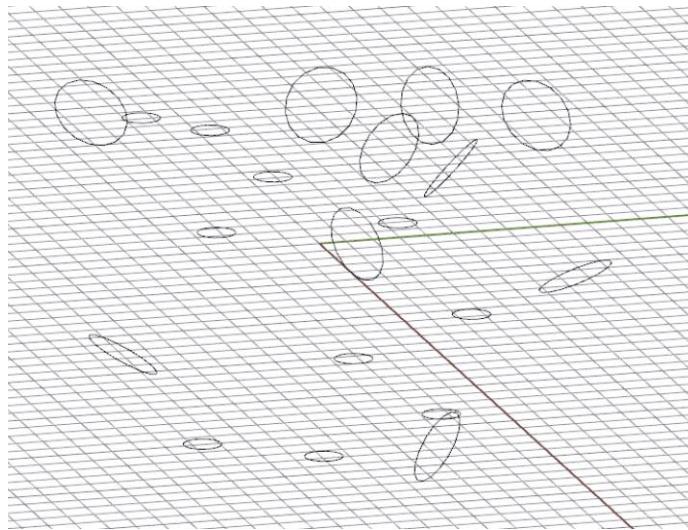


# Next Generation Geomechanics Simulation



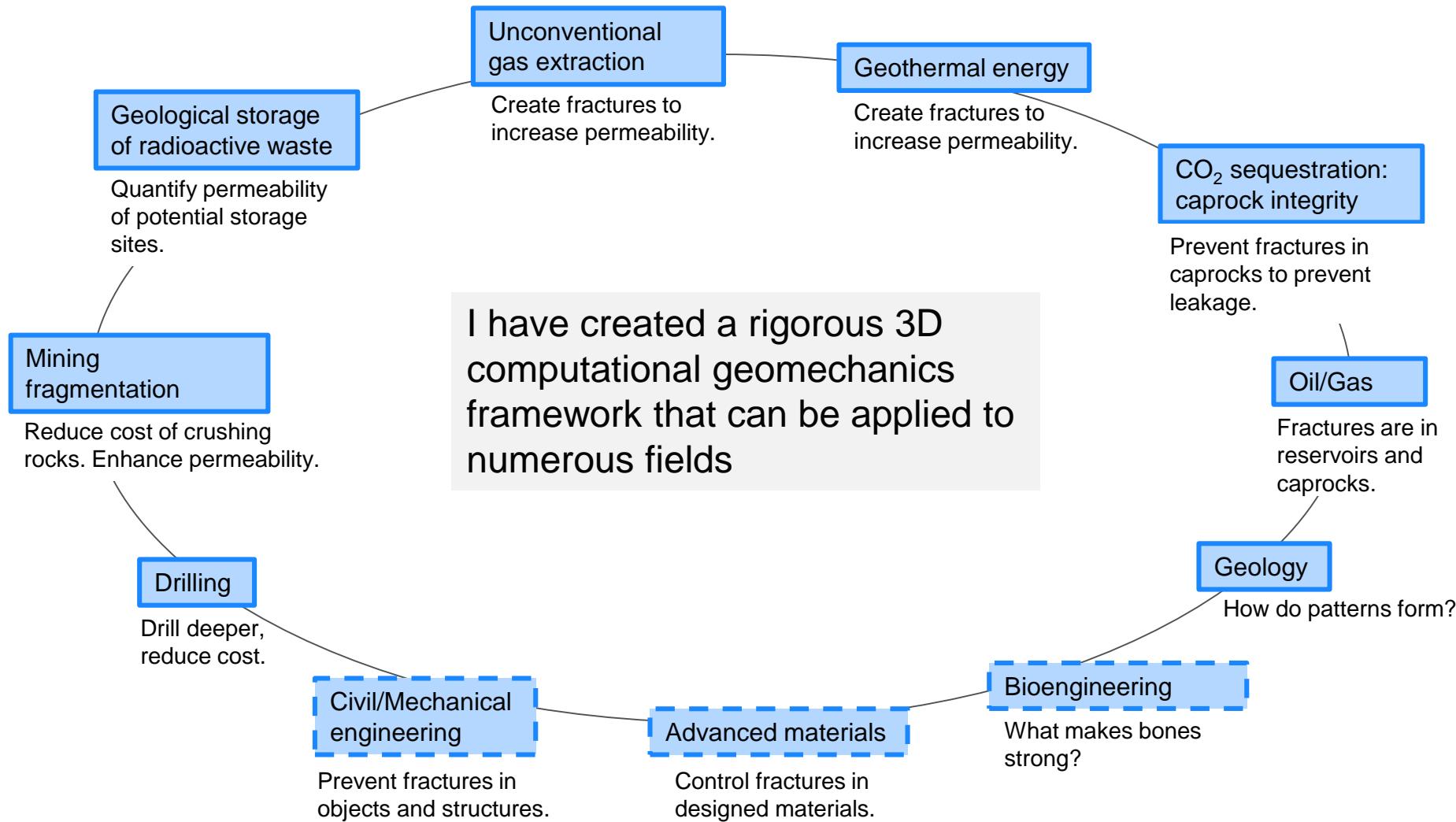
**Dr. Adriana Paluszny**

Dept. of Earth Science and Engineering

Imperial College London

May 23<sup>rd</sup>, 2019

# Fractures underpin a range of Technologies and Fields



# How can we study fractures?

Why develop a computational model?

- Subsurface geomechanical systems are difficult to observe
- High pressure and high temperature *in situ* conditions
- Variety of length and time scales
- Effects of multiple natural or engineered events

Is there a computational method available?

- Civil/Mechanical Engineering: most accurate but focused on the growth of single fractures, do not generally model the post-failure regime
- Reservoir Engineering: does not rigorously model growth
- Hydrogeology: coupled thermo-poro-mechanical tools consider fractures, but not fracture/fault growth, simplified apertures
- Mining: fragmentation modelled using mostly empirical models, not coupled with flow and temperature

There is no “off-the-shelf” solution

### Challenges:

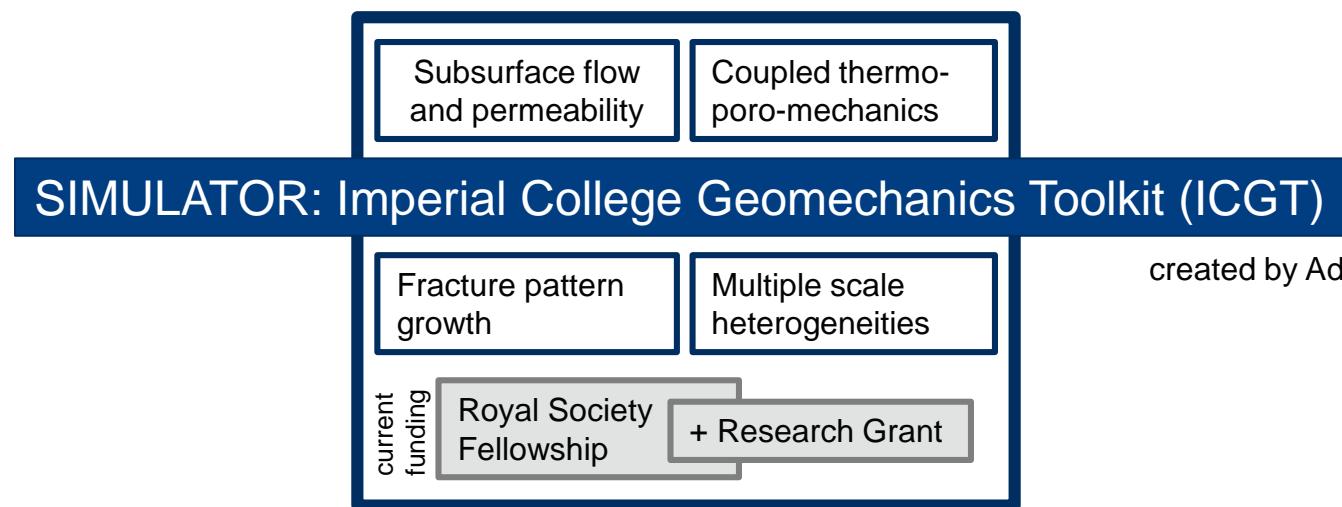
- The problem involves a lot of physics: mechanics, fluid flow, thermal effects
- Solving coupled equations of fluid flow and mechanics is computationally expensive
- It is difficult to resolve geometric changes during growth and resolve intersections
- Requires adjusting the discretisation of the model; this is expensive
- A true coupled simulation requires computing fracture apertures
- The 3D problem is considerably more challenging than in 2D

### My approach:

- ✓ treat each challenge using the most robust technique possible,
- ✓ model fractures in the greatest detail possible,
- ✓ and solve challenges one at a time.

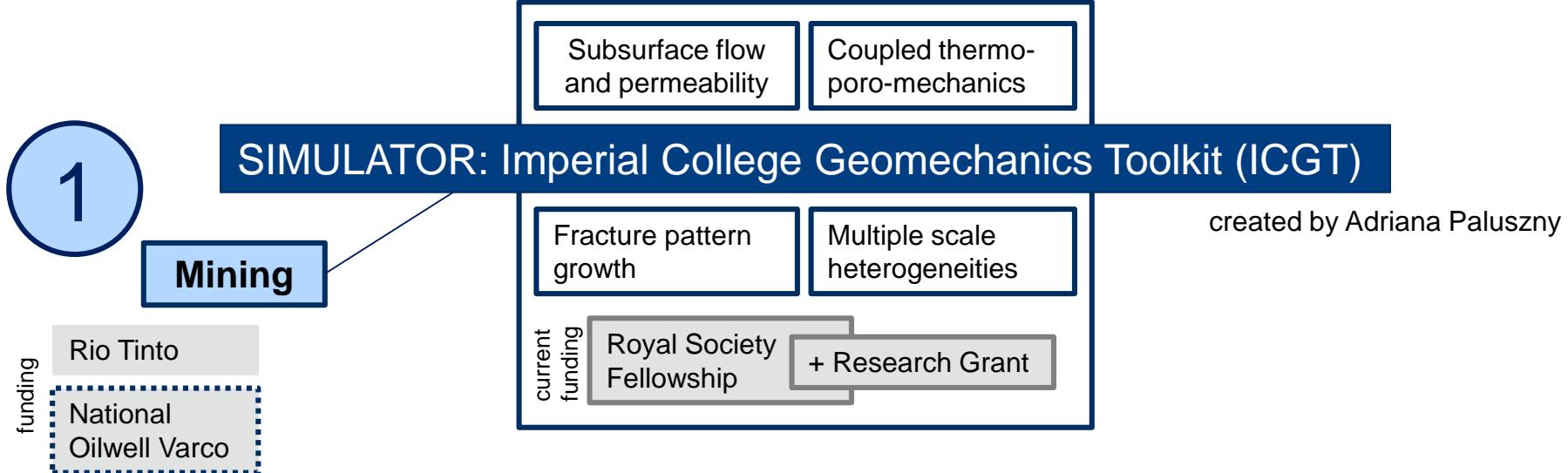
In 2010, I created a new simulator: the **Imperial College Geomechanics Toolkit**

# Overview of my core research

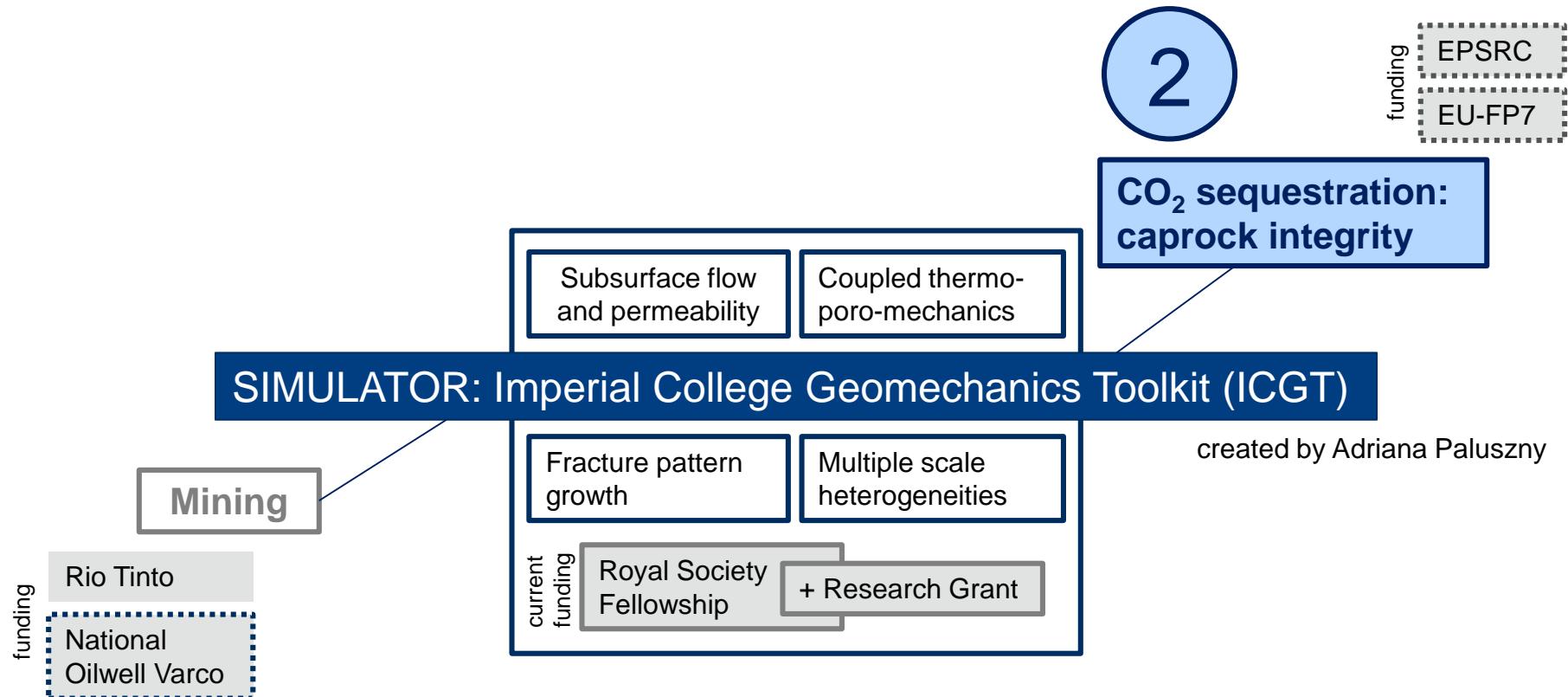


created by Adriana Paluszny

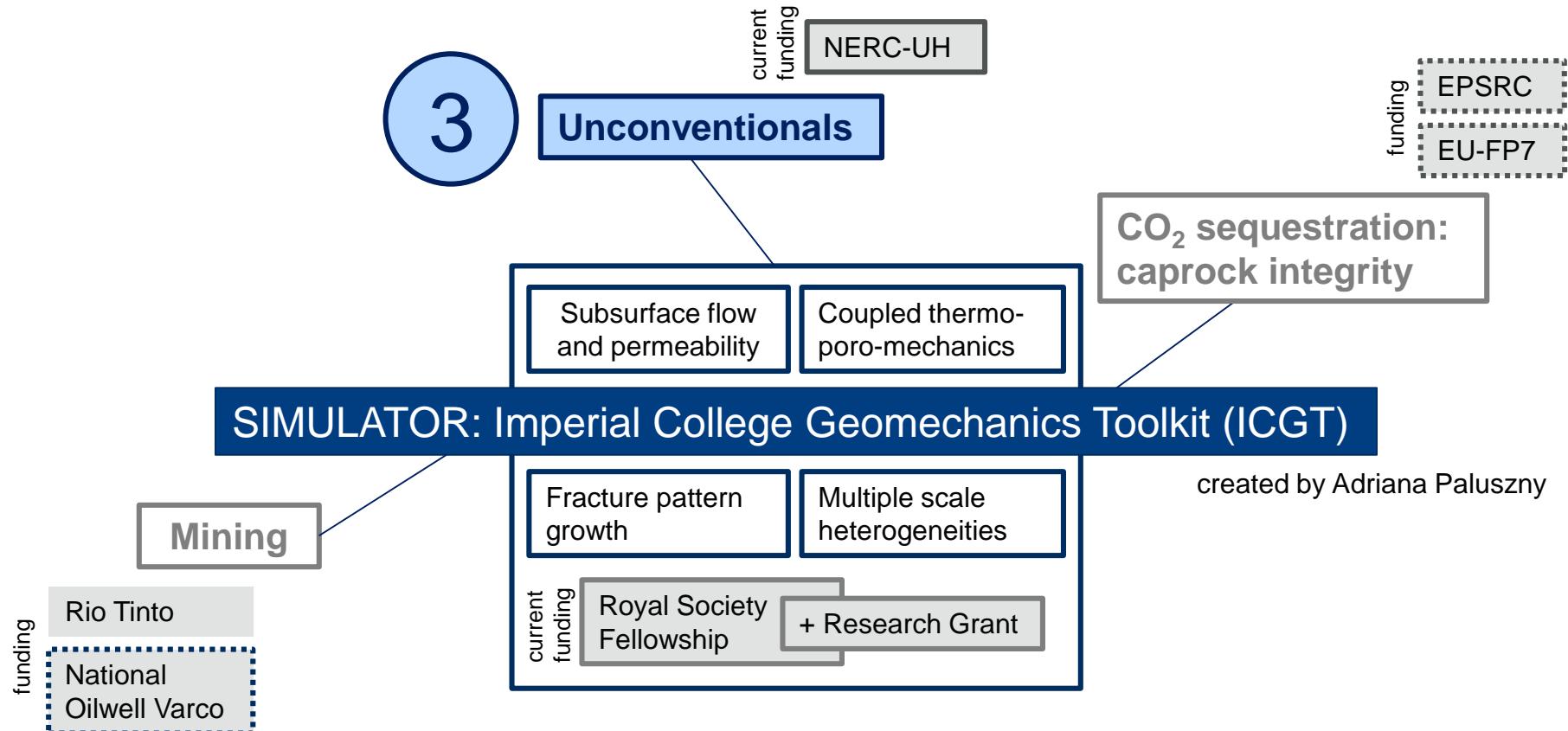
# Overview of my research



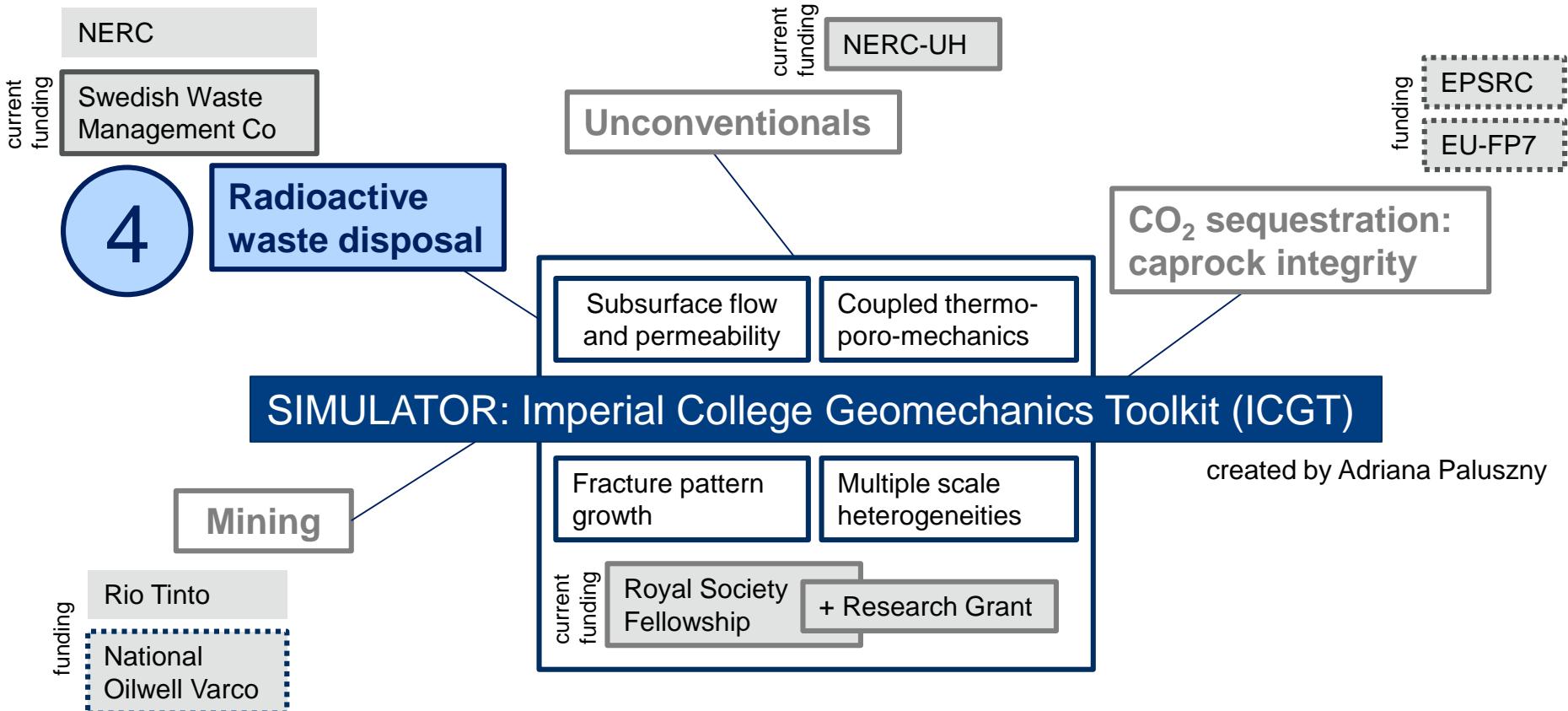
# Overview of my research



# Overview of my research

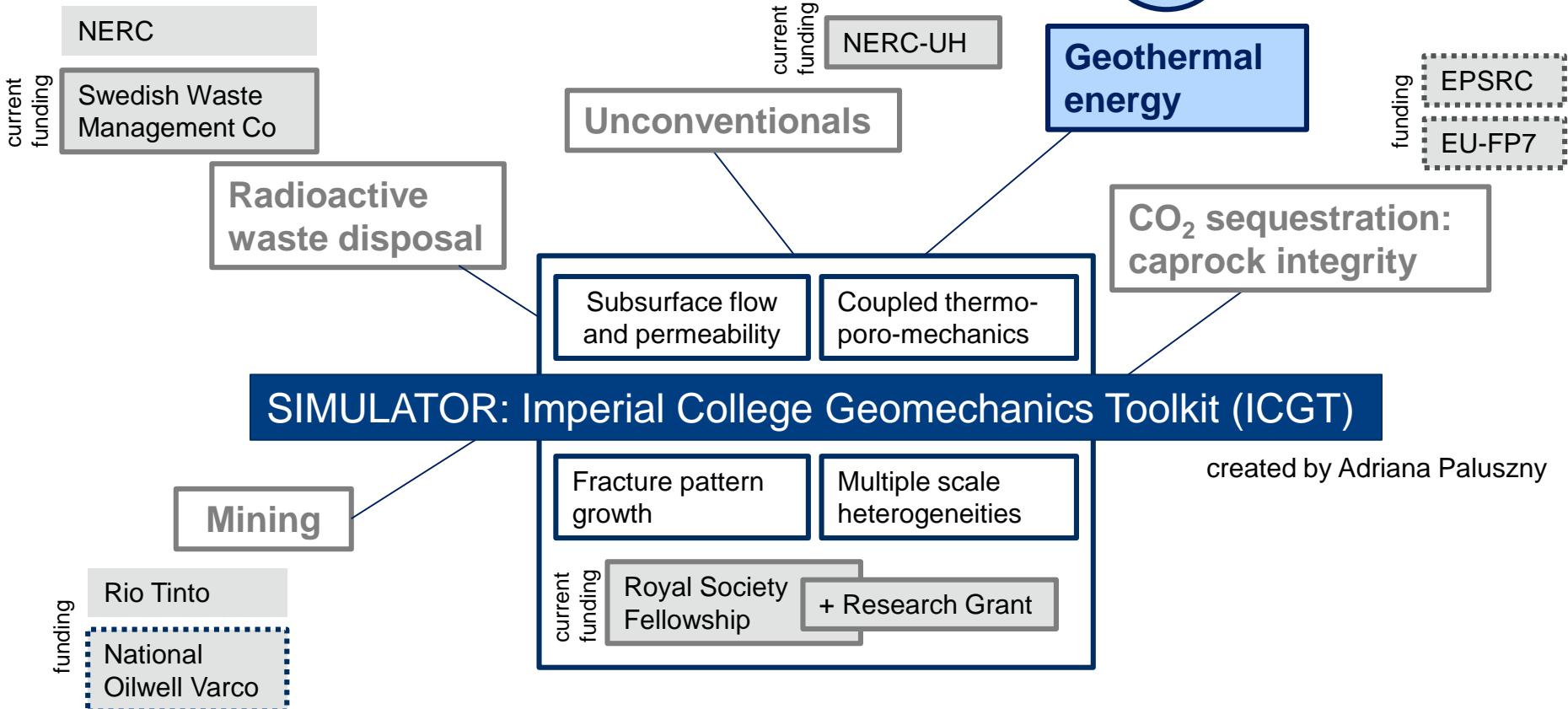


# Overview of my research

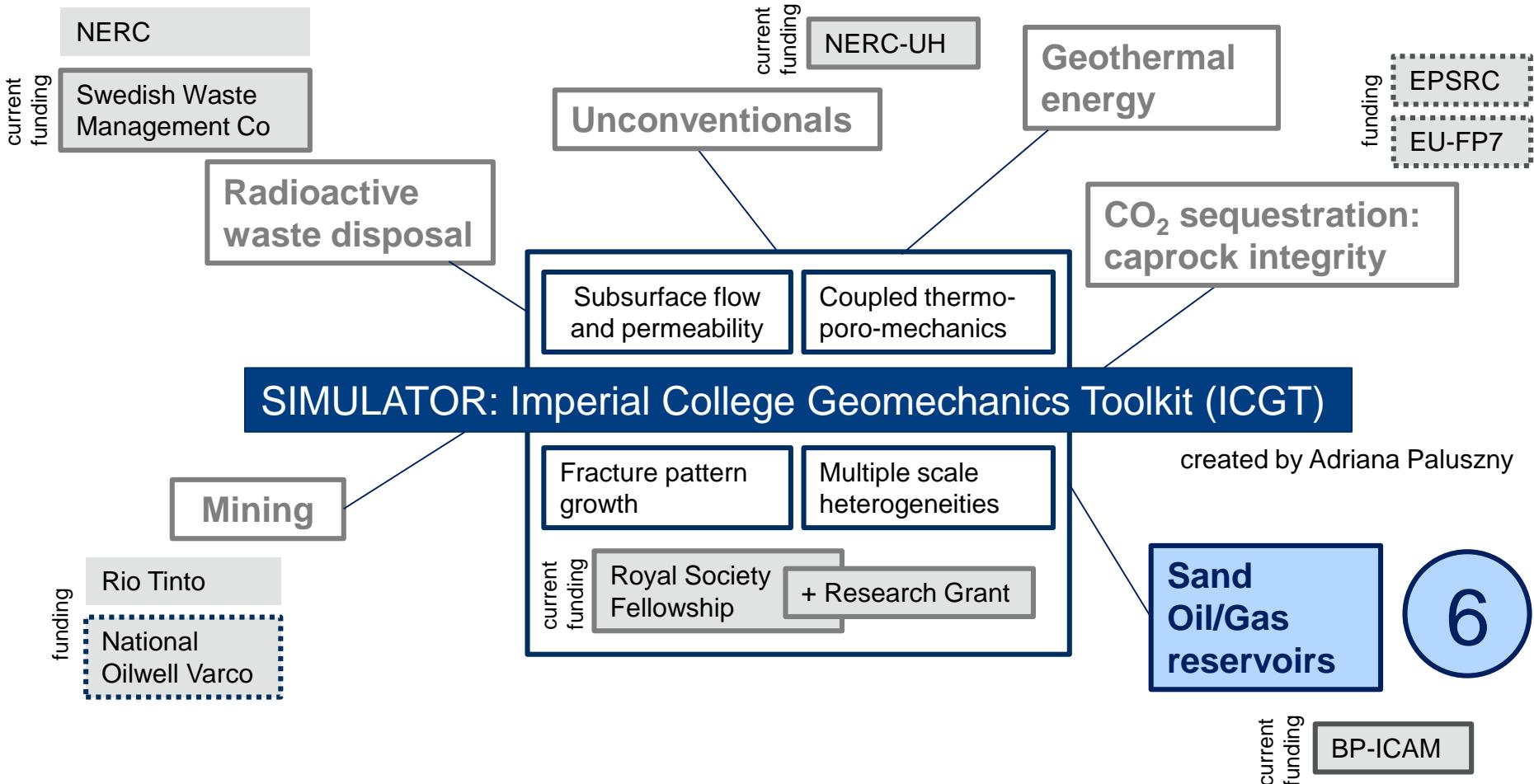


# Overview of my research

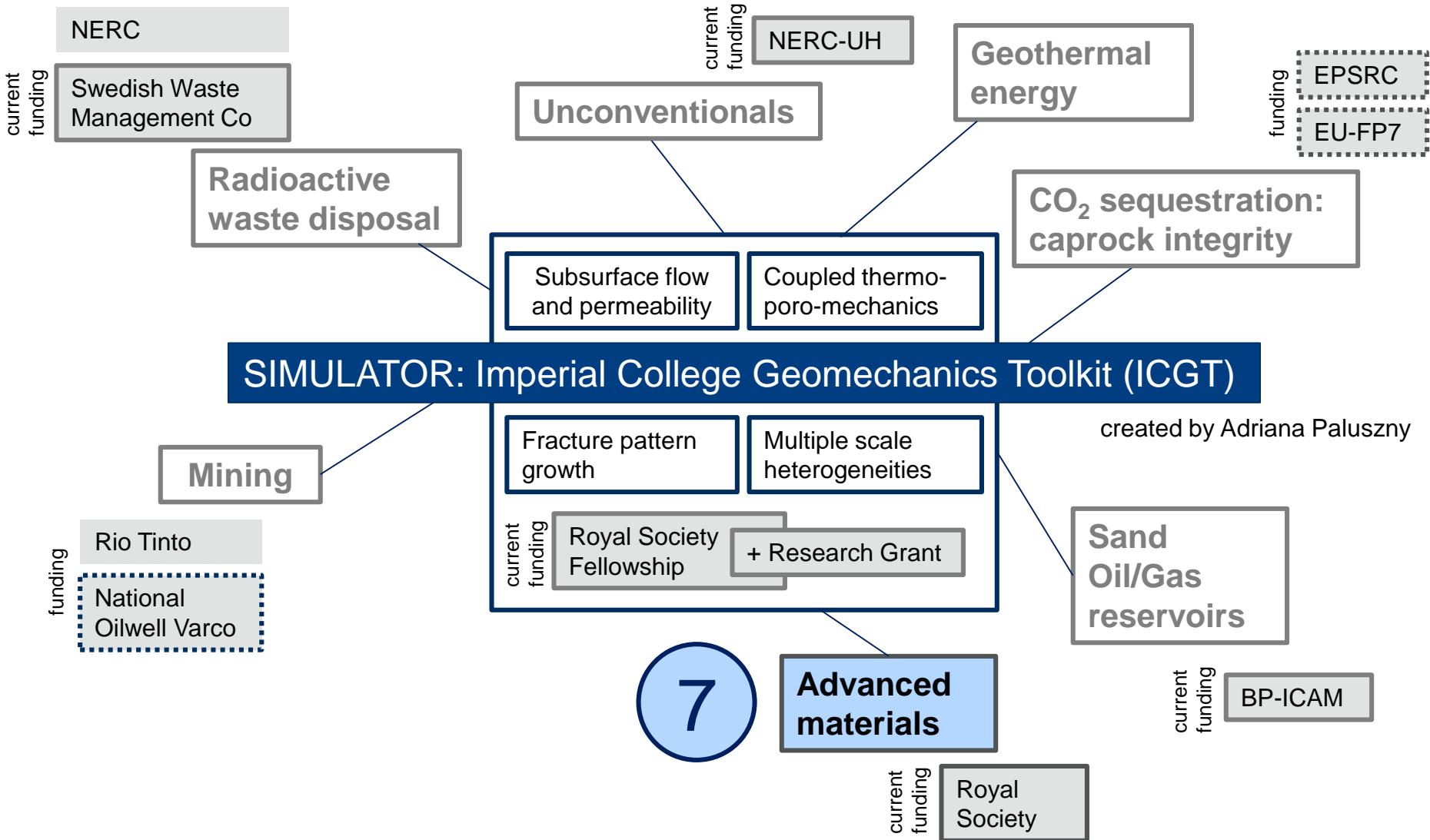
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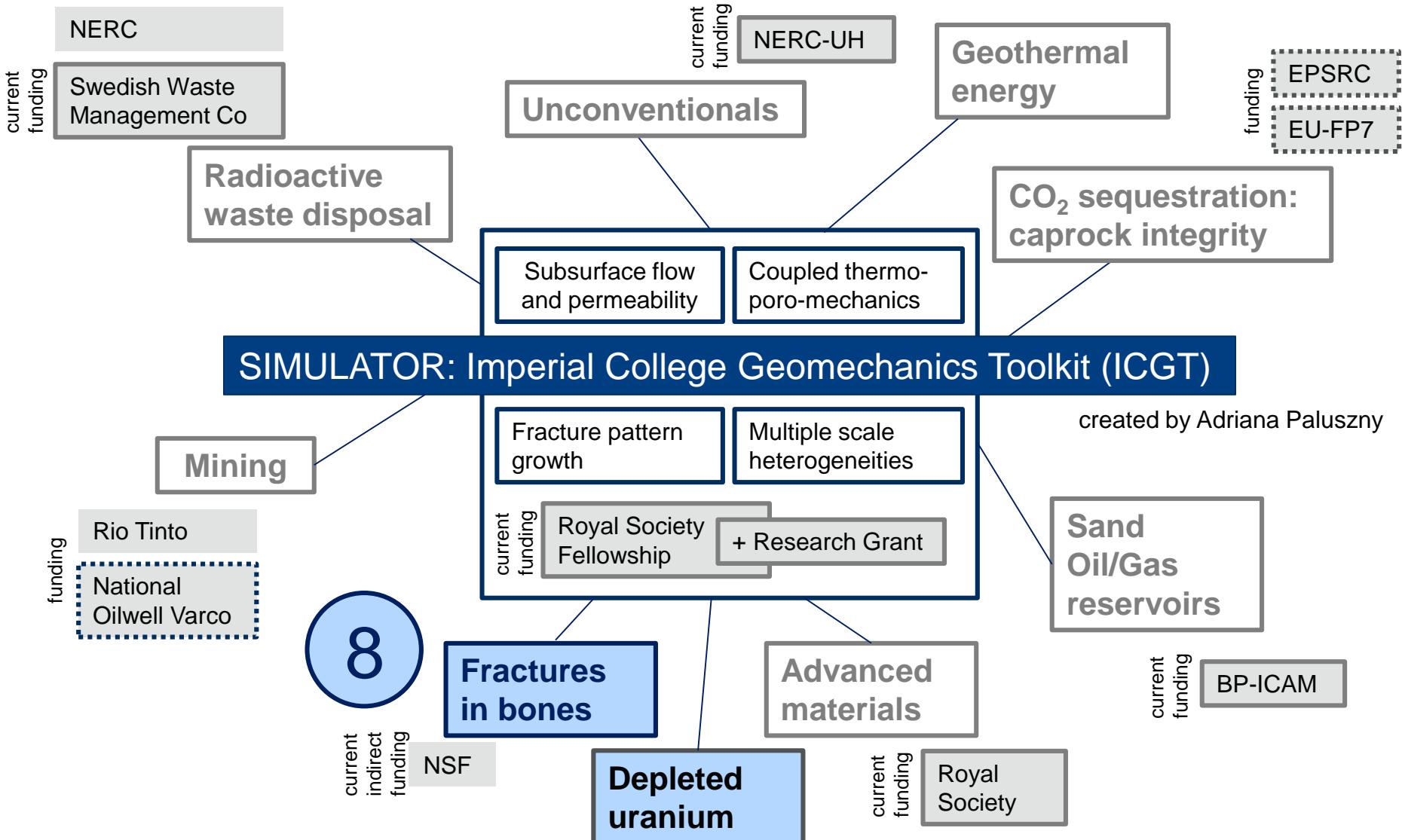
# Overview of my research



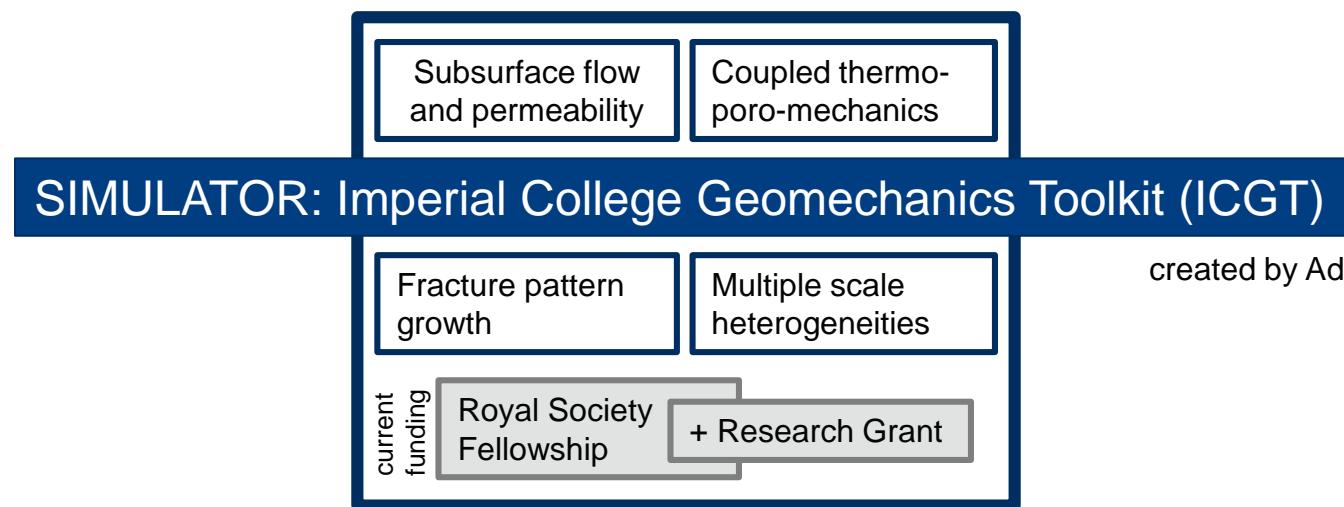
# Overview of my research



# Overview of my research



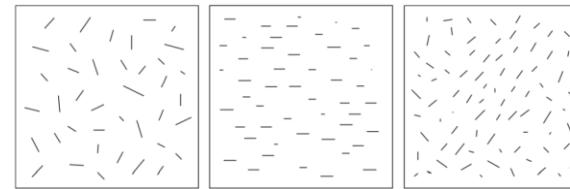
# Overview of my core research



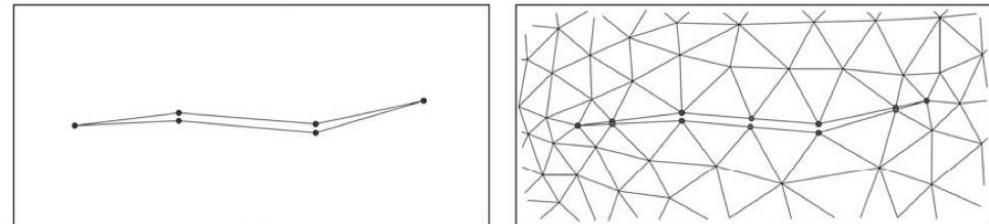
# Simulation Methodology

- Non-planar 3D multiple fracture growth
- Based on the solution of first principle continuum mechanics equations
- Solves monolithically coupled thermo-poro-mechanical deformation
- Computes energy concentrations at the tips

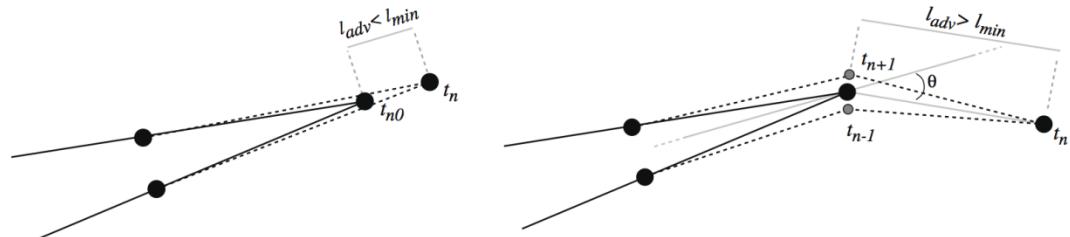
Initial flaws/fractures



Growth independent from mesh: adaptive remeshing



Energy-based growth laws: propagation extension and angle



Paluszny & Matthäi, IJSS, 2009; Paluszny & Zimmerman, CMAME 2011, EFM 2013; Salimzadeh et al., 2017, 2018; various Paluszny ARMA publications

# Governing equations

Measurable input properties (Young's modulus, Poisson's ratio, toughness, friction, matrix permeability, Biot coefficient, thermal coefficients)

The displacement governing equation, the linear momentum balance equation for a fully-saturated fractured rock matrix, is given by:

$$\int_{\Omega} [\operatorname{div}(\mathbf{D}\boldsymbol{\varepsilon} - \alpha p_m \mathbf{I} - \beta_s K(T_m - T_0) \mathbf{I}) + \mathbf{F}] d\Omega + \int_{\Gamma_c} [(\boldsymbol{\sigma}_c - p_f \mathbf{n}_c) + \mathbf{F}_{\Gamma_c}] \partial \Gamma = 0$$

The matrix flow governing equation is given by:

$$\begin{aligned} & \int_{\Omega} \operatorname{div} \left( \frac{\mathbf{k}_m}{\mu_w} (\nabla p_m - \rho_w \mathbf{g}) \right) d\Omega \\ &= \int_{\Omega} \left[ \alpha \frac{\partial (\operatorname{div} \mathbf{u})}{\partial t} + \left( \phi c_w + \frac{\alpha - \phi}{K_s} \right) \frac{\partial p_m}{\partial t} - ((\alpha - \phi) \beta_s + \phi \beta_w) \frac{dT_m}{dt} - Q_{p_m} \right] d\Omega + \int_{\Gamma_c} \frac{k_n}{\mu_w} \frac{\partial p}{\partial \mathbf{n}_c} d\Gamma \end{aligned}$$

Includes tractions and stick/slip conditions for friction solved using a contact-based, augmented-Lagrangian approach (Nejati, Paluszny, Zimmerman, CMAME, 2016)

And, the governing equation for fluid flow through the fracture, incorporating thermal effects, is:

$$\int_{\Gamma} \operatorname{div} \left( \frac{a_f^3}{12\mu_w} \nabla p_f \right) d\Gamma = \int_{\Gamma} \left[ \frac{\partial a_f}{\partial t} + a_f c_w \frac{\partial p_f}{\partial t} - a_f \beta_w \frac{\partial T_f}{\partial t} - Q_{p_f} - \frac{k_n}{\mu_w} \frac{\partial p}{\partial \mathbf{n}_c} \right] d\Gamma$$

where apertures are defined as (Paluszny & Matthäi, 2009):

$$a_f = (\mathbf{u}^+ - \mathbf{u}^-) \cdot \mathbf{n}_c + a_f^c$$

Laminar flow in fractures, Darcy flow in matrix  
Two additional equations govern thermal conduction and advection

## Discretisation of the equations

The finite element method is used to numerically solve governing equations. Spatial discretisation is performed through the Galerkin method, while finite difference techniques are used to solve time evolution.

The set of discretised equations can be expressed in matrix form of

$$\mathbb{S}\mathbb{X} = \mathbb{F}$$

where

$$\mathbb{S} = \begin{bmatrix} \mathbb{S}_{uu} & \mathbb{S}_{up} & \mathbb{S}_{uT} \\ \mathbb{S}_{pu} & \mathbb{S}_{pp} & \mathbb{S}_{pT} \\ \mathbb{S}_{Tu} & \mathbb{S}_{Tp} & \mathbb{S}_{TT} \end{bmatrix}$$

the system is monolithically coupled

and

$$\mathbb{F} = \begin{Bmatrix} F_u \\ F_{p_m} \\ F_{p_f} \\ F_{T_m} \\ F_{T_f} \end{Bmatrix} = \begin{Bmatrix} F + C_{uT_m} \hat{T}_0 \\ C_{p_m}^T \hat{u}^t + M_{p_m,p_m} \hat{p}_m^t - C_{p_m,T_m} \hat{T}_m^t + Q_{p_m} dt + n_G dt \\ C_{p_f}^T \hat{u}^t + M_{p_f,p_f} \hat{p}_f^t - C_{p_f,T_f} \hat{T}_f^t + Q_{p_f} dt \\ C_{T_m u} \hat{u}^t + M_{T_m,T_m} \hat{T}_m^t - C_{T_m p_m} \hat{p}_m^t + Q_{T_m} dt \\ M_{T_f,T_f} \hat{T}_f^t - C_{T_f p_f} \hat{p}_f^t + Q_{T_f} dt \end{Bmatrix}$$

# Stress intensity factors

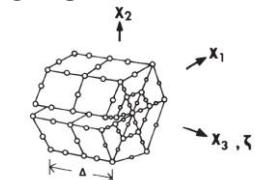
The onset and path of fracture growth is governed by something called the “stress intensity factor”

Once the displacement field is computed we can derive strains and stresses, assuming that the matrix is linear elastic and isotropic

We can define the path independent J-integral (rate of change of net potential energy with respect to crack advance per unit thickness of crack front), as follows

$$J_V = \frac{1}{A_c} \int_V \left( \sigma_{ij} \frac{\partial u_j}{\partial x_k} - W \delta_{ik} \right) \frac{\partial q_k}{\partial x_i} dV$$

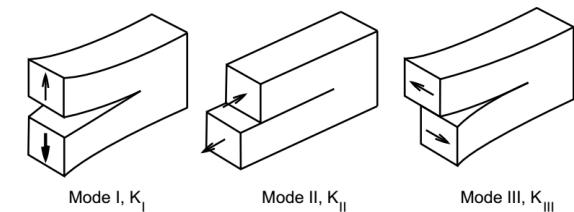
J is essentially the energy flow into the crack tip



and for a linear elastic material  $J = \frac{K^2}{E_{eff}}$  where  $E_{eff}$  is the effective elastic modulus

and the stress intensity factor can be decomposed into the three modalities of deformation (tension, in-plane and out-of-plane shear), as

$$K = \frac{K_I}{2} + \frac{1}{2} \sqrt{K_I^2 + 4(\alpha_1 K_{II})^2 + 4(\alpha_2 K_{III})^2}$$

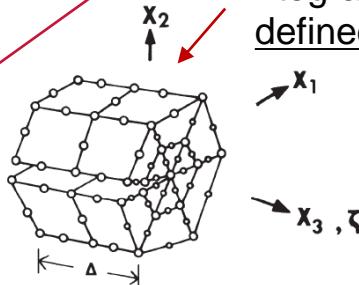


This can be further extended to compute each modality independently using the Nakamura and Parks Interaction Integral. I developed a new method to compute this integral over a virtual domain.

# New method to integrate stress intensity factors

My method to compute this integral over a virtual domain allows modelling 3D fracture growth using unstructured meshes

1960



Integration domain is defined by the mesh

We don't want this!

Cervenka & Saouma 1997

Rajaram *et al.* 2000

2010

Paluszny & Zimmerman, CMAME, 2011

2015

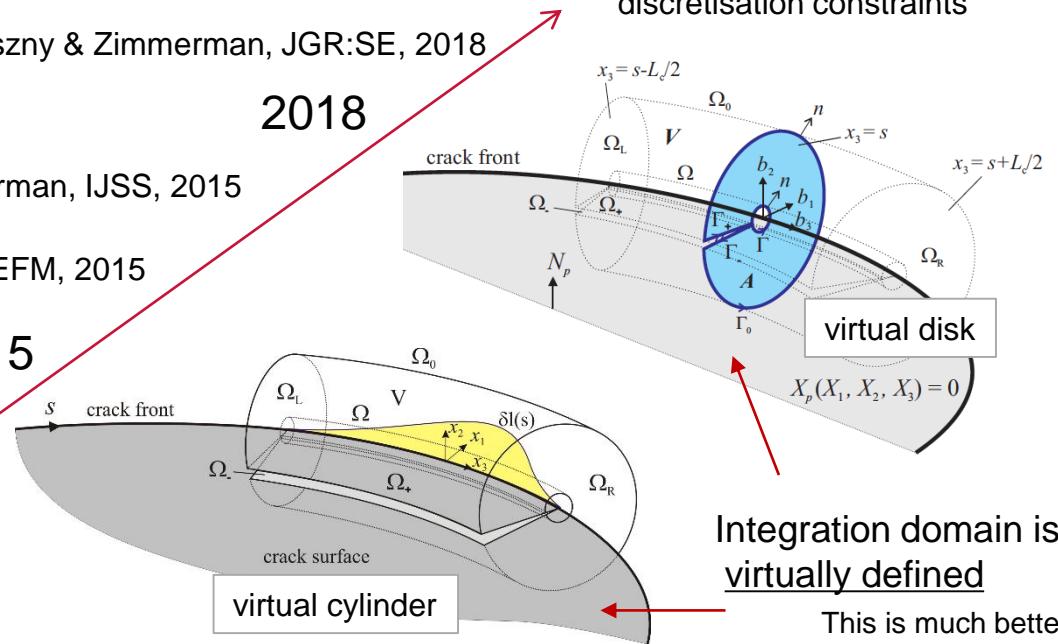
Nejati, Paluszny & Zimmerman, EFM, 2015

Nejati, Paluszny & Zimmerman, IJSS, 2015

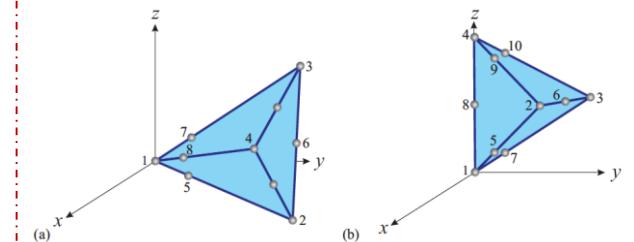
2018

Thomas, Paluszny & Zimmerman, JGR:SE, 2018

Increasing accuracy of energy estimates while relaxing discretisation constraints



Efficient numerical elements for 3D fracture tips: quarter point quadratic tetrahedra



## How stress intensity factors translate into growth

**Propagation Law.** The relative growth of any node  $n$  along a three-dimensional fracture tip is defined as follows:

$$\Delta a_n = \Delta a_{max} \left( \frac{K_n}{K_{max}} \right)^\beta$$

A variation of this method has been validated against outcrop data by Renshaw & Pollard

**Angle Law.** The angle of fracture growth is a function of all three SIFs. Richard et al. (2014) define the propagation angle as

$$\varphi = \mp \left[ A \frac{|K_{II}|}{K_I + |K_{II}| + |K_{III}|} + B \left( \frac{|K_{III}|}{K_I + |K_{II}| + |K_{III}|} \right)^2 \right]$$

where  $\varphi$  is the propagation angle (with  $0^\circ$  being along the fracture plane),  $A = 140^\circ$  and  $B = -70^\circ$ .

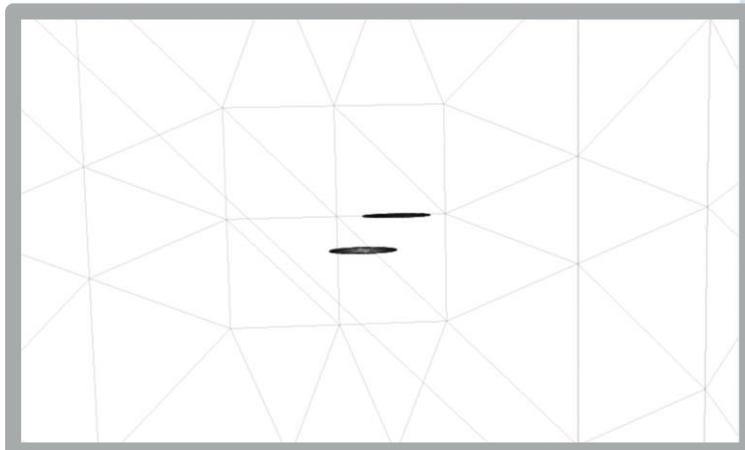
There are many extensively-validated variations for “propagation and angle laws”, and they rely on stress intensity factor computations.

# Discretisation and Geometric representation

Fractures are represented by smooth surfaces and triangles

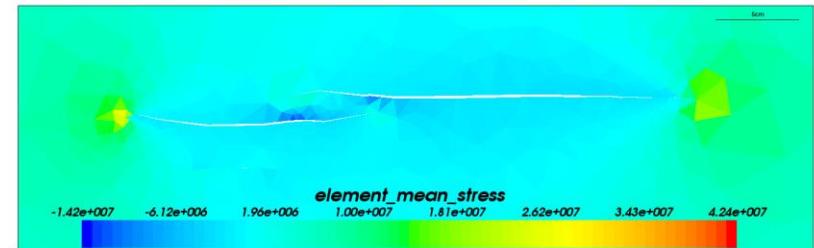
The matrix is discretised by tetrahedra and the fracture by triangles

Developed in C++, parallelised for shared memory workstations

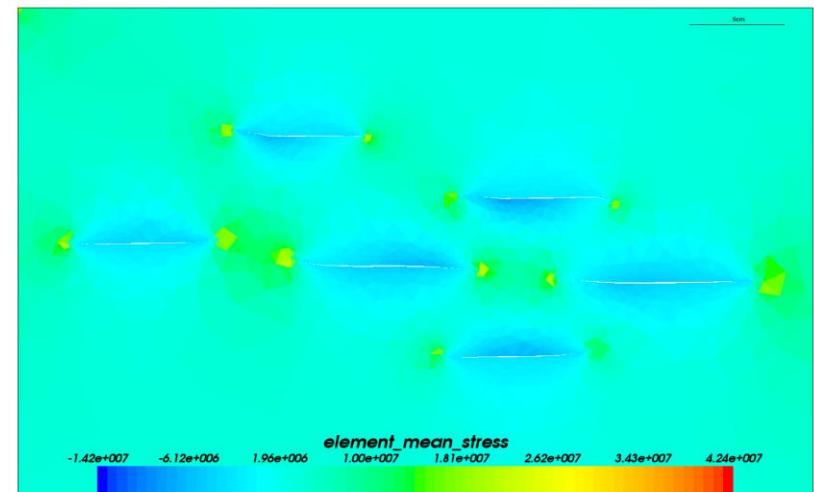


Two fractures growing and interacting under tension

Fractures growing and interacting



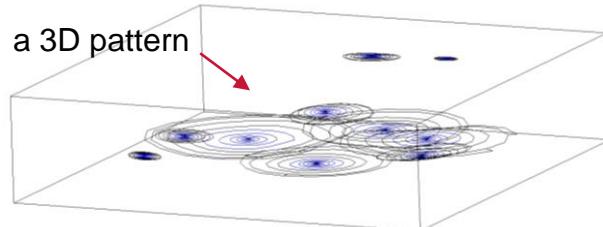
Stress concentrations around the tips and stress shadows around the body of the fracture emerge during the simulation



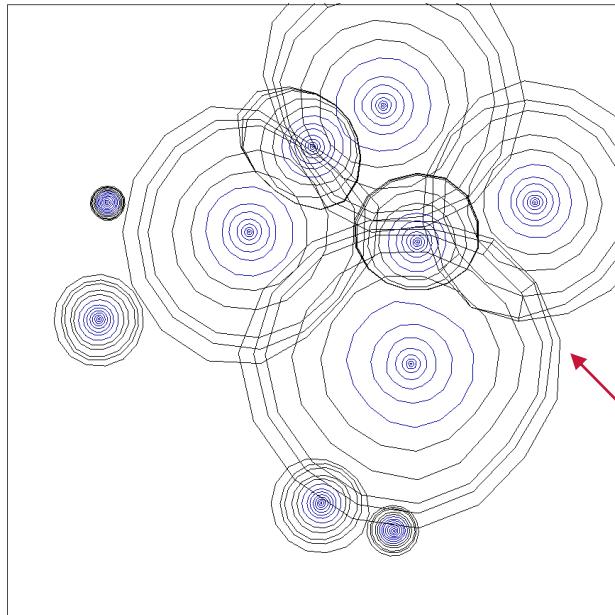
Paluszny & Matthäi, IJSS, 2009  
Paluszny & Matthäi, JGR:SE, 2010

# Fracture set growth

Fractures behave as single larger entities prior to intersection:



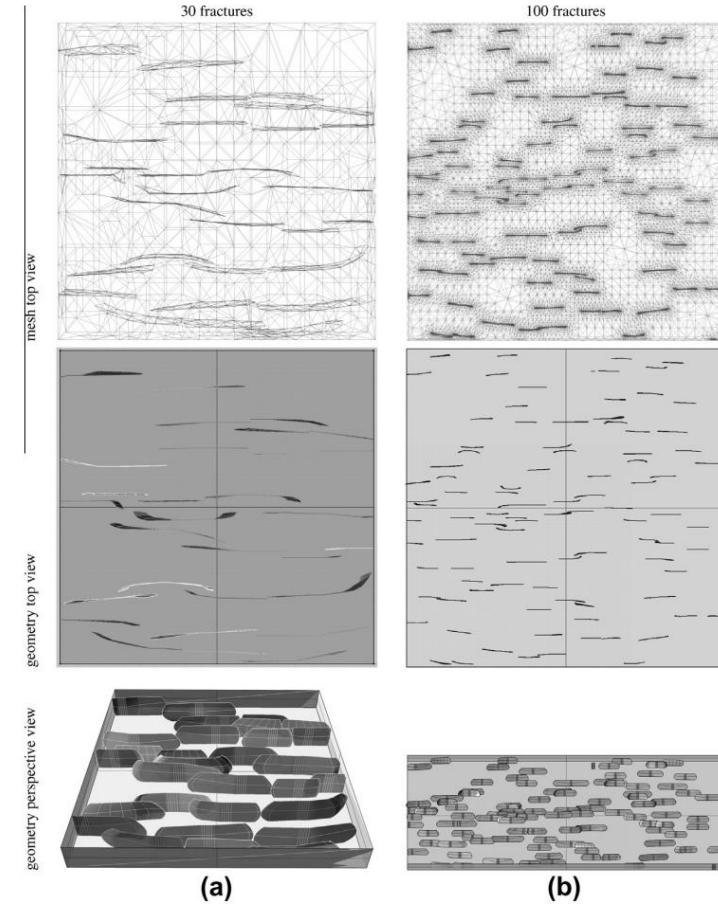
top view of the same 3D pattern



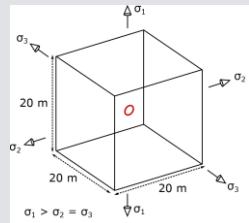
Fractures growing within single layers of rock:

Predicting how patterns are linked to the processes that form them is a key challenge

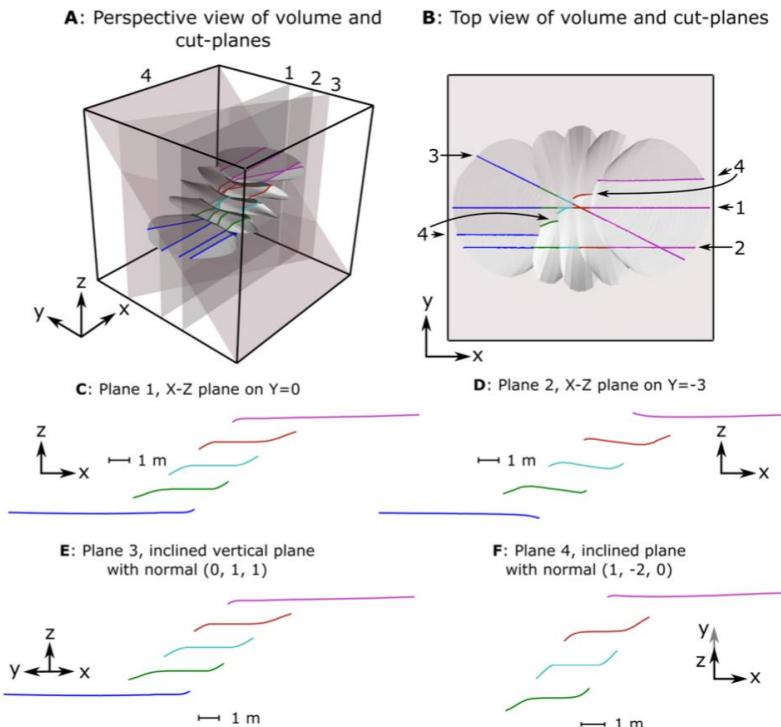
How do pre-existing patterns affect new patterns; can we predict what will happen?



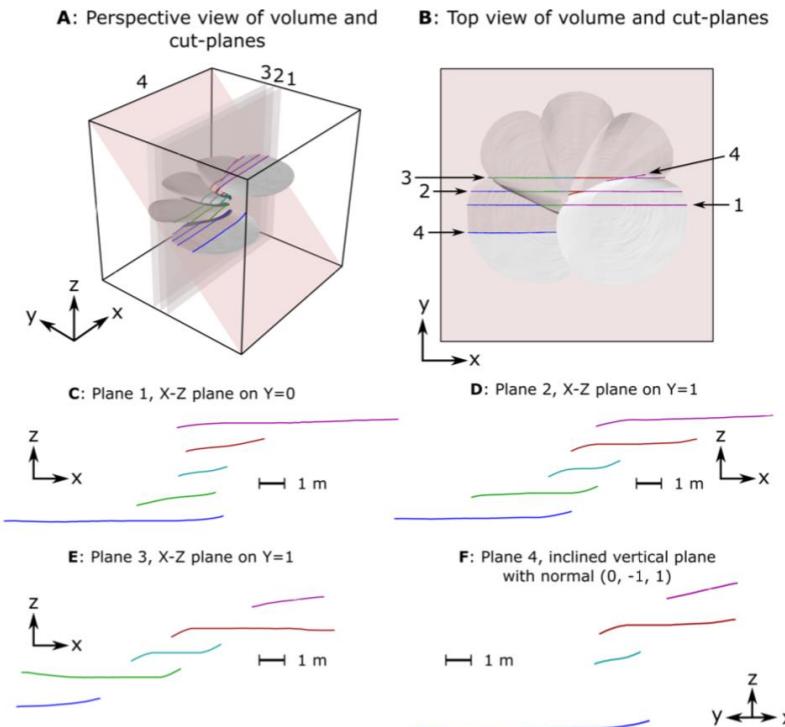
# The growth of a fracture array



aligned array of fractures

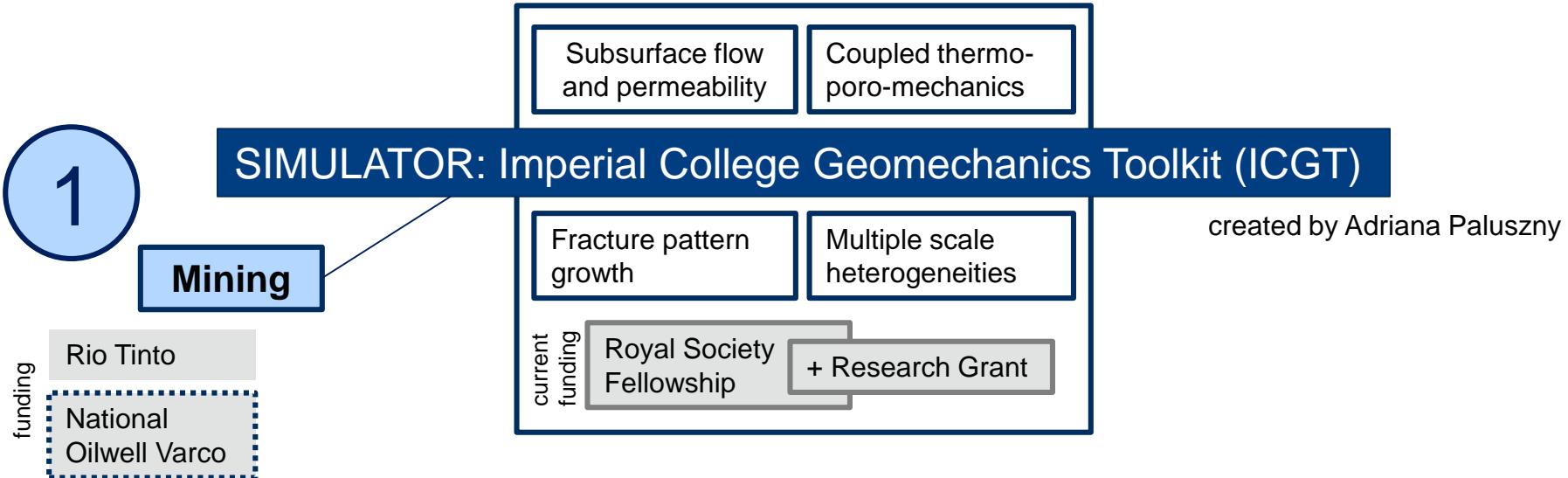


spiral array of fractures



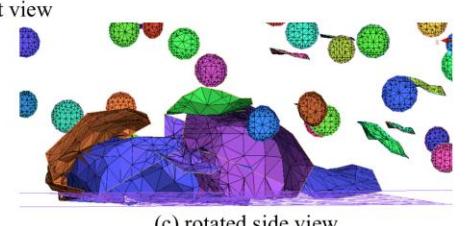
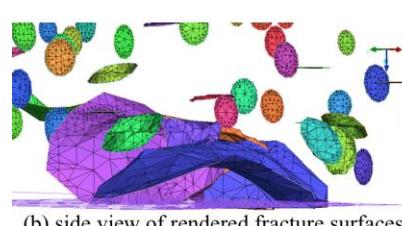
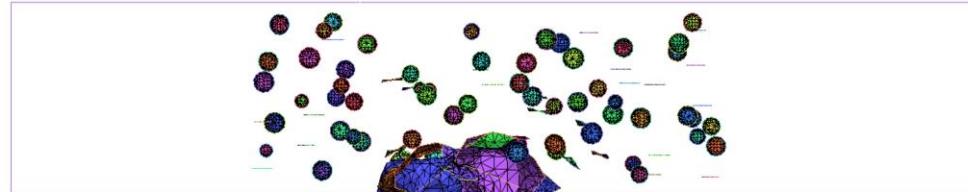
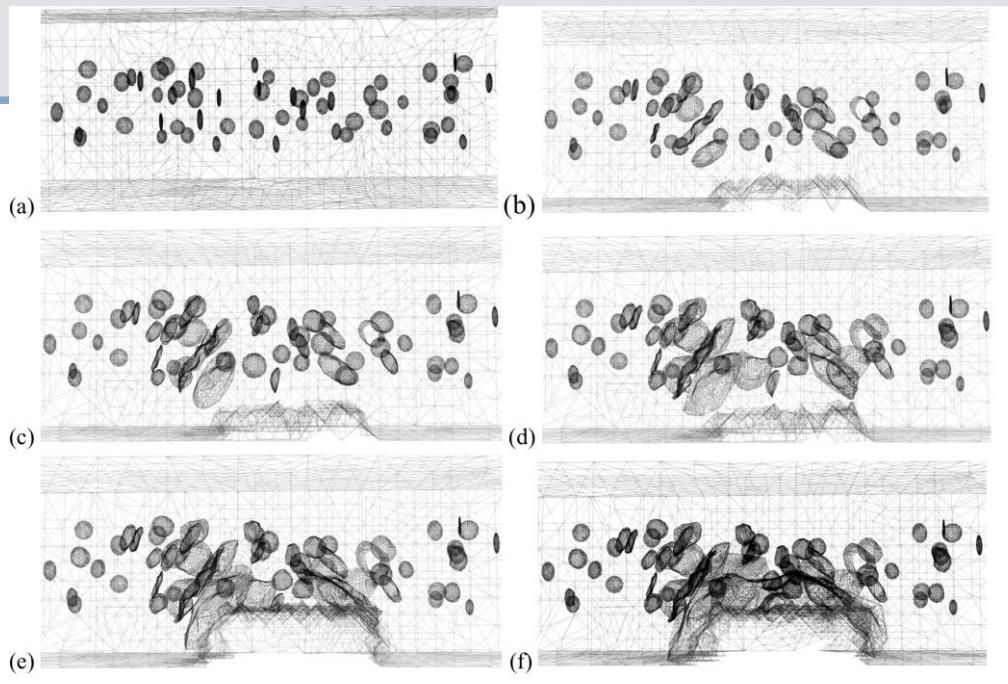
Can we distinguish these in an outcrop?

# Overview of my research



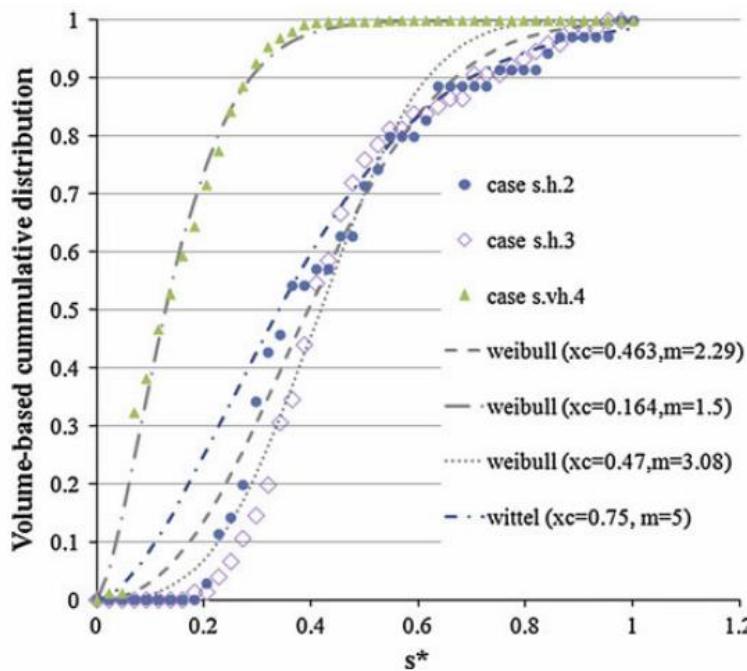
# Fractures and Caving

A fracture set responds to an undercut. Cave shapes depend on the initial fracture pattern.

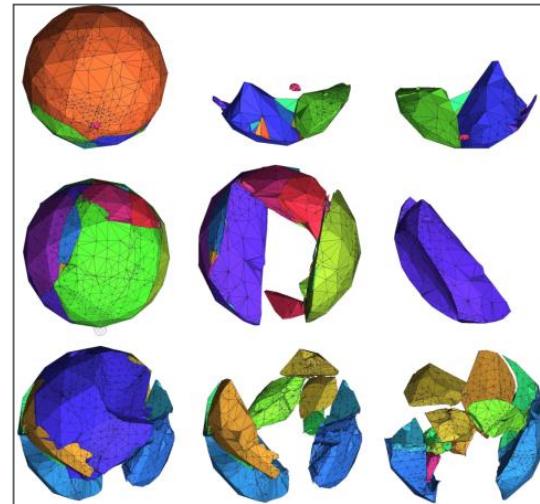


## “Secondary fragmentation” in block caving

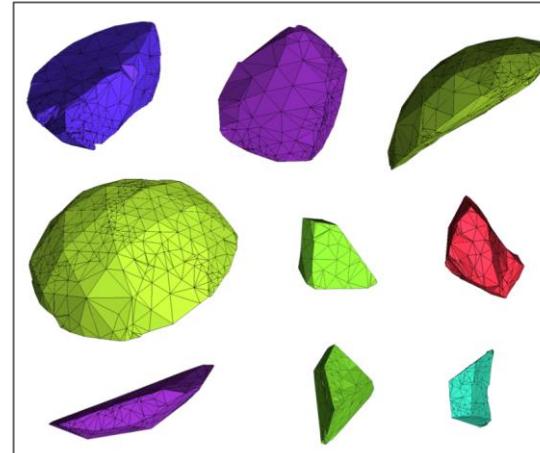
- Modelled fracture leading to fragmentation
- Fragment volumes followed a Weibull distribution that matched experimental results



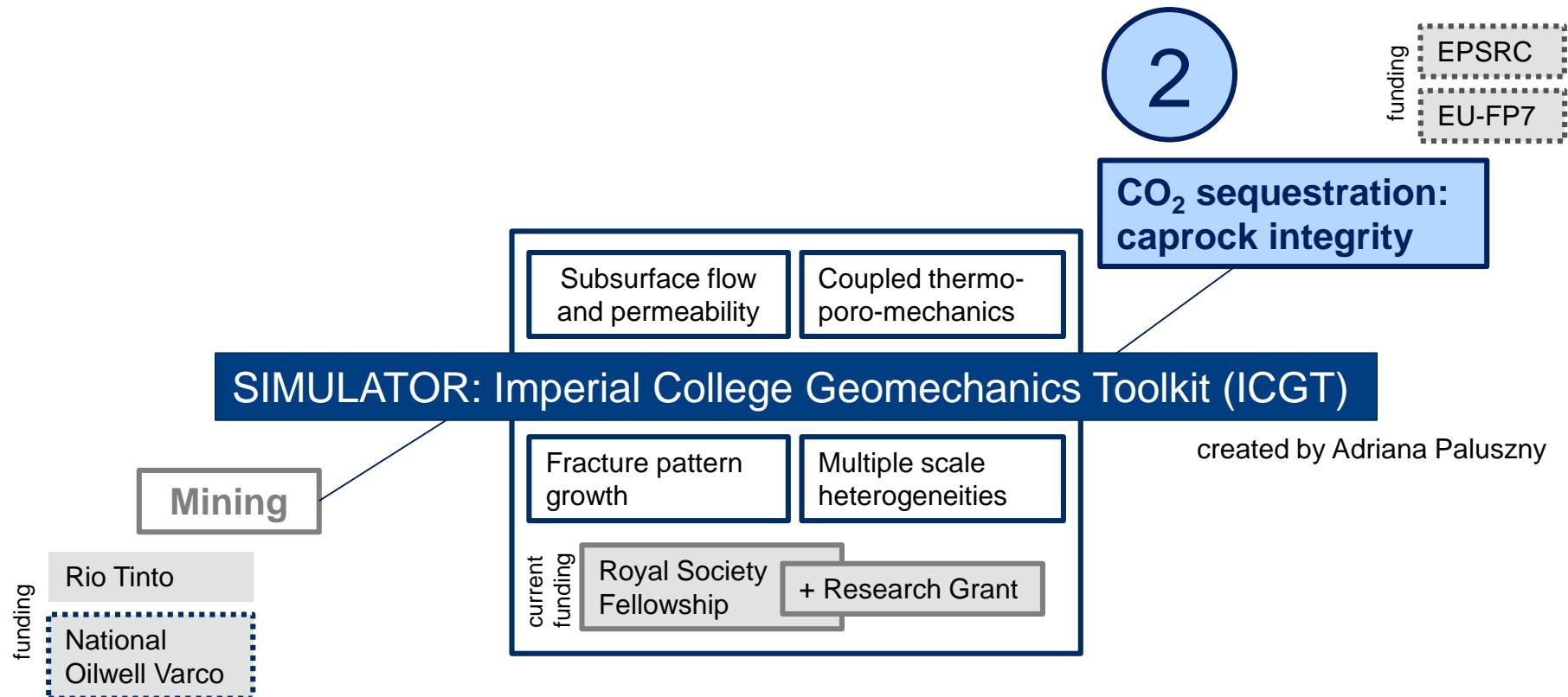
velocity-dependent  
fragmentation  
pattern



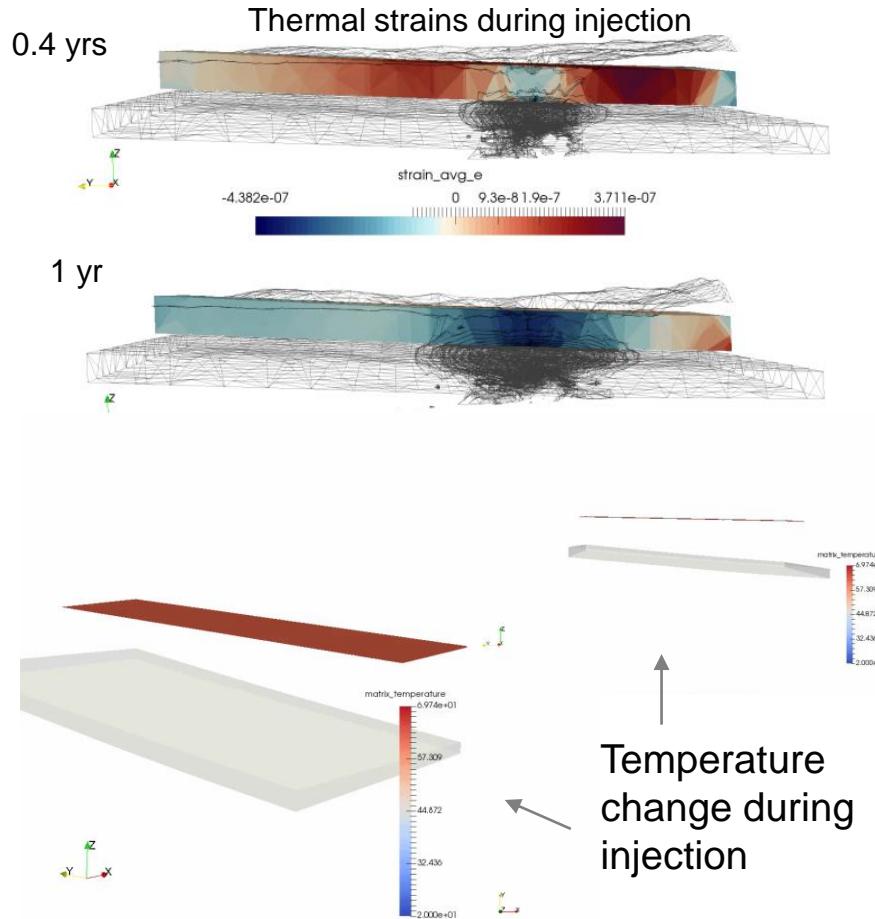
fragment  
shapes



# Overview of my research

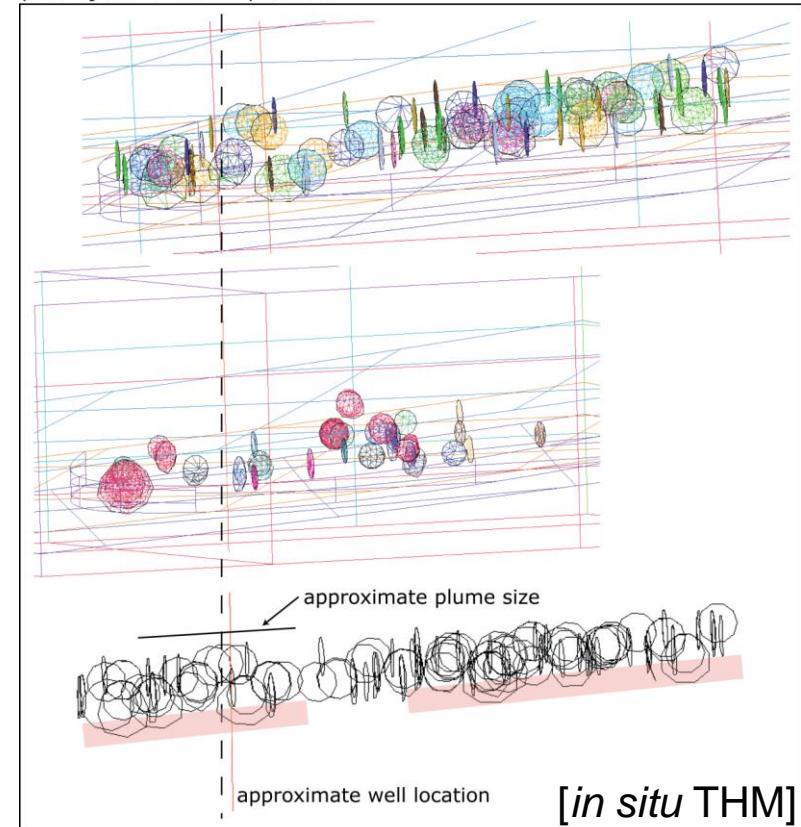


# Fractures in shale caprocks during cold CO<sub>2</sub> injection



Fracture growth is evaluated regionally as a function of local fluid injection

post-injection fracture patterns



co-I  
TRUST project  
large consortium

# Fault apertures as a function of temperature contrast

The Captain sandstone is located at a depth of 2600 m; hence, the vertical stress is set to 55 MPa, and the horizontal stresses are set to 45 MPa. *In situ* temperature is assumed to be 83 C.

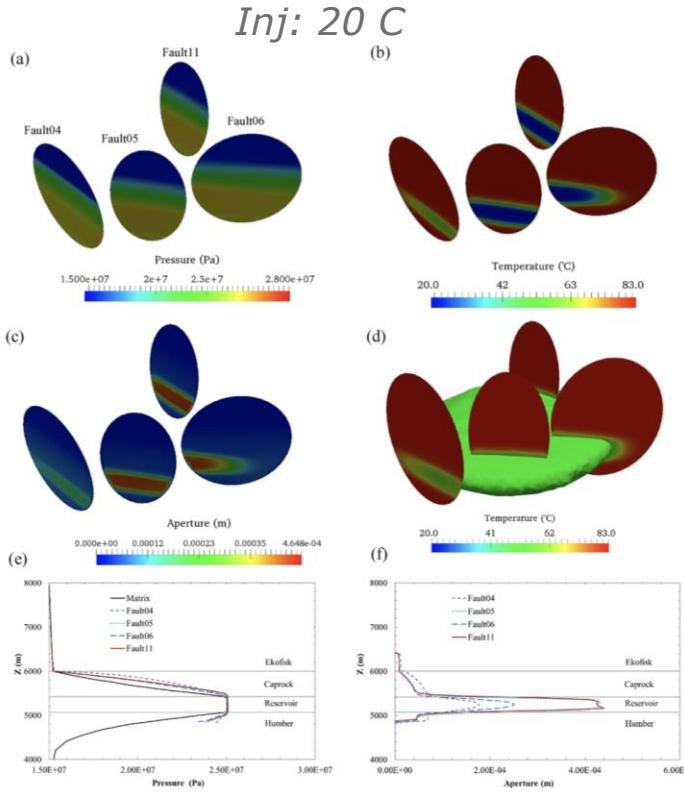


Fig. 2. The fluid pressure (a), temperature (b), and aperture distribution (c), on the faults, the 50 °C temperature plume within the reservoir layer (d), pressure profile along a vertical line passing through faults (e), and the aperture profile along a vertical line passing through the centre of the faults (f), after 160 years for the case:  $E = 20 \text{ GPa}$ ,  $T_{\text{inj}} = 20^\circ\text{C}$ .

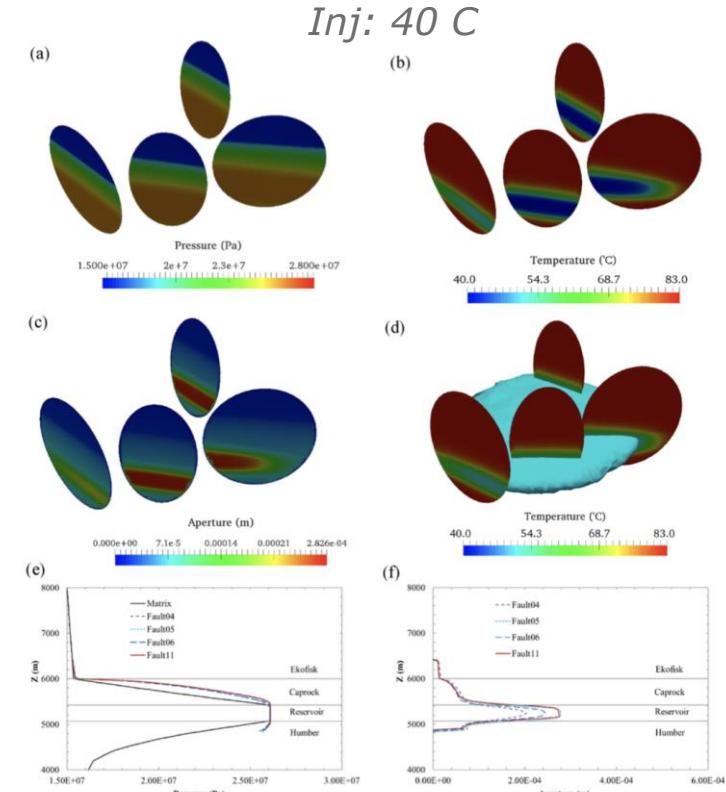
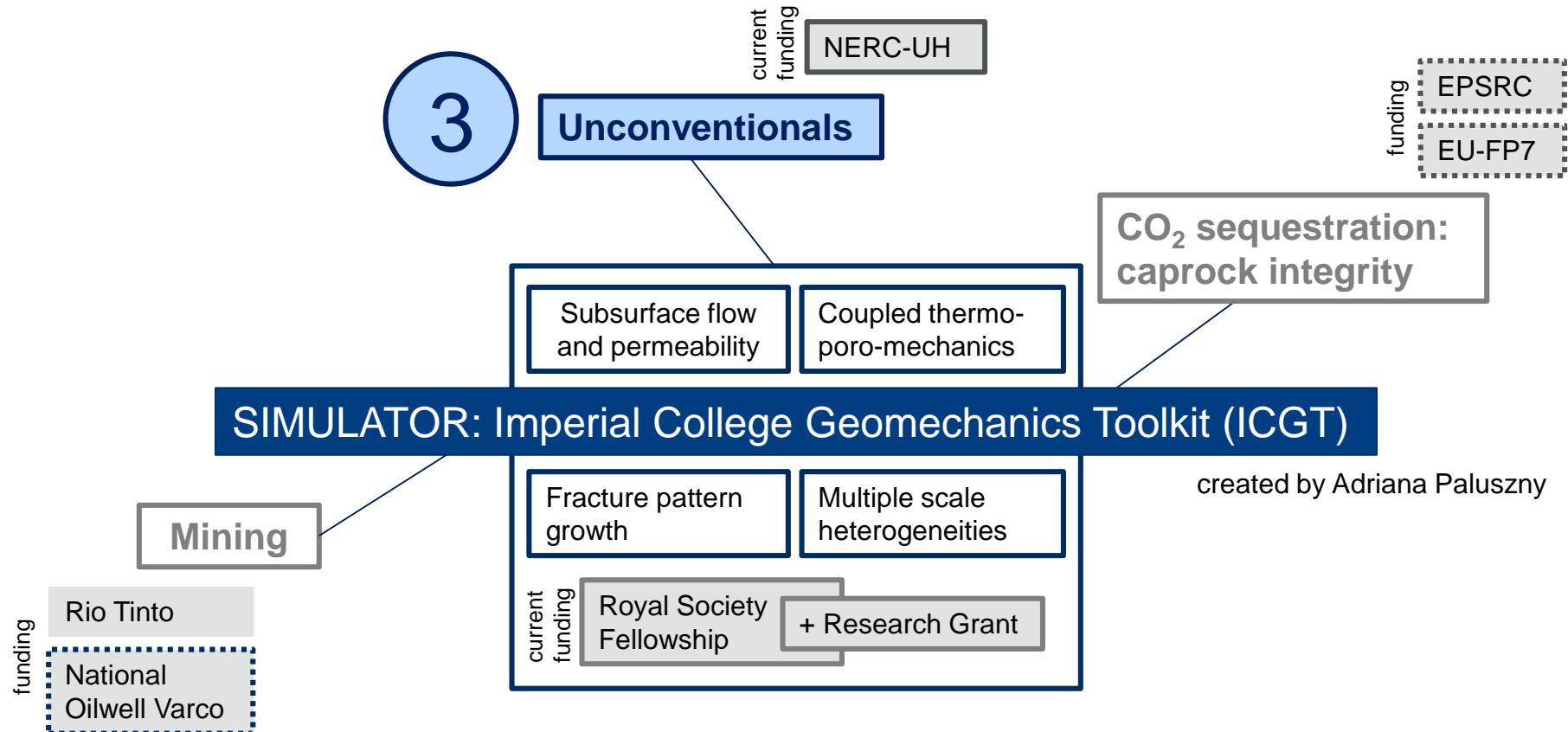
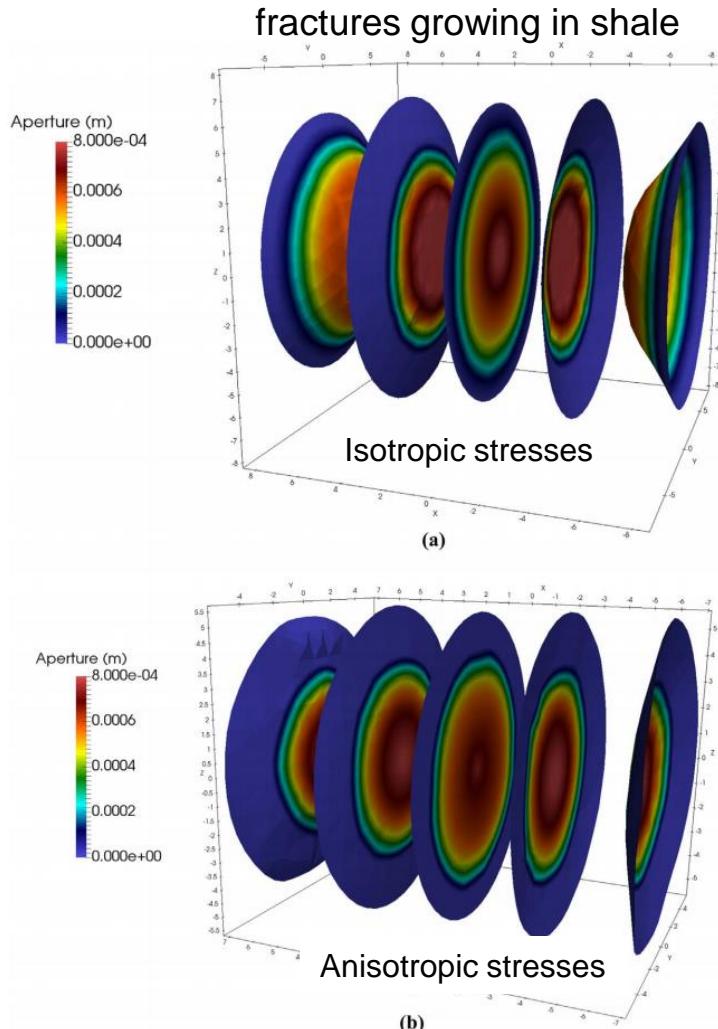


Fig. 3. The fluid pressure (a), temperature (b), and aperture distribution (c), on the faults, the 50 °C temperature plume within the reservoir layer (d), pressure profile along a vertical line passing through faults (e), and the aperture profile along a vertical line passing through the centre of the faults (f), after 160 years for the case:  $E = 20 \text{ GPa}$ ,  $T_{\text{inj}} = 40^\circ\text{C}$ .

# Overview of my research



# Simultaneous growth of multiple hydraulic fractures



- Fractures growing in a poroelastic medium
- Under isotropic and anisotropic *in situ* stresses
- Apertures do not follow the geometry of the fractures
- Apertures are also affected by interaction

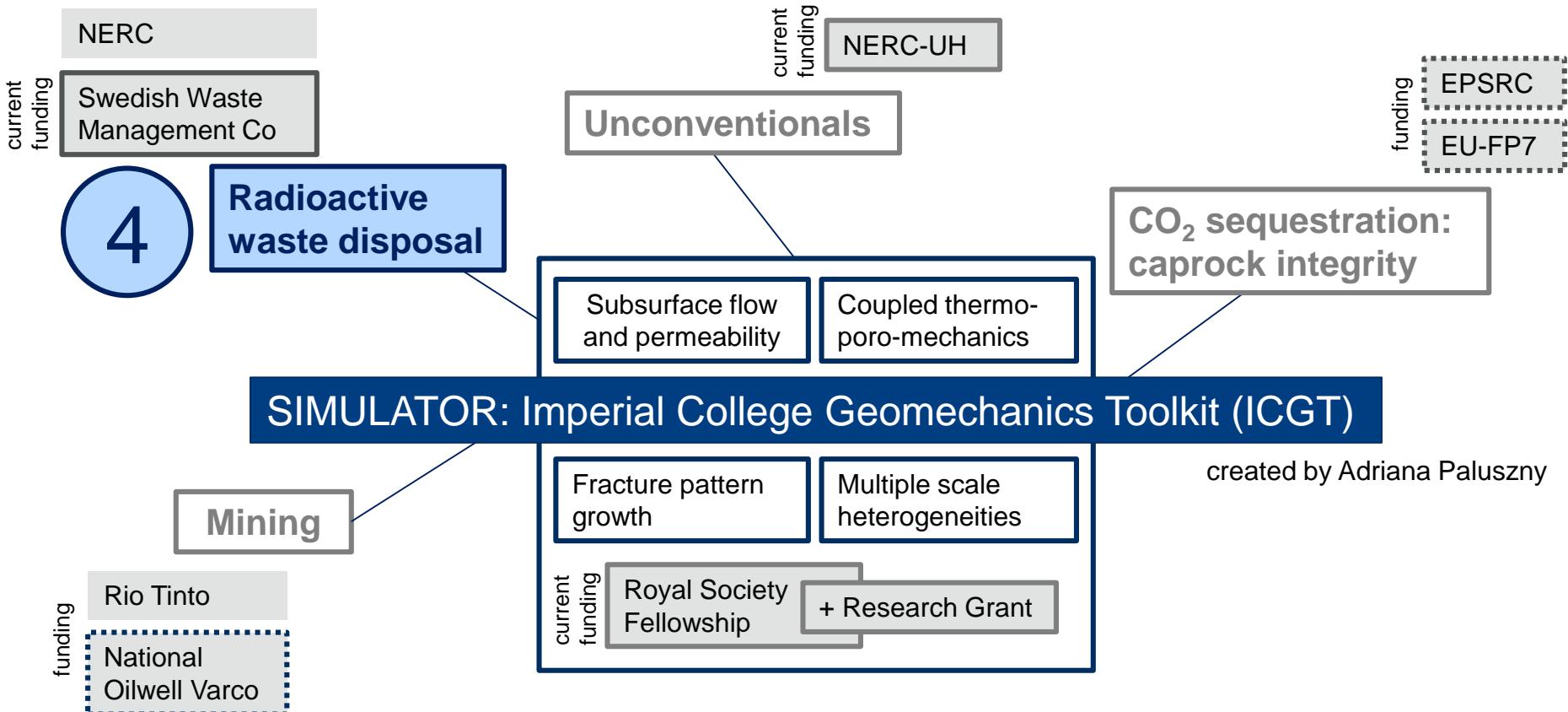
Grant Awarded:  
Effect of heterogeneities  
on growth, as part  
of NERC-UH



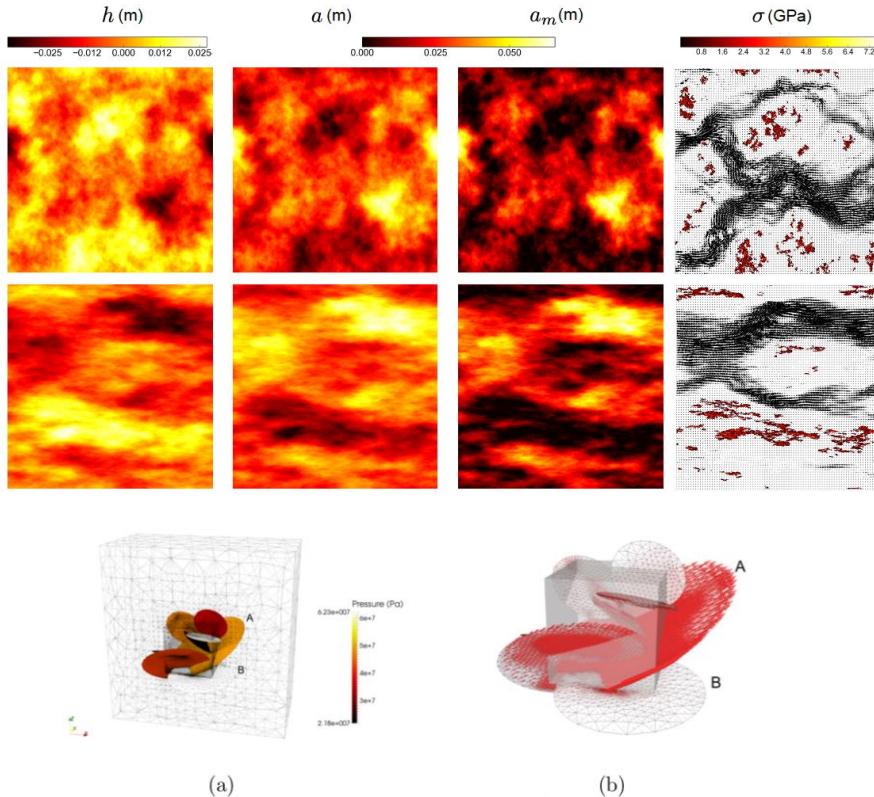
Co-I, Funding:  
PDRA  
Robin Thomas  
2018-2020



# Overview of my research



# Multi-scale modelling of surface roughness effects



Grant awarded:  
 Micro-scale effect on growth  
 and intersections in hydro-  
 mechanically coupled  
 systems!



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 PhD studentship  
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 2019-2022



## Water Resources Research AN AGU JOURNAL

Research Article |  Open Access |  

### Relationship Between the Orientation of Maximum Permeability and Intermediate Principal Stress in Fractured Rocks

Philipp S. Lang, Adriana Paluszny , Morteza Nejati, Robert W. Zimmerman

First published: 19 October 2018 | <https://doi.org/10.1029/2018WR023189>

 SECTIONS

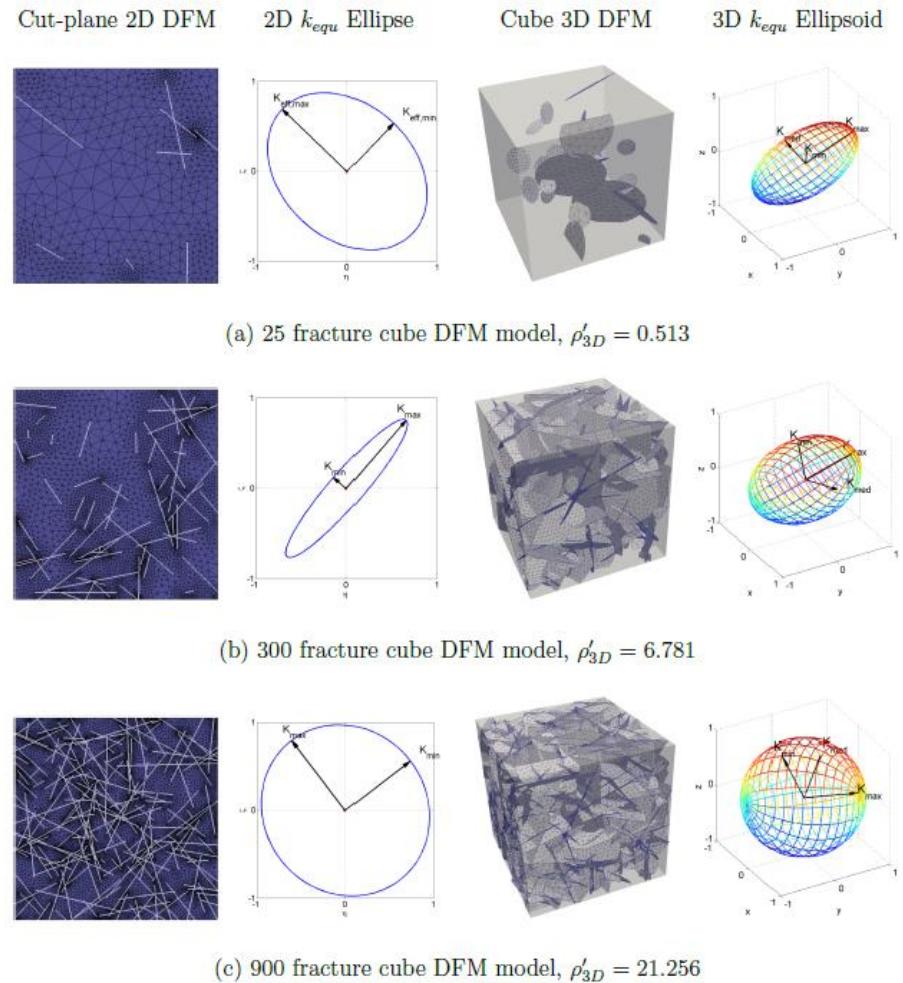
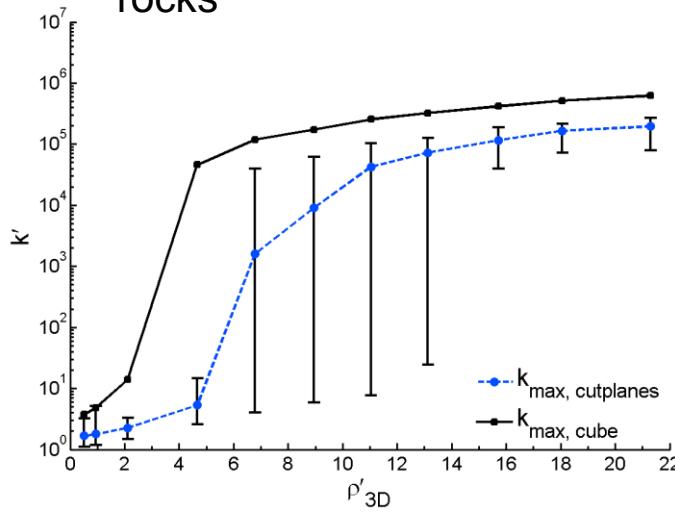
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### Abstract

Flow and transport properties of fractured rock masses are a function of geometrical structures across many scales. These structures result from physical processes and states and are highly anisotropic in nature. Fracture surfaces often tend to be shifted with respect to each other, which is generally a result of stress-induced displacements. This shift controls the fracture's transmissivity through the pore space that forms from the created mismatch between the surfaces. This transmissivity is anisotropic and greater in the

# Tensorial permeability of a fractured rock

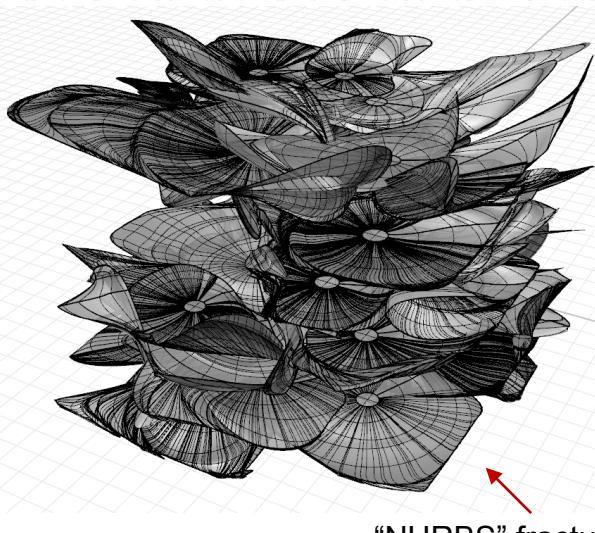
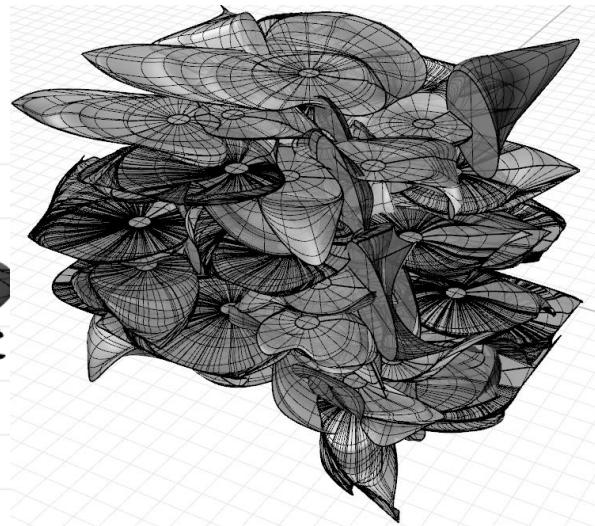
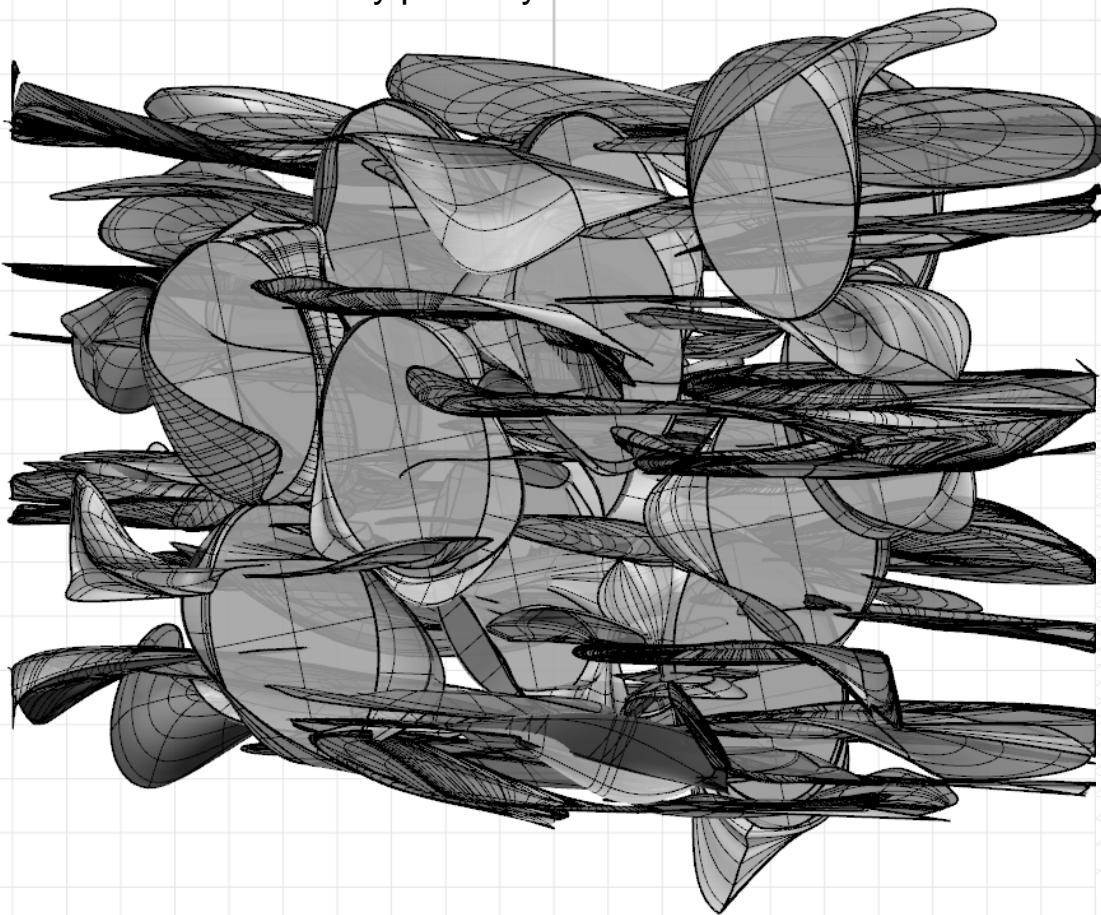
- Permeability of a 3D network is very difficult to approximate based on 2D, both in magnitude and orientation
- Novel method to numerically compute the tensorial permeability of 3D fractured rocks



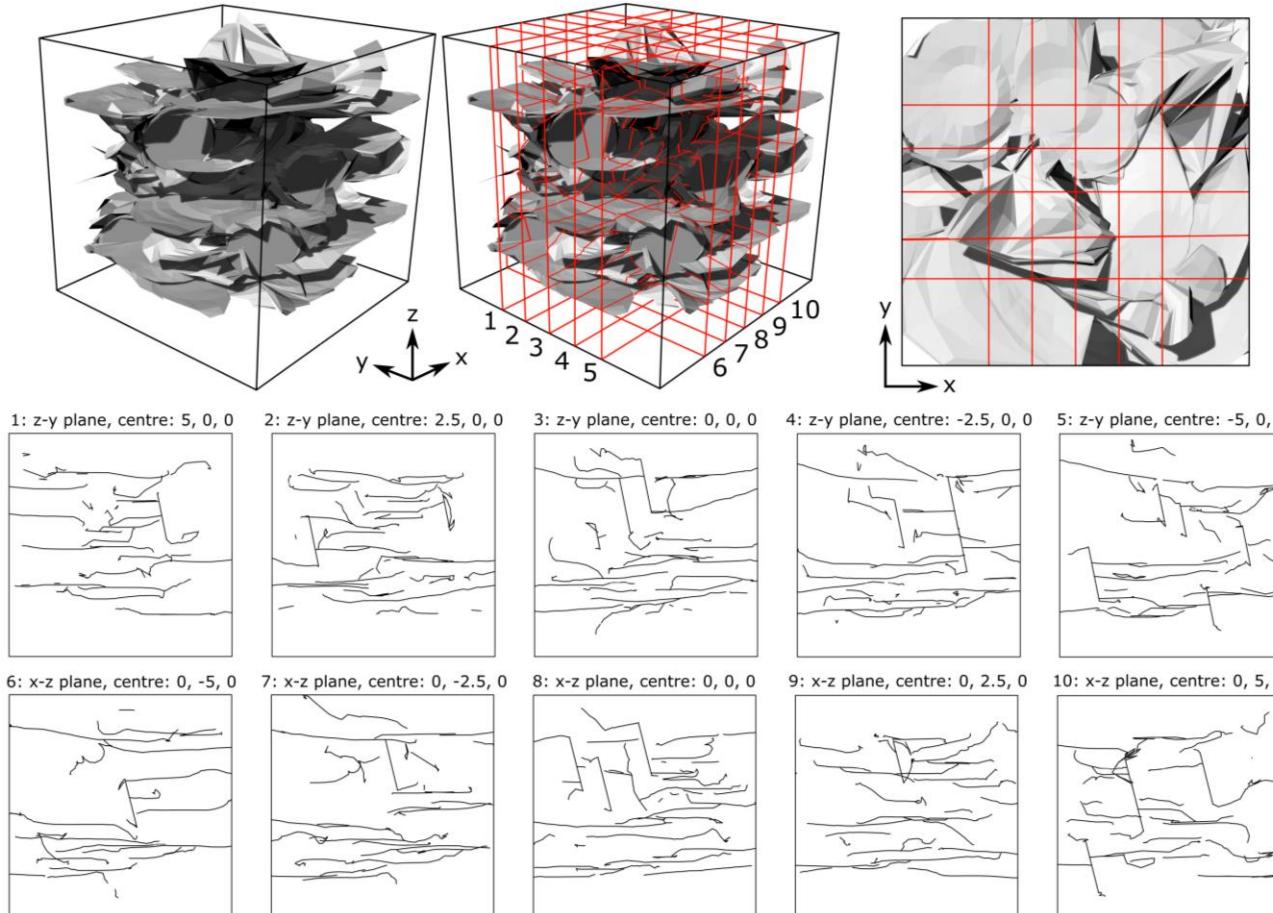
## Network geometry

How do we know if this is “realistic”?

Complex networks develop relationships that go beyond density and connectivity. The interaction of fractures during growth enhances connectivity pathways.



# New methods to quantify the evolving geometry



[Thomas, Paluszny, Zimmerman, submitted]

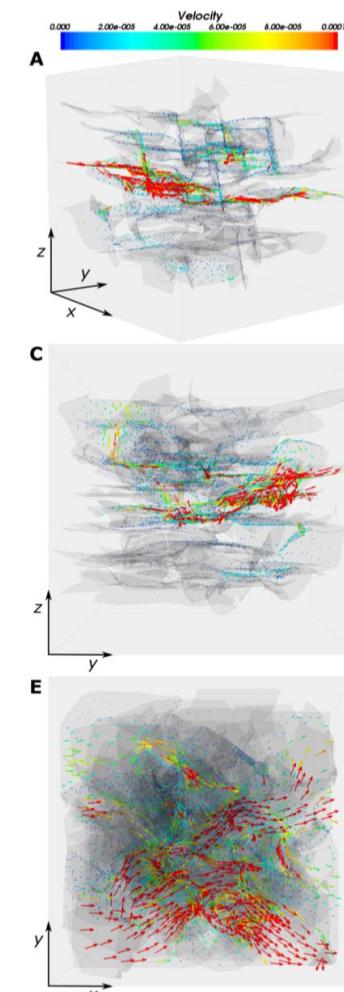
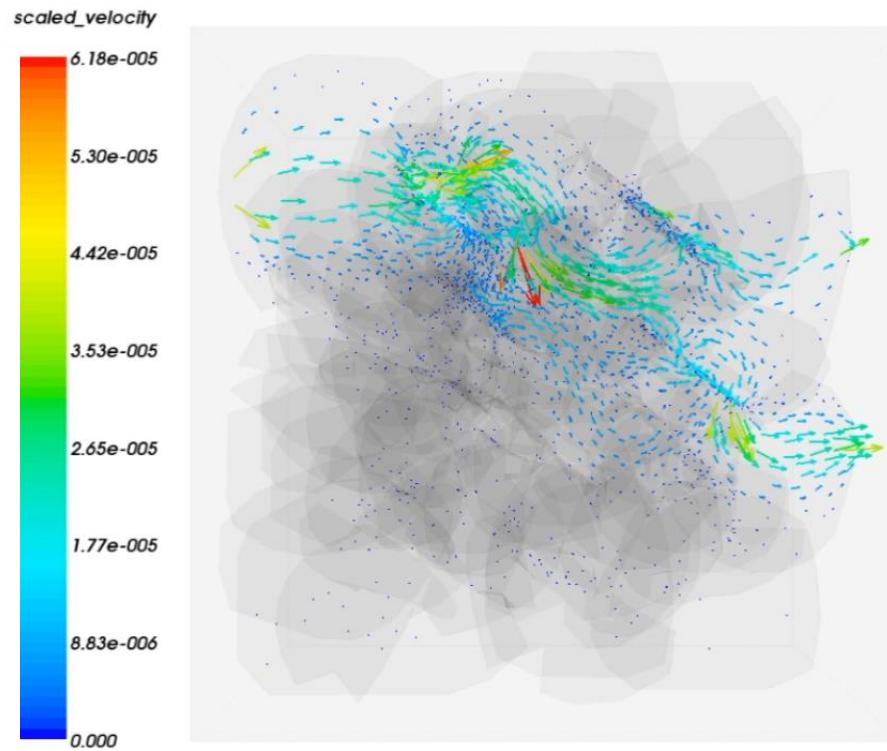
This ability to create complex 3D networks and accurately model coupled thermo-poro-mechanics led to an industrial grant sponsored by SKB (2018-2022)

**SKB** Co-PI  
Industry-funded  
PhD studentship  
Cristina Saceanu  
2018-2020

Numerically generated “outcrops”

# Flow channels

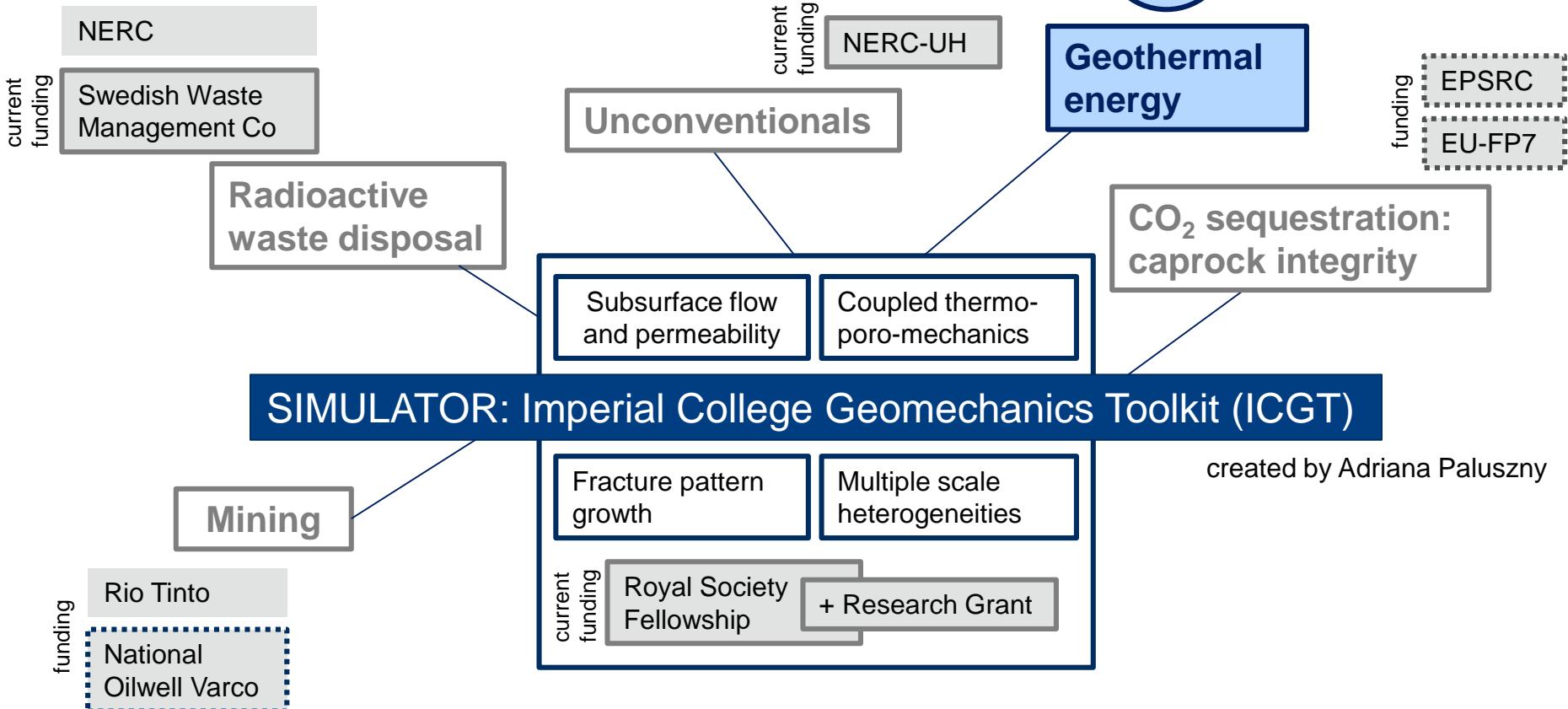
Fluid flow channeling as a result of fracture mechanical interaction and aperture



Paluszny, Thomas, Zimmerman, CouFrac, 2018  
Thomas, Paluszny, Zimmerman, to be submitted 2019 Q2

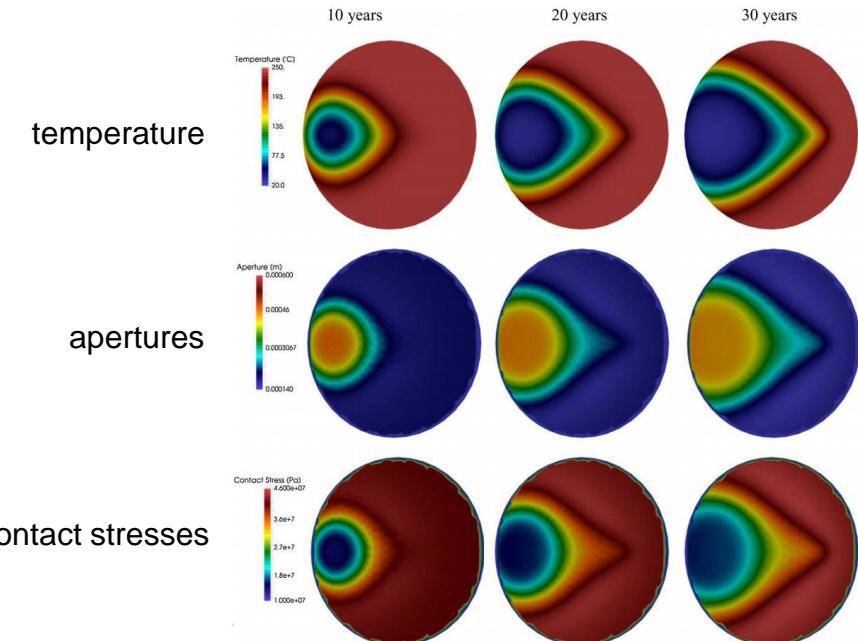
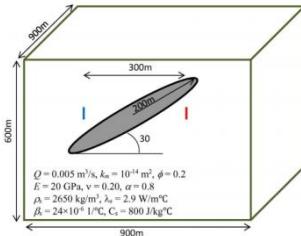
# Overview of my research

5



# Thermo-hydro-mechanical deformation of fractures

Geothermal  
stimulation of a 100 m  
radius fracture



Geothermics 71 (2018) 213–224

Contents lists available at ScienceDirect



journal homepage: [www.elsevier.com/locate/geothermics](http://www.elsevier.com/locate/geothermics)



A three-dimensional coupled thermo-hydro-mechanical model for  
deformable fractured geothermal systems



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## ARTICLE INFO

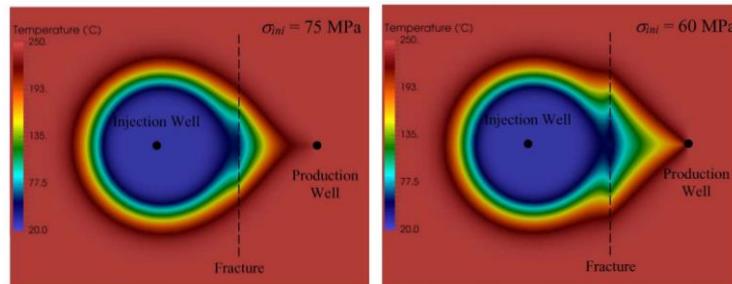
**Keywords:**  
Coupled THM processes  
Fractured geothermal reservoir  
Contact model  
Flow channeling  
Enhanced geothermal systems

## ABSTRACT

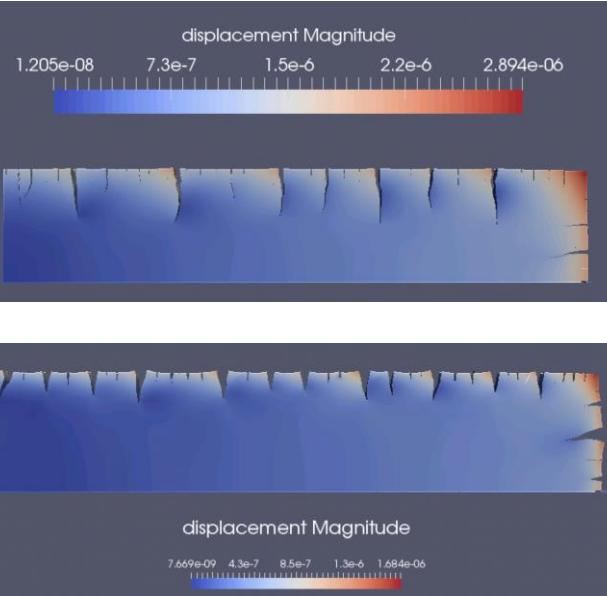
A fully coupled thermal-hydraulic-mechanical (THM) finite element model is presented for fractured geothermal reservoirs. Fractures are modelled as surface discontinuities within a three-dimensional matrix. Non-isothermal flow through the rock matrix and fractures are defined and coupled to a mechanical deformation model. A robust contact model is used to simulate the contact tractions between opposing fracture surfaces in THM calculations. A numerical model has been developed using the standard Galerkin method. Quadratic tetrahedral and triangular elements are used for spatial discretization. The model has been validated against several analytical solutions, and applied to study the effects of the deformable fractures on the injection of cold water in fractured geothermal systems.

Results show that the creation of flow channeling due to the thermal volumetric contraction of the rock matrix is very likely. The fluid exchange heat with the rock matrix, which results in cooling down of the matrix, and subsequent volumetric deformation. The cooling down of the rock matrix around a fracture reduces the contact pressure in the fracture and creates a new fracture aperture. Stress redistribution may reduce the aperture, as the area with lower contact stress on the fracture expands. Stress redistribution reduces the likelihood of fracture propagation under pure opening mode, while the expansion of the area with lower contact stress may increase the likelihood of shear fracturing.

Interaction of a fracture with another  
intersecting fracture, effect on the thermo-poro-  
mechanical apertures



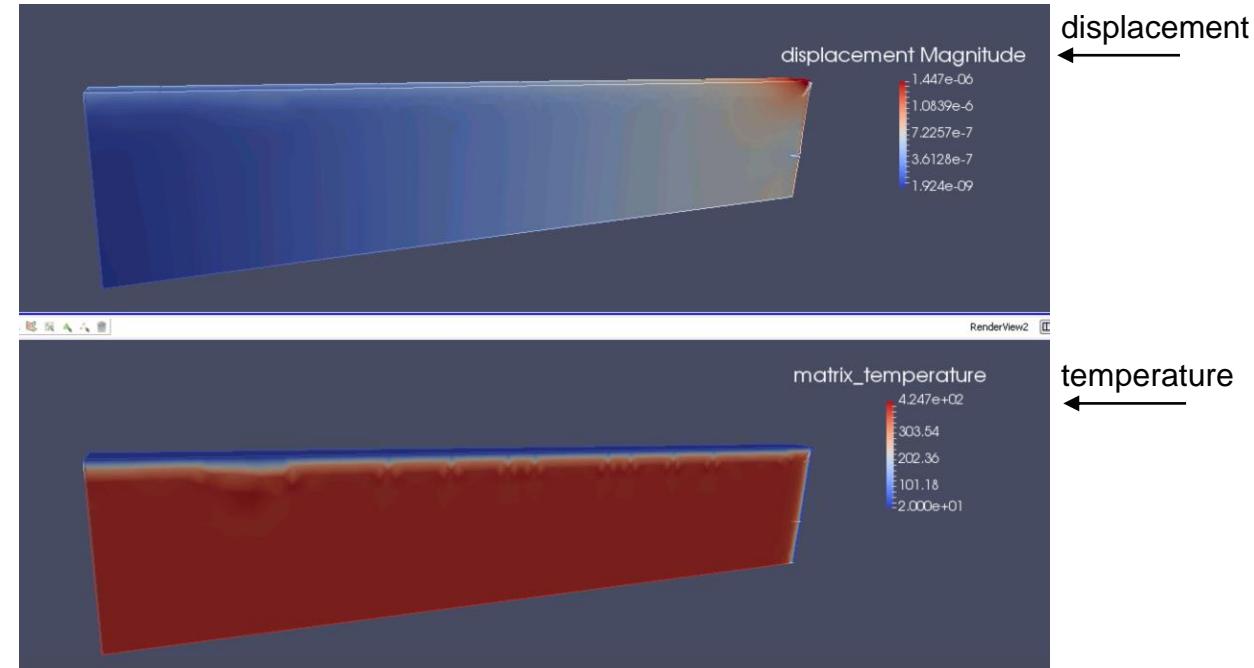
# Modelling of thermal shock-induced fracture growth



Quenching of an aluminium oxide plate 5cm  
400-500 C contrast over seconds

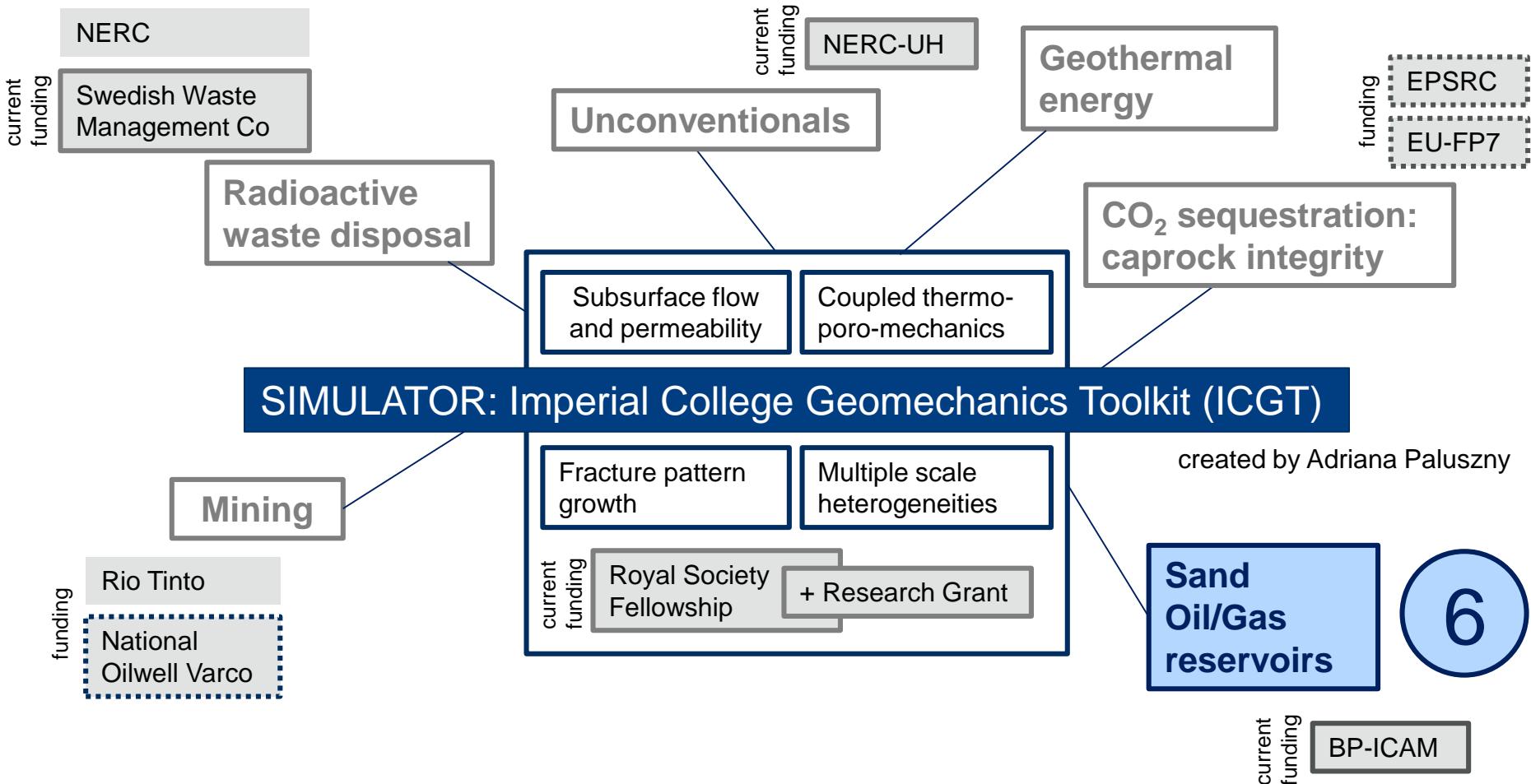
Validation: Towards accurate geothermal thermal fracture predictions

I am currently building this into the simulator's core



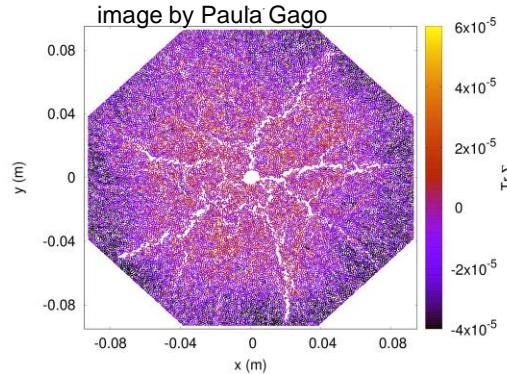
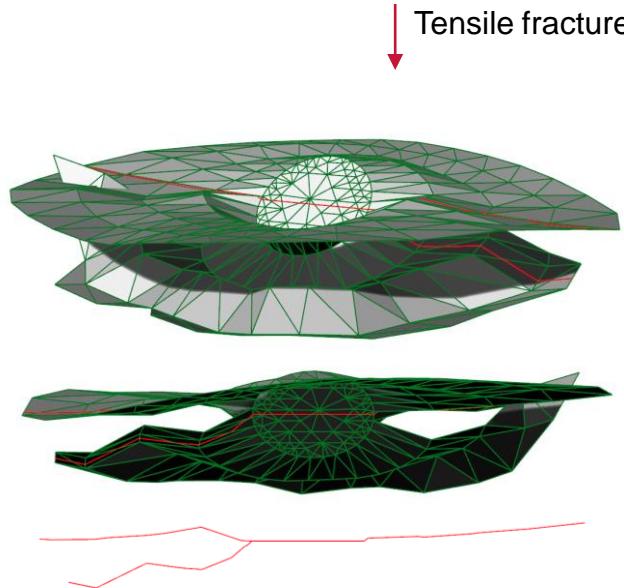
This is part of my strategy:  
Find true validation cases beyond the rock mechanics literature

# Overview of my research



# Fracture growth in soft sand

- Extending the simulator to model fracturing in soft sands
- Using a multi-scale approach involving grain scale modelling (using OpenFoam and CFDEM Liggghts)

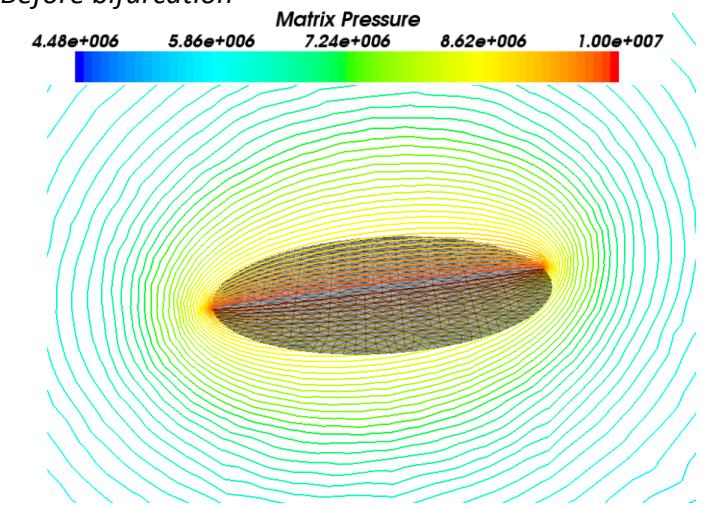


Hydraulic fracture

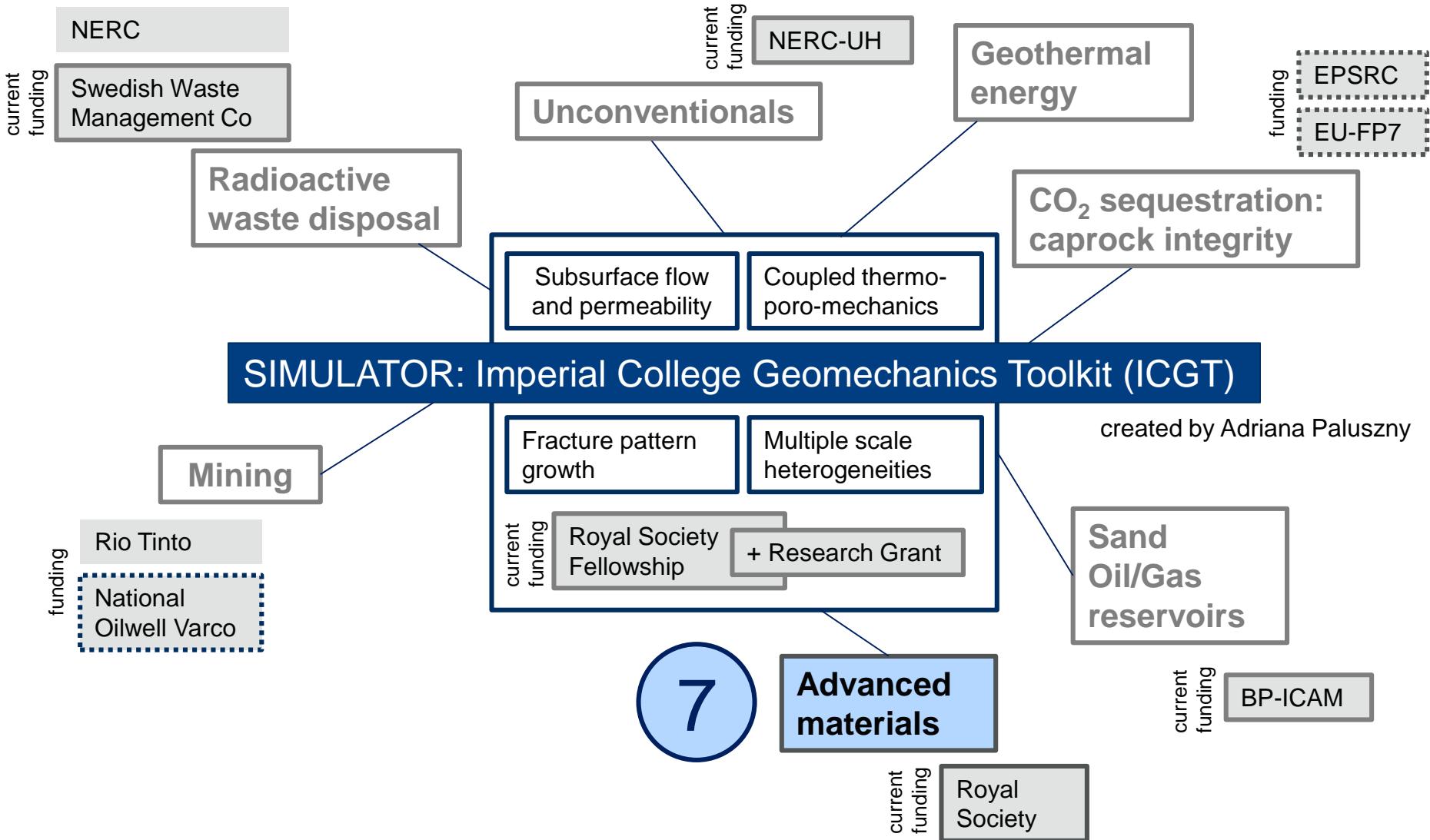
Before bifurcation



After bifurcation

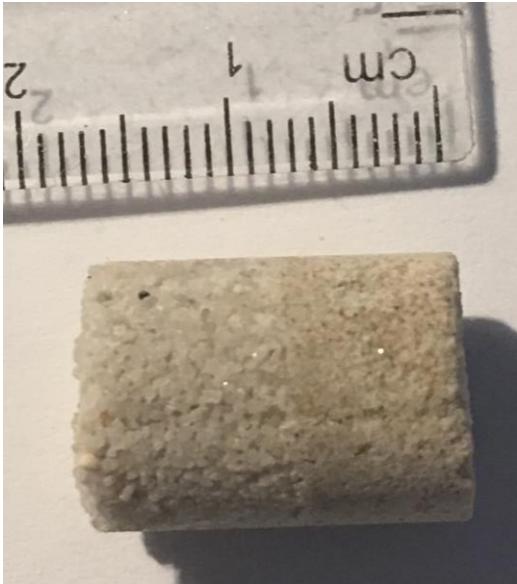


# Overview of my research



# Effect of heterogeneities on growth

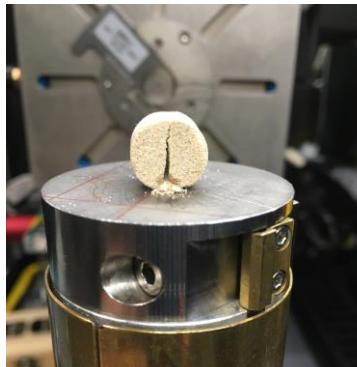
Bio-cemented  
heterogeneous synthetic  
sandstones created at  
Cambridge University



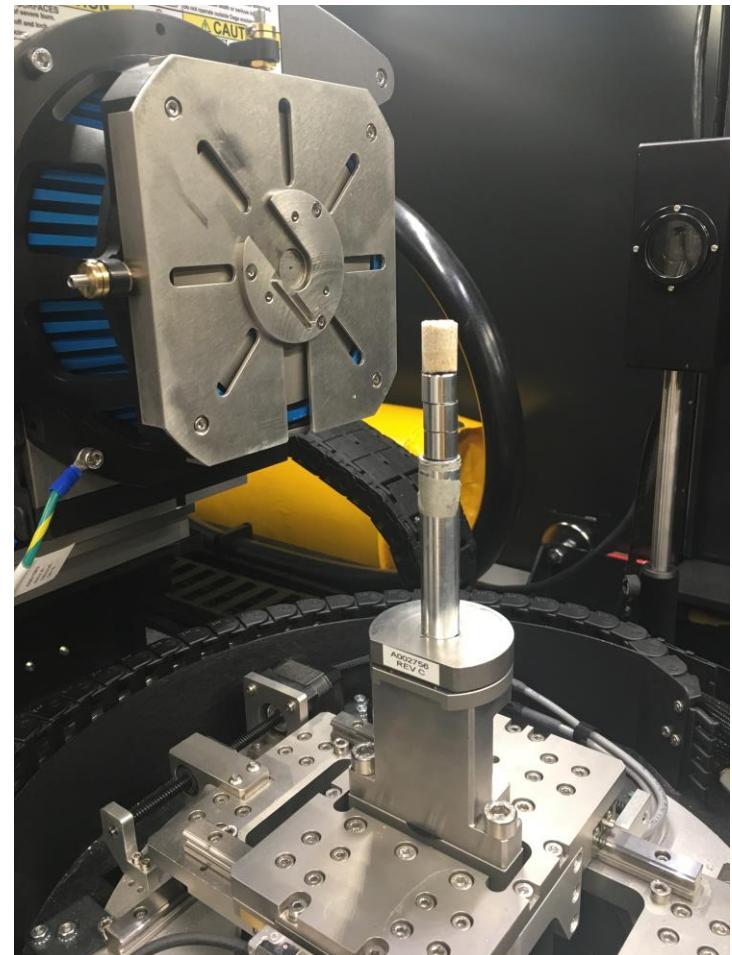
Deformed *in situ*



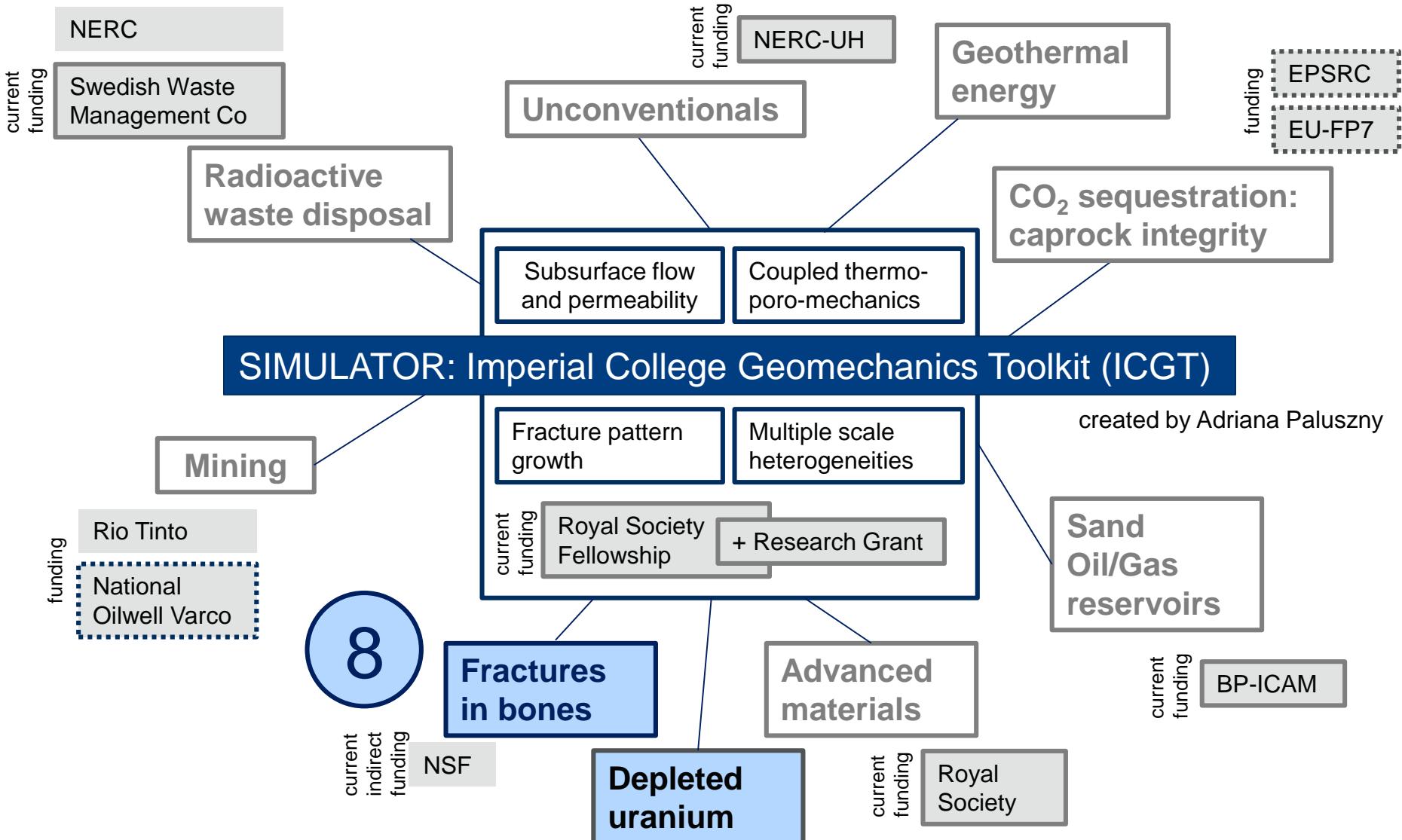
Fractured *in situ*



microCT acquisition for Digital Volume Correlation:  
New validation for stress intensity factors

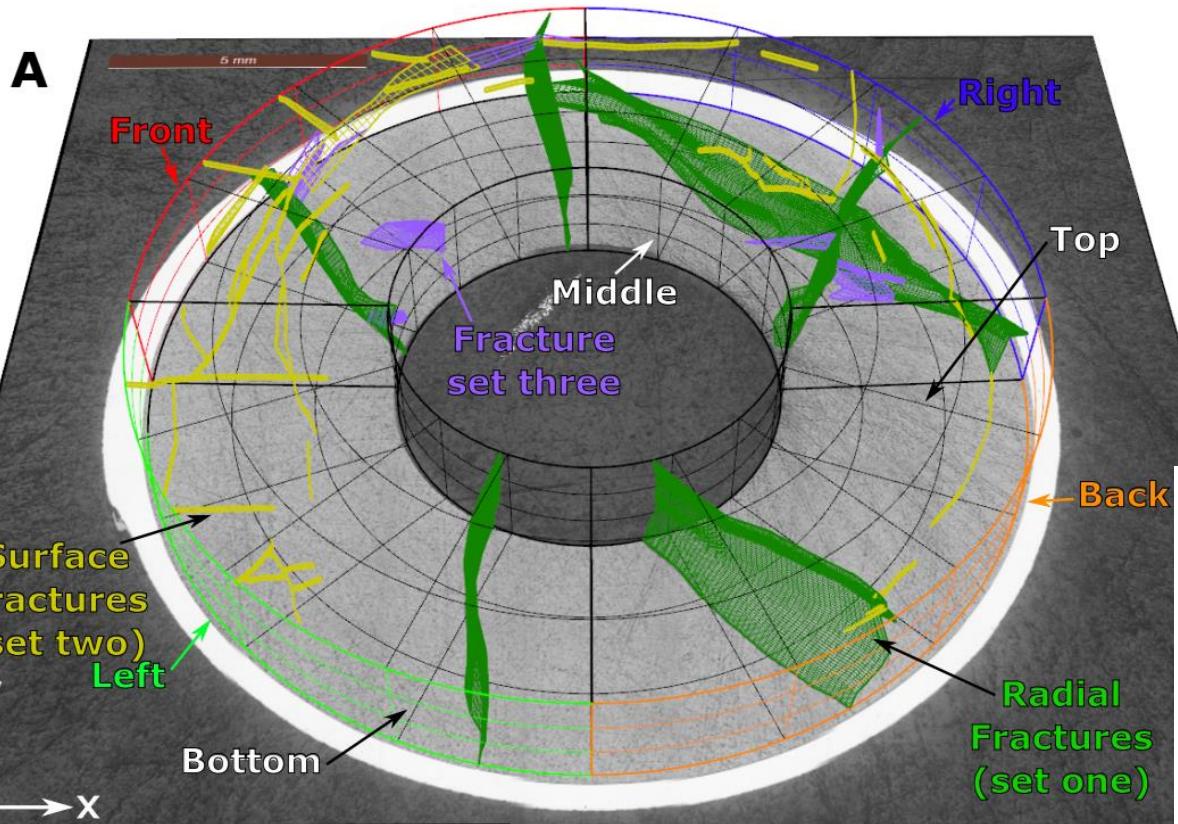


# Overview of my research



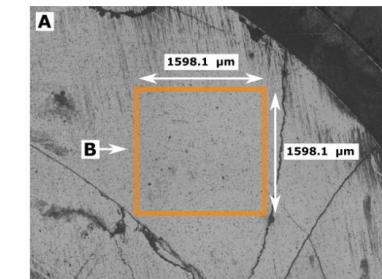
# Permeability of depleted Uranium fuel pins

Reconstructed fracture network from microscopic images of sequentially grinded material

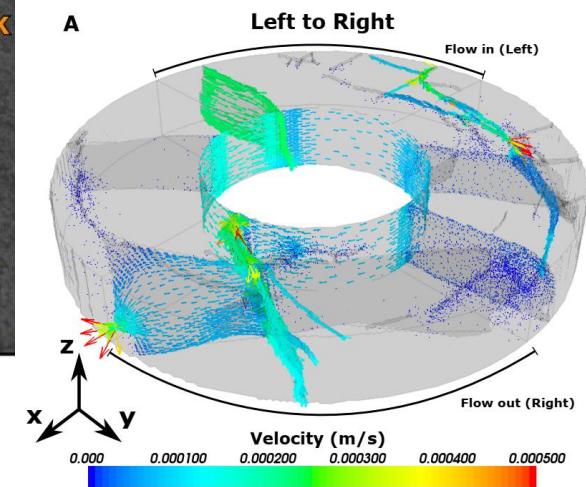


Good match obtained with gas permeability measurements published after submission of this article

Approximated matrix permeability



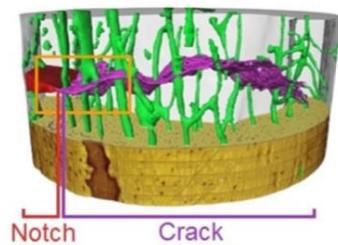
Quantified effective permeability



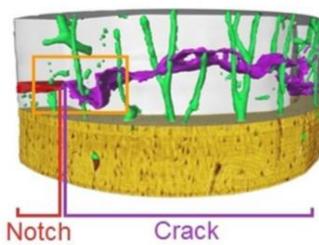
# How tough is brittle bone?

Evaluated the effect of different vascular heterogeneities on crack growth in mouse bones

*oim*+/



Wild Type



Work on bone will continue as NSF funding has been secured by collaborator for two PhD studentships which will model growth using ICGT



Original Article | Free Access

## How Tough Is Brittle Bone? Investigating Osteogenesis Imperfecta in Mouse Bone

Alessandra Carriero , Elizabeth A Zimmermann, Adriana Paluszny ... See all authors

First published: 13 January 2014 | <https://doi.org/10.1002/jbmr.2172> | Cited by: 49

ROR and SJS contributed equally to this work.

SECTIONS

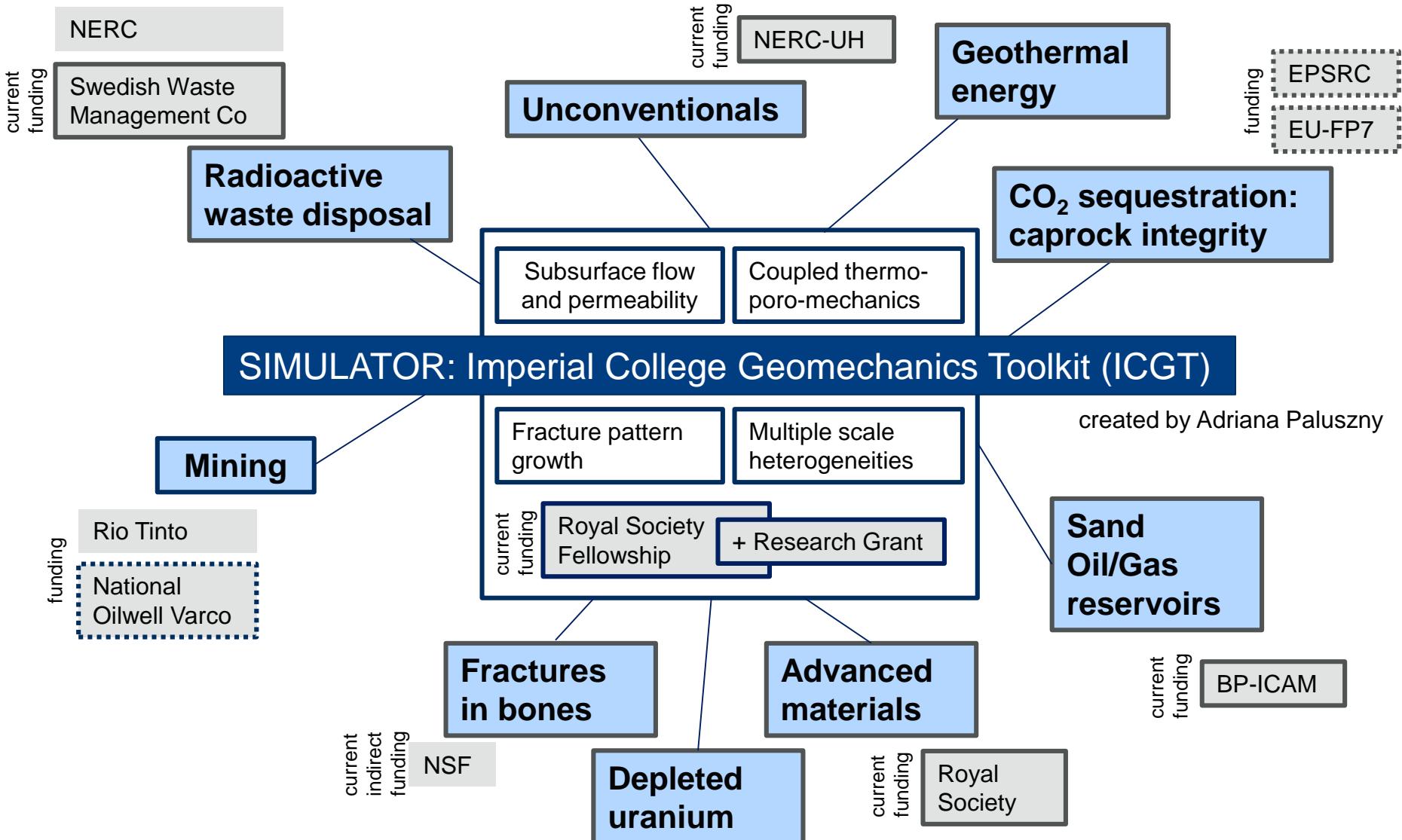
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### ABSTRACT

The multiscale hierarchical structure of bone is naturally optimized to resist fractures. In osteogenesis imperfecta, or brittle bone disease, genetic mutations affect the quality and/or quantity of collagen, dramatically increasing bone fracture risk. Here we reveal how the collagen defect results in bone fragility in a mouse model of osteogenesis imperfecta (*oim*), which has

# Overview of my research



## Funding

