# Sample 12-1

画像復元

ウィーナーフィルタ

画像処理特論

村松 正吾

動作確認: MATLAB R2020a

# **Image restoration**

Wiener filter

Advanced Topics in Image Processing

Shogo MURAMATSU

Verified: MATLAB R2020a

準備

(Preparation)

```
clear
close all
import msip.download_img
msip.download_img
```

```
lena.png already exists in ./data/
baboon.png already exists in ./data/
goldhill.png already exists in ./data/
barbara.png already exists in ./data/
```

パラメータ設定

(Parameter settings)

• sgm:  $\int d^{2}x d^{2$ 

```
sgmuint8 = 10;
sgmw = sgmuint8/255;
```

画像の読込

(Read image)

```
u = rgb2gray(im2double(imread('./data/lena.png')));
sgmu = std(u(:));
meanu = mean(u(:));
```

## 観測画像

#### (Observation image)

カメラの動きによって生じるボケ画像を生成. (Generate a blurred image that might result from camera motion.)

- v = Pu + w
- $\mathbf{w} \sim \text{Norm}(\mathbf{w}|\mathbf{\mu}_w = \mathbf{0}, \sigma_w^2 \mathbf{I})$

```
% Definition of measurment process
psf = fspecial('motion',21,11);
measureproc = @(x) imfilter(x,psf,'conv','circular');
% Simulation of AWGN
v = imnoise(measureproc(u),'gaussian',0,sgmw^2);
```

#### ウィーナーフィルタ

#### (Wiener filter)

画像 uに対する仮定 (Assumptions on the original image u)

• 
$$\mathbf{u} \sim \text{Norm}(\mathbf{u}|\mathbf{\mu}_u = \mathbf{0}, \sigma_u^2 \mathbf{I})$$

問題設定 (Problem settings):

$$\widehat{\mathbf{u}} = \arg\min_{\mathbf{u}} \frac{1}{2\sigma_w^2} \|\mathbf{v} - \mathbf{P}\mathbf{u}\|_2^2 + \frac{1}{2\sigma_u^2} \|\mathbf{u}\|_2^2$$

解 (Solution):

$$\widehat{\mathbf{u}} = \left(\mathbf{P}^T \mathbf{P} + \frac{\sigma_w^2}{\sigma_u^2} \mathbf{I}\right)^{-1} \mathbf{P}^T \mathbf{v} \stackrel{\text{DFT}}{\longleftrightarrow} \widehat{\mathbf{U}}[\mathbf{k}] = \frac{\overline{P[\mathbf{k}]}}{|P[\mathbf{k}]|^2 + \sigma_w^2 / \sigma_u^2} \mathbf{V}[\mathbf{k}]$$

ただし、循環畳み込み行列  $\mathbf{P}$  に対して、(where, for the circular convolution matrix  $\mathbf{P}$ ,)

$$\mathbf{P}^T \overset{\mathrm{DFT}}{\longleftrightarrow} \overline{P[\mathbf{k}]}$$

$$\mathbf{P}^T \mathbf{P} \overset{\text{DFT}}{\longleftrightarrow} \overline{P[\mathbf{k}]} P[\mathbf{k}] = |P[\mathbf{k}]|^2$$

```
% Determine the DFT points
nPoints = 2.^nextpow2(size(u))
```

```
nPoints = 1 \times 2
512 512
```

```
% Ratio of variances between noise w and signal u (ideal estimation)
nsr = sgmw^2/sgmu^2;
% DFT(OTF) of PSF, where the phase response is adjusted to zero
P = psf2otf(psf,nPoints);
% DFT of observation v
```

```
V = fftn(v,nPoints);
% DFT of Wiener filter r
R = conj(P)./(abs(P).^2+nsr);
% IDFT of filtered spectrum
y0 = ifftn(R.*V);
```

### 逆フィルタ

(Inverse filter)

$$\check{\mathbf{u}} = (\mathbf{P}^T \mathbf{P})^{-1} \mathbf{P}^T \mathbf{v} = \mathbf{P}^{-1} \mathbf{v} \stackrel{\mathrm{DFT}}{\longleftrightarrow} \check{\mathbf{U}}[\mathbf{k}] = \frac{\overline{P[\mathbf{k}]}}{|P[\mathbf{k}]|^2} \mathbf{V}[\mathbf{k}] = \frac{1}{P[\mathbf{k}]} \mathbf{V}[\mathbf{k}]$$

```
% IDFT of filtered spectrum
y1 = ifftn(V./P);
```

### 画像表示

(Image show)

```
figure(1)
imshow(u);
title('Original image u')
```



```
figure(2)
imshow(v)
title(sprintf('Blurred image v : PSNR = %5.2f [dB]',psnr(u,v)))
```

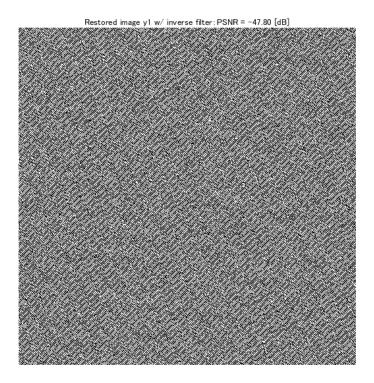


figure(3)
imshow(y0)
title(sprintf('Restored image y0 w/ Wiener filter: PSNR = %5.2f [dB]',psnr(u,y0)))



figure(4)
imshow(y1)

title(sprintf('Restored image y1 w/ inverse filter: PSNR = %5.2f [dB]', psnr(u,y1)))



# ウィーナーフィルタ関数

(Wiener filter function)

• DECONVWNR

```
y2 = deconvwnr(v,psf,nsr);
figure(5)
imshow(y2)
title(sprintf('Restored image y2 w/ DECONVWNR: PSNR = %5.2f [dB]',psnr(u,y2)))
```



 $\hfill \hfill \hfill$