Sample 6-3

標本化

二変量ダウンサンプリング

画像処理特論

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動作確認: MATLAB R2023a

Sampling

Bivariate downsampling

Advanced Topics in Image Processing

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Verified: MATLAB R2023a

準備

(Preparation)

close all

可分離間引き行列の設定

(Setting a separable downsampling factor)

• M: 間引き行列 (downsampling factor)

可分離の場合 (In the separable case)

$$\mathbf{M} = \begin{pmatrix} M_1 & 0 \\ 0 & M_2 \end{pmatrix} \in \mathbb{Z}^{2 \times 2}$$

```
% Vertical downsampling ratio
verticalDFactor = 2;
% Horizontal downsampling factor
horizontalDFactor = 3;
```

入力配列の設定

(Setting an input array)

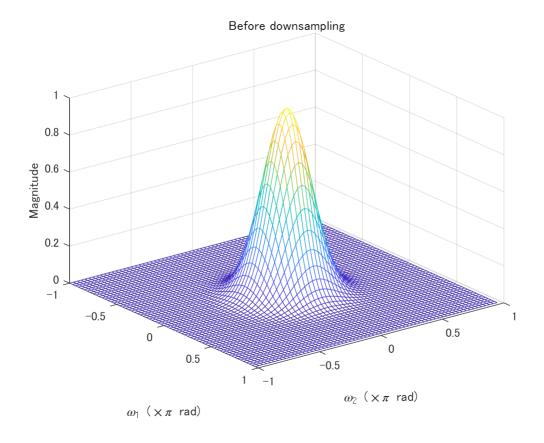
- {u[n]}_n: 入力配列 (input array)
- % Standard deviation

```
sigma = 2;
% Array size
sizeU = 31;
% Generate an array with bivariate Gaussian function
arrayU = fspecial('gaussian', sizeU, sigma);
```

入力配列のスペクトル

(Spectrum of the input array)

```
% Spectrum of u[n]
figure(1)
freqz2(arrayU)
xlabel('\omega_2 (\times\pi rad)')
ylabel('\omega_1 (\times\pi rad)')
title('Before downsampling')
axis ij
```



出力配列の計算

(Computation of the output array)

• $\{v[m]\}_m$: 出力数列 (output array)

$$v[\mathbf{m}] = u[\mathbf{M}\mathbf{m}], \ \mathbf{m} \in \mathbb{Z}^2$$

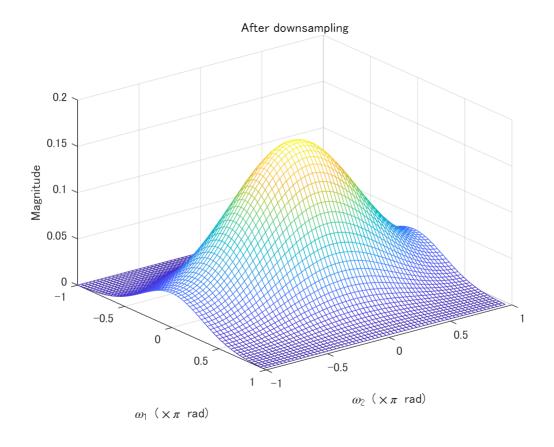
```
% Definition of bivariate separable downsampling
downsample2 = @(x,n) ...
    shiftdim(downsample(...
    shiftdim(downsample(x,...
    n(1)),1),...
    n(2)),1);

% Bivariate separable downsampling
arrayV = downsample2(arrayU, [verticalDFactor horizontalDFactor]);
```

出力配列のスペクトル

(Spectrum of the output array)

```
% Spectrum of v[m]
figure(2)
freqz2(arrayV)
xlabel('\omega_2 (\times\pi rad)')
ylabel('\omega_1 (\times\pi rad)')
title('After downsampling')
axis ij
```



非可分間引き行列の設定

(Setting a non-separable downsampling factor)

• M: 間引き行列 (downsampling factor)

```
一般的な場合 (In the general case)
```

```
\mathbf{M} = \begin{pmatrix} \mathbf{m}_1 & \mathbf{m}_2 \end{pmatrix} \in \mathbb{Z}^{2 \times 2} % Downsampling factor downMtx = [ 1 1 ; -1 1 ];
```

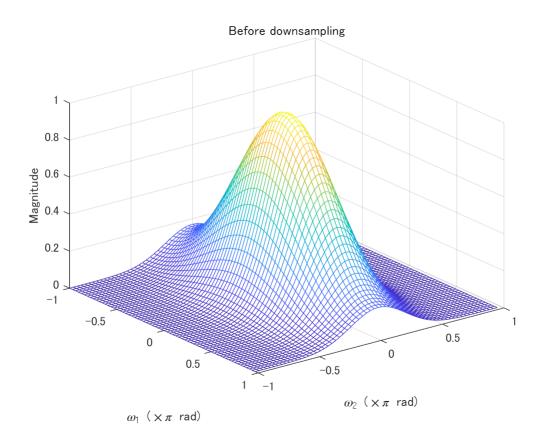
入力配列の設定

(Setting an input array)

```
% Covariance matrix
covMtx = [2 0 ; 0 1/2];
% Array size
sizeU = 31;

% Generate an array with bivariate Gaussian function
arrayU = mygaussian2(sizeU,covMtx);

% Spectrum of u[n]
figure(3)
freqz2(arrayU)
xlabel('\omega_2 (\times\pi rad)')
ylabel('\omega_1 (\times\pi rad)')
title('Before downsampling')
axis ij
```

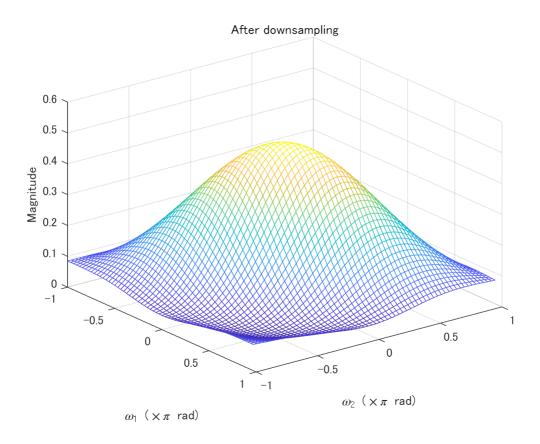


出力配列の計算

(Computation of the output array)

```
% Bivariate non-separable downsampling
arrayV = mydownsample2(arrayU,downMtx);

% Spectrum of v[m]
figure(4)
freqz2(arrayV)
xlabel('\omega_2 (\times\pi rad)')
ylabel('\omega_1 (\times\pi rad)')
title('After downsampling')
axis ij
```



プライベート関数の定義

(Definitions of private functions)

二変量ガウス配列の生成関数 (Generation function of bivariate Gaussian arrays)

```
function x = mygaussian2(sizeX, covMtx)
% MYGAUSSIAN2
%
% Inputs
%
%
    sizeX: size of output array
%
    covMtx: covariance matrix
%
% Output
%
%
    x: array generated by Gauss Func.
sizeHalf = floor(sizeX / 2);
if isscalar(covMtx)
    covMtx = covMtx * eye(2);
end
x = zeros(sizeHalf*2);
iRow = 1;
```

```
for n1 = -sizeHalf:sizeHalf
    iCol = 1;
    for n0 = -sizeHalf:sizeHalf
        p = - 0.5 * [ n0 n1 ] * (covMtx\[ n0 n1 ].');
        x(iRow,iCol) = exp(p);
        iCol = iCol + 1;
    end
    iRow = iRow + 1;
end
x = x / sum(sum(x));
end % of mygaussian2
```

二変量非可分ダウンサンプリング関数 (bivariate non-separable downsampling function)

```
function [outputArray, X, Y] = mydownsample2(inputArray,downMtx,phase)
% MYDOWNSAMPLE2
%
% Inputs
%
%
    inputArray: input array
%
   downMtx: downsampling matrix
%
    phase: downsampling phase
%
% Outputs
%
%
   outputArray: output array
%
          : horizontal sampling points
%
               : vertical sampling points
   Υ
%
if nargin < 3</pre>
    phase = [0 0].';
else
    phase = phase(:);
end
% Size of input array
nRowsInputArray = size(inputArray,1);
nColsInputArray = size(inputArray,2);
nCompInputArray = size(inputArray,3);
% Calculation of the support region after downsampling
vertexPoints(:,1) = [ 0 0 ].';
vertexPoints(:,2) = downMtx \ [ 0 nColsInputArray-1 ].';
vertexPoints(:,3) = downMtx \ [ nRowsInputArray-1 0 ].';
vertexPoints(:,4) = downMtx \ [ nRowsInputArray-1 nColsInputArray-1 ].';
minPoint = floor(min(vertexPoints,[],2));
maxPoint = ceil(max(vertexPoints,[],2));
% Shift the downsampling phase into FPD(downMtx)
```

```
phase = phase - downMtx * floor(downMtx \ phase);
% Downsampling
clear arrayY
iRow = 1;
for m0 = minPoint(1):maxPoint(1)
    iCol = 1;
    for m1 = minPoint(2):maxPoint(2)
        originalPoint = downMtx * [ m0 m1 ].';
        n0 = originalPoint(1) + phase(1);
        n1 = originalPoint(2) + phase(2);
        if n0 >= 0 && n0 < nRowsInputArray && ...</pre>
                n1 >= 0 && n1< nColsInputArray</pre>
            outputArray(iRow, iCol, :) = inputArray(n0 + 1, n1 + 1, :);
        else
            outputArray(iRow, iCol, :) = zeros(1,nCompInputArray,...
                 'like',inputArray);
        end
       iCol = iCol + 1;
    end
    iRow = iRow + 1;
end
Y = minPoint(1):maxPoint(1);
X = minPoint(2):maxPoint(2);
end % of mydownsample2
```

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