

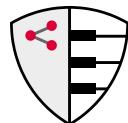
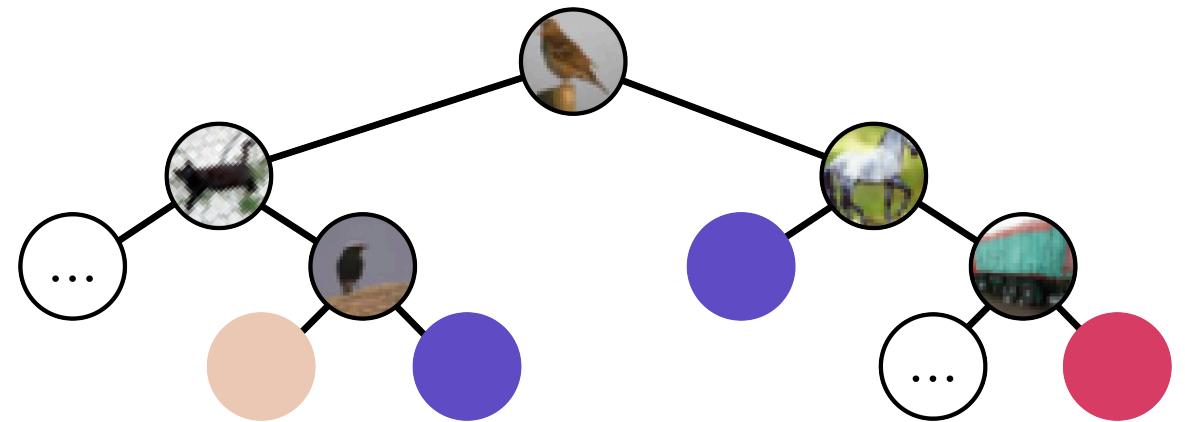
Data-Agnostic Pivotal Instances Selection for Decision-Making Models

PivotTree: Case-based Trees for
relational and non-relational data

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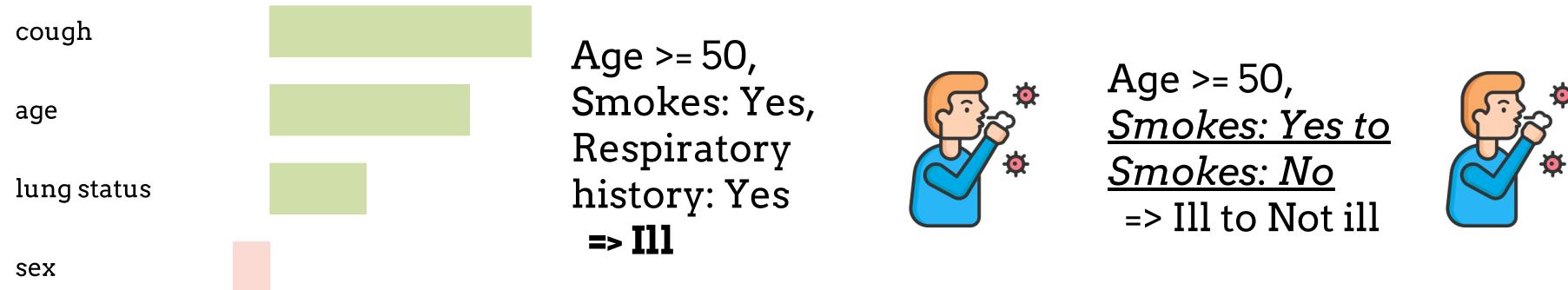
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Italiadomani
PIANO NAZIONALE DI RICERCA E RESILIENZA

Explainability and its many forms

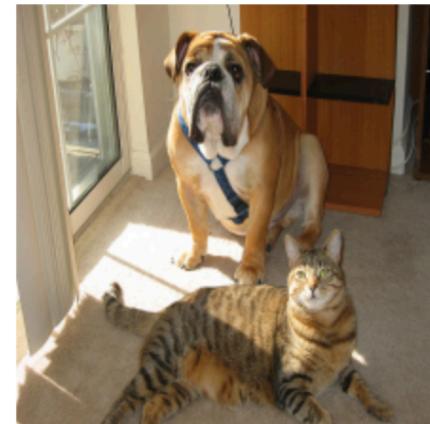
- **Feature importance.** Defines impact: what is *important?* (Local)
- **Decision rules.** Describes: what *decides?* (Semi-global)
- **Counterfactuals.** Contrasts: what to *change?* (Local)



Non-relational data: breaking the mold

Non-relational data has an inherent difficulty in tackling the above tasks, often due to

- Complex relations among features
- Violated assumptions
- Sparsity



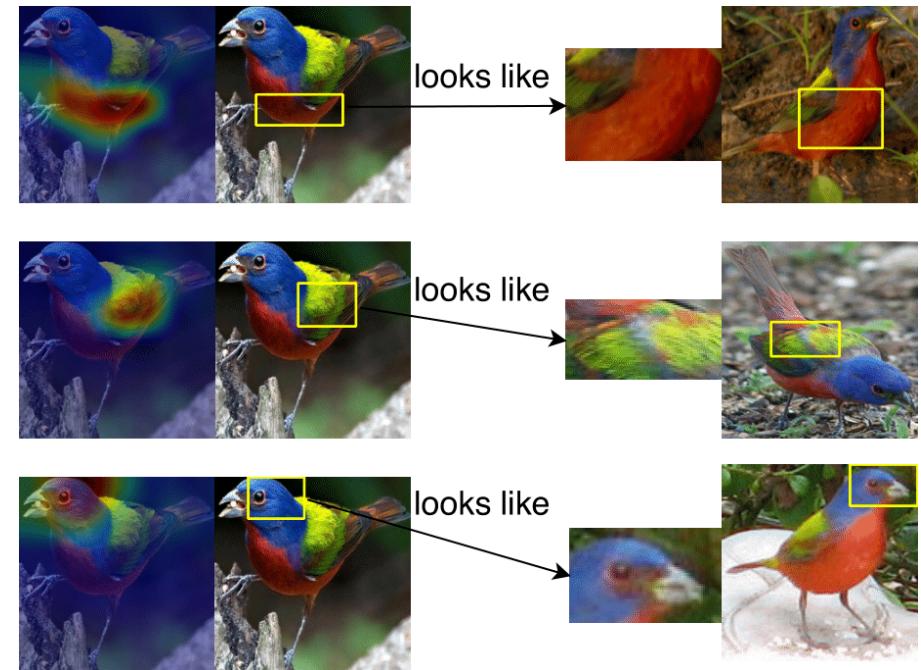
A saliency map requires a perturbation algorithm how to *jointly* perturb pixels, often under the assumption of their independence, thus creating a large amount of possibly out-of-distribution synthetic instances.

Case-based explanations

A.k.a. prototypes, pivots. Define a set of instances, which are explanations **on their own**, and can also be explained

- Importances
- Counterfactuals

By design they tackle sparsity and inter-instance relationships!



The bird in the picture is classified as *Clay-colored sparrow* on the basis of its similarity with some prototypes.

The case-based landscape

- By design
- Data-agnostic
- Factual explanations
- Local or global explanations

- No counterfactuals
- Local *and* global explanation
- No inter-case relationship

Prototype selection for interpretable classification. J. Bien et al.

Deep learning for interpretable image recognition. C. Chen et al.

Interpreting CNNs via Decision Trees. Q. Zhang et al.

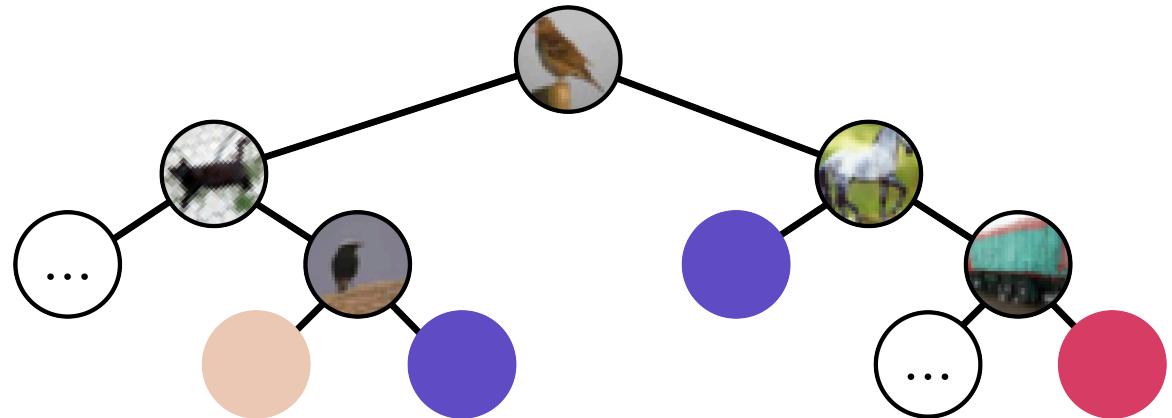
Proximity Forest: an effective and scalable distance-based classifier for time series. Lucas et al.

Prototype selection for interpretable classification. Bien & Tibshirani.

Pivot Tree

Our proposal, **Pivot Tree** is a case-based model for explainable classification

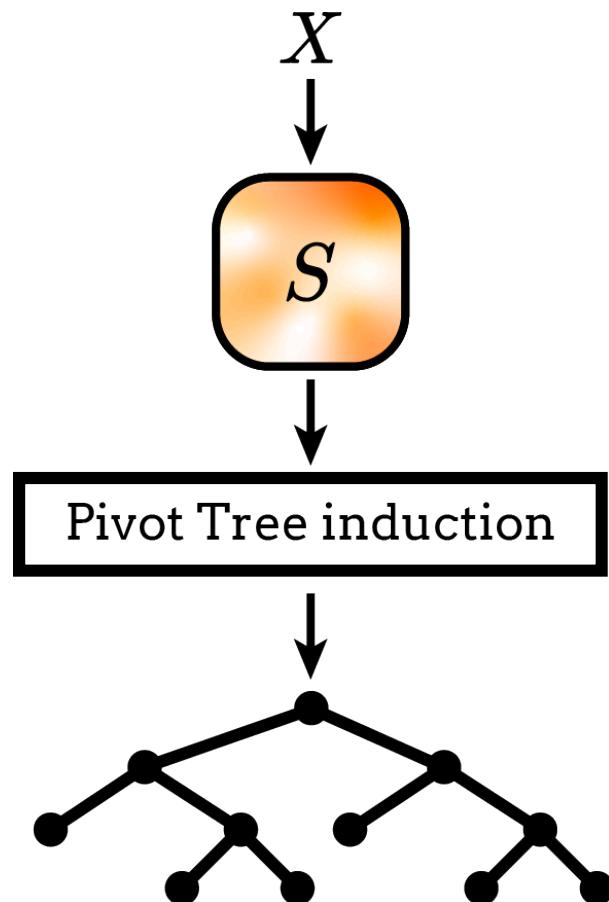
- Data-agnostic
- Factual *and* counterfactual explanations
- Local *and* global explanations
- Hierarchical case structure



A Pivot Tree: instances laid on a tree structure route predictions. Similarity to instances determines routing, and leaves are also associated with a classification label.

Learning a Pivot Tree (PTC)

Pivot Tree Classifier (PTC)



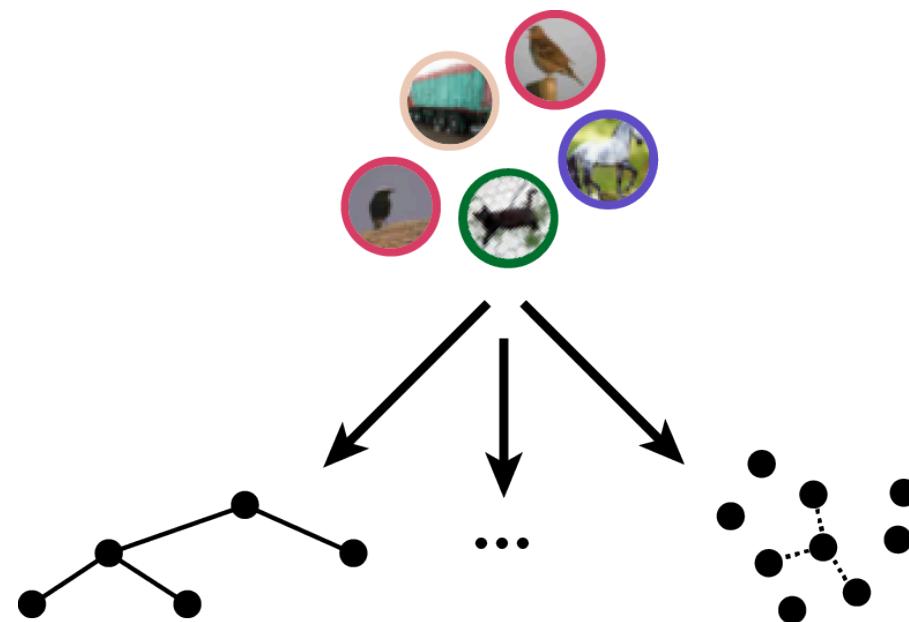
1. Compute a similarity matrix S , possibly embedding data
2. Induce a Decision Tree on S , filtering similarities to
 - **discriminative pivots:** maximizing entropy
 - **descriptive pivots:** maximizing class centrality

Learning a Pivot Selector (PTS)

Pivots in the nodes constitute a dataset themselves!

1. Extract pivots from nodes
2. Train an interpretable model
on top of Pivot Tree

Pivot Tree Selector (PTS)



A qualitative result

Cifar 10



An instance (left), and pivots extracted by Pivot Tree. The cat has **high similarity** to the first two, and **low** to the latter two.

Experiments

Explainability

- Fidelity
- Complexity
- Stability

Competitors

- ε -ball
- k -NN

Datasets

- 11 tabular
- 5 time series
- 3 image + 1 real world
use case of oral
cancer detection
- 5 text

How faithful is Pivot Tree?

	<i>mean</i> ↑	<i>std</i> ↓	<i>rank</i> ↓
PTS + DT	.62	.22	3.1
K-medoids	.61	.22	3.6
ε -ball	.61	.23	3.7
Pivot Tree	.58	.27	3.9
K-means	.62	.22	4.0
Random per class	.60	.22	4.6
Random	.60	.22	5.0

On *f1* score...

- Pivot Tree selector is the best performing model
- Pivot Tree works **better** as a pivot **selector than** a standalone **classifier**
- Models built directly on data lag behind: good data matters

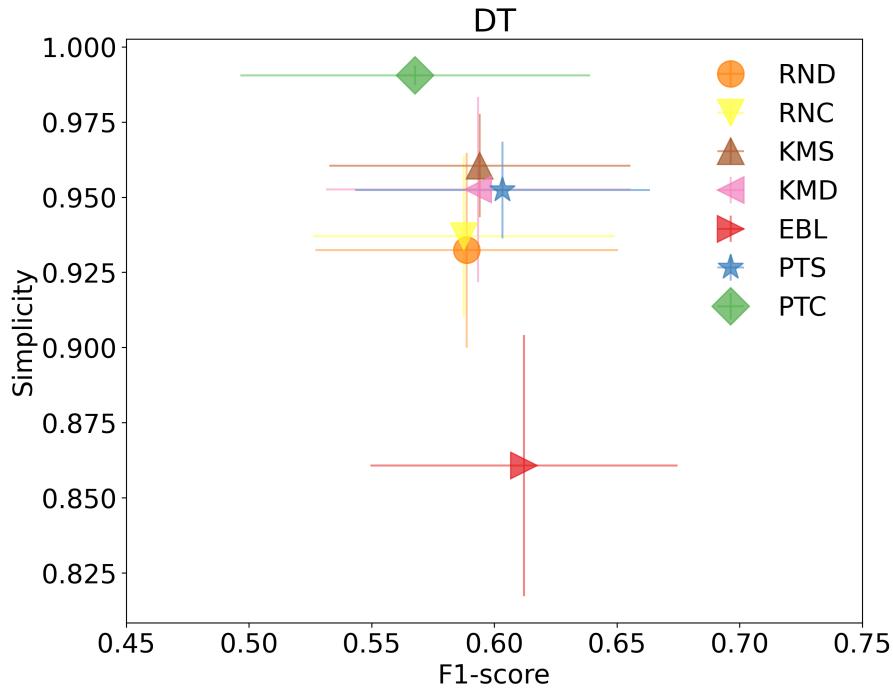
A real-world study: oral cancer detection

A real-world case study on an oral cancer detection dataset.

- 535 images
- 3 classes

	Pivot Tree	Decision Tree	k-NN	CNN
$f1$.834	.833	.811	.854
<i>complexity</i>	9	47	5	

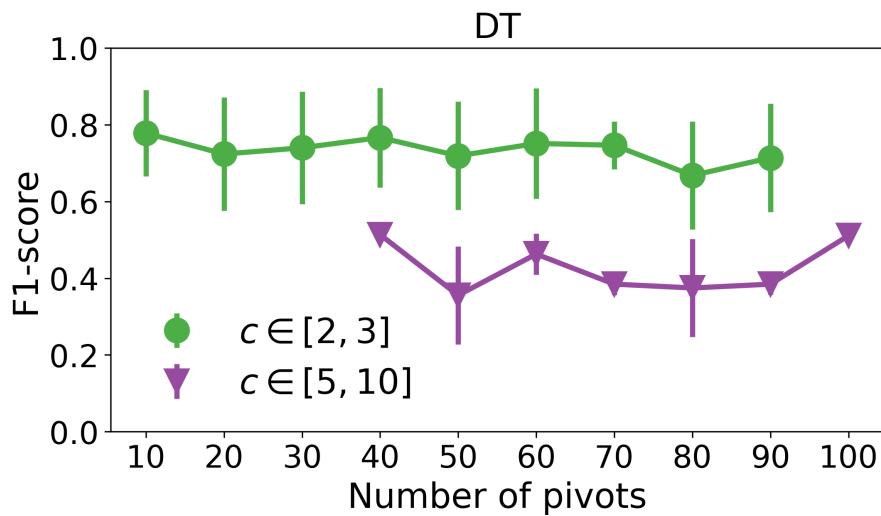
How complex is Pivot Tree?



- When not regularized, Pivot Tree slightly worse than competitors
- More complex models (bottom) are less impacted from regularization

Scatter plot of f_1 score and simplicity of Pivot Tree and its competitors, regularized to use a maximum of 20 pivots.

How stable is Pivot Tree?



Scatter plot of $f1$ score of Pivot Tree as the maximum number of pivots increases. C indicates the number of classes.

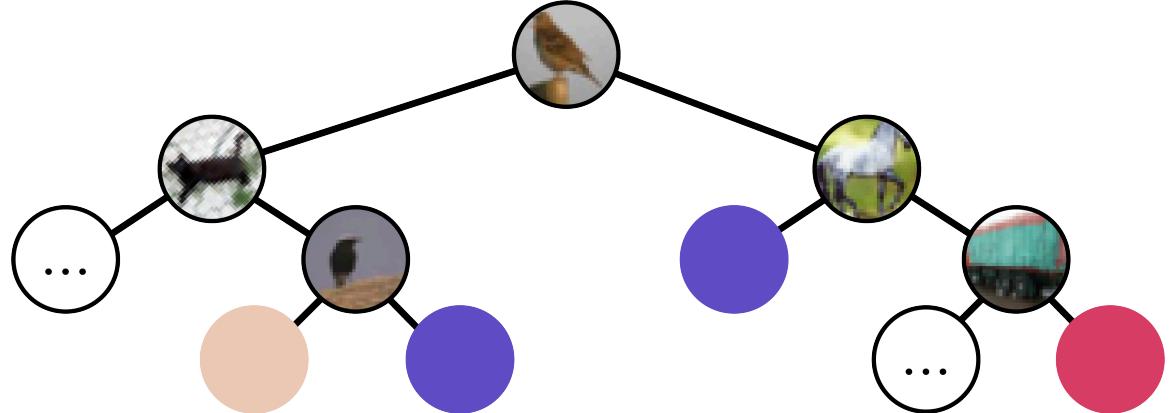
Low variance but decreasing trend as regularization decreases: Occam's razor!

Pivot Tree

An explainable case-based decision tree,
providing factual and counterfactual case-
based explanations.

Future work:

- Proximity splits: to which pivots are instances more similar?
- More powerful downstream models



github.com/msetzu/pivottree

**See you at the
poster session!**