

Program Representation for Control Flow

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Outline

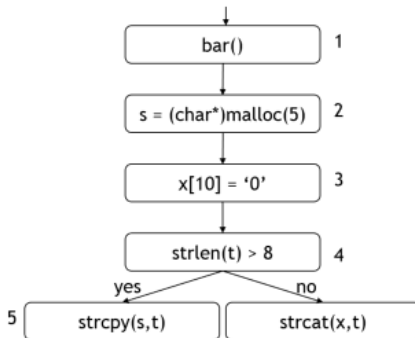
- ▶ Control flow graph (CFG)
- ▶ Call graph
- ▶ Inteprocedural control flow graph (ICFG)

What is program control flow?

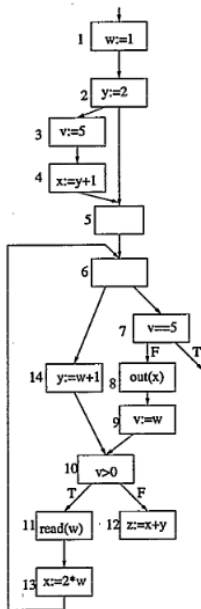
- ▶ *Control flow*: the execution order of statements of a program
- ▶ The problem of identifying control flow: identifying the execution order of statements from program source code (sometimes from binary code)
- ▶ There are three types of control flow: *sequential*, *branch* and *loop*
- ▶ *Control flow graph*: represent such order in a graph representation, the program paths will be available by traversing the graph

Control flow graph and path: sequential and branch

```
bar();  
s = (char*)malloc(5);  
x[10] = '\0';  
if(strlen(t)>8)  
    strcpy(s,t);  
else  
    strcat(x,t);
```



Control flow graph and path: loop



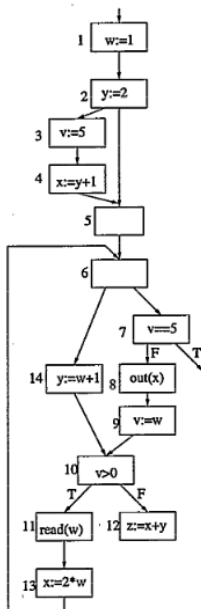
Control flow graph

- ▶ history: 1970, Frances Allen's papers: "Control Flow Analysis" and "A Basis for Program Optimization": using control flow graph to analyze programs for code optimizations
- ▶ it is a directed graph, we also call it CFG
- ▶ each function has a control flow graph
- ▶ has only one entry and one exit
- ▶ the node is a statement (source code) or an instruction (binary code); a node can also be a *basic block* (a sequence of statements/instructions that do not have branches),
- ▶ an edge indicates the order of the two statements/instructions/basic blocks

Other concepts related to program control flow

1. *Path*: a sequence of node on the CFG, including an entry node and an exit node
2. *Trace*: a sequence of instructions performed during execution
3. *Infeasible paths*: paths never can be executed
4. *Path segment*: a subsequence of nodes along the path

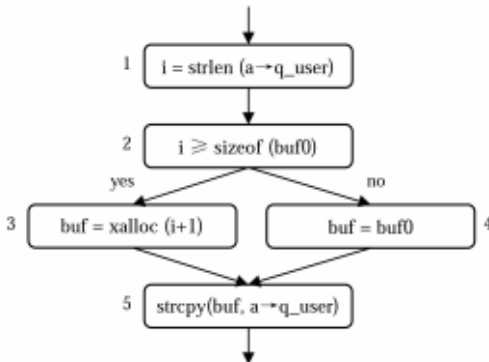
Infeasible path: an example



Control flow graphs and bug finding

Bug detection:

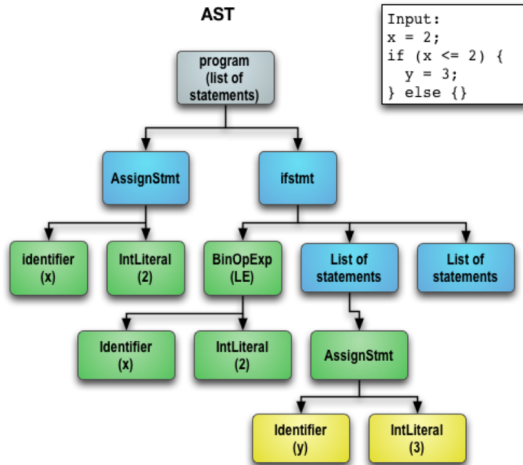
- ▶ using buggy code patterns (code smell) to scan new software: has a large number of false positives
- ▶ finding erroneous/undesired state on paths



Automatically constructing CFG

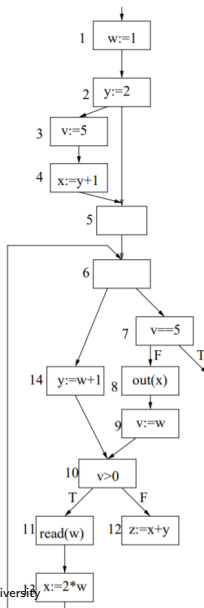
- ▶ Step 1: build *abstract syntax tree (AST)*: parse tree in an abstract form
- ▶ Step 2: convert AST to CFG
- ▶ There are many off-the-shelf tools: llvm for c/c++; soot for java

An Example: AST



Automatic infeasible paths detection [1997:Bodik]

Branch correlation



Reducible CFG and natural loops

Most of the execution time is spent in loops - the 90/10 law, which states that 90% of the time is spent in 10% of the code, and only 10% of the time in the remaining 90% of the code.

1. Loop terminologies: *single loop*, *nested loop*, *inner loop*, *outer loop*
2. CFG is *reducible* if every loop is a *natural loop*, intuitively
 - ▶ there is a single entry node (e)
 - ▶ no jumps into middle of loop (i.e., e dominates all nodes in loop)
 - ▶ requires a *back edge* into loop header ($n \rightarrow e$, $n \in L$)
 - ▶ *back edge* – head (ancestor) dominates its tail (decendent), any edge from tail to head is a back edge

Natural Loops

More formally, a set of nodes L in CFG is a *natural loop* if, L contains a node e , called *loop entry* or *head* [dragon book p.531]:

- ▶ e is not an entry of the entire flow graph
- ▶ e *dominates* all the nodes in the loop: every path from the entry node of the graph to n passes through e , noted as $e \text{ dom } n$
- ▶ no node in L besides e has a predecessor outside L
- ▶ every node in L has a nonempty path, completely within L , to e (back edge)

Reducibility in practice

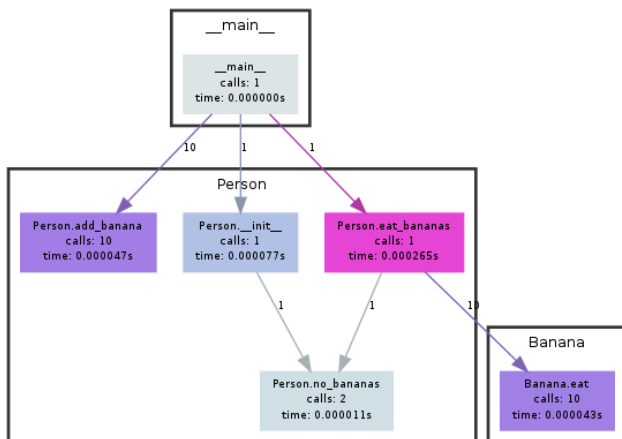
- ▶ If you use only while-loops, for-loops, repeat-loops, if-then(-else), break, and continue, then your control flow graph is reducible.
- ▶ Some languages only permit procedures with reducible control flow graphs (e.g., Java)
- ▶ “GOTO Considered Harmful”: can introduce irreducibility
 - ▶ FORTRAN
 - ▶ C
 - ▶ C++

Interprocedural control flow graph (ICFG)

- ▶ ICFG: representing control flow for the entire program
- ▶ what is a valid interprocedural path and how to represent it in ICFG?
- ▶ Combining: CFG and *call graph*: calling relationships of functions

Call graph

- *Call graph*: representing calling relations between functions, there is an edge from caller to callee See example from wiki ¹



Generated by Python Call Graph v1.0.0
<http://pycallgraph.slowchop.com>

¹https://en.wikipedia.org/wiki/Call_graph

Constructing call graphs

There are off-the-shelf tools: llvm for c/c++; soot for java, except that the following challenges are still under active research:

- ▶ function pointers
- ▶ virtual functions
- ▶ event-driven and framework based architecture like Android:
callbacks (the library code calls user's functions)

Function pointers [2004:atkinson]

Resolving function pointers based on the types in function signatures

```
int (*q) ()
int main() { ...
    char *x = "a";
    int *y = 1;
    (*q) (2, x); ...
    (*q) (3, y);
}
char q1(int x, int *p) { ... }
int q2(int x, int *p) { ... }
int q3(int x, char *p) { ... }
```

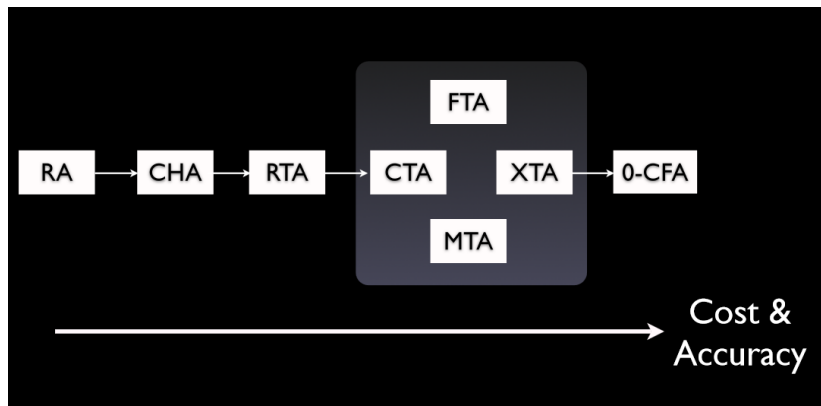
Virtual functions

```
class A {  
public:  
    virtual void f();  
    ...  
};
```

```
int main()  
{  
    A *pa = new B();  
  
    pa->f();  
    ...  
}
```

```
class B: public A {  
public:  
    virtual void f();  
    ...  
};
```

Algorithms for handling virtual functions

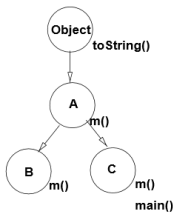


Details see paper: Scalable Propagation-Based Call Graph Construction Algorithms by Frank Tip and Jens Palsberg

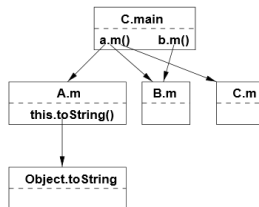
CHA: class hierarchy analysis

```
class A extends Object {  
    String m() {  
        return(this.toString());  
    }  
}  
  
class B extends A {  
    String m() { ... }  
}  
  
class C extends A {  
    String m() { ... }  
    public static void main(...) {  
        A a = new A();  
        B b = new B();  
        String s;  
  
        ...  
        s = a.m();  
        s = b.m();  
    }  
}
```

(a) Example Program



Class Hierarchy



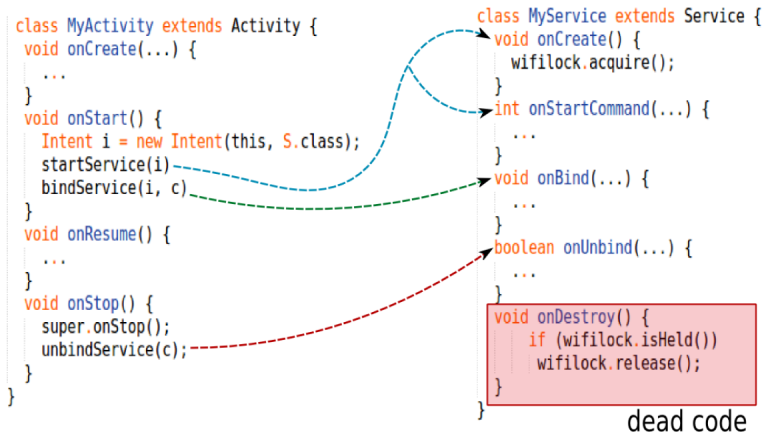
Call Graph

(b) Class Hierarchy and Call Graph

Relations of type Inference, alias analysis, call graph construction in Java

- ▶ Call graph construction needs to know the type of the object receivers for the virtual functions
- ▶ Determine types of the set of relevant variables: type inferences – infer types of program variables
- ▶ Object receivers may alias to a set of reference variables so we need to perform *alias analysis*
- ▶ Alias analysis determines whether two pointers a and b point to the same memory location, e.g., statement `int* b = a` indicates that pointers b and a get the same value (address)

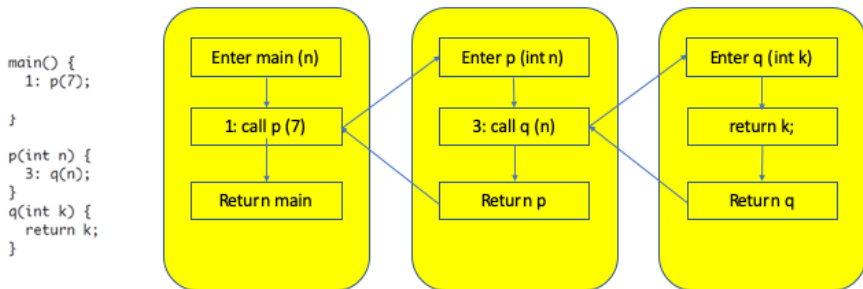
Callbacks



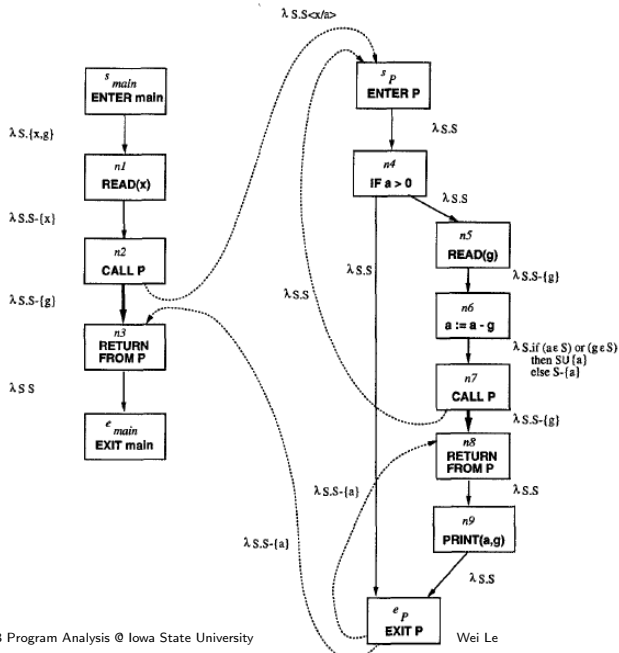
Interprocedural control flow graph (ICFG)

After ICFG and callgraph, let's revisit the concept of ICFG:

- ▶ ICFG: representing control flow for the entire program
- ▶ Finding the potentially valid execution paths for the entire program



ICFG with recursive calls



Getting paths from ICFG

Context-sensitive and realizable paths:

- ▶ *Context-sensitive*: when a call is invoked twice, do we distinguish at which callsite the callee should return (when traversing ICFG for paths)?
- ▶ *Realizable paths*: ICFG contains more paths than valid execution paths. Realizable paths are the paths on ICFG that represent potentially valid executions.

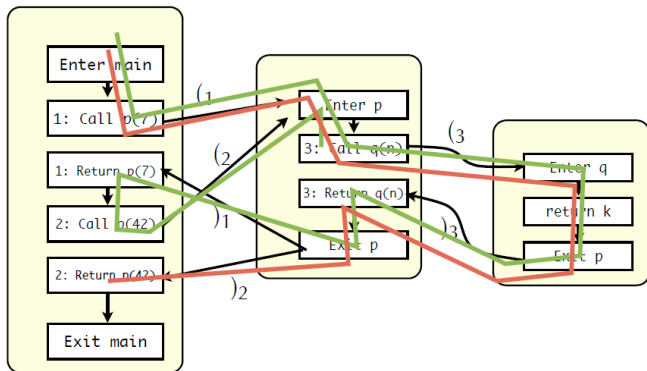
source: Precise Interprocedural Dataflow Analysis via Graph Reachability

ICFG and realizable paths

```
main() {  
  1: p(7);  
  2: x:=p(42);  
}
```

```
p(int n) {  
  3: q(n);  
}
```

```
q(int k) {  
  return k;  
}
```



Representing realizable paths in grammar

Idea: restrict attention to **realizable paths**: paths that have proper nesting of procedure calls and exits

For each call site i , let's label the call edge " $(i$ " and the return edge " $)_i$ "

Define a grammar that represents balanced paren strings

```
matched ::=  $\epsilon$                                 empty string
          |  $e$                                     anything not containing parens
          | matched matched
          |  $(_i$  matched  $)_i$ 
```

- Corresponds to matching procedure returns with procedure calls

Define grammar of partially balanced parens (calls that have not yet returned)

```
realizable ::=  $\epsilon$ 
             |  $(_i$  realizable
             | matched realizable
```

From grammar to language: CFL (context-free language) reachability

Reducing to the CFL reachability problem: Let L be a context-free language over alphabet Σ

- ▶ Let G be graph with edges labeled from Σ
- ▶ Each path in G defines word over Σ
- ▶ A path in G is an L -path if its word is in L

CFL reachability problems

Computing *realizable paths*: $O(n^3)$

- ▶ All-pairs L-path problem: for all pairs of nodes n_1 and n_2 , finding an L-path from n_1 to n_2
- ▶ Single-source L-path problem: for all nodes n_2 , finding an L-path from given node n_1 to n_2
- ▶ Single-target L-path problem: for all nodes n_1 , finding an L-path from n_1 to given node n_2
- ▶ Single-source single-target L-path problem: finding an L-path from given node n_1 to given node n_2

Bug detection on ICFG

- ▶ Enumerate all the paths to check if they are buggy: too many paths
- ▶ *Deman-driven* algorithms: new after 2000
- ▶ Summary based algorithms: summarize the effect of a callee and then use the summary for bug detection

Demand-driven algorithm

See slides

Computing procedural summaries on ICFG

When call p is encountered in context C , with input D , check if procedure summary for p in context C exists.

- ▶ If not, process p in context C with input D
- ▶ If yes, with input D' and output E'
- ▶ If $D' \sqsubseteq D$, then use E'
- ▶ if $D' \not\sqsubseteq D$, then process p in context C with input $D' \sqcap D$ (merge the dataflow)
- ▶ If output of p in context C changes then may need to reprocess anything that called it