A Switched-Capacitor Amplifier for Use in a 2.5bit/stage Pipelined Analog-to-Digital Converter

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Abstract—A switched-capacitor amplifier with a nominal gain of 4 was designed for use in a 2.5 bit/stage pipelined analog-to-digital converter (ADC). The total resolution of the ADC was 10 bits. The sample rate of the ADC was 5kS/s. During the sample phase, differential input voltage was sampled onto 4 capacitors on each differential input. During the hold phase, the stored charge was transfered onto 1 hold capacitor in feedback around an operational transconductance amplifier (OTA). The OTA consisted of a pMOS-input folded cascode stage followed by an nMOS common source stage. The open loop DC gain of the OTA was 110.9dB. The unity gain bandwidth of the OTA was 87.1kHz. The circuit consumed 769.5nW of DC power. Using DC power, this amplifier achieved a Figure of Merit of 150fJ per conversion step.

Index Terms—switched-capacitor amplifier, pipelined analogto-digital converter

I. INTRODUCTION

PIPELINED ADCs require accurate amplification in each stage for proper operation. The residue of each stage must be amplified to be properly processed by the subsequent stage. Pipelined ADCs implementing 2.5 bits per stage with comparator redundancy require a gain of 4.

Switched-capacitor amplifiers are ideal for accurate amplifiers. Since the gain of switched-capacitor amplifiers relies only on ratios of capacitors (as opposed to ratios of multiple types component values), the gain of these amplifiers tends to be quite accurate.

II. SYSTEM LEVEL DESIGN

A. Top Level Schematic

The schematic overall system level design is shown in Figure 1. With ideal switches and ideal OTA, this schematic yields an exact gain of 4. This section overviews the specifications for each of these components.

B. Common Mode Voltage

We know that the common mode voltage at the input and output nodes should be the same for proper operation of the device. To maximize the voltage swing at the output, we must choose V_{CM} to be exactly at mid-rail. Thus,

$$V_{cm} = \frac{V_{DD}}{2} = 0.9V \tag{1}$$

C. Full Scale Voltage

In our design, we can assume that the output of the OTA can swing between V_{ov} and $V_{DD}-V_{ov}$. If we choose our V_{FS} to occupy the entire swing at the output and make the assumption that $V_{ov}\approx 0.2V$, we find that

$$V_{FS} = (V_{DD} - V_{ov}) - V_{ov} = 1.4V$$
 (2)

D. Least Significant Bit Voltage

In our differential amplifier topology, the output can swing from $-V_{FS}$ to V_{FS} . Thus, we can calculate our least significant bit voltage as

$$V_{LSB} = \frac{2V_{FS}}{2^{10}} = 2.73mV \tag{3}$$

E. Sample and Hold Capacitors

We can find the minimum value of the hold and capacitor values from the noise requirements. The specification requires that the noise stored on the capacitors in the circuit be less than half of the quantization noise in the given ADC stage.

Since this is a differential circuit, each half of the circuit contributes noise to the differential input nodes of the OTA. The noise power of each half circuit adds at these inputs. Since there are four capacitors in parallel during the sample phase, their equivalent capacitance is four times a single sample capacitor. Thus, we can calculate the minimum sample capacitance as

$$C_{samp,min} = \frac{kT}{2\left(\frac{V_{LSB}^2}{24}\right)} = 6.65fF$$
 (4)

We found that using sample capacitances in this range provided unacceptable closed loop responses when used in the complete system. In the case of $C_{samp}=15fF$ a full scale input step, output values were approximately $8V_{LSB}$ higher than V_{FS} . This result was unacceptable. We found that to have the error at the output be $\approx V_{LSB}$, we required $C_{samp}=150fF$. The various parasitic capacitances throughout the system level design, especially at the inputs to the OTA, were believed to have necessitated the difference between the minimum tolerable capacitance due to noise and the implemented capacitance.

F. Switches

The implementation of the switches used were complimentary pass transistors, as shown in Figure 2. The width and length of the pMOS and nMOS transistors were chosen to be

$$R_{on} = \frac{1}{(\beta_n + \beta_p) \left(\frac{W}{L}\right) V_{ov}} \tag{5}$$

For minimum sized devices in width and length, $R_{on}=11520\Omega$. Even this value provided a sampling phase time constant that was much faster than required.

G. Clocks

The clocks used were two non-overlapping clocks, each with a frequency of 5kHz. The non-overlapping clocks were buffered by a set of the three inverters as shown in Figure 3.

H. System Level Component Values

The sizes of the transistors used in the switches and clock buffers are shown in Table I. The sizes of the sample and hold capacitors are shown in Table II.

I. OTA Parameters

From our settling requirements, we can find both the required unity gain bandwidth and DC gain for the OTA.

For a full scale step input, the input referred error must be less than $\frac{V_{LSB}}{4}$. This corresponds to an error at the output of V_{LSB} . To determine our specifications, we can allocate half of this error to gain error and the other half to settling error.

For the allocated error of $\frac{V_{LSB}}{2}$ due to gain error at the output, the required closed loop DC gain can be found as

$$A_f = \frac{V_{FS} - \frac{V_{LSB}}{2}}{\frac{V_{FS}}{4}} = 3.9961 \tag{6}$$

This closed loop gain, with $\beta = \frac{1}{4}$, corresponds to an open loop gain of

$$A = \frac{A_f}{1 - A_f \beta} = 72.2dB \tag{7}$$

For the allocated error of $\frac{V_{LSB}}{2}$ due to settling error at the output, the acceptable percentage error can be found as

$$E_{percent} = 1 - \frac{V_{FS} - \frac{V_{LSB}}{2}}{V_{FS}} = 9.7 \times 10^{-2}\%$$
 (8)

This corresponds to having settled for 6.9315τ . For a sampling rate of 5kS/s, our required 3dB bandwidth of the closed loop system is 11.0kHz. For $\beta=\frac{1}{4}$, this corresponds to a unity gain bandwidth of 44.1kHz.

III. TRANSISTOR LEVEL OTA DESIGN

The transistor level implementation of the OTA is shown in Figure 4.

A. Gain Stage

The OTA implemented a folded-cascode stage followed by a common source stage. This topology was chosen for a number of reasons. First, the required DC gain necessitated an open loop gain on the order of $\approx (g_m r_o)^3$. Second, an output common source stage allowed for the use of a Miller compensation capacitor. Since the required unity gain bandwidth was small, a Miller compensation capacitor could enable a phase margin well in excess of 60 degrees. Third, an output common source stage allows for more output voltage swing than an output cascode stage.

After choosing a sampling capacitor value $C_{samp}=150 fF$, the compensation capacitor was chosen to be $C_{comp}=5C_{samp}=750 fF$. To calculate our bias currents in each branch, we first chose that the current in the common source stage was twice the tail current of the folded cascode stage. We can estimate the minimum acceptable bias current of the common source stage as follows. We know that the maximum slew rate our system could encounter will be given by

$$slew_{max} = \frac{2V_{FS}}{\frac{1}{2f_s}} = 28k\frac{V}{s} \tag{9}$$

2

since our output can change from one full scale voltage to the other during just one hold phase of the clocks.

Since we can relate the slew rate and the compensation capacitance to the current, we find

$$I_{slew} = I_{bias,cs} = C_{comp} slew_{max} = 21nA$$
 (10)

Given this minimum bias current, we chose the bias current of the common source stages to be 70nA to ensure settling occurred with the requisite accuracy. This choice yields a folded cascode tail current of 35nA.

To maximize the amount of DC gain that was achieved for this current, transistors M2, M3, M6, M7, M8, M9, M12 and M13 were placed into weak inversion; their inversion coefficients were chosen to be 0.1. Having decreased f_T for these transistors was acceptable since the required unity gain bandwidth of the circuit was so low.

B. Biasing

The majority of the biasing transistors were biased in moderate-strong inversion. Their inversion coefficients were chosen to be around 2. These included transistors M1, M4, M5, M10, M11, M14, M15, M22, M23, M25, M27, M29, M31, M32, M33, M34, M35, M36, M39 and M37. To achieve accurate current mirroring through all of the bias branches, transistors such as M24, M28 and M32 were implemented to set matching drain voltages on other bias transistors.

Since many of the transistor lengths calculated were above the maximum transistor length, in many cases transistors were stacked with their gates connected to achieve an equivalent transistor of the appropriate length. Transistors M25a to M25f form a single equivalent M25 with six times the length of one of the transistors in the stack.

C. Component Values

Table II shows the values of the passive elements used in the OTA. Table X-C shows the sizes of the transistors used in the OTA.

IV. OPEN LOOP OTA RESULTS

Upon completion of our OTA design, we performed various open-loop simulations to verify that we had met our required specifications.

A. Open Loop Differential Frequency Response

Keeping the entire switch capacitor system in perspective, the most important specs for us to hit were those for differential gain for total accuracy and unity-gain bandwidth (UGB) for total speed. Therefore, we measured those performance values for our OTA first. As can be seen in our differential gain plot (Figure 5), we successfully hit our specs for gain and UGB across all three PVT corners (see Table III). The plot also shows that we were able to use compensation capacitance to push our dominant pole to a very low frequency ($\approx 0.1 Hz$).

We also plotted the phase response of our open loop OTA (see Figure 6). From this plot, the low frequency pole seen in the gain response is confirmed. In addition, it can clearly be seen that the additional poles and the zero created by the compensation capacitor has been pushed out beyond our unitygain bandwidth. Our phase margin measurements are shown to be very consistent across PVT corners and all above our spec (see Figure III).

B. Open Loop Common Frequency Mode Response

In order for our OTA to be robust against common-mode noise, it is important for the common mode gain to remain very low across all frequencies. As can be seen in our plots for common mode gain (Figure 7) and common mode phase (Figure 8), common mode changes on the input have a very limited effect on the output.

C. Common Mode Feedback Frequency Response

Our goal in developing a common mode feedback (CMFB) network was to provide circuitry to hold our output node at V_{CM} . To ensure that our circuit was functioning as we intended, we broke our feedback loop at the input of the CMFB network and stimulated the circuit with a small signal source. We then measured the output of the CMFB circuit at the node that feeds back to our cascade branch. Our results can be seen in figures 9 and 10.

V. CLOSED LOOP AMPLIFIER RESULTS

After we verified that we had met our open loop OTA specifications, we replaced the ideal OTA in our system level design with our own OTA design to verify that we still met the system level specifications.

A. Nyquist Rate Sinusoidal Transient Response

The first test we ran on our system was a sine wave input at our full-scale amplitude and the Nyquist frequency. As can be seen in our plot (Figure 11), our system samples the input at the end of the sample phase to be $0.35V\ (V_{FS})$. Over the course of the hold phase, the output slews and then settles linearly to a value of 1.402V. This is within our maximum error value (shown below) and shows that our circuit successfully handles a sine wave input. The maximum input referred error we can tolerate is

$$4 * \frac{V_{LSB}}{2} = 5.4mV \tag{11}$$

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B. Small Step Transient Response

The second test we performed on our closed loop system was a small step input. As can be seen in figure 12, our output shows a fast settling with little to no slewing. We provided an input step of 2mV and observed the output to settle to 8.012mV at the end of the hold phase. This is well within our spec for error so this test was successful.

C. Full Scale Step Transient Response

The third test we performed on our closed loop system was a step input at the full-scale voltage. The results of this test closely resembled those of the sine wave input. The reason for this is that the input is again sampled at the full-scale voltage and the output settles accordingly. This test was successful.

D. Sawtooth Transient Response

The fourth and final test we performed on our closed loop system was a sawtooth input at $f_s/20$. As can be seen from our plot in figure 14, our system has no problem settling to the correct output for small changes in the input (along the ramp of the sawtooth). In addition, our output settles to the correct output in time after the edge of the sawtooth when the input drops from the full-scale voltage to the negative full-scale voltage.

E. Effective Number of Bits

F. Figure of Merit

We calculated our figure of merit based on both the DC power consumption of our system as well as the average overall power of our system. Both values of power are shown in table III and the FOM values are shown below.

$$FOM_{DC-POWER} = \frac{Power_{dc}}{2^{ENOB}f_s} = 150.3fJ \qquad (12)$$

$$FOM_{TOTAL-POWER} = \frac{Power_{total}}{2^{ENOB} f_s} = 441.4 fJ \quad (13)$$

G. Area

With the functionality of our system verified and its performance measured, we made an estimation of the area of our design. To measure the area of the transistors in the design, we used the below formula where $L_{diff}=0.48\mu m$ and $\alpha=1.3$.

$$Area_{transistors} = W * (L + L_{diff}) * \alpha = 55.50pm^2$$
 (14)

To calculate the area of the capacitors in our circuit, we used the below formula across all of our capacitors where $C_{unit-area} = 1 f F / \mu m^2$.

$$Area_{capacitors} = \sum C/C_{unit-area} = 3.00nm^2$$
 (15)

Finally, to calculate the area of the resistors in our circuit, we used the below formula across all of the resistors in our design where $R_s = 10\Omega/\mu m^2$.

$$Area_{resistors} = \sum R/R_s = 8.00 \mu m^2 \tag{16}$$

Adding the above results for area, we came to a total area estimation as shown below.

$$Area_{total} = 8.0036\mu m^2 \tag{17}$$

VI. SUMMARY OF RESULTS

As can be gathered from our numerical results, we successfully reached the goal we set out to accomplish. We designed a 10bit, 5ksample/s amplifier for use in a 2.5bit/stage pipelined analog-to-digital converter which settles to an input referred error value less than $\frac{V_{LSB}}{2}$. In the process of designing this amplifier, we were able to maintain a very low value of total power consumption and as a result, a very respectable figure of merit. Thanks to a well thought out design process, we built and amplifier that not only meets its specs, but also maintains those specs over all PVT corners. If this design was put onto silicon and distributed to customers, we believe that it would prove to be robust enough to handle constant unpredictable use.

VII. POSSIBLE IMPROVEMENTS

While most of the specifications of our finished amplifier are impressive, one that needs optimization is the total area. Because we originally set out to meet a more stringent specification for gain, we were forced to utilize two 40Ω resistors in the CMFB circuit. These two resistors account for the vast majority of the design's area. Because we ultimately were able to attain a gain far greater than the requirement, in future optimizations of the design we would focus on bringing the value (and hence size) of these resistors down to a more reasonable value. In addition, we believe that with redesign of the OTA, we can achieve a much lower power consumption and utilize much smaller compensation capacitors.

VIII. CONCLUSION

Through the design of this amplifier, we were able to attain a good deal of knowledge on new circuit techniques as well as design process. Unlike some of our previous designs, we spent a very long time developing our ideas on paper until we were satisfied that they would give us the results we were looking for. Thanks to this patience, once we put our theories into simulation, we were very pleased with the results. We were able to hit our spec after the first iteration of design and we spent most of the remaining design time optimizing for power and accuracy. This project is quite appropriate for the class because it allows a broad range of students with different backgrounds to show interest. Because the design requires some knowledge of digital theory in addition to the heavy analog theory, a strong need for collaboration was instilled and led to a much more organic learning environment.

IX. SEMINAR RESPONSES: JOSEPH MEYER

A. Dr. Deepnarayan Gupta: Superconductor Electronics and Digital-RF Technology

Dr. Gupta's seminar covered a vague interest of mine: combining superconductor and semiconductor electronics. Before this lecture, I wondered why these sorts of circuits taking advantage of superconductors' almost magical properties weren't more common. It seems that the main reason why these types of systems aren't more common are actually pretty obvious: you need to cool the systems down to 4K. More so than requiring a lot of power, the cooling systems consume a large amount of space, at least a couple of cubic feet. That sort of space requirements make these systems impractical in many scenarios.

Dr. Gupta said that biggest advantage of these systems is the high sensitivity. Indeed, I don't think thermal noise is going to be much of an issue at 4K. Dr. Gupta also mentioned that the primary limiting factors in these systems involved the analog to digital converters and the reliable packaging. The interconnects between modules must be able to handle data transfer at the high frequencies at which these circuits are operating.

I was especially intrigued as to why some the systems from HYPRES involved both high and low temperature superconductors. I asked Dr. Gupta this question and he responded back that having different stages of temperatures allowed for an easier heat load on the low temperature superconductors.

B. Dr. Simone Gambini: More than Moore Comes of Age

Dr. Gambini's lecture provided an interesting and different view about the future of devices. I've typically heard about whats the big, new thing that is going to REPLACE CMOS. Graphene, carbon nanotubes, and quantum electronics all come to mind. However, Dr. Gambini argued more that the future isn't what is going to replace CMOS, but what is going to work with it. Future microelectornic systems will have the ability to interface with many more new different technologies such as silicon photonics, sensors, MEMS devices, printed transistors and other semiconductor materials. Designers of

the future must be able to cover larger different design spaces to create optimal systems.

I found the ideas about circuits embedded into people that sent out information "off body" more than mildly interesting. Specifically, the fact that transmitter design in these systems was vastly more important than receiver design since the transmitter must do its work from within the body.

I was a little skeptical about the ideas and results on the study of the brain that was done. The assumption that any part of the channels of neurons in the brain act linearly seems to me to be overly optimistic. He was pretty upfront about the challenges associated with stimulating and measuring the brain at the same time. We might find that this is all but impossible.

C. Dr. Junhua Shen: The Journey to High Speend and High Resolution SAR ADCs

It is well know that there are immediate tradeoffs in converter design between speed, resolution and power. Dr. Shen showed ways in which to maximize the performance of an ADC by combining elements of various kinds. SAR ADCs are known for being accurate; but slow. The ADC that Dr. Shen presented got around some of the latency problems of a typical SAR ADC by determining the first 5 or so bits with a simpler and faster flash architecture. The inaccuracies and non-idealities of the flash were compensated by redundancies in the bits of the SAR part of the design.

One theme for achieving better performance in design was to convert offset errors and mismatch into noise errors by implementing extra bits or an extra DAC which can be selected to be used. Having three DACs for use in the ADC caused problems when laying out the structure. Three of anything is harder to keep symmetric and even from a layout perspective than an even number of the same thing.

When asked, Dr. Shen said that disturbances caused by agressors and victims were the hardest problems faced through the design because of their unpredictability.

X. SEMINAR RESPONSES: MILES SHERMAN

A. Simone Gambini: More Than Moore Systems

Dr. Gambini gave an informative and interesting perspective on his work and the industry as a whole. While I was previously aware of a good amount of "More Than Moore" work being done, getting a feel for some specific projects was helpful for my understanding. The one aspect of this seminar that stuck with me was the fact that the noise associated with actually stimulating brain activity is actually larger than the brain's signal poses an interesting problem and a demand for a solution. There is definitely a lot of room for major development in this field.

B. Adad Abidi: Armstrong's Circuits & The Worldwide Spread of Radio

Of the three seminars I attended this semester, I would say this one was the most interesting for me. Dr. Abidi presented the work of Edwin Armstrong in a very specific way so as to motivate a connection between the work of the 1920's and the analog design of today. Armstrong's circuits played a major role in influencing the way we communicate today and it is clear when his fundamental designs are found in the large systems of analog communication chips in modern day devices. Armstrong's main focus in his work seems to be resourcefulness since vacuum tubes were so expensive. Modern day engineers can learn a lot from his work. Even though transistors are a commodity now, there is always optimization to be done.

C. Shanthi Pavan: Continuous-Time Delta Sigma Data Converters

This was the final lecture I attended and I probably had the most trouble following this one due to its more in depth technical discussion of a new topic for me. Dr. Pavan discussed new techniques for the elimination of clock-jitter and non-linearities in delta sigma converters. While I could not follow his exact method of innovation, I was certainly able to learn a good amount about the operation of delta sigma converters. These systems operate by oversampling the input at sampling rates much higher than those at the final output of the system. By doing this, the system can then modulate the noise and push it to higher frequencies than those of interest. The signal is then re-sampled and outputted.

TABLES 6

TABLE I SYSTEM LEVEL TRANSISTOR SIZES

Transistor	Width (nm)	Length (nm)	Aspect Ratio
Switch nMOS	190	180	1.055
Switch pMOS	190	180	1.055
Clock Buffer nMOS	1020	250	4.08
Clock Buffer pMOS	250	250	1

TABLE II
PASSIVE COMPONENT VALUES

Component	Value
Resistors	Ω
R0	40M
R1	40M
Capacitors	fF
C_{comp}	750
C_{hold}	150
C_{samp}	150

TABLES 7

Transistor	Width (nm)	Length (nm)	Aspect Ratio
M1 M2	300 750	8000 1000	0.0375 0.75
M3	750	1000	0.75
M4a	281	1000	0.73
M4b	281	10000	0.0281
M4c	281	10000	0.0281
M5a	281	10000	0.0281
M5b	281	10000	0.0281
M5c	281	10000	0.0281
M6	250	1330	0.188
M7	250	1330	0.188
M8	750	1000	0.75
M9	750	1000	0.75
M10a	281	7500	0.0375
M10b	281	7500	0.0375
M11a M11b	281 281	7500 7500	0.0375 0.0375
M110 M12	500	1000	0.0373
M12 M13	500	1000	0.5
M14	300	4000	0.075
M15	300	4000	0.075
M16	250	4000	0.0625
M17	250	4000	0.0625
M18a	250	6800	0.0368
M18b	250	6800	0.0368
M19a	250	6800	0.0368
M19b	250	6800	0.0368
M20a	281	10000	0.0281
M20b	281	10000	0.0281
M20c	281	10000	0.0281
M21	750	1000	0.75
M22a	300	8000	0.0375
M22b	300	8000	0.0375
M23	300	8000	0.0375
M24	1500	1000	1.5
M25a	250	10000	0.025
M25b M25c	250 250	10000 10000	0.025 0.025
M25d	250	10000	0.025
M25e	250	10000	0.025
M25f	250	10000	0.025
M26	750	1000	0.75
M27a	300	8000	0.0375
M27b	300	8000	0.0375
M28	250	1330	0.188
M29a	281	10000	0.0281
M29b	281	10000	0.0281
M29c	281	10000	0.0281
M29d	281	10000	0.0281
M29e	281	10000	0.0281
M29f	281	10000	0.0281
M30	750	1000	0.75
M31a M31b	300 300	8000 8000	0.0375 0.0375
M31b M32a	250	7500	0.0375
M33a	281	10000	0.0333
M33b	281	10000	0.0281
M33c	281	10000	0.0281
M33d	281	10000	0.0281
M33e	281	10000	0.0281
M33f	281	10000	0.0281
M34a	250	7330	0.0341
M34b	250	7330	0.0341
M34c	250	7330	0.0341
M35a	250	7500	0.0333
M35b	250	7500	0.0333
M36a	281	10000	0.0281
M36b	281	10000	0.0281
M36c	281	10000	0.0281
M36d	281	10000	0.0281
M36e	281	10000	0.0281
M36f	281	10000	0.0281
M37 M38	300 281	4000 3750	0.075 0.0749
		7500	0.0749
M39a	281	/ 10.00	(1015/7

TABLES 8

TABLE III
SUMMARY OF SPECIFICATIONS AND RESULTS

Specification	Specification Value	FF Result	TT Result	SS Result
Open Loop OTA DC Gain	72.20dB	102.38dB	110.86dB	112.57dB
Open Loop OTA Phase Margin	60^{o}	75.4^{o}	75.2^{o}	74.3^{o}
Open Loop OTA Unity Gain Bandwidth	44.10kHz	96.93kHz	87.34kHz	68.83kHz
DC Power Consumption	-	747.90nW	769.50nW	803.16nW
Overall Power Consumption	_	_	$2.26\mu W$	_
DC Figure of Merit	_	_	150.3 fJ	_
Overall Figure of Merit	_	_	441.4fJ	_
Overall Area	_	_	$8.0036 \mu m^2$	_

FIGURES 9

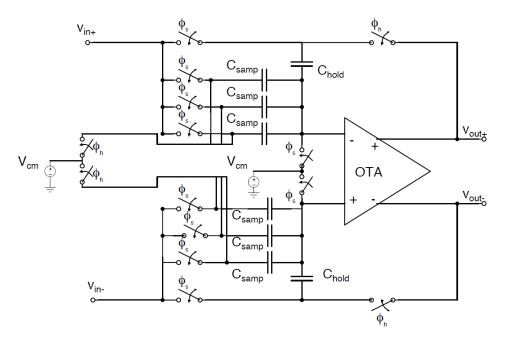


Fig. 1. The system level schematic of the switched-capacitor amplifier.

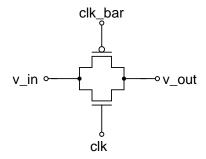


Fig. 2. The schematic of the complimentary pass transistors used as switches at the system level.

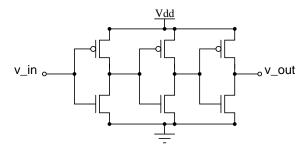


Fig. 3. The schematic of the complimentary pass transistors used as switches at the system level.

FIGURES 10

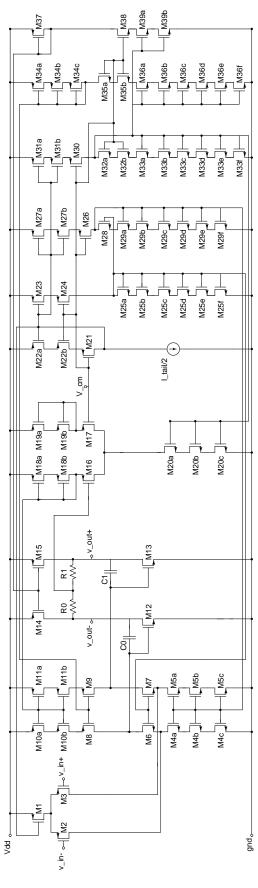


Fig. 4. The transistor level schematic diagram of the OTA.

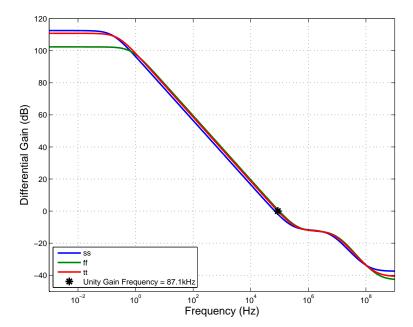


Fig. 5. The open loop differential gain magnitude response of the OTA.

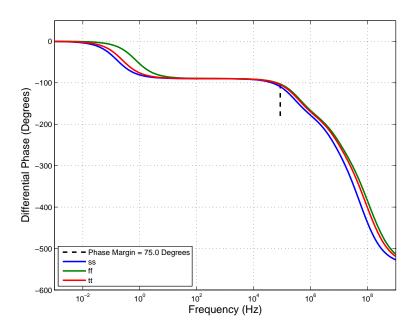


Fig. 6. The open loop differential gain phase response of the OTA.

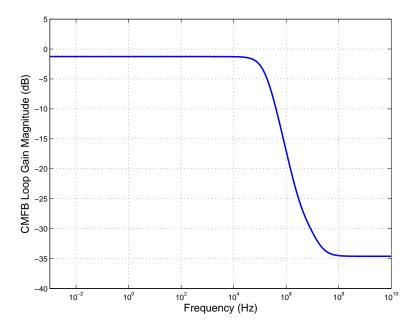


Fig. 7. The open loop common mode gain magnitude response of the OTA.

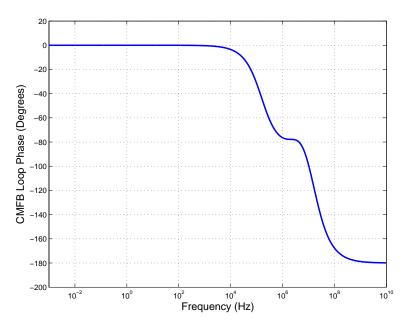


Fig. 8. The open loop common mode gain phase response of the OTA.

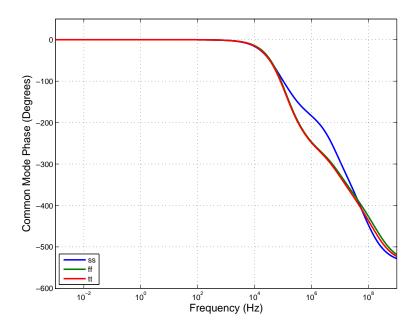


Fig. 9. The common mode feedback network gain phase response.

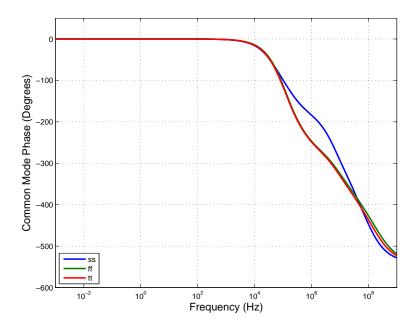


Fig. 10. The common mode feedback network gain magnitude response.

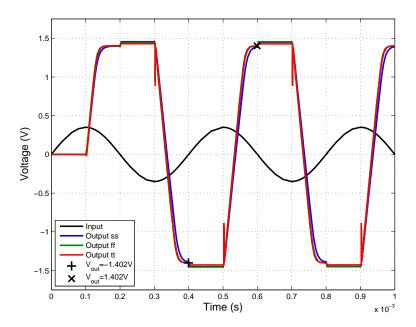


Fig. 11. The closed loop transient response to a full-scale amplitude sinusoid at the Nyquist frequency.

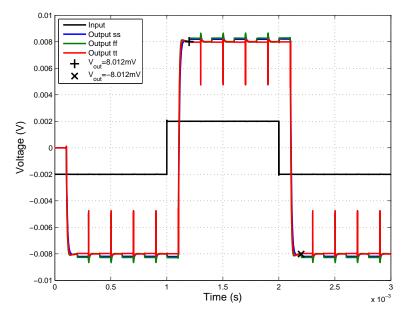


Fig. 12. The closed loop transient response to a small amplitude step input.

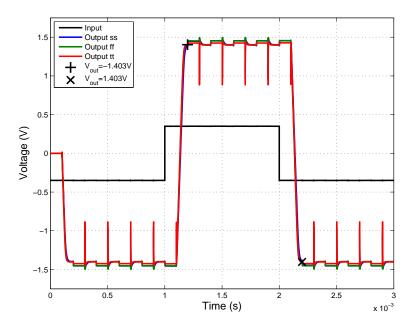


Fig. 13. The closed loop transient response to a full-scale amplitude step input.

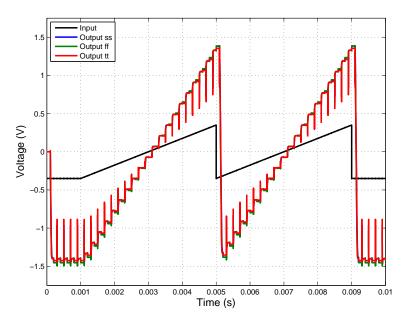


Fig. 14. The closed loop transient response to a full-scale amplitude sawtooth with a frequency of $\frac{f_s}{20}$.