

Statistical Inference Course Project, Part 2

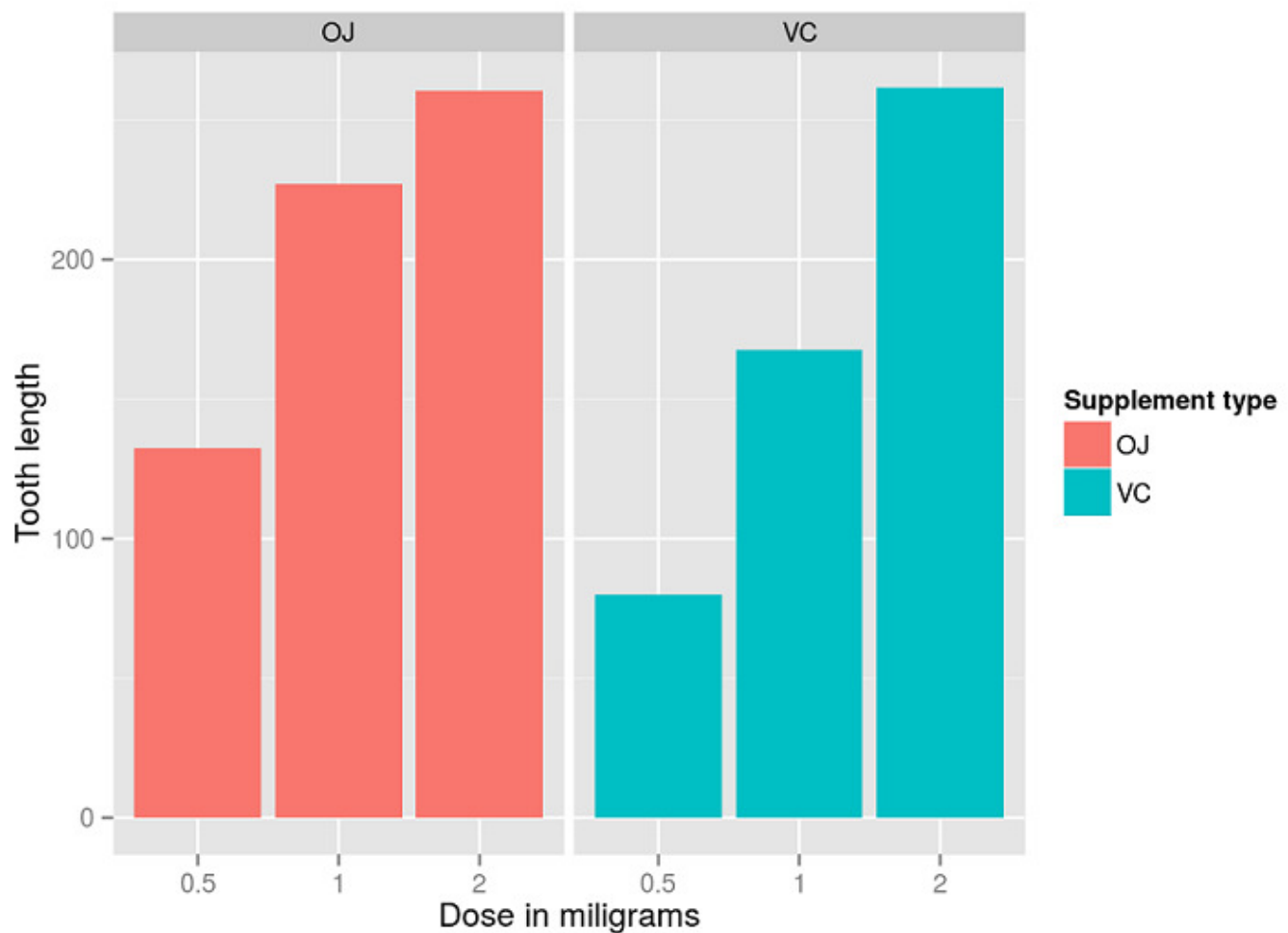
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In the second part of the project, we analyze the ToothGrowth data in the R datasets package. The data is set of 60 observations, length of odontoblasts (teeth) in each of 10 guinea pigs at each of three dose levels of Vitamin C (VC in 0.5, 1 and 2 mg) with each of two delivery methods orange juice (OJ) or ascorbic acid .

```
library(datasets)
library(ggplot2)
ggplot(data=ToothGrowth, aes(x=as.factor(dose), y=len, fill=supp)) +
  geom_bar(stat="identity",) +
  facet_grid(. ~ supp) +
  xlab("Dose in milligrams") +
  ylab("Tooth length") +
  guides(fill=guide_legend(title="Supplement type"))
```

As seen from the below, there is a positive correlation between the tooth length and the dose levels of Vitamin C, for both delivery methods.

The effect of the dose can also be identified using regression analysis. One interesting question that can also be addressed is whether the supplement type (i.e. orange juice or ascorbic acid) has any effect on the tooth length. In other words, how much of the variance in tooth length, if any, can be explained by the supplement type?



```
fit <- lm(len ~ dose + supp, data=ToothGrowth)
summary(fit)
```

```
##
## Call:
## lm(formula = len ~ dose + supp, data = ToothGrowth)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.600 -3.700  0.373  2.116  8.800
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    9.273     1.282     7.23 1.3e-09 ***
## dose           9.764     0.877    11.14 6.3e-16 ***
## suppVC        -3.700     1.094    -3.38 0.0013 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.24 on 57 degrees of freedom
## Multiple R-squared:  0.704, Adjusted R-squared:  0.693
## F-statistic: 67.7 on 2 and 57 DF, p-value: 8.72e-16
```

The model explains 70% of the variance in the data. The intercept is 9.273, meaning that with no supplement of Vitamin C, the average tooth length is 9.273 units. The coefficient of dose is 9.764. It can be interpreted as increasing the delivered dose 1 mg, all else equal (i.e. no change in the supplement type), would increase the tooth length 9.764 units. The last coefficient is for the supplement type. Since the supplement type is a categorical variable, dummy variables are used. The computed coefficient is for suppVC and the value is -3.7 meaning that delivering a given dose as ascorbic acid, without changing the dose, would result in 3.7 units of decrease in the tooth length. Since there are only two categories, we can also conclude that on average, delivering the dosage as orange juice would increase the tooth length by 3.7 units.

95% confidence intervals for two variables and the intercept are as follows.

```
confint(fit)
```

```
##                2.5 % 97.5 %  
## (Intercept)  6.705  11.84  
## dose         8.008  11.52  
## suppVC      -5.890  -1.51
```

The confidence intervals mean that even if we collect a different set of data and estimate parameters of the linear model several times, 95% of the time, the coefficient estimations will be in these ranges as shown above.

For each coefficient (i.e. intercept, dose and suppVC), the null hypothesis is that the coefficients are zero, meaning that no tooth length variation is explained by that variable. All p-values are less than 0.05, rejecting the null hypothesis and suggesting that each variable explains a significant portion of variability in tooth length, assuming the significance level is 5%.