Vibrational-Rotational Spectra of HCl and DCl

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This experiment is concerned with the rotational fine structure of the infrared vibrational spectrum of a linear molecule such as HCl. By interpreting the details of this spectrum, it is possible to obtain the moment of inertia of the molecule and thus the internuclear separation. In addition, the pure vibrational frequency determines the force constant that is a measure of the bond strength. By also investigating DCl, the isotope effect can be observed. ¹

¹ Transcribed (with corrections) from Nibler et al. [1].

Introduction

The infrared region of the spectrum extends from the long-wavelength end of the visible region near 1 μ m out to the microwave region at approximately 1000 μ m. It is common practice to specify infrared frequencies in wavenumber units of "inverse centimeters", cm⁻¹. The wavenumber of a photon, $\tilde{\nu}$, is calculated as:

$$\tilde{\nu} = 1/\lambda = \nu/c\,,\tag{1}$$

where c is the speed of light in cm/s, ν is the frequency in Hz, and λ is the wavelength in cm. Thus, this region extends from $10\,000\,\mathrm{cm^{-1}}$ down to $10\,\mathrm{cm^{-1}}$. Although considerable work is now being done in the far-infrared region (below $400\,\mathrm{cm^{-1}}$), the spectral range from $4000\,\mathrm{cm^{-1}}$ to $400\,\mathrm{cm^{-1}}$ has received the greatest attention because the vibrational frequencies of most molecules lie in this region.

Theory

Almost all infrared work makes use of absorption techniques in which radiation from a source emitting broadband infrared radiation is passed through a sample of the material to be studied. When the frequency of this radiation is the same as the vibrational frequency of the molecule, the molecule may be vibrationally excited. This results in loss of energy from the radiation at that frequency and gives rise to an absorption band. The spectrum of a polyatomic molecule generally consists of several such bands arising from different vibrational motions of the molecule. This experiment involves diatomic molecules, which have only one vibrational mode.

The simplest model of a *vibrating* diatomic molecule is a harmonic oscillator, for which the potential energy depends quadratically on the change in internuclear distance. The allowed energy levels of a

harmonic oscillator, as calculated from quantum mechanics [2], are

$$E(v) = h\nu\left(v + \frac{1}{2}\right),\tag{2}$$

where v is the vibrational quantum number (having integer values 0, 1, 2, ...), ν is the vibrational frequency in Hz, and h is the Planck constant, $6.626 \times 10^{-34} \,\mathrm{J\cdot s}$.

The simplest model of a rotating diatomic molecule is a rigid rotor, or "dumbell", model in which the two atoms of mass m_1 and m_2 are considered to be joined by a rigid, weightless rod. The allowed energy levels for a rigid rotor may be shown by quantum mechanics [2] to be

$$E(J) = \frac{h^2}{8\pi^2 I} J(J+1) , \qquad (3)$$

where the rotational quantum number, J, again takes integer values $0, 1, 2, \dots$ The quantity I is the moment of inertia, which is related to the internuclear distance, r, and the reduced mass, μ , by

$$I = \mu r^2 \,. \tag{4}$$

Since a real molecule is undergoing both rotation and vibration simultaneously, a first approximation to its energy levels, E(v, J) would be the sum of eqs. (2) and (3). A more complete expression for the energy levels of a diatomic molecule is given below [3, 4], with the levels expressed as term values, T, in frequency units of cm⁻¹ rather than as energy values, E, in joules (J):

$$T(v,J) = \frac{E(v,J)}{hc} = \frac{\tilde{v}_e(v+\frac{1}{2}) - \tilde{v}_e \chi_e(v+\frac{1}{2})^2 + B_e J(J+1)}{-D_J J^2 (J+1)^2 - \alpha_e(v+\frac{1}{2}) J(J+1)},$$
(5)

where c is the speed of light in cm/s, $\tilde{\nu}_e$ is the frequency in cm⁻¹ for the molecule vibrating about its equilibrium internuclear separation, r_e , in Ă, and the equilibrium rotation frequency is defined as

$$B_e = \frac{h}{8\pi^2 I_c c} \,. \tag{6}$$

The first and third terms on the right-hand side of eq. (5) are the harmonic-oscillator and rigid-rotor terms with $r = r_e$. The second term (containing the anharmonicity constant, $v_e \chi_e$) takes into account the effect of anharmonicity on the vibrational levels. Since the real potential, U(r), for a molecule differs from a harmonic potential, $U_{\rm HO}$, the real vibrational levels are not quite those given by eq. (2) and a correction term is required.³ The fourth term (involving the centrifugal distortion constant, D_I) accounts for the effects of centrifugal stretching on the

³ See fig. 1

 $^{^{2}}$ Recall that μ is defined by the equation $\mu^{-1} = m_{1}^{-1} + m_{2}^{-1} = (m_{1}m_{2})/(m_{1} + m_{2})$.

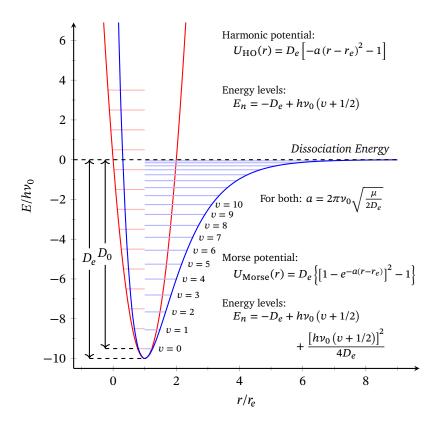


Figure 1: Schematic diagram showing potential energy curves as a function of internuclear separation, r, for a diatomic molecule. The curve for a harmonic oscillator is depicted in red while the Morse potential is drawn in blue. Vibrational levels are shown for each. Note that 0 on the y-axis corresponds to the dissociated system, not any physical representation of "zero energy." This is important when considering your computational results later.

rotational levels. Since a chemical bond is not truly rigid but more like a stiff spring, it stretches somewhat when the molecule rotates. Such an effect is only important for high J values, since the constant D_J is usually very small. The last term in eq. (5), involving α_e , accounts for interactions between vibration and rotation. During a vibration, the internuclear distance r changes; this changes the moment of inertia and affects the rotation of the molecule. The constant α_e is also quite small, but this term should not be neglected.

Selection Rules

The harmonic-oscillator, rigid-rotor selection rules are $\Delta v = \pm 1$ and $\Delta J = \pm 1$; that is, infrared emission or absorption can occur only when these "allowed" transitions take place [4]. For an anharmonic diatomic molecule, the $\Delta J = \pm 1$ selection rule is still valid, but weak transitions corresponding to $\Delta v = \pm 2, \pm 3$, etc. (overtones) can now be observed [4]. Since we are interested in the most intense absorption band (the "fundamental"), we are concerned with transitions from various J'' levels of the vibrational ground state (v'' = 0) to J' levels in the first excited vibrational state (v' = 1). From the still-valid selection rule, we know that the transition must be from J'' to $J' = J'' \pm 1$. Since

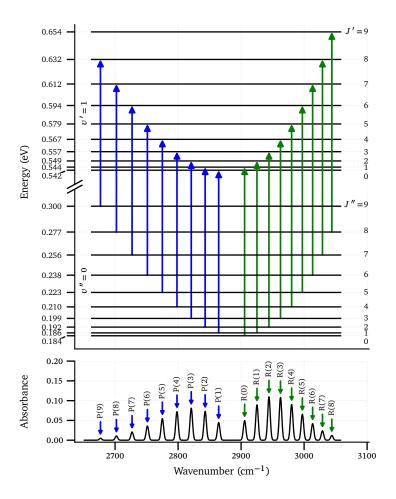


Figure 2: Rotational energy levels for the ground vibrational state (v'' = 0) and the first excited vibrational state (v' = 1) in a diatomic molecule. The vertical arrows indicated allowed transitions in the R and P branches; the numbers above the arrows index the value J''of the lower state. Transitions in the *Q* branch ($\Delta J = 0$) are not shown, since they are not infrared-active.

 $\Delta E = h\nu = hc\tilde{\nu}$, the frequency $\tilde{\nu}$ (in wavenumbers) for this transition will be [T(v',J')-T(v'',J'')]. Applying the selection rule, we find from eq. (5) that

$$\tilde{\nu}_R = \tilde{\nu}_0 + (2B_e - 3\alpha_e) + (2B_e - 4\alpha_e)J'' - \alpha_eJ''^2 \qquad J'' = 0, 1, 2, \dots$$
 (7)

$$\tilde{\nu}_P = \tilde{\nu}_0 - (2B_e - 2\alpha_e)J'' - \alpha_e J''^2 \qquad J'' = 0, 1, 2, \dots$$
 (8)

for $\Delta J = +1$ and $\Delta J = -1$, respectively, where the D_J term has been omitted and $\tilde{\nu}_0$, the frequency of the *forbidden* transition from (v'', J'') = (0, 0) to v' = 1, J' = 0 is defined as

$$\tilde{\nu}_0 = \tilde{\nu}_e - 2\tilde{\nu}_e \chi_e \,. \tag{9}$$

The two series of lines given in eqs. (7) and (8) are called R and P branches, respectively. These allowed transitions are indicated on the energy-level diagram given in fig. 2. If α_e were negligible, eqs. (7) and (8) would predict a series of equally spaced lines separated by $2B_e$ except for a missing line at $\tilde{\nu}_0$. The effect of interaction between

rotation and vibration (non-zero α_e) is to squeeze lines in the R branch closer together and spread the lines in the P branch farther apart, as shown for a typical spectrum in fig. 2.

For convenience, let us introduce a new quantity m, where m = J'' + 1for the R branch and m = -J'' for the P branch, as shown in fig. 2. It is now possible to replace eqs. (7) and (8) with a single equation:

$$\tilde{\nu}(m) = \tilde{\nu}_0 + (2B_e - 2\alpha_e) m - \alpha_e m^2, \tag{10}$$

where *m* takes all integral values and m = 0 yields the frequency \tilde{v}_0 of the forbidden "purely vibrational" transition. If one retains the D_J term of eq. (5) (which assumes $D'' = D' = D_J$), eq. (10) takes the form

$$\tilde{\nu}(m) = \tilde{\nu}_0 + (2B_e - 2\alpha_e) m - \alpha_e m^2 - 4D_J m^3. \tag{11}$$

Thus, a multiple linear regression can be performed to determine \tilde{v}_0 , B_e , α_e , and D_J .

Isotope Effect

When an isotopic substitution is made in a diatomic molecule, the equilibrium bond length, r_e , and the force constant, k, are unchanged, since they depend only on the behavior of the bonding electrons. However, the reduced mass, μ , does change, and this will affect the rotation and vibration of the molecule. In the case of rotation, the isotope effect can be easily stated. From the definitions of B_e and I, we see that

$$\frac{B_e^*}{B_e} = \frac{\mu}{\mu^*} \,, \tag{12}$$

where an asterisk is used to distinguish one isotopologue⁴ from another.

For a harmonic oscillator model, the frequency \tilde{v}_e in wavenumbers is given by

$$\tilde{\nu}_e = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}},\tag{13}$$

which leads to the relation

$$\frac{\tilde{\nu}_e^*}{\tilde{\nu}_e} = \sqrt{\frac{\mu}{\mu^*}} \,. \tag{14}$$

The ratio $\tilde{\nu}_e^*/\tilde{\nu}_e$ differs slightly from this harmonic ratio due to deviation of the true potential function from a quadratic form, as depicted in fig. 1. A closer approximation to the solid curve can be obtained by adding cubic and higher anharmonic terms to the interatomic potential U(r), like so:

$$U(r) = \frac{1}{2}k(r - r_e)^2 + c_1(r - r_e)^3 + c_2(r - r_e)^4 + \dots$$
 (15)

⁴ two molecules which differ only by the nuclear isotopes which make up the molecule

Although somewhat complicated, it can be shown [4, 5] that the c_1 and c_2 terms yield, as the first correction to the energy levels, precisely the $-\tilde{\nu}_{\rho} \chi_{\rho} (v + 1/2)^2$ term given in eq. (5). A similar conclusion is reached if U(r) is taken to have the Morse potential form given by⁵

$$U(r) = D_e \left(\left\{ 1 - \exp\left[-a \left(r - r_e \right) \right] \right\}^2 - 1 \right). \tag{16}$$

In both cases, the mass dependence of $\tilde{v}_e \chi_e$ is found to be greater than for $\tilde{\nu}_e$ and is

$$\frac{\tilde{v}_e^* \chi_e^*}{\tilde{v}_e \chi_e} = \frac{\mu}{\mu^*} \,. \tag{17}$$

Equations (14) and (17) are useful in obtaining the $\tilde{\nu}_0^*$ counterpart of eq. (9),

$$\tilde{\nu}_0^* = \tilde{\nu}_e^* - 2\tilde{\nu}_e^* \chi_e^* = \tilde{\nu}_e \sqrt{\frac{\mu}{\mu^*}} - 2\tilde{\nu}_e \chi_e \frac{\mu}{\mu^*}, \tag{18}$$

and it is seen that a measurement of \tilde{v}_0 for HCl and DCl suffices for a determination of $\tilde{\nu}_e$ and $\tilde{\nu}_e \chi_e$. Alternatively or course, the latter constants can be determined from overtone vibrations ($\Delta v > 0$) of a single isotopic form. 6 However, such overtones generally have low intensity and the transitions may fall outside the range of many infrared instruments, so the isotopic shift method is used in the present experiment.

Since HCl gas is a mixture of H³⁵Cl and H³⁷Cl molecules, a chlorine isotope effect will also be present. Since the ratio of the reduced masses is only 1.0015, high resolution is required to detect this effect. HCl is predominantly H35Cl. If a single peak is seen in the HCl manifold, it can be assumed that the bands are due to H³⁷Cl. At a resolution of <1 cm⁻¹, the band should consist of a series of doublets, with the larger peak due to H³⁵Cl and the smaller peak due to H³⁷Cl. If deuterium is substituted for hydrogen, the ratio of the reduced masses, μ (D³⁵Cl)/ μ (H³⁵Cl), is 1.946 and the isotope effect is quite large.

Vibrational Partition Function [6-8]

The thermodynamic quantities for an ideal gas can usually be expressed as a sum of translational, rotational, and vibrational contributions. We shall consider here the heat capacity at constant volume. At room temperature and above, the translational and rotational contributions to C_v are constants that are independent of temperature. For HCl and DCl,⁷ the molar quantities are

$$\widetilde{C}_v(\text{trans}) = \frac{3}{2}R$$

$$\widetilde{C}_v(\text{rot}) = R.$$
(19)

The vibrational contribution to \tilde{C}_v varies with temperature and can be calculated from the vibrational partition function, q_{vib} using

$$\widetilde{C}_{v}(\text{vib}) = R \frac{\partial}{\partial T} \left(T^{2} \frac{\partial \ln q_{\text{vib}}}{\partial T} \right).$$
 (20)

⁵ The parameter a (in units of 1/Å) is determined by equating k_e to the curvature of the Morse potential at $r = r_e$, yielding

$$a = \sqrt{\frac{k_e}{2D_e}} \,.$$

This three-parameter function has the desired values of $U(r = r_{\rho}) = -D_{\rho}$ and $U(r = \infty) = 0$. It provides a very good approximation to the real potential energy curve at all distances except $r \ll r_e$, a region of no practical significance.

⁶ See Exp. 39 in 1.

⁷ diatomic, and thus linear, molecules

The partition function, q_{vib} , of HCl or DCl is well-approximated by the harmonic-oscillator partition function, $q_{\rm HO}$. Since the energy levels of a harmonic oscillator are given by $\left(v+\frac{1}{2}\right)h\nu$, one obtains [8]

$$q_{\rm HO} = \sum_{v=0}^{\infty} \exp\left[\frac{-\left(v + \frac{1}{2}\right)h\nu}{kT}\right] = \frac{e^{-h\nu/(2kT)}}{1 - e^{-h\nu/(kT)}}.$$
 (21)

Combining eqs. (20) and (21), we find

$$\widetilde{C}_{v}$$
 (vib) = $R \frac{u^{2} e^{-u/2}}{(1 - e^{-u})^{2}}$, (22)

where $u = h\nu/(kT) = hc\tilde{\nu}/(kT) = 143.88\tilde{\nu}/T$.

Safety Precautions

- HCl is a strong acid should be handled cautiously.
- All chemical work should be done in the fume hood and gloves should be worn at all times.
- Always wear safety glasses in the laboratory.
- The cell used to obtain the infrared spectra is valuable and nonreplaceable. Handle it with extreme care. The windows are made from NaCl and are moisture sensitive. Do not touch the lenses with your fingers or expose them to moisture of any kind. If the cell filled with HCl breaks outside the fume hood, notify the instructor immediately and clear the area.

Procedure

This experiment must be performed with an IR spectrometer capable of medium to high resolution (> 2 cm^{-1} resolution). A high-quality grating spectrometer and most FTIR instruments are generally capable of this, and FTIR instruments don't require calibration with external gas standards.

The infrared gas cell is constructed from a short (5 cm to 10 cm) length of large-diameter (2 cm to 4 cm) Pyrex tubing with a vacuum stopcock attached. Infrared-transparent windows are clamped agains O-rings at the ends of the cell or are sealed on the ends with Glyptal resin. For studies concentrating on the region 4000 cm⁻¹ to 500 cm⁻¹, NaCl windows will suffice. When the spectrum of interest extends down to ~400 cm⁻¹, KBr windows are necessary. Both types of salt windows become "foggy" on prolonged exposure to a moist atmosphere and should be protected⁸ when not in use. In the present experiment, inert sapphire windows with transmission down to 1600 cm⁻¹ are particularly convenient and relatively inexpensive.

8 e.g., stored in a desiccator

Filling the Cell and Recording the Spectra

Before beginning the synthesis, power on the FTIR. Prior to starting, purge the 10-cm gas cell (Thorlabs) with nitrogen gas to clean out the cell. This can be accomplished by attaching the tubing from the nitrogen tank regulator to one of the glass ports on the gas cell. Open both stopcocks on the gas cell and slowly open the needle valve on the nitrogen tank⁹ until a steady stream of gas is exiting the open port of the gas cell. After allowing the gas to flow for 2 min, close the stopcock on the gas cell port releasing the gas and immediately close the stopcock on the port receiving the flowing gas, effectively sealing

⁹ Ask the instructor if you are unfamiliar with the use of a regulator.

the gas cell. Immediately close the knob above the regulator nozzle, then close the needle valve controlling the tank's gas flow. Remove the tubing from the gas cell port and take the gas cell to the FTIR to obtain a background spectrum. Return the gas cell to the fume hood for the gas synthesis.

Prepare an indicator solution by dissolving 2 to 4 drops of bromcresol green in 150 mL of DI water in a 200 mL beaker. Attach Tygon tubing to the two stems of the gas cell, lubricating with glycerin to help the tubing slide on the glass. Take the end of one tube and connect it to your water trap. The tubing exiting your water trap should be submerged in your indicator solution. 10

To set up the rest of the apparatus, clamp a 50 mL round-bottom flask to a ring stand. Place \sim 5 mL of D₂O with \sim 5 mL concentrated HCl in the round-bottom flask. Prepare an air condenser (10 cm) by placing a plug of glass wool at the bottom and filling the rest with CaCl₂ (approximately 12 mesh). Insert the stem of the condenser into a stopper, again using glycerin for lubrication, and insert the stopper into the neck of the round-bottom flask. Insert the end of the second tube (attached to the gas cell) into another stopper with a hole, then insert that stopper into the top of the air condenser. With a disposable plastic pipette, obtain ~2 mL of concentrated H₂SO₄. Insert the pipette (carefully so as not to prematurely inject it) into the hole of the second stopper in the round-bottom flask. Once you have verified that all of the holes are plugged, squeeze 1 to 2 drops of sulfuric acid into the solution. You should see vigorous bubbling in the flask. At this point, open the stoppers on the gas cell. Continue to slowly add sulfuric acid drop-wise to the flask, watching the bubbles evolving in the indicator. When the indicator changes color from blue to green/yellow, close the stopcocks on the gas cell and remove the tubing. While the cell is still in the hood, briefly vent the cell to decrease the pressure inside the cell (we want to let out the excess HCl vapor, but not let atmospheric gases diffuse in). Lower gas pressure in the cell will result in narrower spectral lines due to decreased collision broadening. Carefully remove the tubes from the gas cell and proceed to the spectrometer for analysis.

Make sure the experimental settings in the FTIR software are appropriate. The most important change to make is changing the resolution to the smallest possible value. This will allow you to distinguish the individual rotational transitions in the spectrum.

An arrangement for filling the cell is shown in fig. 3.

Theoretical Calculations

The following work will be done during the second week of this lab. You will need to calculate the physical properties of HCl and DCl using

¹⁰ This will fill two roles: as a bubbler, it will prevent atmospheric gases from diffusing back into the cell; and as an indicator, it will show when sufficient HCl has passed through the cell. HCl is highly soluble in water, so the gaseous HCl will quickly acidify the water.

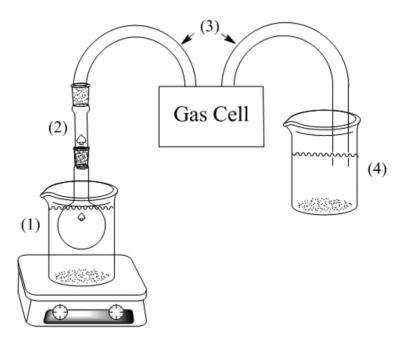


Figure 3: Experimental apparatus. (1) Water bath heating a round-bottom flask containing a mixture of $HCl_{(aq)}$ and $DCl_{(aq)}$. (2) Condenser containing a drying agent. (3) Tygon tubing leading to and from the gas cell. (4) Beaker containing indicator solution. A trap should be put in place to prevent indicator solution from being sucked back in to the gas cell.

Psi4 [9], including the potential energy, equilibrium bond length, and the predicted vibrational and rotational energies for the molecule.

Using Psi4, calculate the potential well for the HCl molecule. Because of the methods used for calculation, the mass of the nuclei doesn't influence geometry, so results will be the same for the four isotopologues. We performed a nearly identical calculation when doing the bond scan exercise on HF. You will need to modify the scan parameters for the Python input printed below. The selected basis set and level of theory make this a quick calculation, so you can set the scan parameters quite large. I recommend scanning from 0.6 Å to 3.5 Å in steps less than 0.05 Å. With this resolution, you should obtain a plot that gives good fidelity around the minimum while showing realistic behavior at long bond lengths.

```
method_list = ['hf', 'remp2', 'pbe0']
basis = '6-311+g(d,p)'
hcl = psi4.geometry("""
Cl 1
r_{vals} = np.arange(0.6, 3.5, 0.05)
hcl_bond = dict()
for method in method list:
```

```
energies = []
for dist in r_vals:
    hcl.r = dist
    hcl.update_geometry()
    e = psi4.energy(method+'/'+basis)
    energies.append(e)
hcl_bond[method] = np.array(energies)
```

Once you have calculated the potential energy surface for the molecule, you'll need to perform a frequency analysis of the HCl molecule. You can use the psi4.diatomic.anharmonicity() function to calculate all the required constants for the molecule. The function takes a list of bond lengths and a list of energies as inputs, and outputs a dictionary of constants. Optionally, you can define the molecule used for computation. In the example shown below, if you leave mol = blank (in other words, accepting the default value), Psi4 will use the last defined molecule. This can sometimes lead to unexpected results... better to explicitly define your molecule. For your lists of bond lengths and energies, use the 'pbe0' data from the bond analysis performed previously so you don't need to recalculate the potential energy curve for each isotopologue (the values won't change anyway, since Psi4 doesn't account for isotopic differences in energy calculations). You need to get anharmonicity constants for H³⁵Cl, H³⁷Cl, D³⁵Cl, and D³⁷Cl, so setting up a loop and saving the results in a dictionary will reduce the amount of repetition in your code. Here is an example of the calculation for H³⁵Cl:

```
h35cl = psi4.geometry("""
Cl@34.968852682
Hal.0078 1 1.0
""")
# The next step would be a good place to wrap your
• loop around to calculate all four
hcl consts['h35cl'] =

    psi4.diatomic.anharmonicity(r_vals,
    hcl_bond['pbe0'], mol=h35cl)
```

Notice how isotopes are defined in Psi4. You'll need to look up appropriate isotopic masses for your four atoms and use that data to define the four required molecules. Notice that the z-matrix for the isotope has the separation between the two atoms set to 1.0. There is no need to create this molecule in its equilibrium geometry, as the anharmonicity calculation will return the equilibrium value as one of the dictionary entries.

Note that the units are not given with the constants. In general, Psi4 provides energies in hartrees, bond lengths in Ångstroms, vibrational constants in wavenumbers, and rotational constants are in hertz.

Data Analysis

- 1. Import your HCl and DCl spectra and index the lines with the appropriate m values, as seen in fig. 2. If the 35 Cl/ 37 Cl splitting is seen, index both sets, but be sure to separate them appropriately. Make a table of these m values and the corresponding frequencies, $\tilde{v}(m)$. Express the frequencies in cm⁻¹ to the tenth of a cm⁻¹. Then, list the differences between adjacent lines, $\Delta \tilde{v}(m)$, which will be roughly $2B_e$, but will vary with m.
- 2. Plot $\Delta \tilde{v}(m)$ against m. If any values seem out of line, check the calculation for that cell.
- 3. Carry out a polynomial least-squares fit to the data using eq. (10) to determine $\tilde{\nu}_0$, B_e , α_e , and their standard errors. Repeat this fitting procedure using eq. (11), noting that high m transitions will be the most important ones in determining D_I , due to its m^3 dependence.
- 4. Using your values of \tilde{v}_0 for HCl and DCl, determine \tilde{v}_e and $\tilde{v}_e \chi_e$ for the various molecules. From \tilde{v}_e , calculate k for HCl.
- 5. Calculate I_e , the moment of inertia, and r_e , the internuclear distance, for both HCl and DCl. Tabulate your experimental and theoretical results, along with your estimates of the experimental uncertainty. Compare your results with literature values found in Kerr, Huber, and Herzberg [3].
- 6. Using your value of \tilde{v}_0 for HCl, calculate \tilde{C}_v (vib) at 298 K and at 1000 K from eq. (22). Compare the spectroscopic value \tilde{C}_v = $5/2R + \widetilde{C}_v(\text{vib})$ with the experimental \widetilde{C}_v value obtained from directly measured values [6, 10] of \widetilde{C}_p and the expression $\widetilde{C}_v = \widetilde{C}_p - R$: $\widetilde{C}_v = 20.80\,\mathrm{J\cdot K/mol}$ at 298 K and 23.20 J·K/mol at 1000 K.

Questions and Further Thoughts

- 1. Compute the ratio of B_e^*/B_e and compare with the rigid-rotor prediction of eq. (12). Based on your experimental data, how constant is r_e for HCl and DCl?
- 2. Compute $B_v = B_e \alpha_e \left(v + \frac{1}{2}\right)$ for the v = 0, 1, and 2 levels of HCl and DCl and, from these, obtain average r_v values for these levels. Comment in your report on the changes in these distances.

- 3. Compare your $\tilde{v}_0^*/\tilde{v}_0$ ratio with the ratio $\sqrt{\mu/\mu^*}$ expected for a harmonic oscillator. How anharmonic is the HCl molecule (i.e., how large is $v_e \chi_e$)?
- 4. Use your values of $\tilde{\nu}_e$ and $\tilde{\nu}_e \chi_e$ and eq. (5) to predict the frequencies of the first overtone transitions of HCl and DCl (ignore the rotational terms). Did you observe any evidence of these overtones in your spectra?
- 5. Do your spectra show any evidence of a ³⁵Cl/³⁷Cl isotope effect? Use eq. (12) to calculate the splitting expected for this effect for several *P* and *R* branch transitions in HCl and DCl.
- 6. Compare your experimental results with the values deduced from your theoretical calculations. For each calculation, report the values for total energy (D_e) , vibration frequency (\tilde{v}_0) , bond length (r_e) , rotation constant B_e , and centrifugal distortion constant D_J . Additionally, you should plot one of the potential energy curves output by Psi4 against the theoretical Morse potential for the molecule. You will need to think carefully about how to match up units for the two curves.

Lab Report Guidelines

As previously stated, your lab report should consist of the following parts:

Title, Author and Date

Introduction and Objective A paragraph describing what we hope to find in this experiment, and how.

Experimental Procedure This should be a very brief general outline of the procedure, written out as a paragraph or two. Give the make and model for any major instruments you used, as well as any important settings. For IR spectroscopy, this especially means the spectral resolution and number of scans.

Results and Discussion This should include answers to the questions in the section "Questions and Further Thoughts". This should not be a separate section, but should instead be included organically in the discussion as a way of filling it out.

Conclusion

References

Appendix Include examples of any calculations that you did by hand. Provide digital copies of any additional inputs used to generate your information.

References

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Further Reading

- MJ Frisch et al. Gaussian 16, Revision B.01. http://gaussian. com/gaussian16.2016.
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