Evaluating Policy Counterfactuals: A "VAR-Plus" Approach Practical Implementation

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EACBN, June 2024

Outline

- 1. Introduction
- 2. Reduced-form Objects
- 3. "Plus" Step
- 4. Constructing the counterfactuals
- 5. Extra application: Financial Conditions Targeting

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Plan for today: construct counterfactuals

Proposition

Suppose that the $SVMA(\infty)$ process (6) is **invertible**; i.e., that

$$\varepsilon_t \in \operatorname{span}(\{y_\tau\}_{-\infty < \tau \le t}).$$

Then knowledge of a) y_t and its autocovariance function $\Gamma_y(\ell)$ and b) policy causal effects Θ_{ν} suffices to construct the policy counterfactuals of interest.

- 1. How do we obtain $\Gamma_{\nu}(\ell)$ and Θ_{ν} ?
- 2. How do we exactly use them to arrive at the desired counterfactuals?

Objects of interest: counterfactuals under alternative policy rule

• Average business cycle: counterfactual second moments

$$\Gamma_y(\ell) = \sum_{m=0}^{\infty} \Theta_m \Theta'_{m+\ell}$$
 vs. $\tilde{\Gamma}_y(\ell) = \sum_{m=0}^{\infty} \tilde{\Theta}_m \tilde{\Theta}'_{m+\ell}$

Note: written in terms of structural IRFs $\{\Theta_m\}$, but under invertibility a rotation $\{\Theta_m P'\}$ suffices.

• Need: Policy Causal effects + Wold IRFs

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• Condt'l forecast: how is the economy predicted to evolve from t onwards? • Init. Cond.

$$\mathbb{E}_{t}\left[y_{t+h}\right] = \sum_{\ell=0}^{\infty} \Theta_{\ell+h} \varepsilon_{t-\ell} \quad \text{vs.} \quad \mathbb{E}_{t}\left[\tilde{y}_{t+h}\right] = \sum_{\ell=0}^{\infty} \tilde{\Theta}_{\ell+h} \varepsilon_{t-\ell}$$

Note: under invertibility, the VAR recovers correct (FI) forecasts.

Need: Policy Causal effects + Forecasts at t

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• Condt'l forecast: how is the economy predicted to evolve from t onwards? • Int. Cond.

$$\mathbb{E}_{t}\left[y_{t+h}\right] = \sum_{\ell=0}^{\infty} \Theta_{\ell+h} \varepsilon_{t-\ell} \quad \text{vs.} \quad \mathbb{E}_{t}\left[\tilde{y}_{t+h}\right] = \sum_{\ell=0}^{\infty} \tilde{\Theta}_{\ell+h} \varepsilon_{t-\ell}$$

Historical evolution: how would a given historical episode have unfolded?

$$y_t = \sum_{\ell=0}^{\infty} \Theta_{\ell} \varepsilon_{t-\ell}$$
 vs. $\tilde{y}_t = \sum_{\ell=0}^{\infty} \tilde{\Theta}_{\ell} \varepsilon_{t-\ell}$

Note: what we need is forecasts and each date. Shock = forecast revision, $(E_t - E_{t-1})[y_{t+h}]$.

• Need: Policy Causal effects + Forecasts at $t \in [t_1, t_2]$.

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 - 2. run_var_fcst_scenario.m: get forecasts at a given date t. Write VAR in companion form, $Y_t = \bar{A}Y_{t-1} + u_t$, then for h > 0, $E_t[Y_{t+h}] = AE_t[Y_{t+h-1}] = \bar{A}^hY_t$

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 - 3. run_var_fcst_evol.m: get forecasts and their revisions for each $t \in [t_1, t_2]$ Same as before, but do it for each $t \in [t_1, t_2]$

- We can get only a part of the Θ_{ν} matrix empirically.
- Note: this can be enough for some applications.
 Approximation with one shock might be quite close of the full counterfactual.

In our paper: second moments and historical evolution.

- We can get only a part of the Θ_{ν} matrix empirically.
- run_var_mp_ad.m Run VAR with Aruoba and Drechsel (2024) shock ordered first, then output gap (Hamilton (2018)-filtered output), inflation, and FFR.
 Sample 1969Q1-2006Q4.

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• Use B-VAR (with loose priors) to get posterior draws, quantify IRF estimation uncertainty.

Get posterior draws for B_{ℓ} , Σ_u in $y_t = \sum_{\ell=1}^p B_{\ell} y_{t-\ell} + u_t$, $u_t \sim N(0, \Sigma_u)$. For each draw, compute IRF. With this, we can obtain confidence sets + Var-Cov matrix of IRFs.

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- Estimate point estimate $\hat{\theta}_{\nu}$ and Variance-Covariance matrix $\hat{V}_{\theta_{\nu}}$ for IRFs. Follow Christiano et al. (2010). Different to most of the literature, use non-diagonal $\hat{V}_{\theta_{\nu}}$ to more accurately reflect informativeness of the data.

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- **Solution:** partial model structure. Only need models of MP transmission.
- We'll match those models to the empirical evidence on MP shocks, then the model extrapolates to full Θ_{ν} .

Aside: why many models?

A: we want to be as robust to model mispecification as possible. Different models extrapolate differently.

• **Notation:** model \mathcal{M}_j has parameters ψ_j . Priors over both: $p(\mathcal{M}_j)$ and $p(\psi_j)$. In our case: 4 "models" RANK and HANK, both in "Ratex" and "Behavioral" versions. Parameters: prob. of price and wage adjustment, investment adj. cost, et.

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- Using asymptotic argument, empirical IRFs satisfy $\hat{\theta}_{\nu} \sim N(\theta_{\nu}, V_{\theta_{\nu}})$. Quasi-likelihood is:

$$\rho(\hat{\theta}_{\nu}|\psi_{j},\mathcal{M}_{j}) \propto \exp\left(-\frac{1}{2}(\theta_{\nu}(\psi_{j},\mathcal{M}_{j}) - \hat{\theta}_{\nu})'V_{\theta_{\nu}}^{-1}(\theta_{\nu}(\psi_{j},\mathcal{M}_{j}) - \hat{\theta}_{\nu})\right) \tag{1}$$

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Let's dig deeper into each step.

- 4 models:
 - 1. HANK + sticky information (similar to Auclert et al. (2020))
 - 2. RANK with habits (similar to Christiano et al. (2005); Smets and Wouters (2007))
 - 3. For both, a ratex and a behavioral version.
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- **Key difference**: behavioral models are less forward-looking.
- We estimate habit parameter (RANK) or sticky information parameter (HANK), price and wage stickiness, inv. adj. cost, and capacity ut. elasticity.

Model Overview: RANK

Households & unions

Representative household with preferences

$$\mathbb{E}_{0}\left[\sum_{t=0}^{\infty}\beta^{t}\left[u\left(c_{t}-hc_{t-1}\right)-v\left(\ell_{t}\right)\right]\right]$$

where $u(x) = \frac{x^{1-\gamma}}{1-\alpha}$ and $v(x) = \nu \frac{x^{1+\varphi}}{1-\alpha}$, and budget constraint

$$c_t + a_t^H = w_t (1 - \tau_t^\ell) \ell_t + d_t^H - \tau_t + \frac{1 + r_{t-1}^n}{1 + \tau_t} a_{t-1}^H$$

Labor supply intermediated by sticky-wage unions (with indexation), gives

$$\pi_t^w - \pi_{t-1} = \kappa_w \chi_t + \beta \mathbb{E}_t \left[\pi_{t+1}^w - \pi_t \right]$$
 where $\chi_t = \varphi \ell_t - (\lambda_t + w_t) + \frac{\bar{\tau}^\ell}{1 - \bar{\tau}^\ell} \tau_t^\ell$

Model Overview: RANK, cont.

Production

- Standard layered structure: intermediate goods producers (capital & labor), retailers, aggregators, and capital goods producers
- Features: variable capacity utilization, nominal rigidities (with indexation), inv. adj. costs
- Pricing decisions give

$$egin{aligned} \pi_t - \pi_{t-1} &= \kappa_{\scriptscriptstyle P}
ho_t^\prime + eta \mathbb{E}_t \left[\pi_{t+1} - \pi_t
ight] \end{aligned}$$

where p_t^l is intermediate goods price. Remaining conditions standard.

Policy

- Fiscal authority: nominal bonds with exponential maturity structure, spend constant fraction of GDP, adjust taxes gradually to maintain long-run budget balance
- Monetary authority: close the model with an arbitrary (determinacy-inducing) rule.
 We'll see later that results are independent of the rule chosen.

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Model variants

- **HANK:** Replace RA by continuum of households subject to idiosyncratic earnings [process as in Kaplan-Moll-Violante] and tight borrowing constraint
 - To get sluggish aggregate consumption: inattention to macro conditions

$$V_t(a, e, s) = \max_{c, a'} \{ u(c) - v(\ell_t) + \beta \mathbb{E}_{t-s} [\theta V_{t+1}(a', e', s+1) + (1-\theta) V_{t+1}(a', e', 0)] \}$$

subject to the budget constraint

$$c + a' = ((1 - \tau_{\ell,t}) w_t \ell_t + d_t^H) e + \frac{1 + r_{t-1}^n}{1 + \tau_t} a + \tau_t, \quad a' \ge \underline{a}$$

where θ is probability of updating, and s is time since last update

• Behavioral frictions: add cognitive discounting [Gabaix (2020)], wage and price PCs are:

$$\pi_{t} - \pi_{t-1} = \kappa_{p} \rho_{t}^{l} + \beta^{p} \mathbb{E}_{t} [\pi_{t+1} - \pi_{t}], \quad \beta^{p} < \beta
\pi_{t}^{w} - \pi_{t-1} = \kappa_{w} \chi_{t} + \beta^{w} \mathbb{E}_{t} [\pi_{t+1}^{w} - \pi_{t}], \quad \beta^{w} < \beta$$

Solution Method - SSJ (Auclert et al., 2021)

- Given $\mathbf{X} = (\mathbf{y}', \mathbf{w}', \mathbf{\pi}')'$ and for monetary shocks \mathbf{v} , we can compute (\approx up to 1st ord.) excess demand/supply in 3 markets: assets, labor and capital for all $t \leq T^{max}$.
- Solution is then written implicitly as:

$$\underbrace{F(\boldsymbol{X}, \boldsymbol{\nu})}_{3T^{max} \times 1} = \underbrace{\begin{pmatrix} \boldsymbol{a}^{d}(\boldsymbol{X}, \boldsymbol{\nu}) - \boldsymbol{a}^{s}(\boldsymbol{X}, \boldsymbol{\nu}) \\ \boldsymbol{\ell}^{d}(\boldsymbol{X}, \boldsymbol{\nu}) - \boldsymbol{\ell}^{s}(\boldsymbol{X}, \boldsymbol{\nu}) \\ \boldsymbol{Labor Market} \\ \boldsymbol{k}^{d}(\boldsymbol{X}, \boldsymbol{\nu}) - \boldsymbol{k}^{s}(\boldsymbol{X}, \boldsymbol{\nu}) \end{pmatrix}}_{Capital Market} = 0$$

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• IFT to get:

$$d\mathbf{X} = -(F_{\mathbf{X}})^{-1}(F_{\boldsymbol{\nu}})d\boldsymbol{\nu} \tag{2}$$

• Function compute_irfs_model.m does this to compute $\Theta_{\nu}(\psi_i, \mathcal{M}_i)$.

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- In order to obtain $\theta_{\nu}(\psi_{j}, \mathcal{M}_{j})$, let $\tilde{\nu}^{*}$ be a $H \times 1$ vector of news shocks, and $\tilde{\boldsymbol{\nu}}^{*} = ((\tilde{\nu}^{*})', \mathbf{0}')'$. Pick $\tilde{\nu}^{*}$ such that the fit is closest to $\hat{\theta}_{\nu}$.
- Abusing notation:

$$\tilde{\nu}^* = \underset{\tilde{\nu}^*}{\operatorname{argmin}} \quad (\Theta_{\nu}(\psi_j, \mathcal{M}_j) \tilde{\nu}^* - \hat{\theta}_{\nu})' V_{\theta_{\nu}}^{-1} (\Theta_{\nu}(\psi_j, \mathcal{M}_j) \tilde{\nu}^* - \hat{\theta}_{\nu})$$

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- Closed form solution:

$$\tilde{\nu}^* = (\tilde{\Theta}'_{1:H,1:H} V_{\theta_v}^{-1} \tilde{\Theta}_{1:H,1:H})^{-1} (\tilde{\Theta}'_{1:H,1:H} V_{\theta_v}^{-1} \hat{\theta}_v)$$
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Same algebra as GLS.

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In the code: compute log density, and omit constant c except for model posterior.

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• Why do it this way? Invariance to assumed MP rule. If we assumed a different rule, we'd get different $\tilde{\nu}^*$, but "fitted values" would be the same.

Sampling from the posterior and posterior model odds

Scripts sample_posterior.m and posterior_model_probs.m.

- Fix a model \mathcal{M}_j
 - 1. We know how to compute $p(\psi_j|\mathcal{M}_j, \hat{\theta}_{\nu}) \Rightarrow$ use RWMH to sample from the posterior.
 - 2. For posterior model odds, obtain marginal likelihood:

$$p(\hat{ heta}_{
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u}|\mathcal{M}_j, \psi_j) p(\psi_j|\mathcal{M}_j) d\psi_j$$

Given posterior draws $\{\psi_i^i\}$, use harmonic mean estimator (Geweke, 1999):

$$\rho(\hat{\theta}_{\nu}|\mathcal{M}_{j}) \approx \left[\frac{1}{N_{use}} \sum_{i=1}^{N_{use}} \frac{f(\psi_{j}^{i})}{\rho(\hat{\theta}_{\nu} \mid \psi_{j}^{i}, \mathcal{M}_{j}) \rho(\psi_{j}^{i}|\mathcal{M}_{j})}\right]^{-1}$$
(5)

where

$$f(\psi) = \tau^{-1} (2\pi)^{-d/2} |\bar{V}_{\psi}|^{-1/2} \exp\left[-0.5(\psi - \bar{\psi})' \bar{V}_{\psi}^{-1} (\psi - \bar{\psi})\right]$$

$$\times \mathbb{I}\left\{ (\psi - \bar{\psi})' \bar{V}_{\psi}^{-1} (\psi - \bar{\psi}) \le F_{\chi_d^2}^{-1}(\tau) \right\}$$

 $ar{\psi}$ is the posterior mean and $ar{V}_{\psi}$ is the posterior covariance matrix. See Herbst and Schorfheide (2016) sec 4.6

Sampling from the posterior and posterior model odds

Scripts sample_posterior.m and posterior_model_probs.m.

- Fix a model \mathcal{M}_j
 - 1. We know how to compute $p(\psi_j|\mathcal{M}_j, \hat{\theta}_{\nu}) \Rightarrow$ use RWMH to sample from the posterior.
 - 2. For posterior model odds, obtain marginal likelihood:

$$p(\hat{ heta}_
u|\mathcal{M}_j) = \int p(\hat{ heta}_
u|\mathcal{M}_j, \psi_j) p(\psi_j|\mathcal{M}_j) d\psi_j$$

• Given $p(\hat{\theta}_{\nu}|\mathcal{M}_i)$, compute posterior model probabilites as:

$$p\left(\mathcal{M}_{j} \mid \hat{\theta}_{\nu}\right) = \frac{p\left(\hat{\theta}_{\nu} \mid \mathcal{M}_{j}\right) p\left(\mathcal{M}_{j}\right)}{\sum_{i=1}^{M} p\left(\hat{\theta}_{\nu} \mid \mathcal{M}_{i}\right) p\left(\mathcal{M}_{i}\right)}$$
(5)

• Can obtain sample across models with the posterior model probabilities.

Outline

- 1. Introduction
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Constructing the counterfactuals

- We have all we need construct counterfactuals!
 - 1. From VARs, we have Wold IRFs and Forecasts at each t of interest. Note: we also have a distribution for this. But for simplicity, fix all these objects at their medians.
 - 2. From the "Plus" step, we obtained a posterior distribution for Θ_{ν} . All reported confidence sets account for this source of uncertainty only.
- **Building Block:** McKay and Wolf (2023) Recall: for a baseline IRF, we can get the counterfactual IRF if we have Θ_{ν}

- Script: get_cnfctl_stats.m
- Need: Policy Causal effects + Wold IRFs

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$$Var(y_t) = \sum_{\ell=0}^{\infty} \tilde{\Psi}_{\ell} \tilde{\Psi}'_{\ell}$$

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$$Var(y_t) = \sum_{\ell=0}^{\infty} \tilde{\Psi}_{\ell} \tilde{\Psi}'_{\ell}$$

Result: full distribution of counterfactual second moments.

- Script: get_historical_scenario.m
- Need: Policy Causal effects + Forecasts at t.

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For plotting: may want to retrend the data.

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For plotting: may want to retrend the data.

Result: full distribution of counterfactual conditional forecast under new rule.

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 - 1. Initial Date: apply McKay and Wolf (2023) to $E_{t_1}[y_{t_1+h}]$. Obtain and save $E_{t_1}[\tilde{y}_{t_1+h}]$. Note: for h=0 this is \tilde{y}_{t_1} so we have the first date done!

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- Result: full distribution of counterfactual evolution under new rule.

Taking Stock

• We know now how to implement the method!

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Taking Stock

- We know now how to implement the method!
- Moving Forward:
 - 1. Empirical evidence on policy shocks is the key missing object.
 - 2. Given that, it is particularly important to understand how different models extrapolate. Our results: RANK vs. HANK is not as important as behavioral vs ratex.

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- Non-fundamental shocks move asset prices significantly. (De Long et al., 1990; Gabaix and Koijen, 2021)
- Also generate non-trivial macro fluctuations.
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- Also generate non-trivial macro fluctuations.
- Q: how should monetary policy be conducted in this context?
- (Bernanke and Gertler, 2000, 2001): focus on macro.

 "There is no significant additional benefit to responding to asset prices."

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Caballero, Caravello, and Simsek (2024): FC Targeting

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 - Lower risk ⇒ financial markets become more *elastic*
 - More elastic markets ⇒ less financial volatility
 - Less financial volatility ⇒ Less macro volatility.
- Policy Counterfactuals: FCT lowers financial and macro volatility.
- The model in the paper does not fit since noise shocks enter nonlinearly Petals

$$p_0 = \ldots + \frac{\sigma_r^2}{\alpha} \mu_0$$

Methodological contribution: need to deal with this.

We generalize MW to allow for noise shocks

Extended set-up:

$$\mathcal{F}_{x}\mathbf{x} + \mathcal{F}_{z}\mathbf{z} + \mathcal{F}_{\mu}(\sigma_{r}^{2}\varepsilon_{\mu,0}) = \qquad \qquad \mathbf{0} \qquad \text{(Finance)}$$

$$\mathcal{H}_{x}\mathbf{x} + \mathcal{H}_{z}\mathbf{z} + \mathcal{H}_{\varepsilon}\varepsilon_{0} = \qquad \qquad \mathbf{0} \qquad \text{(Macro)}$$

$$\mathcal{A}_{z}\mathbf{z} + \mathcal{A}_{x}\mathbf{x} + \mathcal{A}_{v}v_{0} = \qquad \qquad \mathbf{0} \qquad \text{(Policy)}$$

Restriction: σ_r^2 only affects transmission of $\varepsilon_{\mu,0}$ & does so proportionally

Result: Under invertibility, Wold rep + Policy IRFs + identified noise shocks $\{\varepsilon_{u,t}\}$ are sufficient for counterfactuals

- S1. Use MW to obtain counterfactuals, including IRF to noise shock $\hat{\Theta}_{\ell,\mu}$
- S2. Scale it by variance $\tilde{\Theta}_{\ell,\mu} = \hat{\Theta}_{\ell,\mu} \frac{\tilde{\sigma}_r^2}{\sigma^2}$ where $\tilde{\sigma}_r^2$ is solved as a fixed point.

FCI-augmented Taylor rules would have stabilized gaps

• Augmented Taylor rules: $i_t = \rho_i i_{t-1} + (1 - \rho_i)(\phi_\pi \pi_t + \phi_y \tilde{y}_t + \psi(\overline{FCI}_t - FCI_t))$

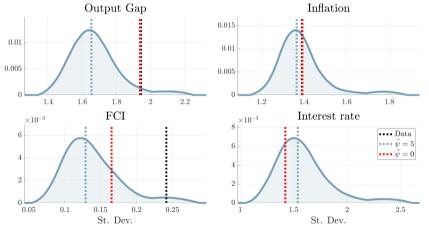


Figure: Benchmark Taylor $\psi=0$ (red). **FCI-augmented Taylor** $\psi>0$ (blue)

FCI-augmented dual mandate would have stabilized gaps

• $\min \sum_{t=0}^{\infty} \beta^t \left[\pi_t^2 + \tilde{y}_t^2 + \lambda_{\Delta i} (i_t - i_{t-1}) + \psi(\overline{FCI}_t - FCI_t))^2 \right]$ s.t implementation lag

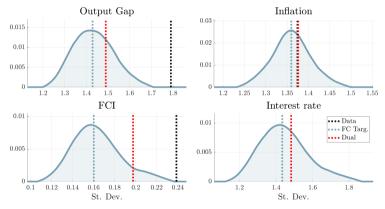
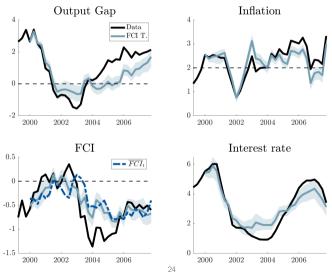


Figure: Flexible Dual Mandate $\psi=0$ (red). Optimal **FCI targeting** ψ^* (blue)

FCI targeting would have stabilized gaps before GFC



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Appendix

Wold VAR: specification details >Ba

- Use unemplyoment, GDP, Investment, Consumption, Hours, TFP, labor productivity, labor share, inflation (GDP deflator), Fed Funds rate.
- Unemployment, inflation and Fed Funds rate are in levels. Everything else is detrended using Hamilton (2018) filter.
- Sample 1960Q1:2019Q4, extend for Covid counterfactual.

Finance Block

- Assets: stock, risk-free bond
- Traders: arbitrageurs (α) , noise (1α)

$$\omega_t^{\mathcal{A}} = rac{E_t[r_{t+1}] + rac{\sigma_{t,r_{t+1}}^2}{2} - r_t^f}{\sigma_{t,r_{t+1}}^2}$$
 $\omega_t^{\mathcal{N}} = 1 + rac{\mu_t}{1 - lpha}$

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$$\Rightarrow E_{t}[r_{t+1}] = r_{t}^{f} + \frac{1}{2}\sigma_{t,r_{t+1}}^{2} - \frac{\mu_{t}}{2}\sigma_{t,r_{t+1}}^{2}$$

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The impact of noise shocks is increasing in return variance.

Finance Block

- Assets: stock, risk-free bond
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Macro Block

- Output-Asset Price $y_t = m + p_t + \delta_t$
- Potential Output $y_t^* = y_{t-1}^* + z_t$
- C-S decomposition $r_{t+1} = \rho (1 \beta) m + (1 \beta) y_{t+1} + \beta p_{t+1} p_t$
- Policy closes the model

Optimal Policy Back

• Fed chooses r_t^f before observing μ_t . Denote $\underline{E}_t[x] \equiv E[x|\mathcal{I}_t - \{\mu_t\}]$.

Optimal Policy Back

- Fed chooses r_t^f before observing μ_t . Denote $\underline{E}_t[x] \equiv E[x|\mathcal{I}_t \{\mu_t\}]$.
- Operational CB does FC Targeting:

$$G^{FCI}(x_t; \bar{p}_t) = \min_{r_t^f, \bar{p}_{t+1}} \underline{E}_t \left[(\tilde{y}_t)^2 + \psi(p_t - \bar{p}_t)^2 \right] + \beta \underline{E}_t [G^{FCI}(x_{t+1}; \bar{p}_{t+1})]$$
 (6)

where \overline{p}_{t+1} denotes an FC target committed one period in advance.

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where \overline{p}_{t+1} denotes an FC target committed one period in advance.

• We evaluate losses using the *original* objective function.

$$G\left(\psi\right) = \underline{E}_{t} \left[\sum_{h=0}^{\infty} \beta^{h} \left(y_{t+h} \left(\psi \right) - y_{t+h}^{*} \right)^{2} \right] \tag{7}$$

Proposition (Stabilization Effects of FC Targeting)

Suppose the planner follows the FCI targeting policy in (6) with $\psi \geq 0$. Then in equilibrium, the output gap is

$$\tilde{y}_t = (\varepsilon_{\delta,t} - \varepsilon_{z,t}) \frac{\psi}{1 + \psi} + \varepsilon_{\mu,t} \frac{\sigma_r^2(\psi)}{\alpha}.$$
 (8)

The present discounted value of squared gaps defined in (7) is

$$G_t(\psi) = \frac{\left(\sigma_z^2 + \sigma_\delta^2\right) \left(\frac{\psi}{1 + \psi}\right)^2}{1 - \beta} + \frac{\sigma_\mu^2 \left(\frac{\sigma_r^2}{\alpha}\right)^2}{1 - \beta} \tag{9}$$

We have $\frac{dG_t(\psi)}{d\psi}|_{\psi=0} < 0$. Thus, $\psi^* = \arg\min_{\psi \geq 0} G_t(\psi) > 0$.

- Starting from $\psi = 0$, macro stabilization losses are second order.
- Macro gains of financial stabilization are first order $\Rightarrow \psi^* > 0$ Back