

# Public Debt and $r^*$

*ChatGPT Explores How Public Debt Could Shape  $r$ -star*

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## Introduction

Public debt is a cornerstone issue for both economists and policymakers. But beyond the question of whether a government should borrow more or less, there's a deeper puzzle: how does public debt influence  **$r$ -star**, the natural rate of interest? Understanding this dynamic is key to grasping the long-term interplay between fiscal policy and macroeconomic stability.

In this post, we'll break down the various channels through which public debt shapes  $r$ -star and explore why maintaining debt sustainability is essential to keeping  $r$ -star in check. Let's dive into the world where fiscal policy and interest rates converge!

## What is $r$ -star?

Before tackling the intricate relationship between public debt and  $r$ -star, let's clarify what  **$r$ -star** represents. It's the real interest rate that keeps the economy on an even keel—neither stimulating nor restraining growth. Essentially, it's where savings and investment reach equilibrium, maintaining stable inflation and full employment.  $r$ -star is a fundamental anchor for monetary policy.

But how does government borrowing affect this seemingly delicate balance?

## Debt Sustainability: The Vital Condition

To comprehend the link between public debt and  $r$ -star, we first need to understand the **debt sustainability condition**. It serves as a rule of thumb for ensuring that a government's debt doesn't spiral out of control, causing economic upheaval.

Mathematically, debt sustainability is framed like this:

$$\Delta d_t \leq (r - g)d_{t-1}$$

Where:

- $d_t$  = debt-to-GDP ratio
- $r$  = real interest rate (or the cost of borrowing)
- $g$  = real GDP growth rate

This formula tells us that for debt to be sustainable, the growth rate of debt should not exceed the difference between the interest rate and the GDP growth rate. If the debt sustainability condition holds, markets remain confident in a government's ability to manage its debt, keeping long-term interest rates stable. But if it fails, that confidence falters, potentially causing long-term interest rates, including  $r$ -star, to rise.

## Transmission Channels: How Public Debt Affects $r$ -star

Now let's explore the primary channels by which public debt influences  $r$ -star. These mechanisms are crucial to understanding how government borrowing affects the broader economy.

### 1. Crowding Out Private Investment

Excessive government borrowing can lead to **crowding out**, where the government competes with private firms for available capital. As a result, interest rates rise, making it more expensive for businesses to borrow and invest. This reduction in private investment distorts the savings-investment balance, pushing  $r$ -star upward.

However, when debt is kept within sustainable bounds, the crowding-out effect is limited, leaving  $r$ -star more stable.

### 2. Market Perception and the Risk Premium

Investors are keenly aware of a government's debt levels. If they perceive the debt as risky, they demand a higher **risk premium**—essentially compensation for taking on additional risk. This raises long-term interest rates, feeding directly into a higher  $r$ -star.

When debt remains sustainable, market confidence keeps risk premiums low, allowing  $r$ -star to align with underlying economic conditions rather than risk perceptions.

### 3. Expectations of Fiscal Policy Adjustments

High debt often creates expectations that future governments will need to adjust fiscal policy, likely through **tax hikes** or **spending cuts**. Such expectations can influence behavior: households and businesses may start saving more in anticipation of harder times, driving down  $r$ -star.

On the other hand, if debt is well managed, expectations of fiscal tightening are subdued, keeping  $r$ -star tied to real economic drivers like productivity growth.

#### 4. Fiscal Policy Flexibility

Sustainable debt levels afford governments greater **fiscal policy flexibility**. In times of economic downturn, they can use fiscal tools to stimulate demand without spooking markets. This flexibility can smooth fluctuations in  $r$ -star, helping stabilize the economy.

Conversely, high debt constrains fiscal maneuverability. With fewer tools at their disposal, governments might see  $r$ -star fall as growth expectations sour.

#### 5. Global Capital Flows

In today's interconnected financial world, public debt in major economies can affect **global capital flows**. When markets perceive debt in large economies as risky, investors demand higher returns, pushing global interest rates higher. This global crowding-out effect elevates  $r$ -star internationally.

However, sustainable debt in key economies can help stabilize global interest rates, anchoring  $r$ -star worldwide.

### Conclusion

Public debt has a significant, multifaceted impact on  **$r$ -star**—the natural rate of interest. Whether through crowding out, risk premiums, or fiscal expectations, government borrowing can either push  $r$ -star higher or keep it stable. The key to managing this delicate balance lies in maintaining **debt sustainability**. When governments borrow responsibly, the economy's natural interest rate remains grounded in fundamental factors like productivity and demographics, rather than debt-driven risks.

In the end, the relationship between public debt and  $r$ -star underscores the broader importance of prudent fiscal policy. By carefully managing debt, governments can maintain a stable  $r$ -star, fostering long-term economic growth without letting borrowing costs spiral out of control.