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# DISCRETE MATHEMATICS

## MATH 381

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BASIC CONCEPTS AND EXAMPLES EXPLAINING THE FUNDAMENTALS OF  
DISCRETE MATHEMATICS.

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Recall:

- Functions  $f: A \rightarrow B$
- Image  $Im(f) = \{f(a) \mid a \in A\}$

If  $f(a) = b$ , say "a is a preimage of b"

- $Gr(f) = \{(a, b) \mid f(a) = b\} \subseteq A \times B$
- $Gr(f) = \{(a, f(a)) \mid a \in A\}$

Graph  $Gr(f)$  is a relation between A and B

Which binary relations (subsets of  $A \times B$ ) are graphs of functions?

- A subset  $s \subseteq A \times B$  is the graph of a function if for every element  $a \in A$ , there is a unique element  $b \in B$  such that  $(a, b) \in S$ .
- key Can't have  $(a, b_1)$  and  $(a, b_2) \in S$  where  $b_1 \neq b_2$  and expect S to be a graph
- (abstraction of "straight line test" about graphs  $f: \mathbb{R} \rightarrow \mathbb{R}$ )

Restriction of Domain

suppose  $f: A \rightarrow B$

Consider  $A' \subseteq A$

DEFINITION the restriction of f to A' is  $f|_{A'}: A' \rightarrow B$  defined by  $(f|_{A'})(a) = f(a), a \in A'$