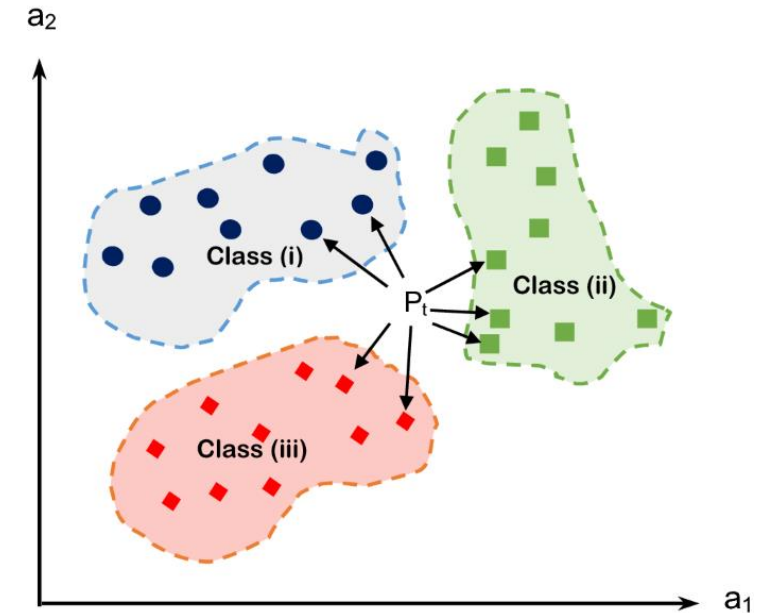


Siddhardhan

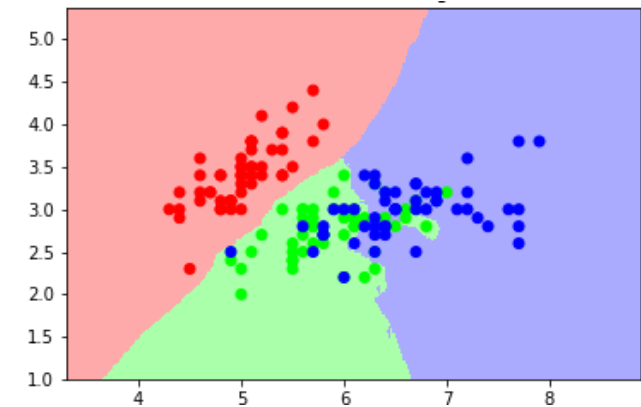
Math behind K-Nearest Neighbors (KNN) Classifier



K-Nearest Neighbors

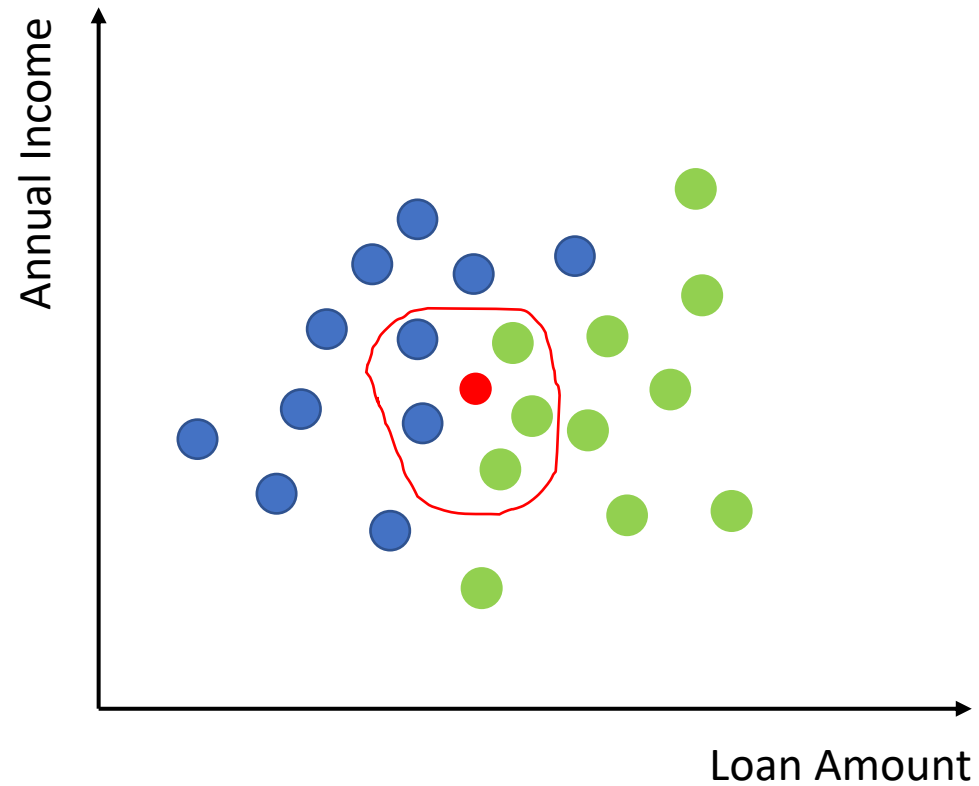
About K-Nearest Neighbors:

1. Supervised Learning Model
2. Used for both Classification & Regression
3. Can be used for non-linear data
4. K - Neighbors



K-Nearest Neighbors

Classification Problem:



K = 5

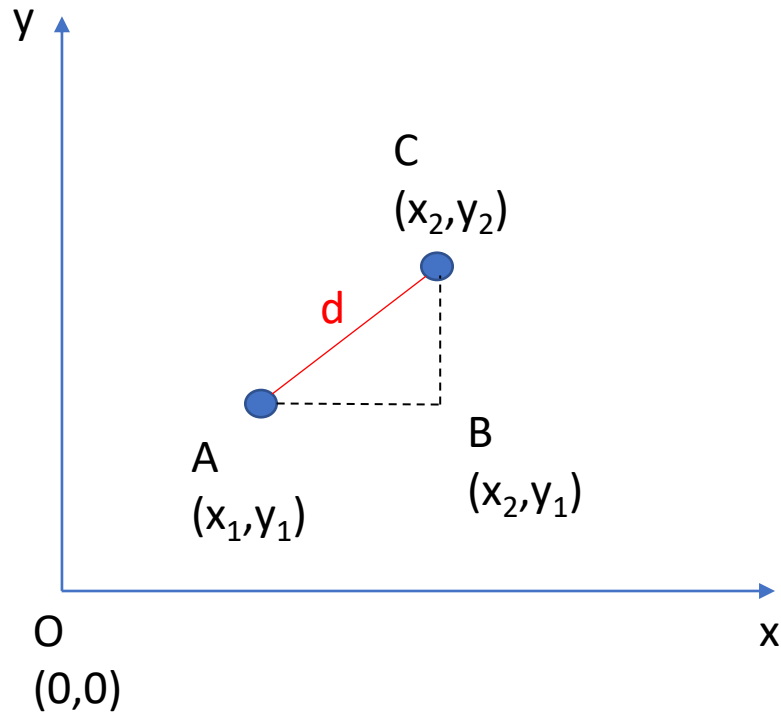
- Didn't repay on time
- Repaid on time

● May not repay the loan on time

To Measure the distance between the data points:

- ❖ Euclidean Distance
- ❖ Manhattan Distance

Euclidean Distance



Pythagoras Theorem:

$$AC^2 = AB^2 + BC^2$$

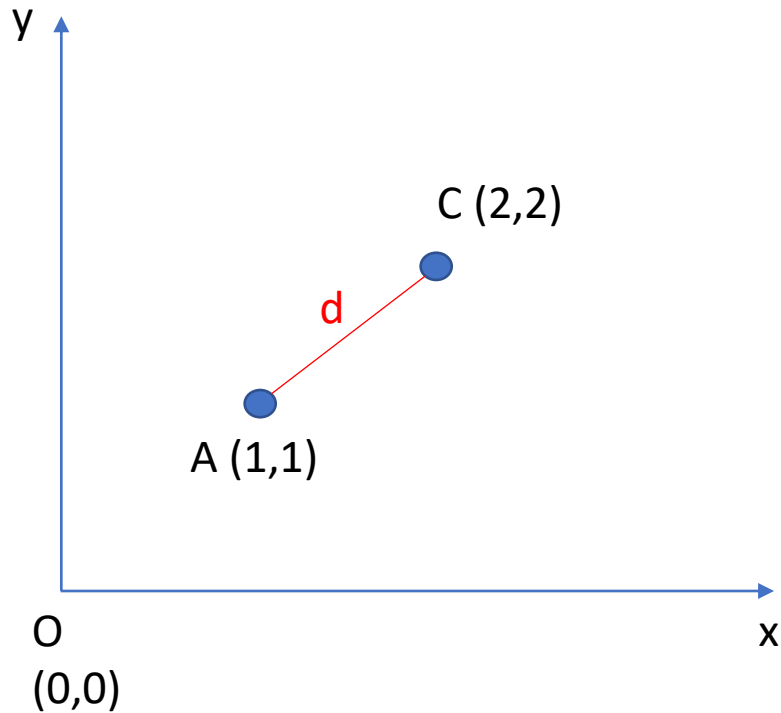
$$AC = \sqrt{AB^2 + BC^2}$$

$$AC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

This distance “d” is called the Euclidean Distance.

Euclidean Distance



Euclidean Distance formula:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$(x_1, y_1) = A (1,1)$$

$$(x_2, y_2) = B (2,2)$$

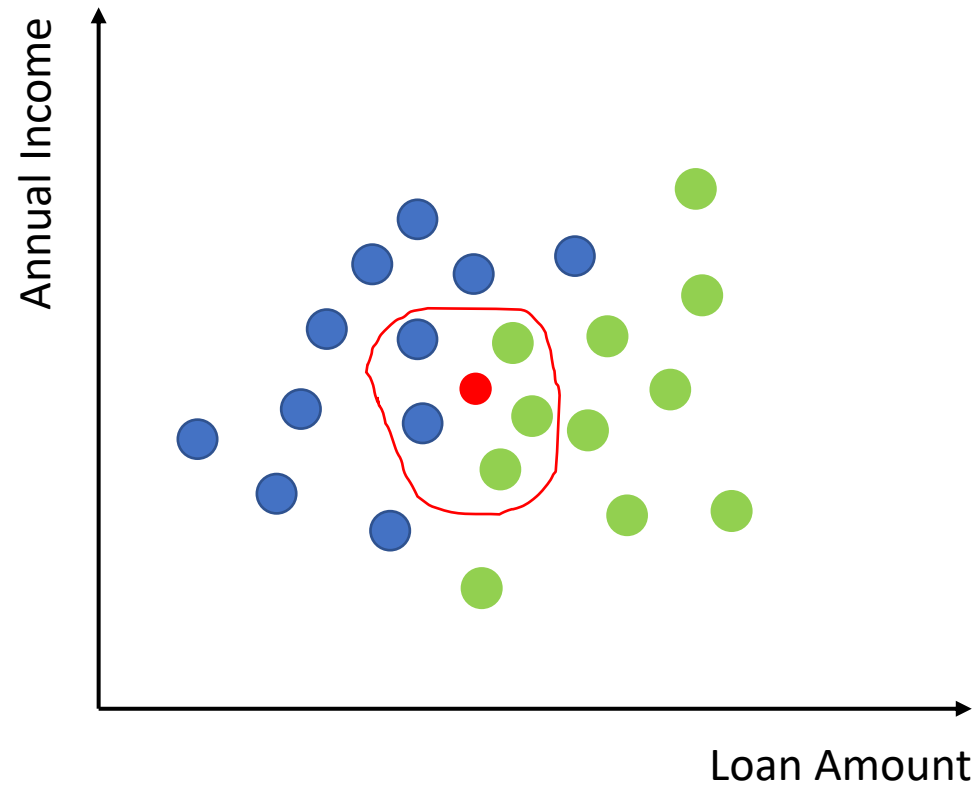
$$d = \sqrt{(2 - 1)^2 + (2 - 1)^2}$$

$$d = \sqrt{1 + 1}$$

$$d = \sqrt{2}$$

K-Nearest Neighbors

Classification Problem:



$K = 5$

● Didn't repay on time

● Repaid on time

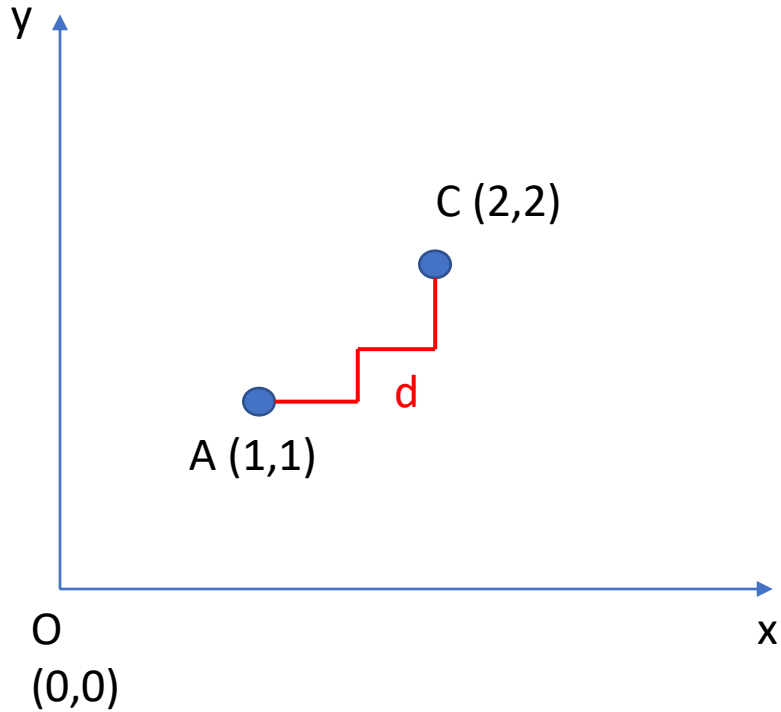
● May not repay the loan on time

To Measure the distance between the data points:

❖ Euclidean Distance

❖ Manhattan Distance

Manhattan Distance



Manhattan Distance formula:

$$d = |x_1 - x_2| + |y_1 - y_2|$$

$$(x_1, y_1) = A (1,1)$$

$$(x_2, y_2) = B (2,2)$$

$$d = |1 - 2| + |1 - 2|$$

$$d = 1 + 1$$

$$d = 2$$

Manhattan distance is preferred over Euclidean distance when there is **high dimensionality** in the data.