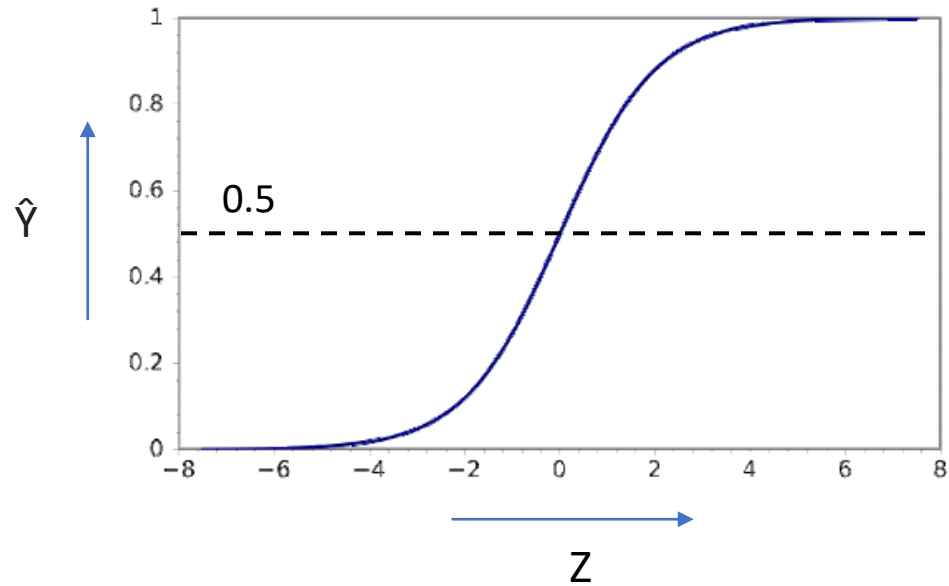


Siddhardhan

# Math behind Logistic Regression



# Logistic Regression



$$\hat{Y} = \frac{1}{1 + e^{-Z}}$$

$$Z = w \cdot X + b$$

*Sigmoid Function*

$\hat{Y}$  - Probability that ( $y = 1$ )

$$\hat{Y} = P(Y=1 \mid X)$$

$X$  - input features

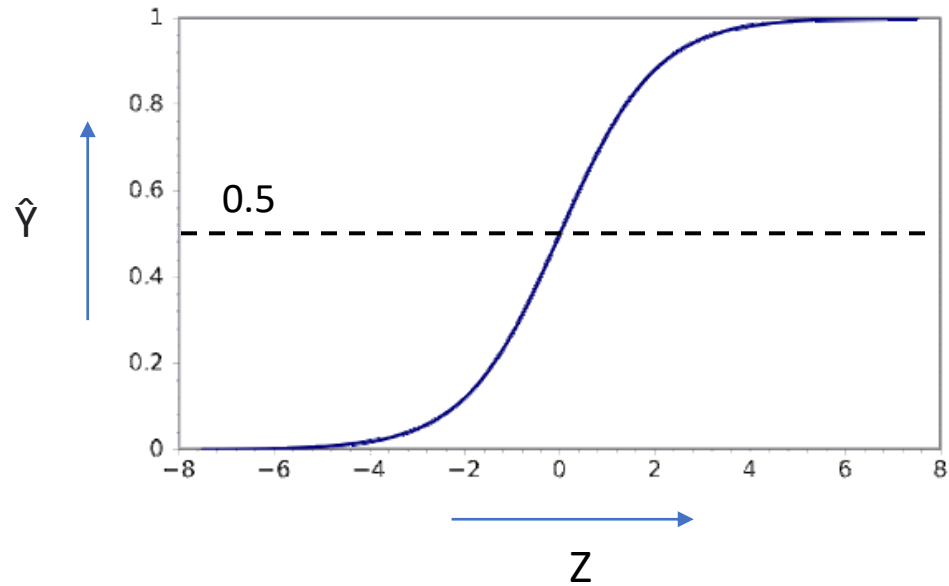
$w$  - weights

( number of weights is equal to the number of input features in a dataset)

$b$  - bias

$$\hat{Y} = \sigma(Z)$$

# Logistic Regression



$$\hat{Y} = \frac{1}{1 + e^{-Z}}$$

*Sigmoid Function*

$$Z = 5X + 10$$

$\hat{Y}$  - Probability that ( $y = 1$ )

$$\hat{Y} = P(Y=1 \mid X)$$

$X$  - input features

$w$  - weights

( number of weights is equal to the number of input features in a dataset)

$b$  - bias

$$\hat{Y} = \sigma(Z)$$

## Logistic Regression

X	-9	-8	0	8	9
$\hat{Y}$					

$$Z = 5X + 10$$

$$\hat{Y} = \frac{1}{1+e^{-Z}}$$

$$X = -9$$

$$Z = 5(-9) + 10$$

$$Z = -35$$

$$\hat{Y} = \frac{1}{1+e^{35}}$$

$$\hat{Y} = 0$$

$$X = -8$$

$$Z = 5(-8) + 10$$

$$Z = -30$$

$$\hat{Y} = \frac{1}{1+e^{30}}$$

$$\hat{Y} = 0$$

$$X = 0$$

$$Z = 5(0) + 10$$

$$Z = 10$$

$$\hat{Y} = \frac{1}{1+e^{-10}}$$

$$\hat{Y} = 1$$

$$X = 8$$

$$Z = 5(8) + 10$$

$$Z = 50$$

$$\hat{Y} = \frac{1}{1+e^{-50}}$$

$$\hat{Y} = 1$$

$$X = 9$$

$$Z = 5(9) + 10$$

$$Z = 55$$

$$\hat{Y} = \frac{1}{1+e^{-55}}$$

$$\hat{Y} = 1$$

## Logistic Regression

X	-9	-8	0	8	9
$\hat{Y}$	0	0	1	1	1

$$Z = 5X + 10 \qquad \hat{Y} = \frac{1}{1+e^{-Z}}$$

$$X = -9$$

$$Z = 5(-9) + 10$$

$$Z = -35$$

$$\hat{Y} = \frac{1}{1+e^{35}}$$

$$\hat{Y} = 0$$

$$X = -8$$

$$Z = 5(-8) + 10$$

$$Z = -30$$

$$\hat{Y} = \frac{1}{1+e^{30}}$$

$$\hat{Y} = 0$$

$$X = 0$$

$$Z = 5(0) + 10$$

$$Z = 10$$

$$\hat{Y} = \frac{1}{1+e^{-10}}$$

$$\hat{Y} = 1$$

$$X = 8$$

$$Z = 5(8) + 10$$

$$Z = 50$$

$$\hat{Y} = \frac{1}{1+e^{-50}}$$

$$\hat{Y} = 1$$

$$X = 9$$

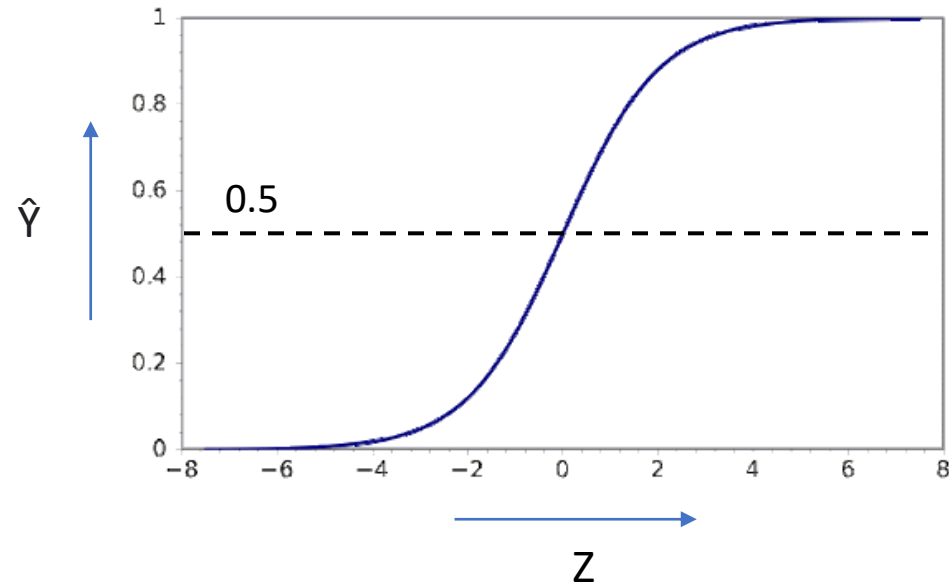
$$Z = 5(9) + 10$$

$$Z = 55$$

$$\hat{Y} = \frac{1}{1+e^{-55}}$$

$$\hat{Y} = 1$$

# Logistic Regression



$$\hat{Y} = \frac{1}{1 + e^{-Z}}$$

$$Z = w.X + b$$

*Sigmoid Function*

**Inference:**

If Z value is a large positive number,

$$\hat{Y} = \frac{1}{1 + 0}$$

$$\hat{Y} = 1$$

If Z value is a large negative number,

$$\hat{Y} = \frac{1}{1 + (\text{large positive number})}$$

$$\hat{Y} = 0$$