# MSD 2019 Final Project

A replication and extension of Wage disparity and team productivity: evidence from Major League Baseball by Craig A. Depken II, 1999

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## Contents

Introduction	1	
Problem Description	1	
Motivation	1	
Data Source	1	
Reproduction	2	
Reproduction Code and Analysis	2	
Reproduction Notes		
Extension	4	
Extension Code and Analysis	4	
Extension Notes	14	
Postface	14	

## Introduction

## **Problem Description**

Our goal was to replicate and extend the results seen in "Wage disparity and team productivity: evidence from major league baseball" by Craig A. Depken II.

#### Motivation

Depken's paper explores whether or not wage disparity impacts a team's performance. He examines this in the context of baseball where there are ready-made measures of both performance (team win percentage) and publicly available information about wages (player salaries). The goal is to determine whether the danger-potential hypothesis (Ramaswamy and Rowthorn, 1991), which suggests that wage disparity indicates completementary skills of team-members and thus leads to better performance, or the team-cohesiveness theory (Levine 1991), which suggests that it creates disfunction and thus negatively impacts performance.

#### **Data Source**

The data is taken from Sean Lahman's baseball database, up to date as of 2019. The database is the most commonly used archive for baseball statistics. The latest version of the data can be accessed at http://www.seanlahman.com/baseball-archive/statistics.

# Reproduction

#### Reproduction Code and Analysis

Read in the data.

```
teams <- read_csv(here('data/teams.csv'))
salaries <- read_csv(here('data/salaries.csv'))</pre>
```

Clean the data by calculating the win percentage and removing an incomplete data point. The Lahman database is clearly missing some data for the 1987 Texas Rangers. For full data, see https://www.baseball-reference.com/teams/TEX/1987.shtml.

```
teams$WSWin <- as.logical(teams$WSWin == 'Y')
teams <- teams %>%
  filter(1985 <= yearID & yearID <= 2016) %>%
  mutate(winPercentage = W / (W + L) * 1000) %>%
  filter(yearID != 1987 & teamID != 'TEX')

salaries <- salaries %>%
  filter(1985 <= yearID & yearID <= 2016) %>%
  mutate(salaryMil = salary / 1000000) %>%
  filter(yearID != 1987 & teamID != 'TEX')
```

Compute total team salaries, measured in millions of dollars.

```
teams <- teams %%
inner_join(salaries) %>%
group_by(yearID, teamID, G, W, L, WSWin, winPercentage) %>%
summarize(totalSalaryMil = sum(salaryMil))
```

Compute the salary share of each player on their respective team for each year.

```
salaries <- salaries %>%
inner_join(teams) %>%
mutate(salaryShare = salaryMil / totalSalaryMil * 100) %>%
mutate(salaryShareSquared = salaryShare^2) %>%
select(yearID, teamID, playerID, salary, salaryShare, salaryShareSquared)
```

Compute the Herfindahl-Hirschman Index for each team's salary. For more information, see https://en. wikipedia.org/wiki/Herfindahl\_index. The index ranges from 0 to 10,000 where smaller values represent more equality and larger values represent more inequality.

```
teams <- teams %>%
inner_join(salaries) %>%
group_by(yearID, teamID, G, W, L, winPercentage, WSWin, totalSalaryMil) %>%
summarize(HHI = sum(salaryShareSquared))
```

Take the subset of the data from the years 1985 to 1998, inclusive, to match the Depken's analysis.

```
teams_old <- teams %>%
filter(1985 <= yearID & yearID <= 1998) %>%
mutate(normalizedYear = yearID - 1985)
```

View the summary statistics of win percentage, total team salary, and team HHI for the subset of data.

```
summary(teams_oldswinPercentage)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
```

```
##
     327.2
             456.8
                      496.9
                              500.1
                                       543.2
                                               703.7
sd(teams_old$winPercentage)
## [1] 67.34053
summary(teams_old$totalSalaryMil)
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
     4.613 14.217 23.655
                             26.220
                                     37.022
                                              72.356
sd(teams_old$totalSalaryMil)
## [1] 14.00647
summary(teams_old$HHI)
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
     427.5
             666.8
                                       876.3
                                              2158.3
##
                      754.7
                              801.5
sd(teams_old$HHI)
```

The results of our reproduction of summary statistics are nearly identical. In particular we see the same values for win percentage (slight differences only due to rounding). Our total salary replication tends to show slightly higher values, in terms of minimum, maximum, and mean. Our reason for this can be seen in the analysis section below. Once again, we see slightly different values for HHI in terms of minimum and mean. This is likely due to slight differences in our dataset and the one used in the original paper. As noted in our intial step, there are occasionally incomplete data points, or teams where not every player was accounted for, and this could be throwing off the mean slightly.

Run the fixed effects regression on data between 1985 and 1998, inclusive.

## [1] 220.2525

Our regression results match the paper's regression results in terms of coefficients being of the same order of magnitude and sign. Notably both show that wage disparity negatively impacts team performance. The difference is coefficients is that our regression claims that every \$1M spent improves win percentage by almost 0.2% vs. the paper claims on 0.17%. In addition, if a team's salary and wage inequality stays constant, for every year later in time they will lose 0.4% win percentage compared to 0.26% in the original paper. It is encouraging that the HHI indices coefficients are quite similar with ours having a -0.046 coefficent and the original paper having one of -0.064.

Run the random effects regression on data between 1985 and 1998, inclusive.

```
## HHI -0.0469241 0.01853488 -2.531665 1.180894e-02
## normalizedYear -4.7782865 1.57044613 -3.042630 2.530509e-03
```

We see similar results when replicated the random effects model, which doesn't have team specifici intercepts. It is notable that the relative changes in coefficients between our fixexd and random effects regressions are very similar to that of the original paper. Namely, our coefficients for salary and year increase in magnitude with HHI staying almost identical. One thing that was odd was that both our intercept and the original intercept had win percentage as greater than 50%.

#### Reproduction Notes

We faced a couple of challenges when considering the context of the data.

First, the original paper did not describe how time fixed effects are accounted for. For example, one may choose to control for different expansion periods or different years. When experimenting with different regression formulas, we found that controlling for different years yielded results most similar to the original paper.

Additionally, the original paper did not include a discussion on how real world practices may affect the data. For example, there is no discussion on how baseball's 25 man roster period or 40 man roster period is handled. Moreover, there is no discussion on how to handle salaries of players that are designated to the minor leagues, cut, or traded to a different team in the middle of a season. We believe that this could have imapeted our summary statistics results. We opted to take the data from the Lahman database verbatim.

#### Extension

#### Extension Code and Analysis

Subset the data to the years 1999 to 2016, inclusive.

```
teams_new <- teams %>%
filter(1999 <= yearID & yearID <= 2016) %>%
mutate(normalizedYear = yearID - 1999)
```

Run the fixed effects regression on data between 1999 and 2016, inclusive.

```
## Estimate Std. Error t value Pr(>|t|)
## totalSalaryMil 0.49949048 0.13266465 3.765061 0.0001868427
## HHI -0.05358433 0.01442365 -3.715033 0.0002267173
## normalizedYear -2.00506563 0.73422847 -2.730847 0.0065462996
```

Run the random effects regression on data between 1999 and 2016, inclusive.

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 503.61973192 15.73186679 32.012713 7.433408e-125
## totalSalaryMil 0.70690261 0.08558449 8.259705 1.226558e-15
```

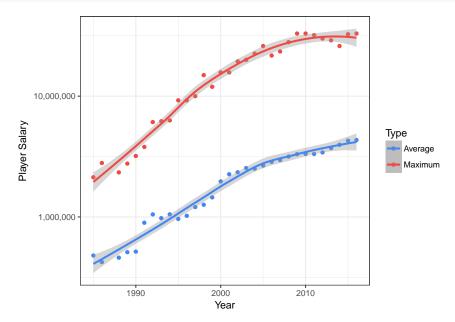
```
## HHI -0.04403327 0.01403935 -3.136419 1.807431e-03
## normalizedYear -2.75511624 0.63636357 -4.329469 1.794894e-05
```

For both models run on the new years, the coefficients match the earlier years in terms of sign. The HHI coefficient is the same in magnitude, but both of the coefficients for salary and time decrease. This makes sense, as the y-values the regression is fitting to are remaining between 40%-70% for a win percentage but total salaries of teams are increasing over time, as is the year. As a result, a million dollar increase in total salary has a comparatively smaller effect on winning than in previous years.

Plot the relationship between annual player salary and time.

```
salary_vs_time <- salaries %>%
group_by(yearID) %>%
summarize(avg = mean(salary), max = max(salary))

ggplot(data = salary_vs_time) +
    geom_point(aes(x = yearID, y = avg, color = 'Average')) +
    geom_smooth(aes(x = yearID, y = avg, color = 'Average')) +
    geom_point(aes(x = yearID, y = max, color = 'Maximum')) +
    geom_smooth(aes(x = yearID, y = max, color = 'Maximum')) +
    scale_color_manual(values = c('#4286f4', '#f44741')) +
    scale_y_log10(labels = comma) +
    labs(color = 'Type') +
    xlab('Year') +
    ylab('Player Salary')
```



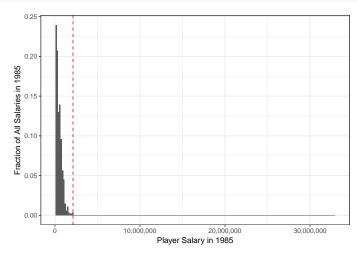
The plot suggests that both the average annual player salary and maximum annual player salary have increased over time. Note that the y-axis is displayed on a log scale. Therefore, the maximum annual player salary is growing at a much faster rate than the average annual player salary.

Plot the distributions of annual player salaries from three different years. First is 1985, the start year determined by the original paper. Second is 1998, the year of the last expansion of Major League Baseball in which the 29th and 30th teams were established. Third is 2016, the most recent year for which salary data is available. The red dashed lines denote the maximum annual player salary of each specific year.

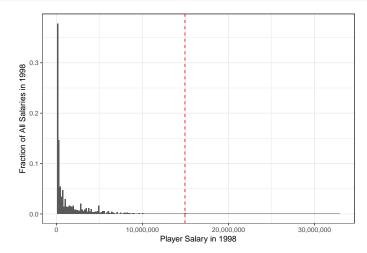
```
salaries_1985 <- filter(salaries, yearID == 1985)
salaries_1998 <- filter(salaries, yearID == 1998)</pre>
```

```
salaries_2016 <- filter(salaries, yearID == 2016)

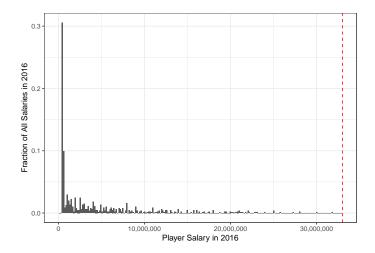
ggplot(data = salaries_1985) +
   geom_histogram(aes(x = salary, y = (..count..) / sum(..count..)), binwidth = 150000) +
   geom_vline(xintercept = max(salaries_1985$salary), color = 'red', linetype = 'dashed') +
   scale_x_continuous(limits = c(0, max(salaries$salary)), labels = comma) + xlab('Player Salary in 198
   ylab('Fraction of All Salaries in 1985')</pre>
```



```
ggplot(data = salaries_1998) +
  geom_histogram(aes(x = salary, y = (..count..) / sum(..count..)), binwidth = 150000) +
  geom_vline(xintercept = max(salaries_1998$salary), color = 'red', linetype = 'dashed') +
  xlim(0, max(salaries$salary)) +
  scale_x_continuous(limits = c(0, max(salaries$salary)), labels = comma) +
  xlab('Player Salary in 1998') +
  ylab('Fraction of All Salaries in 1998')
```



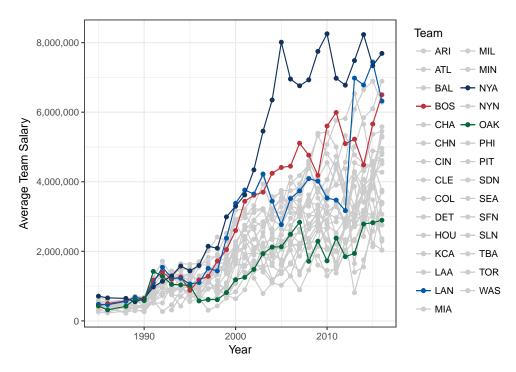
```
ggplot(data = salaries_2016) +
  geom_histogram(aes(x = salary, y = (..count..) / sum(..count..)), binwidth = 150000) +
  geom_vline(xintercept = max(salaries_2016$salary), color = 'red', linetype = 'dashed') +
  scale_x_continuous(limits = c(0, max(salaries$salary)), labels = comma) +
  xlab('Player Salary in 2016') +
  ylab('Fraction of All Salaries in 2016')
```



The plots suggest that we see longer and longer tails as bigger and bigger contracts are awarded over time. In 1998, we see that most annual player salaries are clumped at lower values. In 2016, we see that many annual player salaries are near the league minimum \$507,500 and few annual player salaries are above \$10,000,000.

Plot the relationship between average annual team salary and time. A few key teams are highlighted.

```
current_teamIDs <- c('ARI', 'ATL', 'BAL', 'BOS', 'CHA', 'CHN', 'CIN', 'CLE', 'COL', 'DET',</pre>
                     'HOU', 'KCA', 'LAA', 'LAN', 'MIA', 'MIL', 'MIN', 'NYA', 'NYN', 'OAK',
                     'PHI', 'PIT', 'SDN', 'SEA', 'SFN', 'SLN', 'TBA', 'TEX', 'TOR', 'WAS')
team colors <- c('#cccccc', '#cccccc', '#cccccc', '#BD3039', '#cccccc',
                 '#cccccc', '#cccccc', '#cccccc', '#cccccc',
                 '#cccccc', '#cccccc', '#cccccc', '#0157a8', '#cccccc',
                 '#ccccc', '#cccccc', '#11325b', '#cccccc', '#04683b',
                 '#cccccc', '#cccccc', '#cccccc', '#cccccc',
                 '#cccccc', '#cccccc', '#cccccc', '#cccccc')
colored teamIDs <- c('BOS', 'LAN', 'NYA', 'OAK')</pre>
team_salary_vs_time <- salaries %>%
  filter(teamID %in% current_teamIDs) %>%
  group_by(yearID, teamID) %>%
  summarize(avg = mean(salary)) %>%
  mutate(flag = teamID %in% colored_teamIDs)
underlay_data <- filter(team_salary_vs_time, !flag)</pre>
overlay_data <- filter(team_salary_vs_time, flag)</pre>
ggplot() +
  geom_point(data = underlay_data, aes(x = yearID, y = avg, color = teamID)) +
  geom_line(data = underlay_data, aes(x = yearID, y = avg, color = teamID)) +
  geom_point(data = overlay_data, aes(x = yearID, y = avg, color = teamID)) +
  geom line(data = overlay data, aes(x = yearID, y = avg, color = teamID)) +
  scale_y_continuous(labels = comma) +
  scale color manual(values = team colors) +
  labs(color = 'Team') +
  xlab('Year') +
 ylab('Average Team Salary')
```

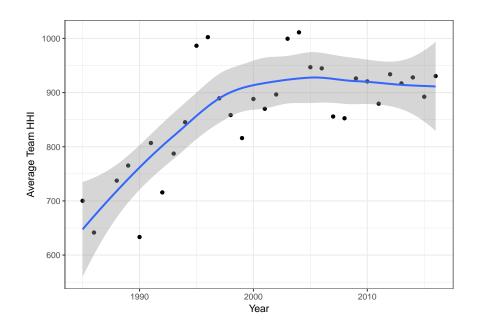


The plot suggests, as is expected, that average annual team salary has increased with time for all teams. Such an increase in expenditure can be attributed to both general inflation and the rise of sports entertainment business. The New York Yankees, the most successful franchise by number of championships, have spent a lot throughout their history. Contrast this with the Oakland Athletics, a franchise who has historically traded for players based on value, who have spent relatively little throughout their history.

Plot the relationship between average team HHI and time.

```
hhi_vs_time <- teams %>%
  group_by(yearID) %>%
  summarize(avg = mean(HHI))

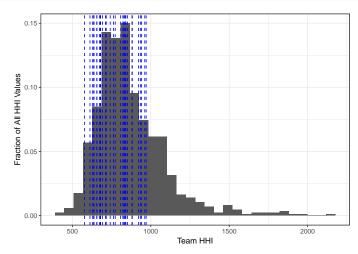
ggplot(data = hhi_vs_time) +
  geom_point(aes(x = yearID, y = avg)) +
  geom_smooth(aes(x = yearID, y = avg)) +
  xlab('Year') +
  ylab('Average Team HHI')
```



The plot suggests that average team HHI has experienced two trends through the lifetime of the data. From 1985 to 1999, we see an increase in intrateam wage disparity. From 2000 to 2016, we see that intrateam wage disparity remains relatively unchanged. This flattening of the curve may seem counterintuitive when considering that maximum annual player salaries have increased at a growing rate over time. We hypothesize that this phenomenon is due to the drastic increases in league minimum salary in the latter period. From 1985 to 1999, the league minimum rose from \$60,000 to \$109,000, or ~81%. From 2000 to 2016, the league minimum rose from \$200,000 to \$507,500, or ~153%. League minimum salary data is taken from https://www.baseball-reference.com/bullpen/Minimum\_salary.

Plot the distribution of team HHI using all teams from 1985 to 2016. The dashed vertical lines represent HHI values for teams that won the World Series.

```
ggplot(data = teams) +
  geom_histogram(aes(x = HHI, y = (..count..) / sum(..count..))) +
  geom_vline(data = filter(teams, WSWin), aes(xintercept = HHI), color = 'blue', linetype = 'dashed') +
  xlab('Team HHI') +
  ylab('Fraction of All HHI Values')
```

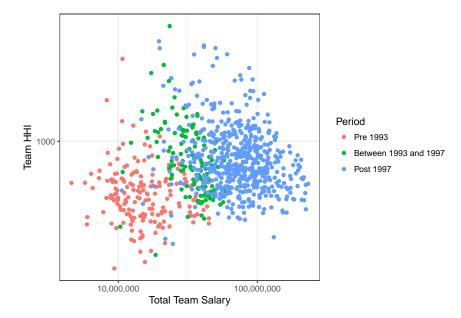


The plot suggests that too much intrateam wage disaprity can negatively affect a team's chances of winning the World Series. Namely, all teams that won the World Series between 1985 and 2016 had an intrateam HHI

of less than 1,000. For reference, an HHI of less than 1500 is considered to reflect a competitive marketplace, an HHI of 1,500 to 2,500 is considered to reflect a moderately concentrated marketplace, and an HHI of 2,500 or greater is considered to reflect a highly concentrated marketplace. We hypothesize that this finding is relevant to baseball itself and may not hold when considering other sports. Baseball is a game in which every player must take turns batting in a specified order, unlike basketball in which a single player can control the ball every possession. Hence, the affect of a star player on the outcome of a game is smaller in baseball relative to other sports. In other words, depth of a roster is far more important in baseball. Signing a star player to a huge contract may hurt a team's ability to offer decent contracts to other important role players, which may ultimately hurt a team's performance.

Plot the relationship between team HHI and total team salary. The data is split by time period based on the 1993 expansion and the 1998 expansion.

```
year_to_period <- function(year) {</pre>
  if (year <= 1992)
    return('Pre 1993')
  else if (1993 <= year & year <= 1997)
    return('Between 1993 and 1997')
  else
    return('Post 1997')
}
hhi_vs_total_salary <- mutate(teams, period = year_to_period(yearID))</pre>
hhi_vs_total_salary$period <- factor(hhi_vs_total_salary$period,
                                      levels = c('Pre 1993', 'Between 1993 and 1997', 'Post 1997'))
ggplot(data = hhi_vs_total_salary) +
  geom_point(aes(x = totalSalaryMil * 1000000, y = HHI, color = period)) +
  scale_x_log10(labels = comma) +
  scale_y_log10() +
  labs(color = 'Period') +
  xlab('Total Team Salary') +
  ylab('Team HHI')
```



The plot suggests some form of clustering between the three time periods. Since total team salary can be used as a proxy for time, we see that the average team HHI exhibits a similar growing and then flattening

trend seen in a previous plot.

Compute the Gini coefficient for each team's salary. For more information, see https://en.wikipedia.org/wiki/Gini\_coefficient. The index ranges from 0 to 1 where smaller values represent more equality and larger values represent more inequality.

```
gini <- salaries %>%
  group_by(yearID, teamID) %>%
  summarize(gini = Gini(salary))
teams <- inner_join(teams, gini)</pre>
```

Compute the Atkinson coefficient for each team's salary. For more information, see https://en.wikipedia.org/wiki/Atkinson\_index. The index ranges from 0 to 1 where smaller values represent more equality and larger values represent more inequality.

```
atkinson <- salaries %>%
  group_by(yearID, teamID) %>%
  summarize(atk = Atkinson(salary))
teams <- inner_join(teams, atkinson)</pre>
```

Subset the data after the Gini coefficient and Atkinson coefficient have been computed.

```
teams_old <- teams %>%
  filter(1985 <= yearID & yearID <= 1998) %>%
  mutate(normalizedYear = yearID - 1985)

teams_new <- teams %>%
  filter(1999 <= yearID & yearID <= 2016) %>%
  mutate(normalizedYear = yearID - 1999)
```

Run the fixed effects regression using the Gini coefficient on data between 1985 and 1998, inclusive.

```
## Estimate Std. Error t value Pr(>|t|)
## totalSalaryMil 2.312489 0.4521101 5.114879 5.559085e-07
## gini -129.827687 58.3962938 -2.223218 2.693371e-02
## normalizedYear -3.793613 1.8442237 -2.057025 4.053398e-02
```

Run the random effects regression using the Gini coefficient on data between 1985 and 1998, inclusive.

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 539.115522 24.3427437 22.146868 1.404711e-67
## totalSalaryMil 2.495248 0.3775998 6.608182 1.532621e-10
## gini -133.160525 54.5170461 -2.442548 1.510025e-02
## normalizedYear -4.559438 1.6394568 -2.781066 5.724596e-03
```

Run the fixed effects regression using the Gini coefficient on data between 1999 and 2016, inclusive.

```
##
                      Estimate Std. Error
                                             t value
                                                         Pr(>|t|)
## totalSalaryMil
                     -218.5193970 58.0041403 -3.767307 1.852177e-04
## gini
## normalizedYear
                    -2.7481628  0.7167617  -3.834137  1.425403e-04
Run the random effects regression using the Gini coefficient on data between 1999 and 2016, inclusive.
gini random new <- lm(formula = winPercentage ~ totalSalaryMil + gini + normalizedYear,
                      data = teams new)
summary(gini random new)$coefficients[1:4,]
##
                      Estimate Std. Error
                                              t value
                   550.1960765 32.40207090 16.980275 9.795202e-52
## (Intercept)
## totalSalaryMil
                     -158.9308612 55.31835762 -2.873022 4.232464e-03
## gini
## normalizedYear
                    -3.2653945 0.62553010 -5.220204 2.591533e-07
With both the Gini and Atkinson coefficient used in place of the HHI index, our regressions are very similar
to that of our replications/extensions and the original work. Specifically, the signs remain the same, while
the magnitude of the coefficient for both total salary and year stay roughly the same (total salary is slightly
larger and year slightly smaller). The coefficients for the Gini index and the Atkinson index are much bigger
because the value of this ranges between 0-1 as opposed to between 0-10,000 for HHI. This result is significant
because it suggests that perhaps HHI metric used in the original paper is a solid one and consistent with
most economist's understanding of income inequality.
Run the fixed effects regression using the Atkinson coefficient on data between 1985 and 1998, inclusive.
atk_fixed_old <- lm(formula = winPercentage ~ totalSalaryMil + atk + normalizedYear +
                                               teamID + 0,
                    data = teams old)
summary(atk_fixed_old)$coefficients[1:3,]
##
                     Estimate Std. Error
                                            t value
                                                        Pr(>|t|)
                     ## totalSalaryMil
                  -179.252498 65.9775739 -2.716870 6.966615e-03
## atk
                    -3.413854 1.8123452 -1.883667 6.056128e-02
## normalizedYear
Run the random effects regression using the Atkinson coefficient on data between 1985 and 1998, inclusive.
atk_random_old <- lm(formula = winPercentage ~ totalSalaryMil + atk + normalizedYear,
                     data = teams old)
summary(atk_random_old)$coefficients[1:4,]
##
                                            t value
                                                         Pr(>|t|)
                     Estimate Std. Error
## (Intercept)
                   509.553006 11.7544621 43.349751 1.975329e-139
## totalSalaryMil
                     2.555104 0.3759984 6.795518 4.948012e-11
## atk
                  -181.545622 61.0995554 -2.971308
                                                     3.179705e-03
                    -4.188912 1.6071160 -2.606478 9.556548e-03
## normalizedYear
Run the fixed effects regression using the Atkinson coefficient on data between 1999 and 2016, inclusive.
atk_fixed_new <- lm(formula = winPercentage ~ totalSalaryMil + atk + normalizedYear +
                                               teamID + 0,
```

t value

Pr(>|t|)

data = teams\_new)

Estimate Std. Error

summary(atk fixed new)\$coefficients[1:3,]

##

## totalSalaryMil

```
## atk -267.2160401 60.5183651 -4.415454 1.242698e-05
## normalizedYear -2.8583544 0.7142924 -4.001659 7.268982e-05
```

Run the random effects regression using the Atkinson coefficient on data between 1999 and 2016, inclusive.

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 512.1999193 17.31125767 29.587678 2.179218e-113
## totalSalaryMil 0.8479434 0.08182447 10.362956 5.387417e-23
## atk -193.0102061 57.91250941 -3.332790 9.212586e-04
## normalizedYear -3.3980916 0.62691299 -5.420356 9.131764e-08
```

With both the Gini and Atkinson coefficient used in place of the HHI index, our regressions are very similar to that of our replications/extensions and the original work. This is the case when we ran regressions using either index for all four cases: 1985-1998 fixed effects, 1985-1998 random effects, 1999-2016 fixed effects, and 1999-2016 random effects. Specifically, the signs remain the same, while the magnitude of the coefficient for both total salary and year stay roughly the same (total salary coefficient is slightly larger and year coefficient slightly smaller in comparison to when using HHI). The coefficients for the Gini index and the Atkinson index are much bigger because the value of this ranges between 0-1 as opposed to between 0-10,000 for HHI. This result is important because it suggests that the HHI metric used in the original paper is a solid one and consistent with most economist's understanding of income inequality.

Run a k-fold linear regression to generate a validation error and analyze predictive performance. Here we include all teams from 1985 to 2016 as potential training data points. We used the fixed effects model.

```
num folds <- 5
num_rows <- nrow(teams)</pre>
shuffle_idx <- sample(1:num_rows, num_rows, replace = FALSE)</pre>
teams_k_fold <- teams[shuffle_idx,] %>%
  ungroup() %>%
  mutate(fold = (row_number() %% num_folds) + 1) %>%
  mutate(normalizedYear = yearID - 1985)
validate err <- c()</pre>
train_err <- c()</pre>
for (f in 1:num folds) {
  curr_train <- filter(teams_k_fold, fold != f)</pre>
  model <- lm(formula = winPercentage ~ totalSalaryMil + HHI + normalizedYear + teamID + 0,
               data = curr_train)
  train err[f] <- sqrt(mean((predict(model, curr train) - curr trainswinPercentage) ^ 2))
  curr_validate <- filter(teams_k_fold, fold == f)</pre>
  validate_err[f] <- sqrt(mean((predict(model, curr_validate) - curr_validate$winPercentage) ^ 2))</pre>
}
avg_validate_err <- mean(validate_err)</pre>
se_validate_err <- sd(validate_err) / sqrt(num_folds)</pre>
avg_train_err <- mean(train_err)</pre>
se_train_err <- sd(train_err) / sqrt(num_folds)</pre>
```

Use the linear regression trained on 1985 to 1998 data and predict on 1999 to 2016 data. We used the random effects model.

In this case we see an average error of 6.4 +/- 1.5 win% for the fixed effects and 6.6 +/- 1.5% for the random effects. While in an absolute sense these are relatively accurate, in a larger context they are less impressive. This is because the range of outcomes are reasonably between 40-70 win %, so 6.5% error represents roughly 20% of the range of possible outcomes. In a real world setting it means that the prediction could be off by almost 10 games. The fixed effects model was slightly more accurate than the random effects because it was trained on random selection of all data, as opposed to just the early years. Furthermore it has the additional parameter of team specific intercepts, as opposed to a general intercept, which likely allows for a better fitting of the data.

#### **Extension Notes**

- use this area for challenges and/or general notes, move analysis to under the relevant code block
- Coefficients of different inequality indexes are the same sign and have the same predictive impact (magnitudes are different because HHI has a wider range than the other two which are between 0 and 1), so we just picked HHI for the predictive models.
- Used fixed effects model when split data independent of time, ie teams from 1985 and 2016 are in the training set. Meanwhile used random effects model when split data based on time, ie teams from 1985-2011 were in training set and 2012-2016 were test set. The use of the random effects model for the latter was to account for the fact that teams might be dominant in early years but not so much in more recent years, ie dont want to worry about team being good in 80s/90s and bad in 2010s. Also handles the issue of teams not existing in training set but potentially in validation set (since teams come and go, move cities, rebrand, etc)
- 6.4%-6.6% error in win percentage predictions for both kinds of regressions. This isn't amazing given that the range of reasonable values is roughly 40%-70% win percentage

# Postface

The following is a list of all packages used to generate these results.

```
sessionInfo()
```

```
## R version 3.4.3 (2017-11-30)
## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS Sierra 10.12.6
##
## Matrix products: default
## BLAS: /Library/Frameworks/R.framework/Versions/3.4/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/3.4/Resources/lib/libRlapack.dylib
## locale:
```

```
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
##
## attached base packages:
## [1] stats
                graphics grDevices utils
                                              datasets base
## other attached packages:
## [1] bindrcpp_0.2
                        forcats 0.3.0
                                        stringr 1.3.0
                                                        dplyr 0.7.4
## [5] purrr_0.2.4
                        readr 1.1.1
                                        tidyr_0.8.0
                                                        tibble_1.4.2
## [9] ggplot2_2.2.1
                       tidyverse_1.2.1 scales_0.5.0
                                                        ineq_0.2-13
## [13] here_0.1
##
## loaded via a namespace (and not attached):
## [1] reshape2_1.4.3
                        haven_1.1.1
                                          lattice_0.20-35 colorspace_1.3-2
## [5] htmltools_0.3.6 yaml_2.1.17
                                          rlang_0.2.0
                                                           pillar_1.2.1
## [9] foreign_0.8-69
                        glue_1.2.0
                                          modelr_0.1.1
                                                           readxl_1.0.0
## [13] bindr_0.1
                         plyr_1.8.4
                                          munsell_0.4.3
                                                           gtable_0.2.0
## [17] cellranger_1.1.0 rvest_0.3.2
                                          psych_1.7.8
                                                           evaluate_0.10.1
## [21] labeling 0.3
                        knitr 1.20
                                          parallel 3.4.3
                                                           broom 0.4.3
## [25] methods_3.4.3
                         Rcpp_0.12.15
                                          backports_1.1.2
                                                           jsonlite_1.5
                                          digest 0.6.15
## [29] mnormt_1.5-5
                         hms 0.4.1
                                                           stringi_1.1.6
                        rprojroot_1.3-2
## [33] grid_3.4.3
                                         cli_1.0.0
                                                           tools_3.4.3
## [37] magrittr 1.5
                         lazyeval_0.2.1
                                          crayon_1.3.4
                                                           pkgconfig_2.0.1
## [41] xml2_1.2.0
                        lubridate_1.7.3
                                         assertthat_0.2.0 rmarkdown_1.9
## [45] httr 1.3.1
                        rstudioapi_0.7
                                          R6 2.2.2
                                                          nlme 3.1-131
## [49] compiler_3.4.3
```