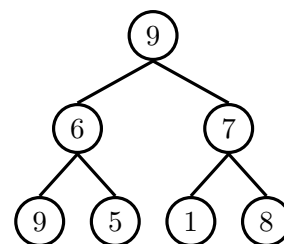


1 Min-Heapify This

1.1 In general, there are 4 ways to heapify. Which 2 ways actually work?

- Level order, bubbling up
- Level order, bubbling down
- Reverse level order, bubbling up
- Reverse level order, bubbling down



1.2 (a) Show the heapification of the tree.

(b) Now, insert the value 2.

(c) Finally, remove the value 1.

2 Motivation

- 2.1 (a) In the worst case, how long does it take to index into a linked list?
- (b) In the worst case, how long does it take to index into an array?
- (c) In the worst case, how long does it take to insert into a linked list?
- (d) Assuming there's space, how long does it take to put a element in an array?
- (e) What if we assume there is no more space in the array?
- (f) Given what we know about linked lists and arrays, how could we build a data structure with efficient access and efficient insertion?

3 Hash Table Basics

```

3.1 public class BadHashMap<K, V> implements Map<K, V> {
    private V[] array;
    public void put(K key, V value) {
        this.array[key.hashCode() % this.array.length] = value;
    }
}

```

```

interface Map<K, V> {
    boolean containsKey(K key);
    V get(K key);
    void put(K key, V value);
    int size();
}

```

- (a) Why do we use the % (modulo) operator?
- (b) What are collisions? What data structure can we use to address them?
- (c) Why is this a bad HashMap?

- 3.2 (a) Draw the diagram that results from the following operations on a Java HashMap. Integer::hashCode returns the integer's value.

```

put(3, "monument");
put(8, "shrine");
put(3, "worker");
put(5, "granary");
put(13, "worker");

```



- (b) Suppose a resize occurs, doubling the array to size 10. What changes?

4 Hash Codes *Extra Practice*

4.1 What does it mean for a hashcode to be valid?

4.2 Which of the following hashcodes are valid? Good?

```
class Point {  
    private int x, y;  
    private static int count = 0;  
    public Point(int x, int y) {  
        this.x = x;  
        this.y = y;  
        count += 1;  
    }  
}
```

(a) **public void** hashCode() {
 System.out.print(**this.x** + **this.y**);
}

(b) **public int** hashCode() {
 Random random = **new** Random();
 return random.nextInt();
}

(c) **public int** hashCode() {
 return this.x + **this.y**;
}

(d) **public int** hashCode() {
 return count;
}

(e) **public int** hashCode() {
 return 4;
}