6.

1455 19.2 Chapter Recap

1456 **Chapter 20**

1457 **Conclusion / Expected Outcomes**

1458 **20.1 What is this chapter about**

1459

1460 The aim of this study is to experiment with two different languages working together
1461 and/or contributing in providing a solution. Mixing and matching conflicting characteristics
1462 may lead to a behaviour similar to that of a multi paradigm language. The points to be
1463 looked at are efficiency of the emulation, semantics of the resulting embedding.

1464 Moreover, this will be an attempt to answer the question how practical PROLOG fits
1465 into HASKELL.

1466 **20.2 Chapter Recap**

Chapter 21

Editing to do

This Chapter needs to be removed from the final work.

Meeting on 5th Novemeber 2015

1. Write about this chapter and chapter conclusion for all chapters
2. Till haskell why haskell chapter 11 wait for feedback
3. In the remaining chapters write according to flow == move around stuff or add new content.

2015-10-29

1. Abstract is too long and incorrect.
2. Remove first ¶ from intro.
3. Thesis statement is close to being an abstract.

Either

4. We need a convention for what words to capitalize in chapter and section titles.

Mehul

5. Chapter 13.5 needs fleshing out.
6. **Rewrite (Section) Chapter 3.2**. You are now in a position to state what your contributions are. In some sense everything else flows around this.
7. Fix the reference at the bottom of page 2:
`citewikipro- log,somogyi1995logic,website:prolog1000db`. **SOLVED**
8. Write enough of Chapters 13–16 that we can decide what material is needed in Chapters 9, 10, and ??.
9. [mainly done] If you don't like the shape of the paragraphs that you get without paragraph, use something like
`\setlength{\parindent}{3em}`
`\setlength{\parskip}{2\baselineskip}`
 to adjust either the initial paragraph indent, or the inter-paragraph space.
10. Rewrite (Section) Chapter 3 in formal English.
11. “re-curses” means to swear again (*p* 9). **Changed to recurs**
12. I am not sure that I agree with the use of “reflective” on *p* 8 (*l* 25). Reflection often means run-time introspection (for instance the Java `.getClass()` method). In computer science, reflection is the ability of a computer program to examine (see type introspection) and modify its own structure and behavior (specifically the values, meta-data, properties and functions) at runtime.
13. Supply your credentials in the front material (what degrees do you have?). (Search for `%% Supply your credentials in proposal1.tex`.)
14. The abstract is too long. UNBC guidelines limit Masters' theses abstracts to 150 words.

15. Citation `logic-classes` is not defined (in `./prologinhaskell.tex`).

David

16. Clean up the non-exclusive license page in `unbcthesis.cls`

17. Incorporate `unbcthesis.cls` into Mehul's work.

18. Review Chapter 2

19. Review Chapter 3

20. Review Chapter 4

21. Review Chapter 5

22. Review Chapter 6

23. Review Chapter 7

24. Review Chapter 8

25. Review Chapter 18

21.1 Editing suggestions from David

Thoughts on Chapter 14

- Do not use naked `\refs`: “*the generic methodology from 13*” should be “*the generic methodology from **Chapter 13***”.
- You should say more about [?], either here or in an earlier section and reference that discussion here. For instance, it isn't clear that `prolog-0.2.0.1` comes from [?].
- See my comments below. I suspect that longer listings should be separate figures.

```

1 data VariableName = VariableName Int String
2     deriving (Eq, Data, Typeable, Ord)
3 data Atom          = Atom          !String
4                   | Operator      !String
5     deriving (Eq, Ord, Data, Typeable)
6 data Term = Struct Atom [Term]
7           | Var VariableName
8           | Wildcard
9           | PString    !String
10          | PInteger   !Integer
11          | PFloat     !Double
12          | Flat [FlatItem]
13          | Cut Int
14     deriving (Eq, Data, Typeable)
15 data Clause = Clause { lhs :: Term, rhs_ :: [Goal] }
16             | ClauseFn { lhs :: Term, fn :: [Term] -> [Goal] }
17     deriving (Data, Typeable)
18 type Program = [Sentence]
19 type Body    = [Goal]
20 data Sentence = Query    Body
21              | Command Body
22              | C Clause
23     deriving (Data, Typeable)

```

Figure 21.1: A sample Minted figure

- Line 7 on p 55 is not a complete sentence.
- I suspect that § 14.2 should start with a sentence like

The prolog-0.2.0.1 ([?]) was written by Indira Ghandi and consists of 718 HASKELL files. It implements data base assertions and cuts but lacks any IO facilities...

and then go on to discuss the syntax.

Thoughts on Chapter 13 I am looking at what are currently lines 145–on in `proto1.tex`, and I am not sure whether

1. the text should be loose—as you have it, or floated to a figure, as shown in Figure 13.2.

2. I am also not sure whether I like the inlined code, or whether I would prefer to have it `\inputminted` from a HASKELL file. I suppose that this depends on your work-flow. Thoughts?

I am not sure what conventions you are following with respect to code in text. At some point you have `FlatTerm` in italics (à la *FlatTerm*); at other points you have it typeset in straight double quotes (`"FlatTerm"`) and I don't know what the different typesetting implies.

Just above Section 13.5 you mention a generic function `map`, which for STANDARD ML and HASKELL readers likely means the function with signature $(a \rightarrow b) \rightarrow ([a] \rightarrow [b])$. Why not `fmap`?

I am not sure what the point of the ¶ before Section 13.5 is.

Thoughts on 1.1 We need to firmly fix in mind who the target audience is. Some possibilities

1. Undergraduate Physics students
2. Undergraduate Computer Science students
3. Future graduate students of Casperson who have just begun their thesis work.
4. Simon Peyton-Jones.

If we assume (3), then the material in the first paragraph and part of the second are unnecessary.

Thoughts on 1.3 I am unsure that I can summarize this subsection in two sentences. I don't know what the problem statement is at the end of it.

Thoughts on 1.4 Rename to "Thesis Organization".

Thoughts on Chapter 2 Here are some potential keywords from Chapter 2: • Hindley-Milner type systems • Horn clauses • λ -calculi • HASKELL • SCALA • declarative programming languages • foreign function interfaces • functional programming • implementing Prolog in other languages • language embedding • language families • language paradigms • logic programming • meta-programming • monads • paradigm integration • quasi-quotation • the typed λ -calculus • the untyped λ -calculus .

What is the overall message?

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