





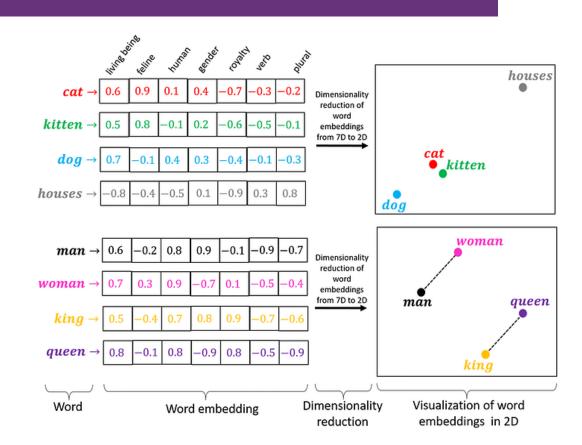
307307 Part 2 – Introduction to Large Language Models





Preface

- In the previous section, we used Bow and TDIDF to convert documents and words into numerical representations.
- These representations were simple, they had no semantics for words, just on/off switches for existing and non-existing words in a document.
- In this part of the course, we want to convert words into meaningful list of numbers.
- These numbers are called <u>Word Embeddings</u>.
- We will use Neural Networks to create these Word Embeddings.









Introduction to Neural Networks

The Perceptron





Outcomes

- Fundamentals of neural networks
- Evolution from single perceptrons to MLPs
- Detailed MLP architecture (input, hidden, and output layers)
- Mathematical representations
- Various activation functions (Sigmoid, ReLU, etc.)
- Backpropagation and training methodologies
- Loss functions and optimization techniques
- Architecture design considerations
- Real-world applications
- Advantages and limitations
- Modern MLP variants and implementations





History of Neural Networks

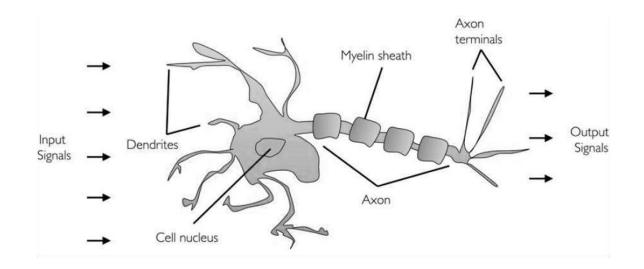
- In 1943, researchers Warren McCullock and published their first concept of simplified brain cell.
- This was called McCullock-Pitts (MCP) neuron.
- They described such a nerve cell as a simple logic gate with binary outputs.
- Multiple signals arrive at the dendrites and are then integrated into the cell body, and, if the accumulated signal exceeds a certain threshold, an output signal is generated that will be passed on by the axon.

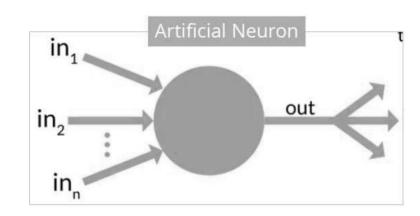


Warren Sturgis McCulloch (1898 – 1969)



Walter Harry Pitts, Jr. (1923 – 1969)



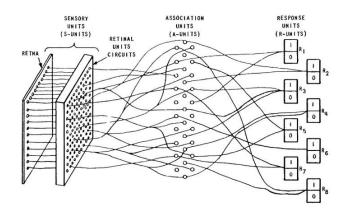




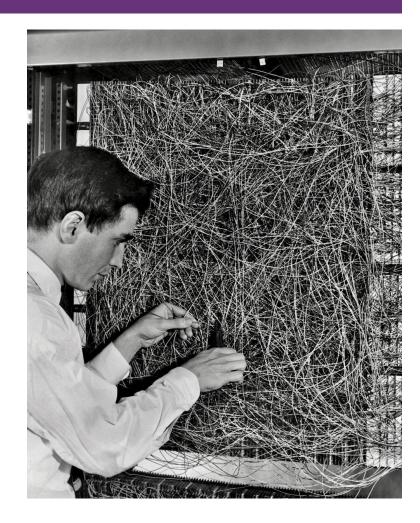


The Perceptron: Building Block of Neural Networks

- In 1953, inspired by McCullock work, Frank Rosenblatt invented the Perceptron.
- The Perceptron is the simplest form of a neural network
- Binary classifier: separates data into two categories
- Models a single neuron with multiple inputs and one output











The Perceptron

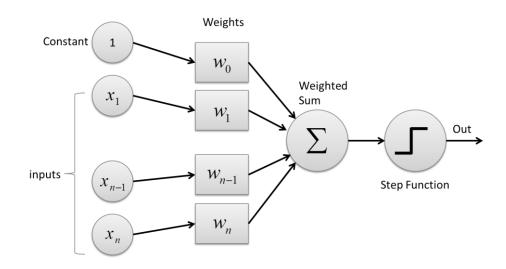
• Inputs: x₁, x₂, ..., x_n

• Weights: w₁, w₂, ..., w_n

• Bias: b

• Activation function: Step function

• Output: 1 if weighted sum > threshold, 0 otherwise





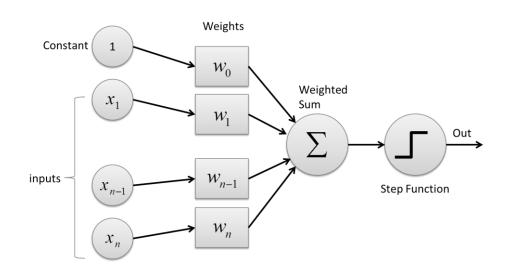


How a Perceptron Works

- 1. Multiply each input by its corresponding weight
- 2. Sum all weighted inputs
- 3. Add the bias term
- 4. Apply the activation function
- 5. Output the result

Mathematically:

- $z = w_1x_1 + w_2x_2 + ... + w_nx_n + b$
- output = activation(z)

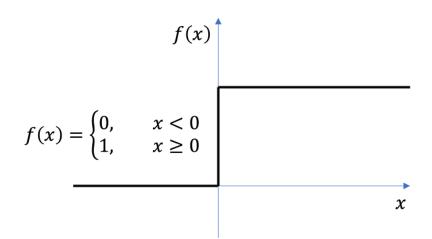






Perceptron Activation Function

- Step Function:
 - Output: 1 if $z \ge 0$, 0 if z < 0
 - Used in original perceptrons
 - Not differentiable at 0







Perceptron Learning Rule

For each training example:

- Calculate predicted output y_pred
- 2. Calculate error: error = y_true y_pred
- 3. Update weights: w_new = w_old + learning_rate * error * x
- 4. Update bias: b_new = b_old + learning_rate * error



Step-by-Step Hand Calculation for AND Gate

Let's work through the perceptron learning algorithm by hand for the AND gate:

- Training data: X = [[0,0], [0,1], [1,0], [1,1]], y = [0, 0, 0, 1]
- Learning rate (η) = 0.1
- Initial weights (randomly assigned): $w_1 = 0.3$, $w_2 = -0.1$
- Initial bias: b = 0.2

First Iteration:

Example 1: $(0,0) \rightarrow 0$

- Inputs: $x_1 = 0$, $x_2 = 0$
- Weighted sum: $z = w_1x_1 + w_2x_2 + b = 0.3(0) + (-0.1)(0) + 0.2 = 0.2$
- Activation: output = 1 (since z > 0)
- True output: y = 0
- Error: error = y output = 0 1 = -1
- Weight updates:
 - $w_1 = w_1 + \eta$ * error * $x_1 = 0.3 + 0.1$ * (-1) * 0 = 0.3
 - $w_2 = w_2 + \eta$ * error * $x_2 = -0.1 + 0.1$ * (-1) * 0 = -0.1
 - $b = b + \eta * error = 0.2 + 0.1 * (-1) = 0.1$





Step-by-Step Hand Calculation for AND Gate

Example 2: $(0,1) \rightarrow 0$

- Inputs: $x_1 = 0$, $x_2 = 1$
- Weighted sum: $z = w_1x_1 + w_2x_2 + b = 0.3(0) + (-0.1)(1) + 0.1 = 0$
- Activation: output = 1 (since $z \ge 0$)
- True output: y = 0
- Error: error = y output = 0 1 = -1
- Weight updates:
 - $w_1 = w_1 + \eta$ * error * $x_1 = 0.3 + 0.1$ * (-1) * 0 = 0.3
 - $w_2 = w_2 + \eta$ * error * $x_2 = -0.1 + 0.1$ * (-1) * 1 = -0.2
 - $b = b + \eta * error = 0.1 + 0.1 * (-1) = 0$

Example 3: $(1,0) \rightarrow 0$

- Inputs: $x_1 = 1$, $x_2 = 0$
- Weighted sum: $z = w_1x_1 + w_2x_2 + b = 0.3(1) + (-0.2)(0) + 0 = 0.3$
- Activation: output = 1 (since z > 0)
- True output: y = 0
- Error: error = y output = 0 1 = -1
- Weight updates:
 - $w_1 = w_1 + \eta * error * x_1 = 0.3 + 0.1 * (-1) * 1 = 0.2$
 - $w_2 = w_2 + \eta$ * error * $x_2 = -0.2 + 0.1$ * (-1) * 0 = -0.2
 - $b = b + \eta * error = 0 + 0.1 * (-1) = -0.1$



Step-by-Step Hand Calculation for AND Gate

Example 4: $(1,1) \rightarrow 1$

- Inputs: $x_1 = 1$, $x_2 = 1$
- Weighted sum: $z = w_1x_1 + w_2x_2 + b = 0.2(1) + (-0.2)(1) + (-0.1) = -0.1$
- Activation: output = 0 (since z < 0)
- True output: y = 1
- Error: error = y output = 1 0 = 1
- Weight updates:
 - $w_1 = w_1 + \eta$ * error * $x_1 = 0.2 + 0.1$ * 1 * 1 = 0.3
 - $w_2 = w_2 + \eta$ * error * $x_2 = -0.2 + 0.1$ * 1 * 1 = -0.1
 - $b = b + \eta * error = -0.1 + 0.1 * 1 = 0$

End of Iteration 1:

- Updated weights: $w_1 = 0.3$, $w_2 = -0.1$
- Updated bias: b = 0



Second Iteration

Example 1: $(0,0) \rightarrow 0$

- Inputs: $x_1 = 0$, $x_2 = 0$
- Weighted sum: $z = w_1x_1 + w_2x_2 + b = 0.3(0) + (-0.1)(0) + 0 = 0$
- Activation: output = 1 (since $z \ge 0$)
- True output: y = 0
- Error: error = y output = 0 1 = -1
- Weight updates:
 - $w_1 = w_1 + \eta$ * error * $x_1 = 0.3 + 0.1$ * (-1) * 0 = 0.3
 - $w_2 = w_2 + \eta * error * x_2 = -0.1 + 0.1 * (-1) * 0 = -0.1$
 - $b = b + \eta * error = 0 + 0.1 * (-1) = -0.1$

Example 2: $(0,1) \rightarrow 0$

- Inputs: $x_1 = 0$, $x_2 = 1$
- Weighted sum: $z = w_1x_1 + w_2x_2 + b = 0.3(0) + (-0.1)(1) + (-0.1) = -0.2$
- Activation: output = 0 (since z < 0)
- True output: y = 0
- Error: error = y output = 0 0 = 0
- Weight updates (no change as error = 0):
 - $w_1 = 0.3$
 - $w_2 = -0.1$
 - b = -0.1
- After several iterations, the perceptron will converge to weights that correctly classify all AND gate examples.





Python Implementation Perceptron from Scratch

```
from sklearn.linear model import Perceptron
import numpy as np
   # Training data for AND gate
X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
y = np.array([0, 0, 0, 1])
   # Initialize and train Perceptron
model = Perceptron(max iter=100, eta0=0.1, random state=42)
model.fit(X, y)
# Results
print("Weights:", model.coef )
print("Bias:", model.intercept )
print("Predictions:", model.predict(X))
Weights: [[0.2 0.2]]
Bias: [-0.2]
Predictions: [0 0 0 1]
```

The code shows a scikit-learn Perceptron implementation for the AND gate problem.

The code:

1.Imports NumPy, scikit-learn's Perceptron, and matplotlib

2. Sets up the training data for the AND gate

3.Initializes a Perceptron with 100 max iterations and a random seed of 42

4. Trains the perceptron on the AND gate data

5. Prints the learned weights, bias, and predictions

The output shows:

- Weights: [[0.2 0.2]] The perceptron learned to assign a weight of 0.2 to both inputs
- Bias: [-0.2] The bias is -0.2
- Predictions: [0 0 0 1] The perceptron correctly classified all four examples of the AND gate

With these weights and bias, the decision function is: $0.2 \times (input1) + 0.2 \times (input2) - 0.2$

For the four input combinations:

- [0,0]: $0.2\times0 + 0.2\times0 0.2 = -0.2 < 0 \rightarrow \text{output } 0$
- [0,1]: $0.2 \times 0 + 0.2 \times 1 0.2 = 0 \rightarrow \text{output } 0$
- [1,0]: $0.2 \times 1 + 0.2 \times 0 0.2 = 0 \rightarrow \text{output } 0$
- [1,1]: $0.2 \times 1 + 0.2 \times 1 0.2 = 0.2 > 0 \rightarrow \text{output } 1$

This perceptron implements the AND gate logic.

The decision boundary is the line $2x_1 + 2x_2 - 0.2 = 0$, which separates the point (1,1) from the other three points.

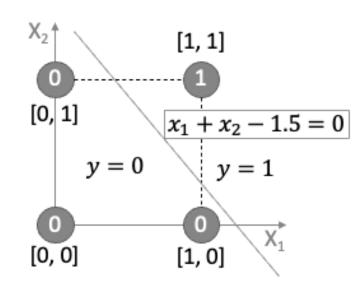




Decision Boundary

- The perceptron learns a decision boundary: $w_1x_1 + w_2x_2 + b = 0$
- Points above the line are classified as 1
- Points below the line are classified as 0
- For AND gate, only the point (1,1) should be above the line

X ₁	X ₂	У
0	0	0
0	1	0
1	0	0
1	1	1

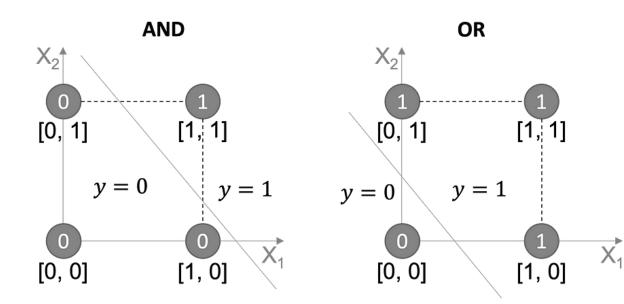


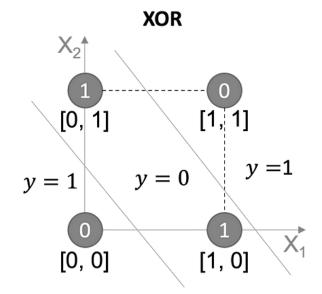




Limitations of Simple Perceptron

- Can only learn linearly separable patterns
- Cannot solve XOR problem (need multiple layers)
- No probabilistic output
- Simple update rule isn't suitable for complex problems











Introduction to Neural Networks

Multi-Layer Neural Network





The Multi-Layer Percecptron (MLP)

Limitations of the Perceptron

While useful for linearly separable problems, the single perceptron cannot solve complex problems like XOR classification, as demonstrated by Minsky and Papert in their 1969 book "Perceptrons."



The Multi-Layer Perceptron addresses the limitations of the single perceptron by introducing:

- Multiple layers of neurons
- Non-linear activation functions
- More sophisticated learning algorithms







Structure of an MLP

Definition: An MLP is a class of feedforward artificial neural network that consists of at least three layers of nodes: **input**, **hidden**, and **output** layers.

Key Feature: Each neuron in one layer is connected to every neuron in the next layer (fully connected).

1. Input Layer

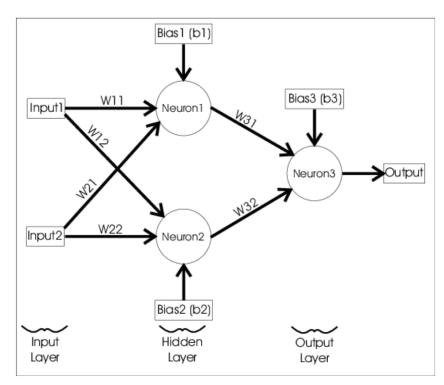
- Receives the raw input features
- One neuron per input feature
- No computation occurs here; inputs are simply passed forward

2. Hidden Layer(s)

- One or more layers between input and output
- Each neuron in a hidden layer:
- Receives inputs from all neurons in the previous layer
- Computes a weighted sum
- Applies a non-linear activation function
- Passes the result to the next layer

3. Output Layer

- Produces the final prediction or classification
- Structure depends on the task:
 - Regression: Often a single neuron with linear activation
 - Binary classification: One neuron with sigmoid activation
 - Multi-class classification: Multiple neurons (one per class) with softmax activation



The Neural Network Model to solve the XOR Logic (from: https://stopsmokingaids.me/)

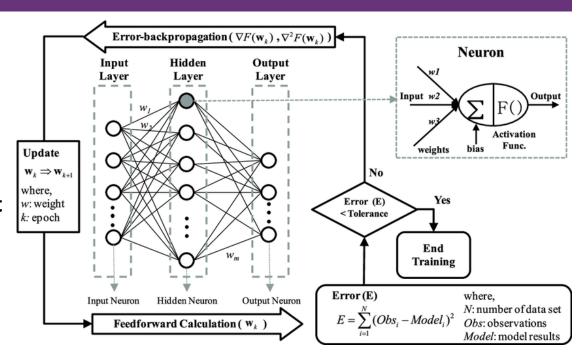




How Neural Networks Learn

Training Process:

- 1. Feed data into the network.
- 2. Compute the output using weights.
- 3. Compare the output with the correct answer (loss calculation).
- 4. Adjust weights using **backpropagation** & **gradient descent** to improve accuracy.
- **Loss Function**: MSE for regression, Cross-Entropy for classification.
- **Optimization**: Backpropagation + Gradient Descent (or Adam).



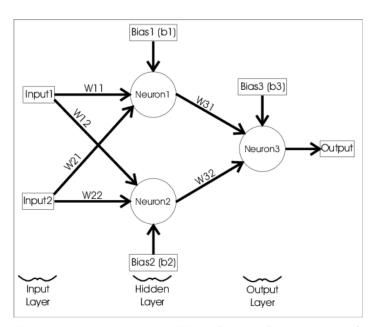






Multi-Layer Perceptron

```
from sklearn.neural_network import MLPClassifier
 import numpy as np
# XOR input and output
X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
y = np.array([0, 1, 1, 0])
# Define MLP with 1 hidden layer of 2 neurons (minimal config for XOR)
mlp = MLPClassifier(hidden layer sizes=(2,), activation='tanh', solver='adam', learning rate init=0.01,
    max iter=10000, random state=42)
 # Train the model
mlp.fit(X, y)
# Make predictions
 predictions = mlp.predict(X)
print("Predictions:\n", predictions)
 print("\nWeights (input to hidden):\n", mlp.coefs [0])
print("\nBias hidden:\n", mlp.intercepts [0])
print("\nWeights (hidden to output):\n", mlp.coefs [1])
 print("\nBias output:\n", mlp.intercepts [1])
                                Weights (hidden to output):
Weights (input to hidden):
                                 [[-4.37775211]
[ 4.46553876]]
[-2.73418453 -3.17014048]]
                                 Bias output:
Bias hidden:
[ 1.21994174 -1.63451199]
                                 [3.61855675]
```



The Neural Network Model to solve the XOR Logic (from: https://stopsmokingaids.me/)









Introduction to Word Embeddings





How Did We Represent Words Pre-2013

- Traditional models like Bag-of-Words (BoW) or TF-IDF, treat words as independent, ignoring semantic similarity.
- One-hot encoding: Sparse, binary vectors (dimension = vocabulary size)
- Example: "king" and "queen" are as unrelated as "king" and "banana" in BoW.

Word	Dimension 1 (cat)	Dimension 2 (dog)	Dimension 3 (fish)	Dimension 4 (bird)
cat	1	0	0	0
dog	0	1	0	0
fish	0	0	1	0
bird	0	0	0	1





The Evolution of Word Representations

- Problem: How do we represent meaning mathematically?
- **Solution**: Distributional hypothesis "You shall know a word by the company it keeps" (J.R. Firth, 1957)
- J.R. Firth **did not** provide a detailed technical implementation like an algorithm or computational method. His statement was more of a **linguistic philosophy** or a **theoretical principle**, not a specific engineering method.
- He worked mostly in the 1930s–1950s, before computers were widely used for language processing. His idea influenced the later development of:
 - Collocational analysis (studying which words often appear together)
 - Contextual analysis in linguistics
- And much later, it inspired the distributional hypothesis in computational linguistics, especially by scholars like Zellig Harris and later computational models (Word2Vec, etc.)
- In short:
 - Firth introduced the principle → Later researchers and engineers built models based on it.







Word2Vec (Tomas Mikolov et al., 2013)

Developed by Tomas Mikolov and team at Google.

Key Innovation

Transformed NLP by creating dense vector representations through prediction-based models

Two Architectures

- Continuous Bag of Words (CBOW):
 - Predicts target word from context words
 - Faster training, better for frequent words
- Skip-gram:
 - Predicts context words from target word
 - Better for rare words, captures more semantic information

Characteristics

- Uses shallow neural networks and trains on local context windows.
- Typically, 100-300 dimensions (vs. vocabulary size)
- Linear relationships: king man + woman ≈ queen
- Efficient training through negative sampling
- Limitations: Fixed vectors, one vector per word regardless of context





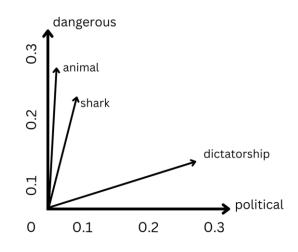


Vector Spaces and Word Embeddings

What is a Vector Space?

- A mathematical space where each word is represented as a point (or vector) in multidimensional space.
- Words are encoded as dense numerical vectors instead of one-hot or sparse representations (Word Embeddings) e.g., "king" \rightarrow [0.21, 0.72,..., 0.35]
- Word Embeddings captures semantic and syntactic relationships about/between words.
- Each dimension potentially captures semantic meaning.
- These vectors are learned from text by models like Word2Vec or GloVe.

Word	Dimension 1 (political)	Dimension 2 (dangerous)
shark	0.05	0.22
animal	0.03	0.25
dangerous	0.07	0.32
political	0.31	0.04
dictatorship	0.28	0.15







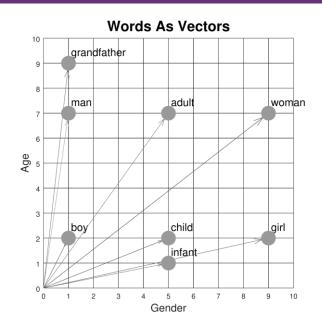
Vector Spaces and Word Embeddings

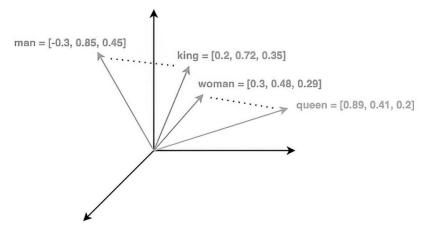
Why Use a Vector Space?

- Makes it possible to compare, visualize, and manipulate meanings of words using math.
- Enables operations like:
 - Similarity: "king" is close to "queen"
 - Analogy: "king" "man" + "woman" ≈ "queen"

Properties of Vector Space

- Semantic relationships are preserved (e.g., "shark" is closer to "dangerous" than "political").
- Similar meanings → closer vectors.
- Dissimilar meanings → vectors farther apart.

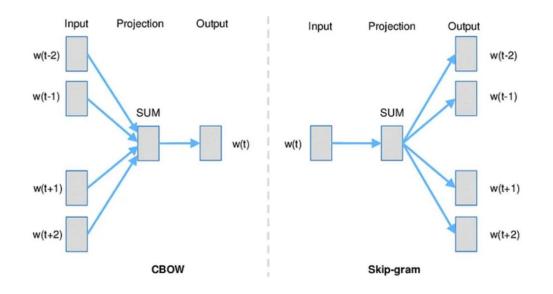


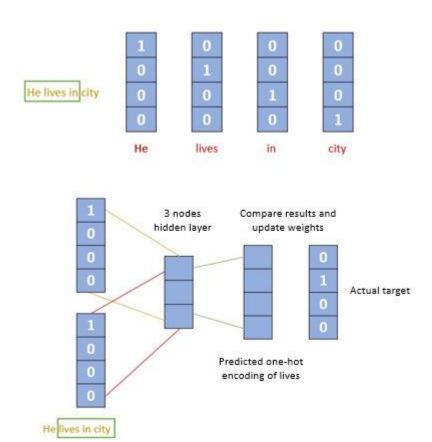






CBow and Skip-Gram Models





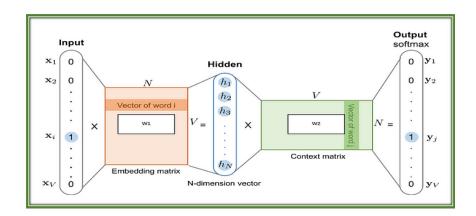




Skip-gram Architecture (Word2Vec)

This diagram illustrates how Word2Vec's **Skip-gram model** works:

- **Input**: A one-hot encoded vector for the center word (word *i*).
- Embedding Matrix: Multiplies the input vector to produce a dense embedding (N-dimensional vector) this becomes the vector representation of the input word.
- Context Matrix: The dense vector is then multiplied with another matrix to predict surrounding context words via softmax output.
- **Output**: A probability distribution over the vocabulary, aiming to maximize the likelihood of actual context words.
- This training process helps learn **meaningful word vectors** based on how words appear in context.



https://python.plainenglish.io/understanding-word-embeddings-tf-idf-word2vec-glove-fasttext-996a59c1a8d3





Glove (Pennington, Socher, Manning 2014)

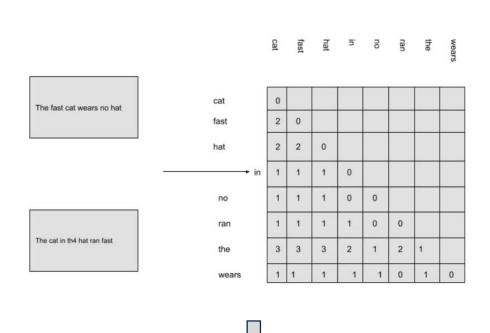
- Developed by Stanford NLP Group (Pennington, Socher, Manning)
- Key Innovation

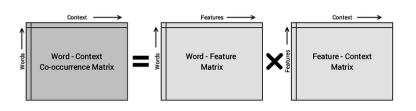
Bridges the gap between count-based methods and prediction-based methods by using global co-occurrence statistics to learn word vectors

- Approach
- Builds a word-word co-occurrence matrix over a large corpus
- Learns embeddings by factorizing the matrix using a weighted least squares objective

Characteristics

- Captures global statistical information while maintaining useful properties of local context
- Produces dense word vectors (typically 100–300 dimensions)
- Linear relationships in vector space are preserved: king man + woman
 ≈ queen
- Trained on massive corpora (Wikipedia, Common Crawl)
- Limitations: Ignores context variability—still one vector per word regardless of usage









Measuring Similarity Between Word Vectors

Why Compare Word Vectors?

- Word embeddings map words into a vector space.
- Words with similar meanings are placed close together in that space.
- To quantify this "closeness," we use vector similarity.

Cosine Similarity

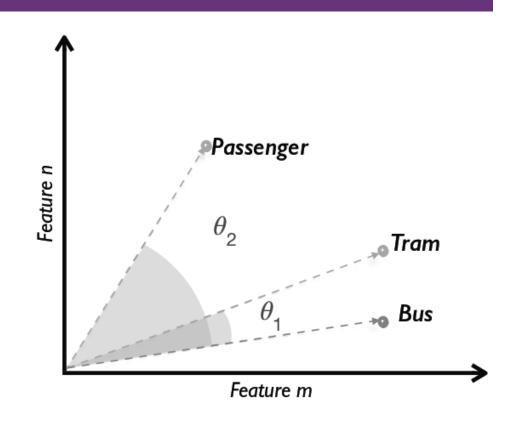
Most common metric used to compare word vectors:

$$\operatorname{cosine_similarity}(\vec{A}, \vec{B}) = \frac{\vec{A} \cdot \vec{B}}{\|\vec{A}\| \|\vec{B}\|}$$

- Measures the angle between two vectors (not their magnitude).
- Ranges from -1 to 1:
 - 1 → Same direction (very similar)
 - $0 \rightarrow Orthogonal$ (unrelated)
 - $-1 \rightarrow$ Opposite directions (very different)

Intuition

- Vectors for "king" and "queen" will have high cosine similarity.
- Vectors for "apple" and "keyboard" will have low similarity.







Learn Embeddings based on a New Corpus

```
from gensim.models import Word2Vec
# Sample corpus
sentences = [['data', 'science', 'is', 'fun'],
     ['machine', 'learning', 'is', 'powerful'],
     ['data', 'and', 'learning', 'are', 'related']]
# Train the model
model = Word2Vec(sentences, vector size=50, window=2, min count=1, workers=2)
# Access the embedding for a word
print("Vector for 'data':\n", model.wv['data'])
# Find similar words
print("Words similar to 'data':", model.wv.most similar('data'))
Vector for 'data':
[-0.01723938 0.00733148 0.01037977 0.01148388 0.01493384 -0.01233535
 -0.01120002 0.01420908 0.00670508 0.01445134 0.01360049 0.01506148
 -0.00757831 -0.00112361 0.00469675 -0.00903806 0.01677746 -0.01971633
 0.0199297 -0.00872489 -0.00119868 -0.01139127 0.00770164 0.00557325
 0.01378215 0.01220219 0.01907699 0.01854683 0.01579614 -0.01397901
-0.01831173 -0.00071151 -0.00619968 0.01578863 0.01187715 -0.00309133
 0.00302193 0.00358008]
Words similar to 'data': [('are', 0.16563551127910614), ('fun', 0.13940520584583282), ('learning', 0.1267007291316986), ('powerful', 0.08872982114553452), ('is', 0.011071977205574512), ('and', -0.027849990874528885),
```







Compute Word Similarities

Use Fake Embeddings as an Example

```
import numpy as np
from sklearn.metrics.pairwise import cosine_similarity
# Fake word vectors (3D for simplicity)
word vectors = {
    "king": np.array([0.8, 0.65, 0.1]),
    "queen": np.array([0.78, 0.66, 0.12]),
    "man": np.array([0.9, 0.1, 0.1]),
    "woman": np.array([0.88, 0.12, 0.12]),
    "apple": np.array([0.1, 0.8, 0.9]),
def similarity(w1, w2):
   return cosine_similarity([word_vectors[w1]], [word_vectors[w2]])[0][0]
print("Similarity(king, queen):", similarity("king", "queen"))
print("Similarity(man, woman):", similarity("man", "woman"))
print("Similarity(king, apple):", similarity("king", "apple"))
```







Compute Word Similarities

Use Real Embeddings from Gensim Library

```
import gensim.downloader as api
from gensim.models import Word2Vec
# Load pre-trained Word2Vec model
word2vec model = api.load("word2vec-google-news-300")
# Find similar words
similar words = word2vec model.most similar('computer', topn=5)
print("Words similar to 'computer':", similar words)
# Word analogies
result = word2vec_model.most_similar(positive=['woman', 'king'],
   negative=['man'], topn=1)
print("king - man + woman =", result)
# Train your own Word2Vec model
sentences = [["cat", "say", "meow"], ["dog", "say", "woof"]]
model = Word2Vec(sentences, vector size=100, window=5, min count=1, workers=4)
# Get vector for a word
cat vector = model.wv['cat']
print("Vector for 'cat':", cat_vector[:5]) # Show first 5 dimensions
```

Gensim

Gensim is a powerful open-source Python library designed specifically for unsupervised topic modeling and natural language processing tasks, with a strong focus on working with large corpora. It excels in handling word embeddings and semantic similarity, offering efficient implementations of models like Word2Vec, FastText, and Doc2Vec. Gensim is known for its memory-efficient, streaming-based approach, which allows it to process text data without loading everything into memory. This makes it especially useful for working with real-world, large-scale text data.







Word Embeddings Example using Spacy Library

- pip install spacy
- python -m spacy download en_core_web_md

```
import spacy
nlp = spacy.load("en_core_web_md")

word1 = nlp("king")
word2 = nlp("queen")
print("Similarity:", word1.similarity(word2))
```

spaCy

spaCy is a fast and robust natural language processing library for Python that provides industrial-strength tools for text preprocessing and linguistic analysis. It comes with pre-trained models for multiple languages and supports features like tokenization, part-of-speech tagging, named entity recognition, dependency parsing, and sentence segmentation. spaCy is designed for performance and ease of use in production environments and integrates well with deep learning libraries. While it's not primarily focused on word embeddings, it includes pre-trained word vectors and supports similarity comparisons out of the box.







Contextual Word Embeddings (e.g., ELMo, BERT)

Key Innovation

Unlike static embeddings (Word2Vec, GloVe), contextual models generate **different vectors for the same word** depending on its context.

Approach

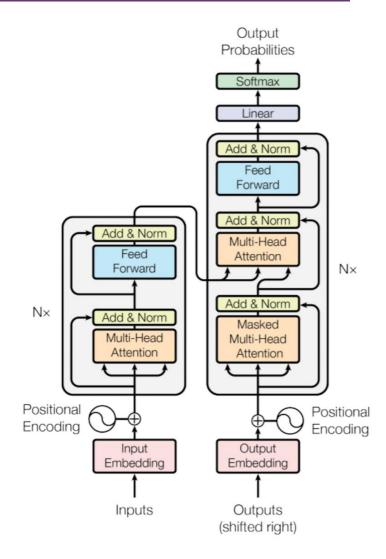
Uses deep, pre-trained neural networks (often transformer-based) Embeddings are derived from entire sentences, capturing syntax and semantics dynamically

Examples

- ELMo (2018): Contextualizes word representations using deep bi-directional LSTMs Neural Networks
- BERT (2018): Transformer-based neural networks trained with masked language modeling and next sentence prediction
- GPT (2018): Transformer-based unidirectional language model focused on generation.

Characteristics

- Embeddings are context-sensitive (e.g., "bank" in "river bank" vs. "savings bank")
- Each word is embedded based on its role in the sentence.
- Embeddings vary for the same word depending on its position and meaning.
- Significantly improve performance on downstream NLP tasks.
- Limitations: Computationally intensive; harder to interpret than static embeddings







Practical Implementation: BERT in Python

```
import torch
from transformers import BertModel, BertTokenizer
# Load pre-trained BERT model and tokenizer
tokenizer = BertTokenizer.from pretrained('bert-base-uncased')
model = BertModel.from pretrained('bert-base-uncased')
# Input text
text = "The quick brown fox jumps over the lazy dog."
# Tokenize input
inputs = tokenizer(text, return tensors="pt")
# Get BERT embeddings
with torch.no grad():
  outputs = model(**inputs)
# Last hidden states contain contextual embeddings for each token
last hidden states = outputs.last hidden state
# Get embedding for the first token (after [CLS])
word embedding = last hidden states[0, 1].numpy()
print(f"BERT embedding for 'The' (first 5 dimensions): {word embedding[:5]}")
# Get embeddings for full sentence (CLS token)
sentence embedding = last hidden states[0, 0].numpy()
```





Applications of Word Embeddings in NLP

1. Semantic Similarity

Measure how similar two words, phrases, or documents are by comparing their vector representations. Example: Identifying that "doctor" and "physician" are closely related.

2. Text Classification

Used as input features for tasks like spam detection, sentiment analysis, and topic classification. Embeddings provide rich, dense input for machine learning models.

3. Named Entity Recognition (NER)

Help identify proper nouns and classify them into categories like person, location, or organization. Embedding-based models improve contextual understanding of named entities.

4. Machine Translation

Map words from one language to another by aligning embeddings in multilingual space. Improves translation accuracy by leveraging semantic proximity.

5. Question Answering & Chatbots

Used to understand queries and match them with appropriate answers or responses. Enable bots to interpret intent and context more accurately.

6. Information Retrieval

Enhance search engines by retrieving results based on semantic meaning, not just keyword matches. Example: Searching for "heart attack" returns documents containing "cardiac arrest."







GenAl and Large Language Models

Overview

- What is generative Al
- Large language models
- Tokens
- Tokens versus parameters
- Prompt engineering
- Zero-shot, one-shot and few-shot learning
- Prompt guide
- Generative AI systems examples
- Large language models getting started
- OpenAI ChatGPT
- OpenAl tools

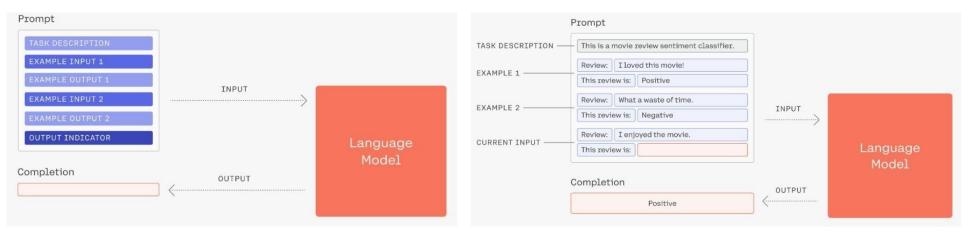
- ChatGPT command types
- ChatGPT plugins
- What about the students?
- Office 365 Copilot Windows 11 Copilot
- What are our options?
- What about Turnitin?
- Practical use in learning and teaching
- Assessment redesign for generative Al
- Resources and further reading





Generative AI (GenAI)

- Type of Artificial Intelligence that leverages AI to generate content or data
- Data can include text, images, audio, video, 3D models, code and video games
- Typically created in response to prompts (prompt engineering)
- Prompts are constructed inputs to language models to generate useful output
- Usually given with examples zero shot versus few shot learning



Source: docs.cohere.com https://docs.cohere.com/docs/prompt-engineering





Large language models

- Type of machine learning model/algorithm
- Performs variety of natural language processing (NLP) tasks
- Learn, understand, and process human language efficiently
- E.g., generate/classify text, answer questions conversationally
- Uses hundreds of billions parameters





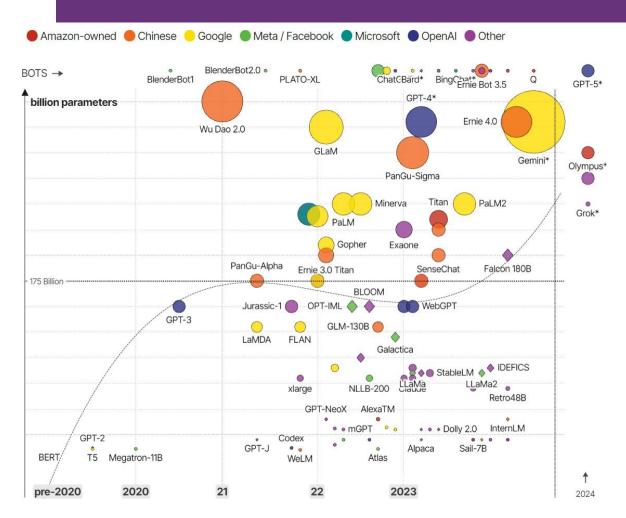
Large language models

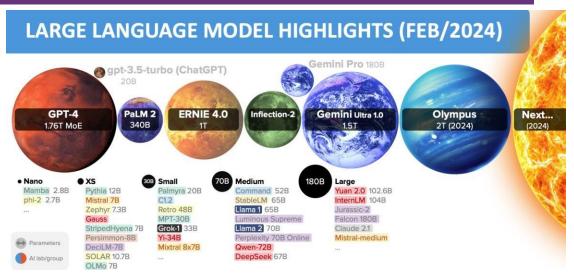
- Trained with large amounts of data
- Based on neural networks (Transformers) that learn context and understanding through sequential data analysis
- Uses self-supervised learning to predict the next token in a sentence, given the surrounding context
- Process is repeated over and over until the model reaches acceptable level of accuracy
- GPT-4 (Generative Pre-trained Transformer)





Large language models (LLM)





Source: https://lifearchitect.ai/models/

Source: informationisbeautiful.net

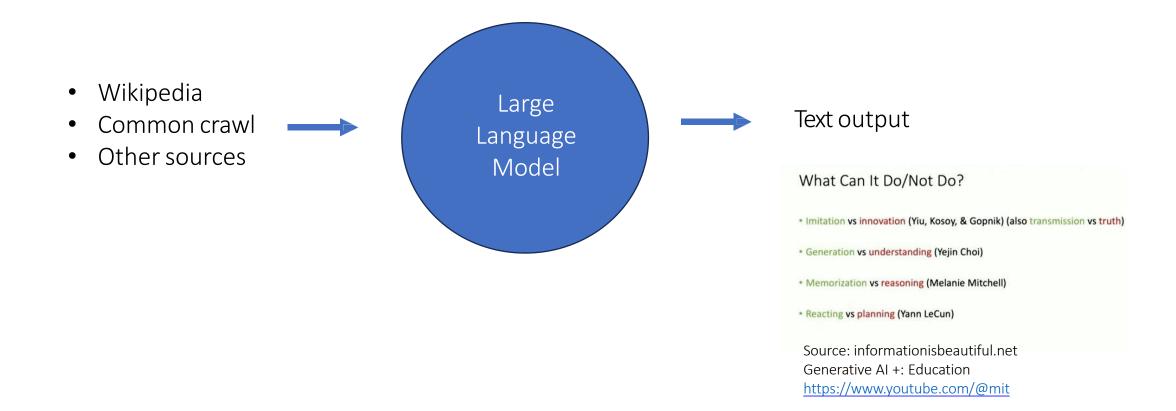
 $\underline{https://information is beautiful.net/visualizations/the-rise-of-generative-ai-large-language-models-llms-like-chatgpt/defined by the resulting and the r$





Large language models training

LLMs return similar patterns to data it is trained on (not thinking)







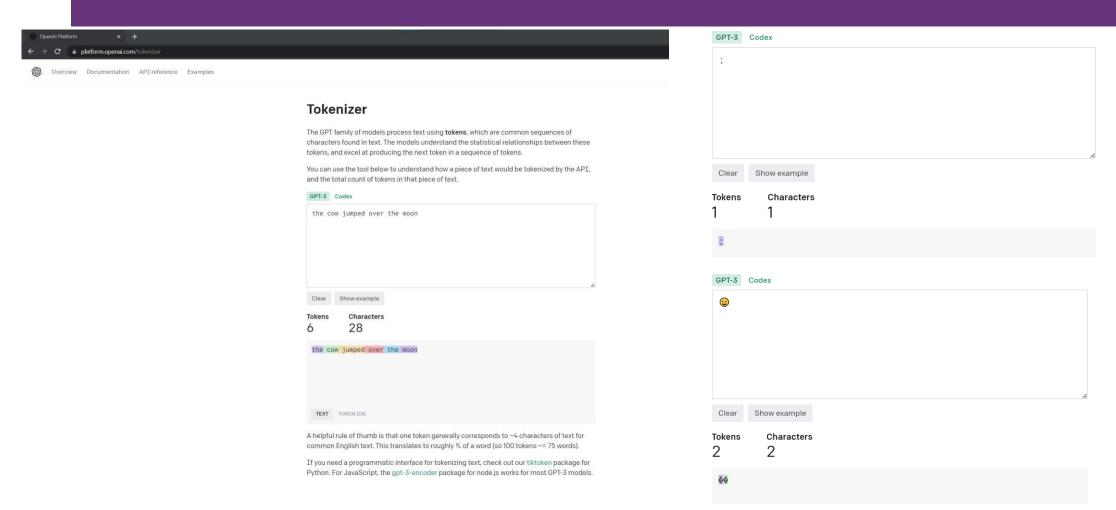
Tokens

- Basic units of text/code LLM uses to process or generate language
- Can be characters, words, sub-words, segments of text or code
- Tokens generally = ~4 characters of text for common English
- $\frac{3}{4}$ of a word 100 tokens ~= 75 words
- GPT models process text using tokens
- Common sequences of characters found in text
- Understands the statistical relationships between these tokens
- Used to predict next token in a sequence of tokens





Tokens

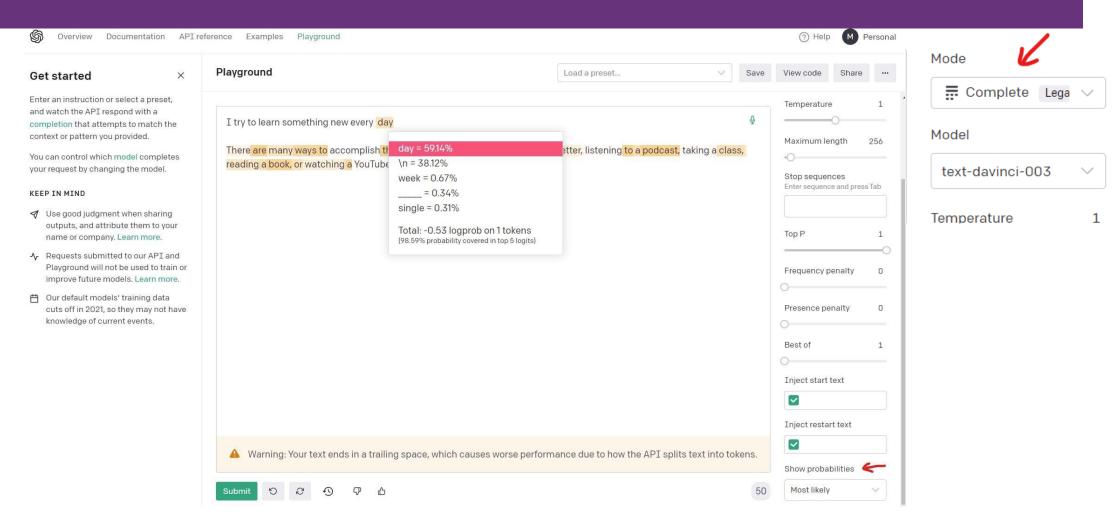


https://platform.openai.com/tokenizer
https://lunary.ai/openai-tokenizer





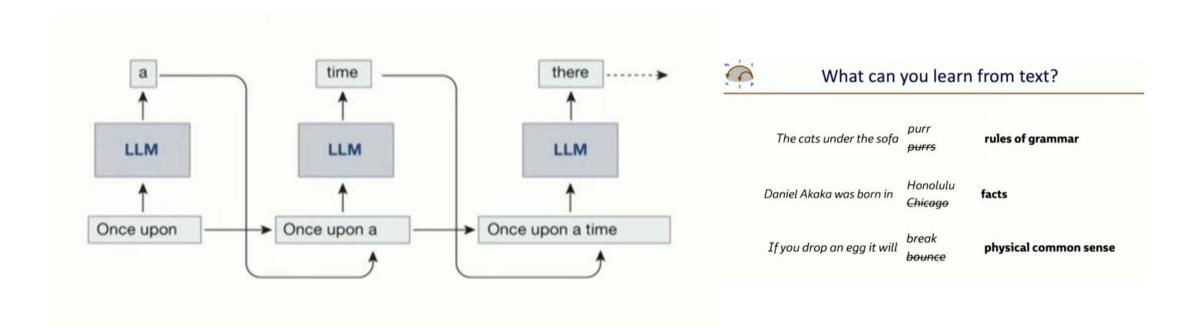
Tokens







Tokens and structure



Source:

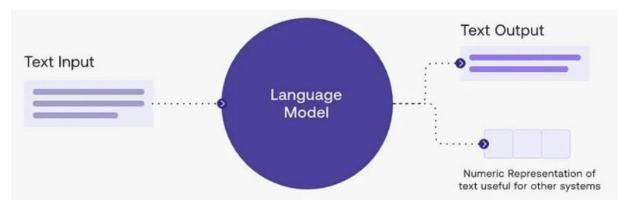
Shanahan M, McDonell K, Reynolds L. Role play with large language models. Nature. 2023 Nov;623(7987):493-498. doi: 10.1038/s41586-023-06647-8 Epub 2023 Nov 8. PMID: 37938776.





Tokens versus parameters

- Large language model (LLM) context
- Token is a basic unit of meaning e.g., word, punctuation mark
- Parameters = numerical values that define model behaviour
- Adjusted during training to optimize model's ability to generate relevant and coherent text



Large language model

Takes an input and produces a token as an output

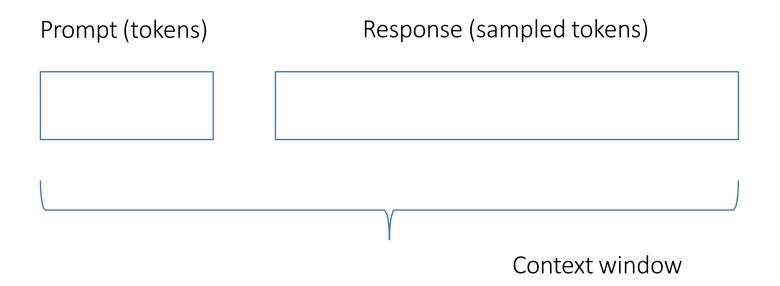
Source: medium.com





Why are tokens important?

- Context window in large language models
- Length of text model can process and respond to in given instance
- Constraints length of prompt and response



gpt-4 8000 tokens gpt-4-32k 32000 tokens

gpt-4 6000 words gpt-4-32k 24000 words

ChatGPT-4 currently has a cap related to message frequency – 128,000 tokens





Cost is based on tokens used

How much does GPT-4 cost?

Updated today

The following information is also on our Pricing page.

We are excited to announce GPT-4 has <u>a new pricing model</u>, in which we have reduced the price of the prompt tokens.

For our models with **128k** context lengths (e.g. gpt-4-1106-preview and gpt-4-1106-vision-preview), the price is:

- \$10.00 / 1 million prompt tokens (or \$0.01 / 1K prompt tokens)
- \$30.00 / 1 million sampled tokens (or \$0.03 / 1K sampled tokens)

For our models with 8k context lengths (e.g. gpt-4 and gpt-4-0314), the price is:

- \$30.00 / 1 million prompt token (or \$0.03 / 1K prompt tokens)
- \$60.00 / 1 million sampled tokens (or \$0.06 / 1K sampled tokens)

For our models with 32k context lengths (e.g. gpt-4-32k and gpt-4-32k-0314), the price is:

- \$60.00 / 1 million prompt tokens (or \$0.06 / 1K prompt tokens)
- \$120.00 / 1 million sampled tokens (or \$0.12 / 1K sampled tokens)

https://help.openai.com/en/articles/7127956-how-much-does-gpt-4-cost

us	Iculate how much it will cost to generate a certain number of words by ing OpenAl GPT-3.5 and GPT-4 APIs.
	Enter number of words:
	100000
	(10k) (100k) (500k) (1m)
	Select the base language model:
	GPT-4 8K (\$0.06/1k tokens)
	Estimated price to generate 100000 words: \$8.8000
Δε	OpenAI bills you based on the number of tokens sent in your prompt
~3	
pli	us the number of tokens returned by the API, I am taking an assumptio
pli of	a prompt length of 200 words for every 1000 words generated by the
pli of	
of AF	a prompt length of 200 words for every 1000 words generated by the
of AF	a prompt length of 200 words for every 1000 words generated by the PLI am adding that cost to the final cost as well.

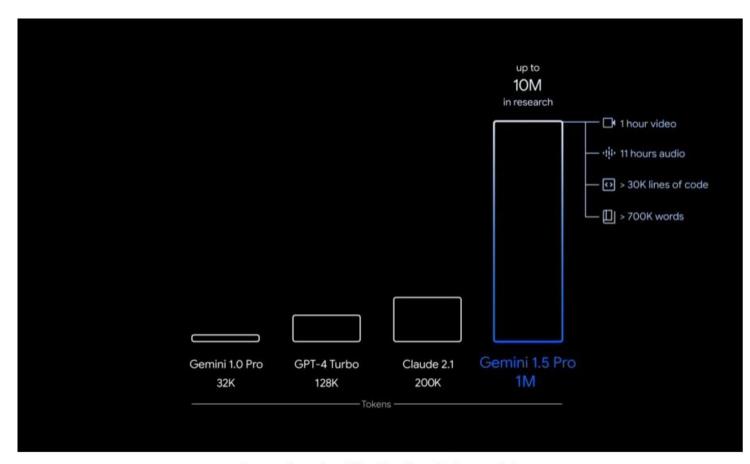
https://invertedstone.com/tools/openai-pricing/

Gemini 1.5 - 1 million multimodal tokens



/ 1,000,000 tokens







◆ Gemini 1.5 Pro

326,914 tokens

1.5 Pro can seamlessly analyze, classify and summarize large amounts of content within a given prompt. For example, when given the 402-page transcripts from Apollo 11's mission to the moon, it can reason about conversations, events and details found across the document.

Context lengths of leading foundation models

https://blog.google/technology/ai/google-gemini-next-generation-model-february-2024/#architecture