Sample 10-5

冗長変換

 ℓ_0 -ノルム最小化

画像処理特論

村松 正吾

動作確認: MATLAB R2020a

Redundant transforms

 ℓ_0 -norm minimization

Advanced Topics in Image Processing

Shogo MURAMATSU

Verified: MATLAB R2020a

準備

(Preparation)

```
close all
```

非線形近似の設定

(Settings of non-linear approximation)

```
% # of Coefs.
K = 32;
% 直交マッチング追跡(OMP)法/マッチング追跡(MP)法
isOmp = true;
```

入力信号の生成

(Generation of input sequence)

```
% # of input samples
nSamples = 128;

% Random process in AR(1) model
rng('default');
w = 0.1*randn(nSamples,1);
w(floor(end/2)) = 1;
u = filter(1,[1 -0.95],w);
```

合成辞書

(Synthesis dictionary)

```
% Synthesis filters
f0 = [ 1 1 ]/2;
f1 = [ -1 1 ]/2;

% (Circular) convolution matrix
nF = max(length(f0),length(f1));
X = [zeros(nF-1,nSamples-nF+1) eye(nF-1); eye(nSamples)]; % Circular extension matrix
C = [zeros(nSamples,nF-1) eye(nSamples) zeros(nSamples,nF-1)]; % Clipping matrix

% Atoms in (circular) convolution matrix
d0 = C*convmtx(f0.',nSamples+nF-1)*X;
d1 = C*convmtx(f1.',nSamples+1)*X;
```

辞書 (Dictionary) D

```
% Dictionary D (Global matrix representation of synthesis filter bank)
D = zeros(nSamples,2*nSamples);
D(:,1:2:end) = d0;
D(:,2:2:end) = d1;
disp(D)
```

1 列から 27 列

0.5000	-0.5000	0	0	0	0	0	0	0	0	0
0.5000	0.5000	0.5000	-0.5000	0	0	0	0	0	0	0
0	0	0.5000	0.5000	0.5000	-0.5000	0	0	0	0	0
0	0	0	0	0.5000	0.5000	0.5000	-0.5000	0	0	0
0	0	0	0	0	0	0.5000	0.5000	0.5000	-0.5000	0
0	0	0	0	0	0	0	0	0.5000	0.5000	0.5000
0	0	0	0	0	0	0	0	0	0	0.5000
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

-0

•	•	•	•	•	•	•	•	•	•	
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
U										
0	0	0	0	0	0	0	0	0	0	0
										•
0	0	0	0	0	0	0	0	0	0	0
0	α		0							0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										•
0	0	0	0	0	0	0	0	0	0	0
a	0	0	0	0		0	0	0	0	0
0	0				0	0			0	0
0	0	0	0	0	0	0	0	0	0	0
										-
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										-
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										U
0	0	0	0	0	0	0	0	0	0	0
										_
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										U
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										U
0	0	0	0	0	0	0	0	0	0	0
										•
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										V
0	0	0	0	0	0	0	0	0	0	0
										•
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										U
0	0	0	0	0	0	0	0	0	0	0
										-
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										U
0	0	0	0	0	0	0	0	0	0	0
										-
0	0	0	0	0	0	0	0	0	0	0
a	0	0	0	0	0	0	0	0	0	0
0			0			Ø				Ø
0	0	0	0	0	0	0	0	0	0	0
										-
0	0	0	0	0	0	0	0	0	0	0
a	0	0	0	0	0	0	0	0	0	0
0										0
0	0	0	0	0	0	0	0	0	0	0
										•
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										U
0	0	0	0	0	0	0	0	0	0	0
^	^		^	•	^	•	^	•	^	
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
						· ·				O
0	0	0	0	0	0	0	0	0	0	0
		0	0	0			0			α
0	0	U		U	0	0		0	0	0 0 0
0	0	0	0	0	0	0	0	0	0	0
	0	C		0	Δ.			0	0	
0	0	0	0	0	0	0	0	0	0	О
0	0	0	0	0	0	0	0	0	0	а
										0 0 0 0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	Ω
		Ø		Ø	Ø	Ø	0	Ø		Ø
0	0	0	0	0	0	0	0	0	0	0
		•	•	-	•	-	•	-	•	-
0	0	0	0	0	0	0	0	0	0	0
								0		0
0	0	0	0	0	0	0	0	0	0	0 0 0 0
0	0	0	0	0	0	0	0	0	0	a
		•	•		•	•	•	•		-
0	0	0	0	0	0	0	0	0	0	0
0		0	0	ρ	0	0	0	0		Ω
	0	v	v	0	v	V		v	0	
0	0	0	0	0	0	0	0	0	0	0
				•						-
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0		0	0	0	0	Ω
		v			0					О
0	0	0	0	0	0	0	0	0	0	0
		^				0		0		0 0 0 0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										Ð
0	0	0	0	0	0	0	0	0	0	0
										^
0	0	0	0	0	0	0	0	0	0	0

0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	
0		0				0			0		
	0		0	0	0		0	0		0	
0 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0	
28 列から											
0	0	0	0	0	0	0	0	0	0	0	
0 0	0	0	0	0	0	0	0	0	0	0	
0 0 0	0 0 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0	
0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	
0 0 0 0	0 0 0 0	0 0 0 0	0 0 0	0 0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	
0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	
0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	
0 0 0 0 0	0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0 0	
0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	
0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	
0 0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0 0	9 9 9 9 9 9	0 0 0 0 0 0 0							
0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0 0	
0 0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0 0	9 9 9 9 9 9	0 0 0 0 0 0 0							
0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	9 9 9 9 9 9 9	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0	9 9 9 9 9 9 9	0 0 0 0 0 0 0	0 0 0 0 0 0 0	
0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	9 9 9 9 9 9 9 9	0 0 0 0 0 0 0 0	9 9 9 9 9 9 9	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0	9 9 9 9 9 9 9	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	
0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	9 9 9 9 9 9 9	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	
0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	9 9 9 9 9 9 9 9	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	9 9 9 9 9 9 9 9	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	
0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	
0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	9 9 9 9 9 9 9 9	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0.
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	Ø. Ø.
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 -0.5000 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 -0.5000 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 -0.5000 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 -0.5000 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 -0.5000 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 -0.5000 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0.5000 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 -0.5000 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								
0 0 0 0 0 0 0 0 0 0 0.5000 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 -0.5000 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0.5000 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 -0.5000 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0								

0	0	۵	۵	۵	0	0	0	۵	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
		0	0	0						
0	0				0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0	0	0
0										0
0	0	0	0	0	0	0	0	0	0	0 0
0	0	0	0	0	0	0	0	0	0	0
		0								0
0	0		0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	a
										0 0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0		0	0	0	0	0
					0					0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0 0 0
0	0	0	0	0	0	0	0	0	0	a
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
										0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0 0 0
		0		0			0		0	9
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	a
		•		•			0	•	0	0
0	0	0	0	0	0	0	0	0	0	0 0 0 0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	a
		•		•	0		0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	a
		9	0	9	0	0	Ø	9	0	9
0	0	0	0	0	0	0	0	0	0	0 0 0 0
0	0	0	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0	0	0
0		Ø		Ø			Ø			О
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	a
		Ø					e .			0 0 0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0		-	ū	•
V	О	О	О	О	О	О	• • •			

ℓ0-擬ノルム最小化による非線形近似

(Non-linear approximation with ℓ_0 -pseudo-norm minimization)

```
\hat{\mathbf{s}} = \arg\min_{\mathbf{s} \in \mathbb{R}^L} \|\mathbf{s}\|_0 \text{ s.t. } \mathbf{v} = \mathbf{D}\mathbf{s}
```

貪欲法による分析処理と係数選択 (Analysis process and coefficient selection by a greedy algorithm)

- マッチング追跡法 (Matching Pursuit; MP)
- 直交マッチング追跡法(Orthogonal MP; OMP

```
% Initializaton
M = size(D,2);
e = ones(M,1);
a = zeros(M,1);
g = zeros(M,1);
s = zeros(M,1);
v = zeros(nSamples,1);
r = u - v;
supp = [];
k = 0;
while k < K
    % Matching process
    rr = r.'*r;
    for m = 1:M %setdiff(1:M, sup)
        d = D(:,m);
        g(m) = d.'*r; \% \gamma m = \langle dm, r \rangle
        a(m) = g(m)/(d.'*d); % Normalize \alpha m = \gamma m/||dm||^2
        e(m) = rr - g(m)*a(m); % < r-dm/||dm||^2,r>
    end
    % Minimum value search (pursuit)
    [~,mmin]= min(e);
    % Update the support
    supp = union(supp,mmin);
    if isOmp % Orthogonal Matching Pursuit
        Ds = D(:,supp);
        s(supp) = pinv(Ds) * u;
        k = k + 1;
    else % Matching Pursuit
        s(mmin) = s(mmin) + a(mmin);
        k = length(supp);
    end
    % Synthesis process
    v = D*s;
    % Residual
    r = u - v;
end
```

近似結果 (Approximation result)

```
v = D*s;
```

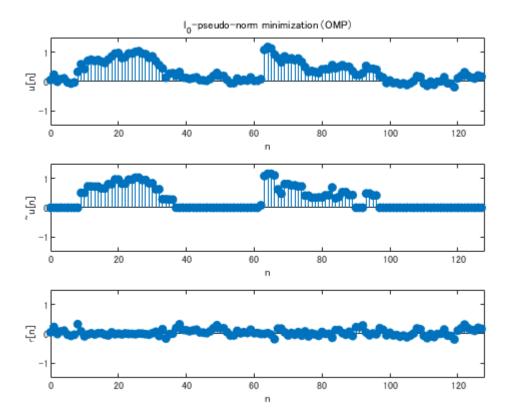
近似誤差 (Residual)

```
r = u - v;
```

グラフ描画

(Graph plot)

```
figure(1)
% Input
subplot(3,1,1)
stem(0:nSamples-1,u,'filled')
axis([0 nSamples -1.5 1.5])
xlabel('n')
ylabel('u[n]')
if isOmp
    method = '(OMP)';
else
    method = '(MP)';
end
title(['l_0-pseudo-norm minimization ' method])
% NLA
subplot(3,1,2)
stem(0:nSamples-1,v,'filled')
axis([0 nSamples -1.5 1.5])
xlabel('n')
ylabel('~u[n]')
% Residual
subplot(3,1,3)
stem(0:nSamples-1,r,'filled')
axis([0 nSamples -1.5 1.5])
xlabel('n')
ylabel('r[n]')
```



MSE 評価 (MSE evaluation)

mse = 0.013168

© Copyright, Shogo MURAMATSU, All rights reserved.