

PSTAT 175: Lab D

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Today

- ▶ Review: Cox PH Model
- ▶ Review: Log-Log Plot
- ▶ Stratified Model

veteran dataset

We will still use veteran data set in survival package from Veterans' Administration Lung Cancer study.

```
head(veteran)
```

##	trt	celltype	time	status	karno	diagtime	age	prior
## 1	1	squamous	72	1	60	7	69	0
## 2	1	squamous	411	1	70	5	64	10
## 3	1	squamous	228	1	60	3	38	0
## 4	1	squamous	126	1	60	9	63	10
## 5	1	squamous	118	1	70	11	65	10
## 6	1	squamous	10	1	20	5	49	0

veteran dataset

- ▶ trt: 1=standard 2=test
- ▶ celltype: 1=squamous, 2=smallcell, 3=adeno, 4=large
- ▶ time: survival time
- ▶ status: censoring status
- ▶ karno: Karnofsky performance score (100=good)
- ▶ diagtime: months from diagnosis to randomisation
- ▶ age: in years
- ▶ prior: prior therapy 0=no, 10=yes

See [R: Veterans' Administration Lung Cancer study](#) for more details.

Review: Cox PH Model

Semiparametric model for hazard function:

$$h(t, X) = h_0(t)e^{\sum_{i=1}^p \beta_i X_i}.$$

- ▶ $h_0(t)$ is called *the baseline hazard function*.
- ▶ $h_0(t)$ only relies on t .
- ▶ Time-independence.

Review: Cox PH Model

We want to see if there is a significant difference between cancer cell types.

```
fit = coxph(Surv(time,status)~celltype,data=veteran)
summary(fit)
```

Review: Cox PH Model

call:

```
coxph(formula = surv(time, status) ~ celltype, data = veteran)
```

n= 137, number of events= 128

	coef	exp(coef)	se(coef)	z	Pr(> z)	
celltypesmallcell	1.0013	2.7217	0.2535	3.950	7.83e-05	***
celltypeadeno	1.1477	3.1510	0.2929	3.919	8.90e-05	***
celltypelarge	0.2301	1.2588	0.2773	0.830	0.407	

signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

	exp(coef)	exp(-coef)	lower .95	upper .95
celltypesmallcell	2.722	0.3674	1.656	4.473
celltypeadeno	3.151	0.3174	1.775	5.594
celltypelarge	1.259	0.7944	0.731	2.168

Concordance= 0.608 (se = 0.029)

Rsquare= 0.166 (max possible= 0.999)

Likelihood ratio test= 24.85 on 3 df, p=2e-05

wald test = 24.09 on 3 df, p=2e-05

Score (logrank) test = 25.51 on 3 df, p=1e-05

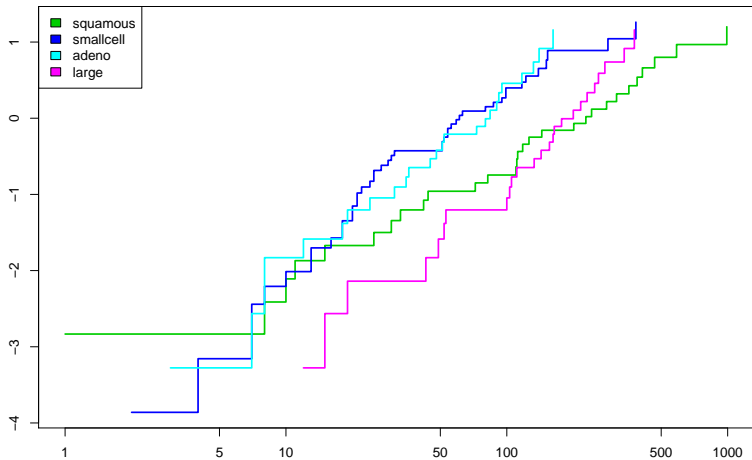
Figure 1: summary(fit)

Review: Log-Log Plot

We can use the following codes to draw the log-log plot:

```
veteran.km = survfit(Surv(time,status)~celltype,  
                     data=veteran)  
plot(veteran.km, fun='cloglog', col=3:6,lwd=2)  
#levels(veteran$celltype)  
legend('topleft',c("squamous","smallcell",  
                   "adeno","large"),fill = 3:6)
```


Review: Log-Log Plot



Review: Cox PH Model (with covariates)

We want to test the effect of `celltype`, controlling the `diagtime` covariate.

```
fit2 = coxph(Surv(time,status)~celltype+diagtime,  
             data=veteran)  
fit3 = coxph(Surv(time,status)~diagtime,data=veteran)  
#summary(fit2)  
#summary(fit3)
```

Review: Cox PH Model (with covariates)

Call:

```
coxph(formula = Surv(time, status) ~ celltype + diagtime, data = veteran)
```

n= 137, number of events= 128

	coef	exp(coef)	se(coef)	z	Pr(> z)	
celltypesmallcell	0.982017	2.669835	0.254398	3.860	0.000113	***
celltypeadeno	1.180827	3.257068	0.294902	4.004	6.22e-05	***
celltypelarge	0.234520	1.264302	0.277552	0.845	0.398133	
diagtime	0.009137	1.009179	0.008539	1.070	0.284562	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

	exp(coef)	exp(-coef)	lower .95	upper .95
celltypesmallcell	2.670	0.3746	1.6216	4.396
celltypeadeno	3.257	0.3070	1.8273	5.806
celltypelarge	1.264	0.7910	0.7338	2.178
diagtime	1.009	0.9909	0.9924	1.026

Concordance= 0.622 (se = 0.03)

Rsquare= 0.172 (max possible= 0.999)

Likelihood ratio test= 25.86 on 4 df, p=3e-05

Wald test = 25.38 on 4 df, p=4e-05

Score (logrank) test = 26.86 on 4 df, p=2e-05

Figure 2: summary(fit2)

Review: Cox PH Model (with covariates)

```
call:
coxph(formula = Surv(time, status) ~ diagtime, data = veteran)

n= 137, number of events= 128
```

	coef	exp(coef)	se(coef)	z	Pr(> z)
diagtime	0.009100	1.009142	0.008978	1.014	0.311

	exp(coef)	exp(-coef)	lower .95	upper .95
diagtime	1.009	0.9909	0.9915	1.027


```
Concordance= 0.509 (se = 0.03 )
Rsquare= 0.007 (max possible= 0.999 )
Likelihood ratio test= 0.91 on 1 df, p=0.3
Wald test = 1.03 on 1 df, p=0.3
Score (logrank) test = 1.02 on 1 df, p=0.3
```

Figure 3: summary(fit3)

Review: Cox PH Model (with covariates)

Degree of Freedom is:

$$df = 4 - 1 = 3.$$

Two ways to compute the likelihood ratio statistic:

```
#lrt2 = 2*(fit2$loglik[2]-fit3$loglik[2])  
#pchisq(lrt2, df=3, lower.tail = FALSE)  
lrt1 = summary(fit2)$logtest[1] - summary(fit3)$logtest[1]  
pchisq(lrt1, df=3, lower.tail = FALSE)
```

```
##          test  
## 1.583109e-05
```

p-value is small \implies the effect of celltype is significant if we consider diagtime

Review: Cox PH Model (PH assumption)

`cox.zph()` is used to test the Proportional Hazards Assumption of a Cox Regression.

```
cox.zph(fit2)
```

##	rho	chisq	p
## celltypesmallcell	0.05683	0.43383	0.5101
## celltypeadeno	0.14724	2.93832	0.0865
## celltypelarge	0.20260	5.32714	0.0210
## diagtime	0.00401	0.00221	0.9625
## GLOBAL	NA	7.08153	0.1316

p-value is small ($0.0210 < 0.05$) \implies the PH assumption is violated.

Stratified Cox PH Model

According to our analysis, the celltype may rely on time t (or the baseline may rely on celltype). For different celltype, we use different baseline. (the parameters of diagtime are same.)

```
fitSC = coxph(Surv(time,status)~diagtime+strata(celltype),  
              data=veteran)  
summary(fitSC)
```

Stratified Cox PH Model

call:

```
coxph(formula = Surv(time, status) ~ diagtime + strata(celltype),  
      data = veteran)
```

n= 137, number of events= 128

	coef	exp(coef)	se(coef)	z	Pr(> z)
diagtime	0.009883	1.009932	0.008323	1.187	0.235

	exp(coef)	exp(-coef)	lower .95	upper .95
diagtime	1.01	0.9902	0.9936	1.027

Concordance= 0.533 (se = 0.059)

Rsquare= 0.009 (max possible= 0.993)

Likelihood ratio test= 1.23 on 1 df, p=0.3

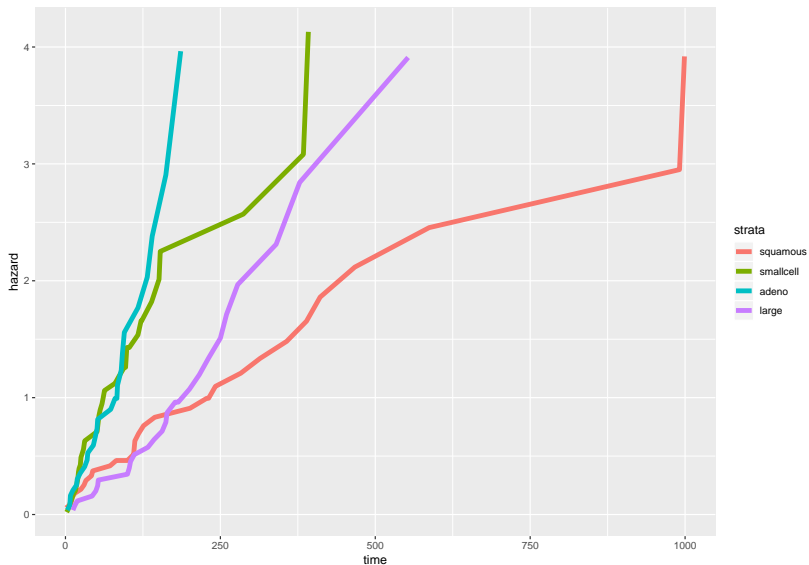
wald test = 1.41 on 1 df, p=0.2

Score (logrank) test = 1.42 on 1 df, p=0.2

Figure 4: summary(fitSC)

Stratified Cox PH Model

We can plot their baseline hazard function using `basehaz()` function:



Stratified Cox PH Model

Codes:

```
bhaz = basehaz(fitSC)
ggplot(bhaz)+
  geom_line(aes(x=time,y=hazard,colour=strata), size=2)
```

Stratified Cox PH Model

Finally, we want to see if there is a significant interaction between diagtime and celltype.

```
fitSC = coxph(Surv(time,status)~diagtime+strata(celltype),  
#Fit the stratified model with interaction :  
fitSC.int = coxph(Surv(time,status)~  
                  strata(celltype)*diagtime, data=veteran  
#Compute GLRT statistic:  
lrt = 2*(fitSC.int$loglik[2]-fitSC$loglik[2])  
#p-value:  
pchisq(lrt,df=3,lower.tail = FALSE)
```

```
## [1] 0.1739869
```

p-value is large \Rightarrow the interaction term is not significant