



# Asymptotically Optimal Validated Asynchronous Byzantine Agreement

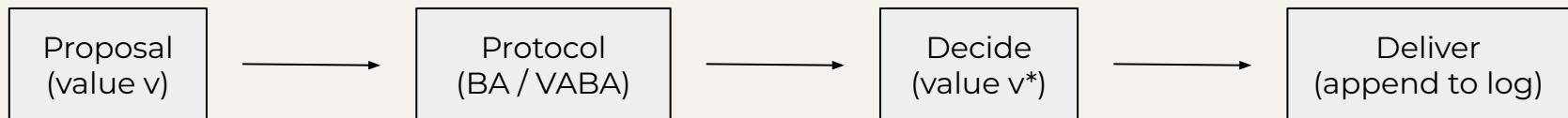
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# Introduction

**General Goal:** Make a distributed system behave like one server

## Standard approach

- **Atomic Broadcast:** All replicas get the same operations in the same order
- **State Machine Replication:** All replicas move through the same sequence of states

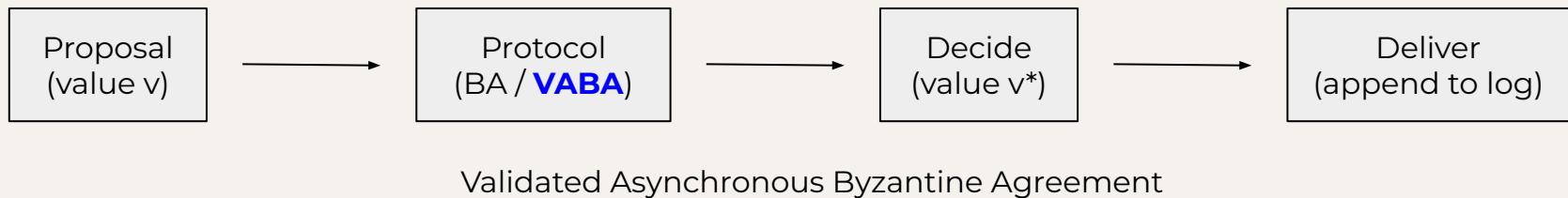


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# Introduction

**Cachin et al. [10]**

- Defined Atomic Broadcast & VABA in the authenticated asynchronous model.
- Resilience:  $n = 3f + 1$  → Optimal
- Running Time:  $O(1)$  → Optimal
- Expected Word Communication:  $O(n^3)$  → Not optimal

**Specific Goal:**

- Achieve  $O(n^2)$  on Expected Word Communication while maintaining optimality on Resilience and Time.

# Introduction

## Byzantine Agreement (BA)

- **Validity:** If all honest parties propose value  $v$ , then they must decide value  $v$  when terminate.
  - **Weakness**
    - Decide on a value proposed by faulty party.
    - Decide a constant value => No progress
- **Synchronous:** All messages are delivered within  $\Delta$ 
  - Synchronous
  - Eventual synchronous
  - Partially synchronous
  - Weakly synchronous (e.g. PBFT)
  - **Weakness**
    - Real-World networks can have unpredictable message delays

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## Validated Asynchronous Byzantine Agreement (VABA)

- **Quality:** The decided value  $v$  was proposed by an honest party with  $p \geq 0.5$
- **External Validity:** If an honest party decides a value  $v$ , then  $\text{EX-PB-VAL}(v) = \text{True}$ .
- **Asynchronous:** No timing assumption on the network.

# Provable-Broadcast

Sender  $P_s$

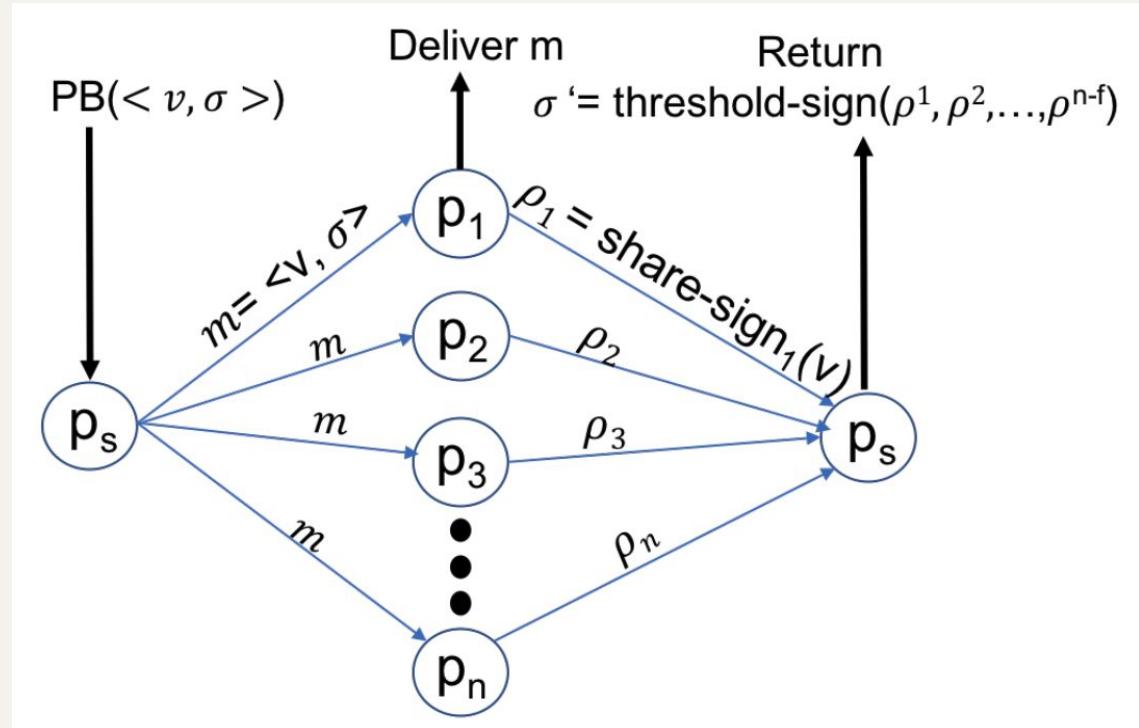
- $v$ : value
- $\sigma$ : proof

Receiver (other parties)

- $\rho$ : signature share

Sender  $P_s$

- wait until receiving  $n-f$  signature shares
- $\sigma'$ : threshold signature



# The Structure of a VABA View

A VABA view is comprised of three core phases:

- **Leader-nomination**
  - Provide all parties/replicas the opportunity to promote a value.
- **Leader-election**
  - Randomly selects a party as leader to promote their value.
- **View-change**
  - Synchronize all parties on the chosen leader's progress to safely finalize the value or move to the next view.

# Leader Nomination

- Every party acts as a leader of its own **Proposal-Promotion** instance.
- All Proposal-Promotion instances run in parallel.
- Each party tries to promote its own value.

**Goal:** Ensure that at least one honest value makes sufficient progress to be safely used later.

# Proposal-Promotion Overview

- Each leader runs four **Provable-Broadcast** steps:
  - Initial broadcast
  - Key
  - Lock
  - Commit
- What strengthens at each stage is the cryptographic evidence attached to the value.

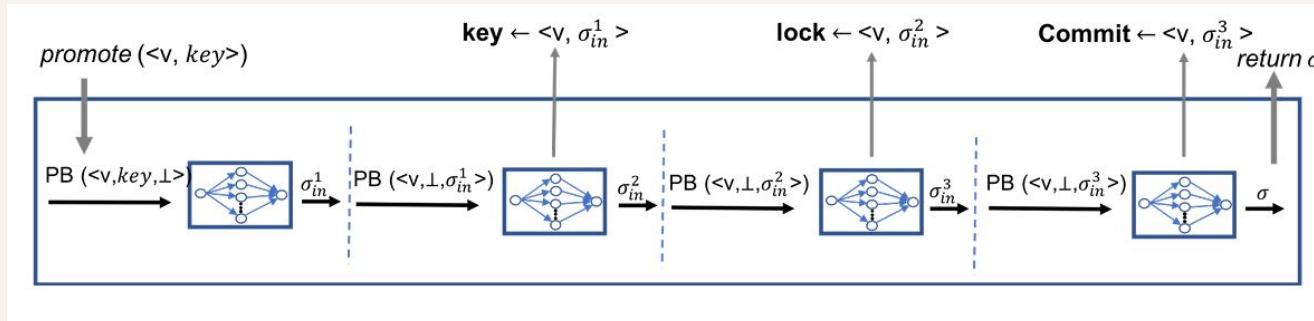
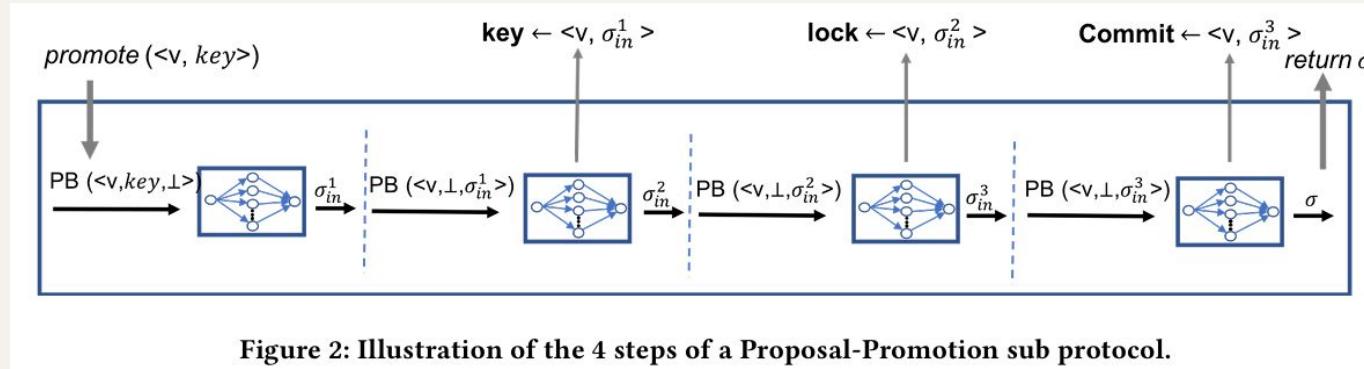


Figure 2: Illustration of the 4 steps of a Proposal-Promotion sub protocol.

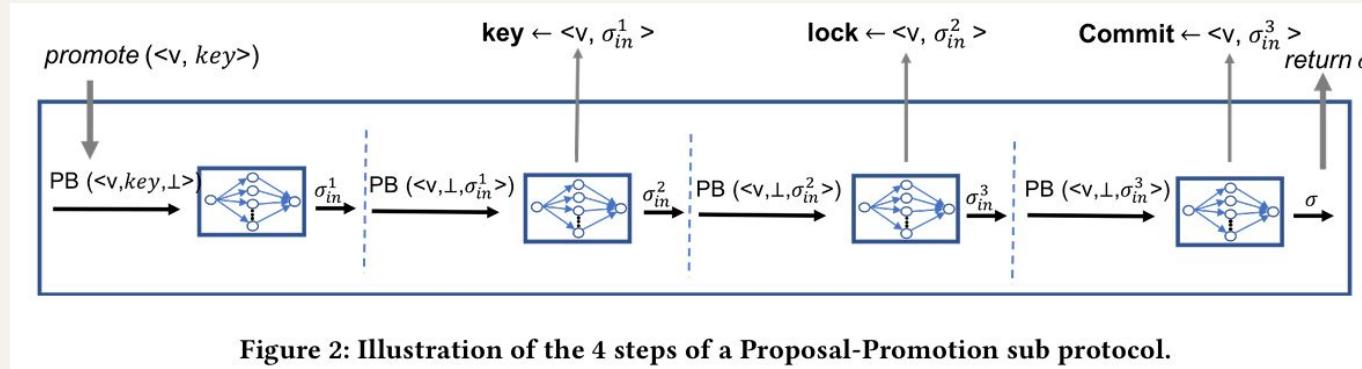
# Proposal-Promotion: Initial Broadcast

- Leader distributes its value with external validity proof.
- Parties verify and send back signature shares.
- Leader builds a certificate after  **$2f + 1$**  signature shares proving the value is valid.



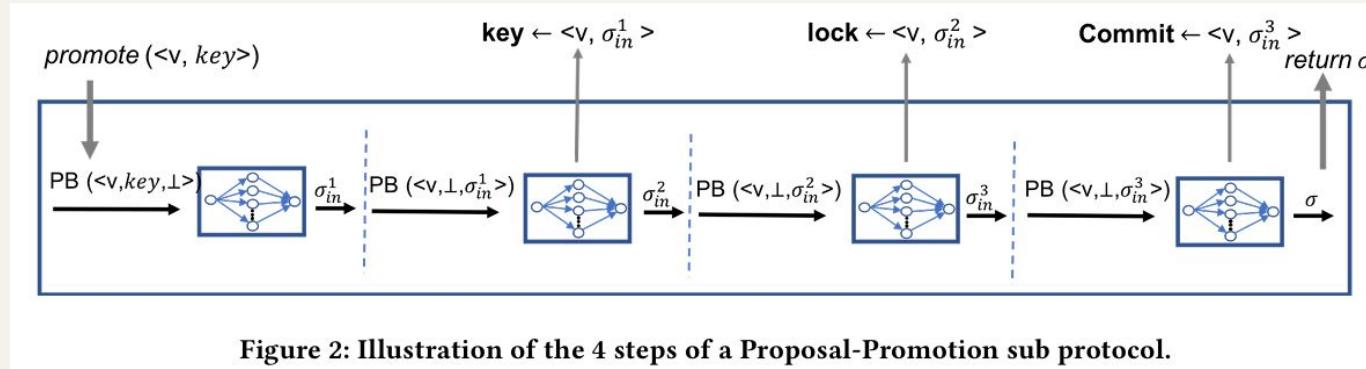
# Proposal-Promotion: Key Stage

- Parties deliver the value and store it as key.
- Leader creates Key certificate after receiving  $2f + 1$  signature shares which act as proof:
  - “Enough honest parties have seen this value.”
- This marks the value as a legitimate candidate.



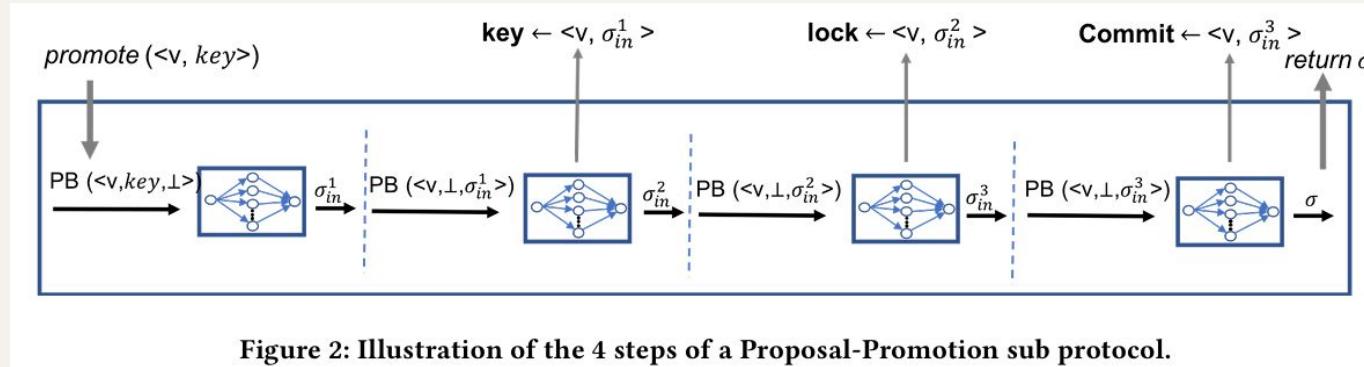
# Proposal-Promotion: Lock Stage

- Parties deliver and store the lock.
- Lock certificate proves enough parties are committed to protecting this value.
- Conflicting values cannot progress safely after this point.



# Proposal-Promotion: Commit Stage

- Parties deliver and store the commit.
- Commit certificate proves the value is now finalizable.
- No other value can compete with a committed value.

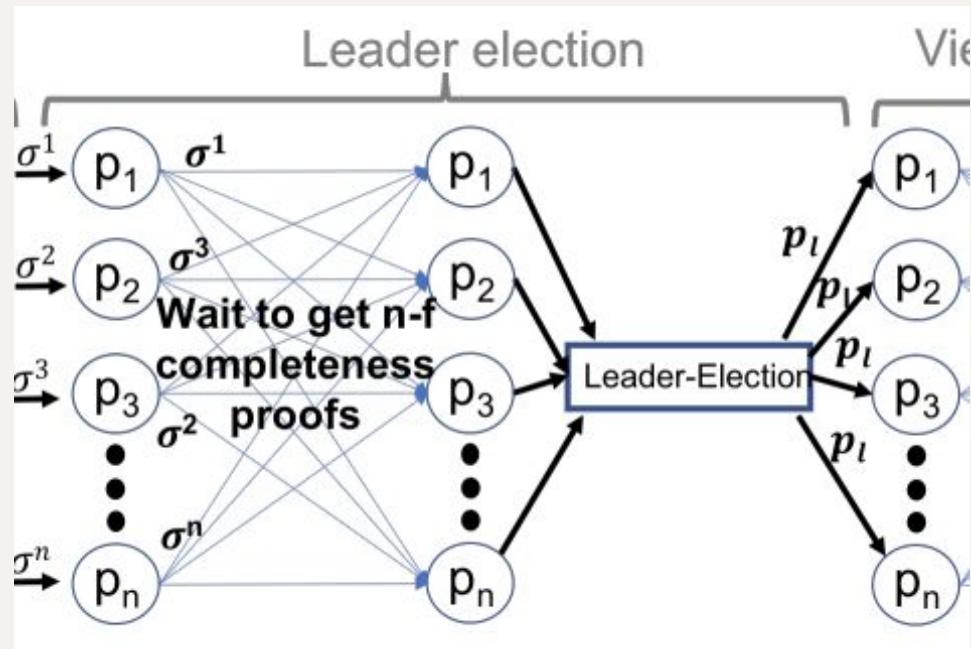


# The Coin Toss

- Includes private function  $\text{coin-share}_i$
- Includes two public function  $\text{coin-share-validate}$  &  $\text{coin-toss}$
- Given  $f + 1$  valid coin shares, coin toss return a unique & pseudorandom number
  - Range 1 to  $n$

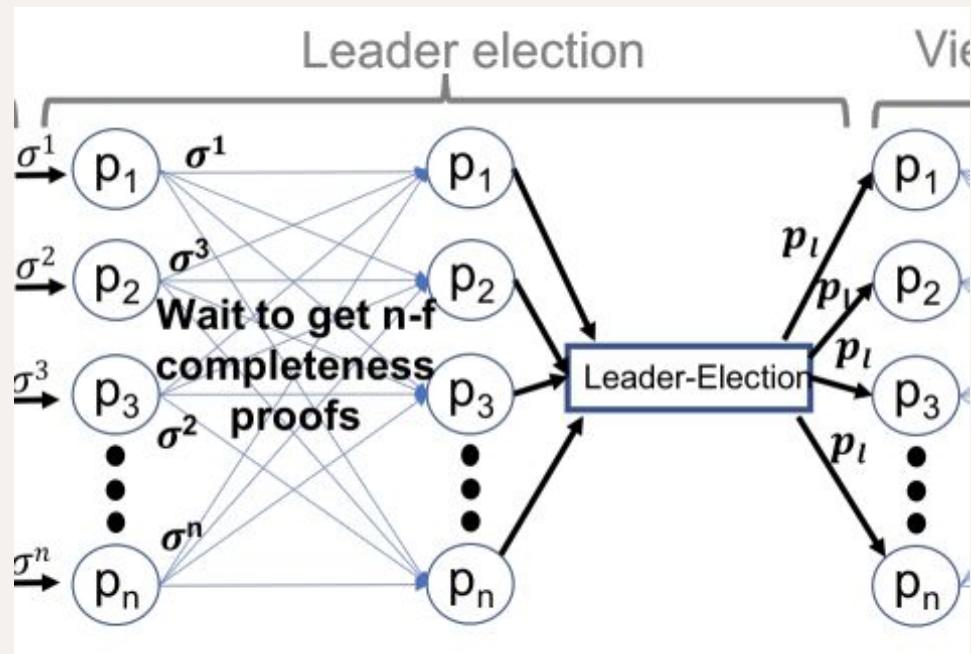
# Entering Leader Election

- Broadcast Done(value, proof)
- Collect  $n - f$  Done messages
- Send Skip-share message
- Collect  $n - f$  valid Skip-shares
- Send Skip message
- Collect valid Skip message and move to Leader Election



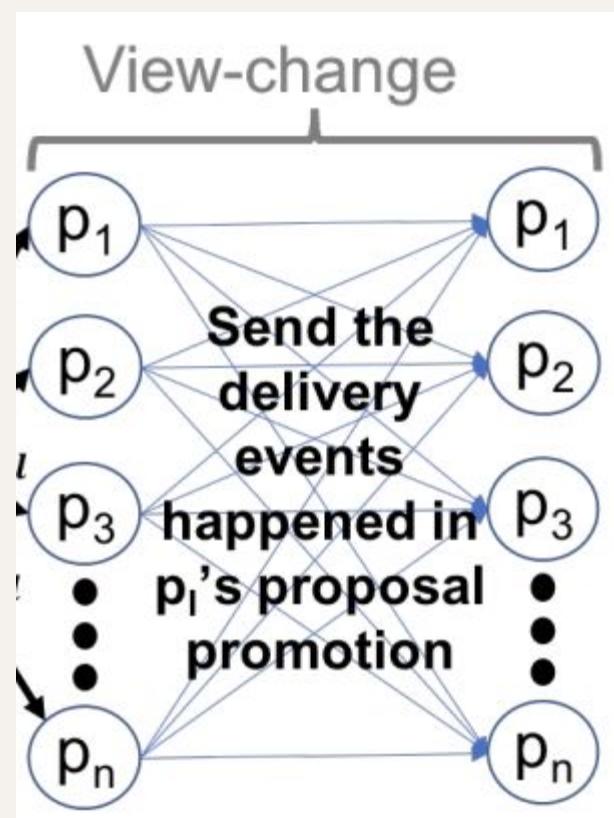
# Leader Election

- Collect  $f + 1$  valid coin shares
- Then Coin toss
  - Unique & pseudorandom value
  - Range 1 to n
- Move to View-Change Phase



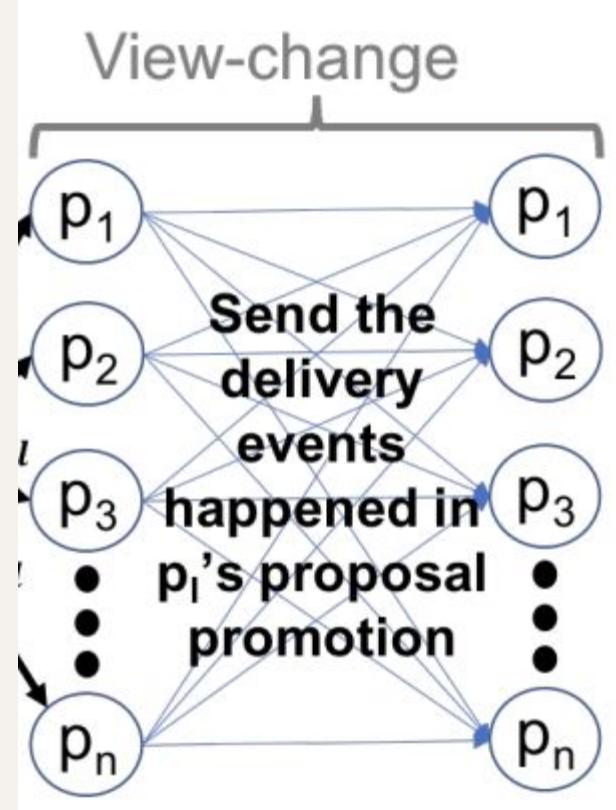
# Good View Change

- Broadcast View-change message
- Collect  $n - f$  view-change messages
- Process these messages
- If valid **COMMIT** proof for value  $v$  decide value  $v$



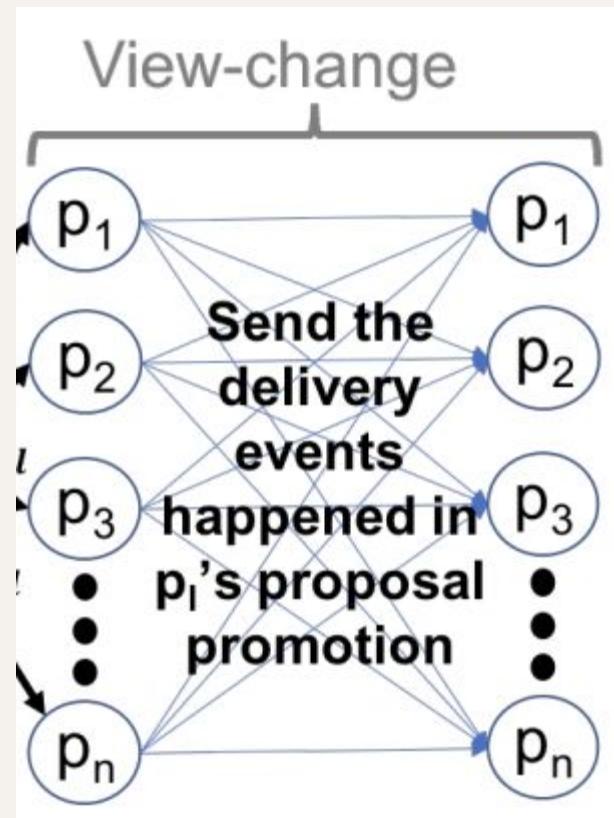
# Bad View Change

- Leader was slow, crashed, or malicious
- If Leader contains a LOCK, update local LOCK variable
- If Leader contains no LOCK but has a KEY, update local KEY variable
- If Leader is empty, keep previous state



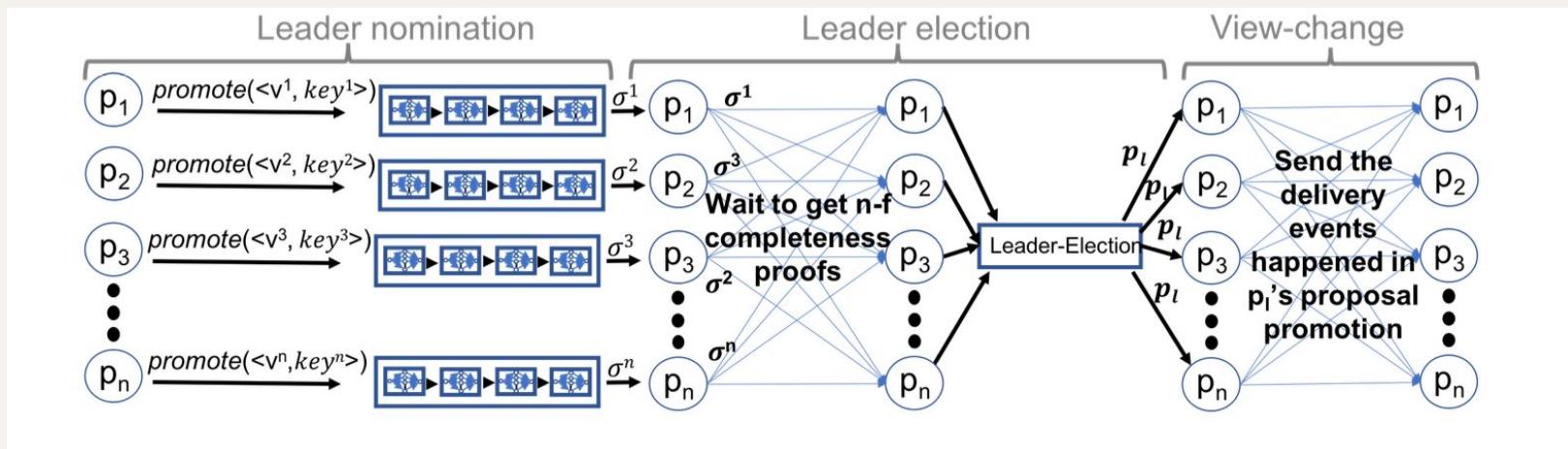
# Key Locking Mechanism

- Lock Safety: Prevents Overwriting Commitment
  - If value  $v$  is committed LOCK will be set to current view
- Key Safety: Prevents Conflicting Proposals
  - If value  $v$  is committed, no party can commit a different value in future views
- Key Progress: Guarantees Liveness:
  - Locked part will always have a valid KEY to promote in the next view



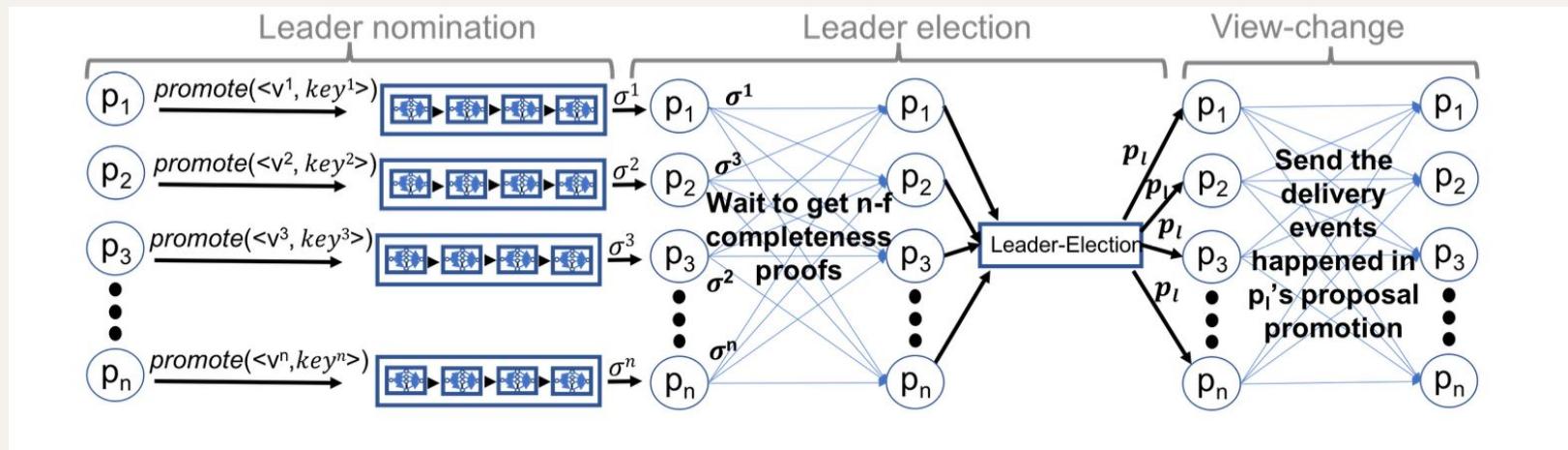
# Complexity Analysis

- Resilience:  $f < n/3$
- Time: Expected  $O(1)$
- Communication: Expected  $O(n^2)$



# Limitations

- Heavy Cryptography (The CPU Bottleneck)
- Probabilistic Latency dependent on a coin toss



# Conclusion

- First protocol to achieve Optimal Resilience, Optimal Time, AND Optimal Communication in the Asynchronous authenticated setting
- Replaced timeouts (PBFT) with knowledge of progress (Key/Lock/Commit)
- Replaced leader-generated proofs (PBFT) with replica-enforce history (Lock Safety)