Geometric Interpretations.

1.
$$\frac{1}{3}$$

5.
$$2\pi \ln a$$

6.
$$\frac{\pi}{2}$$

${\bf Combinatorial\ Applications.}$

1.
$$\frac{4 + \ln 3}{8}$$

2.
$$\frac{1}{2}$$

3.
$$2 \ln 2 - 1$$

4.
$$\frac{2 - \ln^2 2 - \ln 4}{4}$$

5.
$$\frac{1+\ln 2}{2}$$

Algebraic Manipulations.

1.
$$\frac{486}{5}$$

2.
$$\frac{14}{3}$$

6.
$$\frac{1}{2}$$

Assorted Integrals.

1.
$$\frac{20}{3}$$

2.
$$\frac{5}{2} \ln \frac{8}{3}$$

4.
$$\ln 2 - 1$$

5.
$$\frac{\pi}{4}$$

6.
$$\frac{2}{5}$$

7.
$$\frac{\pi}{8}$$

8.
$$2 - \frac{\pi^2}{6}$$

9.
$$\frac{\pi \ln \pi}{2}$$

10.
$$\frac{1}{2}$$

11.
$$\frac{\pi}{8}$$

12.
$$\frac{\pi^2}{2}$$

13.
$$\frac{\pi}{2e}$$