$$(x_{1},y_{1}) = (0.0 \pm 0.2, 0.0 \pm 0.3)$$

$$(x_{2},y_{2}) = (3.0 \pm 0.3, 4.0 \pm 0.2)$$

$$\Delta x = 3.0 - 0.0 = 3.0$$

$$\Delta x = \sqrt{0.2^{2} + 0.3^{2}} = 0.4$$

$$\Delta y = 4.0 - 0.0 = 4.0$$

$$\delta y = 5x = 0.4$$

$$d = \sqrt{x^{2} + y^{2}}$$

$$\theta = \arctan(\frac{y}{x})$$

$$Sd = \sqrt{\frac{1}{2}(x^{2} + y^{2})^{\frac{1}{2}}(2xSx)^{2}} + \frac{1}{2}(x^{2} + y^{2})^{\frac{1}{2}}(2ySy)^{2}}{4(3^{2} + 4^{2})^{\frac{1}{2}}(6\cdot 0.4)^{2}} + \frac{1}{4}(3^{2} + 4^{2})^{\frac{1}{2}}(8\cdot 0.4)^{2}}{4(3^{2} + 5)\cdot 1024} = \sqrt{.16} = 0.4$$

$$d = 5 \pm 0.4$$

$$Sd = \sqrt{\frac{1}{2}(x^2+y^2)^{1/2}(2xSx)^2 + \left(\frac{1}{2}(x^2+y^2)^{1/2}(2ySy)\right)^2}$$

$$= \sqrt{\frac{1}{4}(3^2+4^2)^{-1}(6\cdot0.4)^2 + \frac{1}{4}(3^2+4^2)^{-1}(8\cdot0.4)^2}$$

$$= \sqrt{0.0576} + 0.1024 = \sqrt{.16} = 0.4$$

$$d = 5 \pm 0.4$$

1) b)
$$N = N_0 e^{-x/\lambda}$$

 $N = (1000) e^{-1/0.25} = 1000 e^{-4} = 18.32 \epsilon 6$
 $8N^2 = \left(\frac{\partial N}{\partial N_0} 8N_0\right)^2 + \left(\frac{\partial N}{\partial x} 5x\right)^2 + \left(\frac{\partial N}{\partial \lambda} 5\lambda\right)^2$
 $= \left(e^{-x/\lambda} \cdot 8N_0\right)^2 + \left(\frac{-N_0}{\lambda} e^{-x/\lambda} 5x\right)^2 + \left(\frac{N_0 x}{\lambda^2} e^{-x/\lambda} 5\lambda\right)^2$
 $= e^{-2x/\lambda} \left(8N_0^2 + \left(\frac{N_0 5x}{\lambda}\right)^2 + \left(\frac{N_0 x 5x}{\lambda^2}\right)^2\right)$

$$SN = e^{-x/2} \left(25E12 + 1.6E15 + 9.2E17 \right)^{1/2}$$

 $0.0183.9.6E8$
 $SN = 1.7E7$

1) c)
$$y^2 a + bx$$

 $y^2 2.5 + 4.0.05$
 $z 2.7$

$$u = bx$$

$$5u = |x|5b \quad \text{or} \quad |bx|\sqrt{\frac{5b}{b}^2 + (\frac{5x}{x})^2}$$

$$= 0.2\sqrt{0.004 + 0.00625} = 0.02$$

$$Sy = \sqrt{5a^2 + 8b^2} = \sqrt{0.09041} = 0.3$$

$$Sy = \sqrt{Sa^2 + Sb^2}$$
 $y = 2.7 \pm 0.3 \text{ m}$

= 10.09041 For both cases, Sa is the major = D.3 source of uncertainty, so Sy is unchanged.

$$c_n = aT + bT^3$$

$$= u + v$$

$$\delta u = \sqrt{\left(\frac{\delta a}{a}\right)^2 + \left(\frac{\delta T}{T}\right)^2}$$

$$a = 1.35 \pm 0.05 \text{ mJ/mol·K}^2$$

 $b = 0.021 \pm 0.001 \text{ mJ/mol·K}^4$
 $T = 5.0 \pm 0.5 \text{ K}$

$$SV = \sqrt{\left(\frac{5L}{b}\right)^2 + \left(\frac{38T}{T}\right)^2}$$

$$Sc_M = \sqrt{\left(\frac{5U}{b}\right)^2 + \left(\frac{38T}{V}\right)^2}$$

$$\frac{\delta u}{u} = 0.11$$
 $\frac{\delta v}{v} = 0.30$
 $c_M = 9.38 \pm 1.1$

$$=\sqrt{(0.74)^2+(0.797)^2}=1.1$$

2. a) 5.6 ± 0.7 7 + 3.70± 0.03 }-Error 41/3, can be ignored 9.3 ± 0.7 - direct addition $((0.7)^2 + (0.03)^2)^{1/2} = \sqrt{0.4909}$ ± 0.7) - quadratire b) 5.6 ± 0.7? ± 2.3 ± 0.1) - Error <1/3, can be ignored 7.9 ± 0.8 . direct $((0.7)^2 + (0.1)^2)^{1/2} = \sqrt{0.50}$ ± 0.7 guadrature c) 5,6 ± 0.77 + 4.1 ± 0.2) - Error <1/3, can be ignored 9.7 ± 0.9 - direct - Error negligible (41/3) $(0.7)^2 + (0.2)^2$ $\sqrt{0.53}$ [+0.7] -quadrature d) 5.6 ± 0.7 7.5 ± 1 - direct $((0.7)^2 + (0.3)^2)^{1/2} = \sqrt{0.58}$ ± 0.8 - quadrature

i.
$$\delta g = \delta a + \delta b + \delta c = 4 cm$$

ii.
$$\delta g = \delta a + \delta b + \delta c = 4 cm$$

$$\frac{\delta g}{191} = \frac{\delta a + \delta b + \delta c}{4 + b - c} = 40\%$$

$$\frac{59}{191} = \frac{5c}{|c|} + \frac{5t}{|t|} = \frac{30\%}{30\%}$$

iv.
$$89 = \frac{89}{191} \cdot |91 = \frac{70}{50} \cdot \frac{\text{cm} \cdot 9}{50}$$

i.
$$\delta q = (\delta a)^2 + (\delta b)^2 + (\delta c)^2$$

$$= 2 cm$$

$$\frac{\delta q}{191} = \sqrt{\frac{(\delta a)^2 + (\delta b)^2 + (\delta c)^2}{(a+b+c)^2}}$$

$$= 10\%$$

ii.
$$\delta q = \sqrt{(\delta a)^2 + (\delta b)^2 + (\delta c)^2}$$

$$= \frac{2 cm}{|q|}$$

$$\frac{\delta q}{|q|} = \sqrt{\frac{(\delta a)^2 + (\delta b)^2 + (\delta c)^2}{(a+b-c)^2}}$$

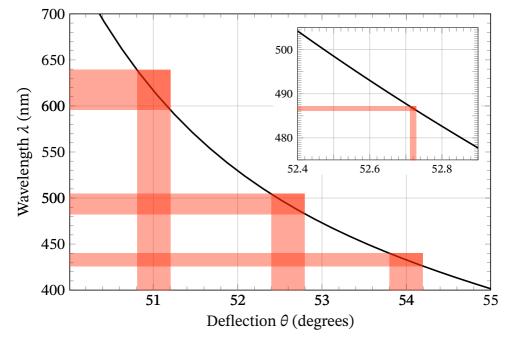
$$\frac{\delta q}{|q|'} = \sqrt{\left(\frac{\delta c}{|c|}\right)^2 + \left(\frac{\delta t}{|t|}\right)^2}$$

$$= 30\%$$

iv.
$$\delta g = \frac{\delta g}{|g|} . |g| = \frac{50 \text{ cm} \cdot g}{5}$$

$$\frac{Sg}{191} = \sqrt{\frac{Sm}{m}^2 + \left(\frac{Sb}{b}\right)^2 + \left(\frac{St}{t}\right)^2}$$

$$= 30\%$$



4. a)
$$\theta_1 = 51.0 \pm 0.2^{\circ}$$

 $\theta_2 = 52.6 \pm 0.2^{\circ}$

$$\lambda_1 = 615 \pm 20 \text{ nm}$$
 $\lambda_2 = 595 \pm 10 \text{ nm}$
 $\lambda_3 = 430 \pm 5 \text{ nm}$

C) Assuming plot is approx. straight in the region, scale error by 1/4 for each
$$\lambda_1 = 615 \pm 5 \text{ nm}$$
 $\lambda_2 = 595 \pm 3 \text{ nm}$ $\lambda_3 = 430 \pm 1 \text{ nm}$

d)
$$l_z = 587 \pm l_{nm}$$

Prediction was reasonable.

$$S = (0.0 \pm 0.1) \qquad y = 3.0 \pm 0.1$$

$$Q = xy + x^{2}/y$$

$$(5q)^{2} = \frac{\delta q}{\delta x} Sx + \frac{\delta q}{\delta y} \delta y$$

$$= \left[(y + 2x/y) \delta x \right]^{2} + \left[(x - x^{2}/y^{2}) \delta y \right]^{2}$$

$$= \left[(3 + 2 - 10/3) \cdot 0.1 \right]^{2} + \left[(6 - (6/3)^{2}) \cdot 0.1 \right]^{2}$$

$$Sq^{2} = (0.7)^{2} + (0.2)^{2}$$

(b)
$$\frac{1}{f} = \frac{1}{p} + \frac{1}{q}$$
 $f = \frac{pq}{p+q}$
a) $Sf^{2} = \left(\frac{\partial f}{\partial p} Sp\right)^{2} + \left(\frac{\partial f}{\partial q} \delta_{q}\right)^{2}$

$$Sf^{2} = \left[\frac{(p+q) \cdot q - pq}{(p+q)^{2}} Sp\right]^{2} + \left[\frac{(p+q) \cdot p - pq}{(p+q)^{2}} Sq\right]^{2}$$

$$= \frac{1}{(p+q)^{4}} \left[\frac{(pq+q^{2} - pq)Sp}{(pq+q)^{2}} + \frac{(p^{2} + pq - pq)Sq}{(p+q)^{2}} Sq\right]^{2}$$

$$Sf = \frac{1}{(p+q)^{4}} \left[\frac{(pq+q^{2} - pq)Sp}{(p+q)^{4}} + \frac{pq}{(p+q)^{4}} Sp\right]^{2} + \left[\frac{(p^{2} + pq - pq)Sq}{(p+q)^{4}} + \frac{pq}{q^{4}} Sq^{2}\right]$$

$$Sub \quad u = \frac{1}{p^{4}} Sp \quad \delta v = \frac{1}{q^{2}} \delta q$$

$$E = u + v \implies f = u^{-1}$$

$$Sf = \left(\frac{df}{du}Su\right)Su \quad Su = \sqrt{Su^{2} + Sv^{2}}$$

$$= u^{-2} Su \quad = \sqrt{\frac{1}{p^{4}}} Sp^{2} + \frac{1}{q^{4}} Sq^{2}$$

$$f^{2}Su = \sqrt{\frac{1}{p^{4}}} Sp^{2} + \frac{1}{q^{4}} Sq^{2}$$

$$\sqrt{\frac{1}{p^{4}}} Sp^{2} + \frac{1}{q^{4}} Sq^{2}} \cdot \sqrt{\frac{pq}{p^{4}}} = \frac{1}{(p+q)^{2}} \sqrt{\frac{q^{4}}{p^{2}}} Sp^{2} + \frac{pq}{p^{4}} Sq^{2}$$