

```
> restart:
```

Question 4B:

```
> `mod` := mods:
chin_result := chrem([x^2 + 2*x + 4, x^2 + 3*x + 6], [5, 7]):
printf("\nThe polynomial u(x) in the symmetric range Z mod 35 is:
%a.\n", chin_result);
```

The polynomial $u(x)$ in the symmetric range $Z \bmod 35$ is: $x^2+17x-1$.

Question 4D:

```
> poly_A := x^4 + x^3 + x + 1:
poly_B := x^3 + 1:
char_F := 2:
printf("\nInput Polynomials:\nA: %a.\nB: %a.\n", poly_A, poly_B);
```

Input Polynomials:

A: x^4+x^3+x+1 .

B: x^3+1 .

```
> res_one := expand(poly_A * poly_B) mod char_F:
printf("\n A*B in Z mod 2 is: %a.\n", res_one);
```

$A*B$ in $Z \bmod 2$ is: x^7+x^6+x+1 .

```
> res_two := Gcdex(poly_A, poly_B, x) mod char_F:
printf("\n The monic GCD of A,B in Z mod 2 is: %a.\n", res_two);
```

The monic GCD of A,B in $Z \bmod 2$ is: x^3+1 .

```
> res_three := Rem(poly_A, poly_B, x) mod char_F:
printf("\n The remainder of A,B in Z mod 2 is: %a.\n", res_three)
;
```

The remainder of A,B in $Z \bmod 2$ is: 0.

```
> res_four := Gcdex(poly_A, poly_B, x, 's', 't') mod char_F:
printf("\n The monic GCD of A,B in Z mod 2 is: %a and the value
of S and T is: %a and %a respectively.\n", res_four, s, t);
```

The monic GCD of A,B in $Z \bmod 2$ is: x^3+1 and the value of S and T is: 0 and 1 respectively.

```
> (* Chinese Remainder Problem *)
```

```
crp := proc(u1::polynom, u2::polynom, m1::polynom, m2::polynom,  
p::posint)
```

```
local U, U_1, U_2, M_1, M_2, V_1, V_2, P:  
U_1, U_2, M_1, M_2, P := u1, u2, m1, m2, p:
```

```
V_1 := Rem(U_1, M_1, y) mod p:  
printf("\nValue of V1: %a.\n", V_1);  
Gcdex(M_1, M_2, y, 's', 't') mod p:  
printf("The inverse of M1: %a.\n", s);
```

```
V_2 := Rem((U_2-U_1)*s, M_1, y) mod p:  
printf("Value of V2: %a.\n", V_2);
```

```
U := (V_1 + V_2*M_1) mod p:  
U := expand(U) mod p:
```

```
return printf("Recovered U: %a.\n", U);  
end proc:
```

```
> u_1, u_2 := y^2, y^2 + y + 1:  
m_1, m_2 := y^3 + y + 1, y^3 + y^2 + 1:  
  
crp(u_1, u_2, m_1, m_2, 2):
```

```
Value of V1: y^2.  
The inverse of M1: y.  
Value of V2: y^2+y.  
Recovered U: y^5+y^4+y^3+y^2+y.
```