

```

> restart:
with(LinearAlgebra):
=
> CREATEVANMAT := proc(paramA::posint)

local n,xVals,i,j,vanMat,valln:
n := paramA:

xVals := [seq(x[i],i=1..n)]:
vanMat := Matrix(n,n):

for i from 1 to n do:
local k:
k := 1:
valln := xVals[i]:
for j from 1 to n do:
if j=1 then:
vanMat[i,j] := 1:
else:
vanMat[i,j] := valln^k:
k := k+1:
fi:
od:
od:

return vanMat:
end proc:
=
> n := 4:
vanMat := CREATEVANMAT(n):
vanMat;

```

$$\begin{bmatrix} 1 & x_1 & x_1^2 & x_1^3 \\ 1 & x_2 & x_2^2 & x_2^3 \\ 1 & x_3 & x_3^2 & x_3^3 \\ 1 & x_4 & x_4^2 & x_4^3 \end{bmatrix}$$

(1)

```

> alphaB := [seq(i,i=1..n)]:
  alphaB;
                                     [1, 2, 3, 4]
(2)
=
> BBVAN := proc(paramA::list(integer))

  local alpha,p,mat,det,res,i,temp:

  alpha := paramA:

  temp := vanMat:
  temp := subs([seq(x[i]=alpha[i],i=1..n)],temp):
  res := Determinant(temp):

  return res:
end proc:
=
> BZ := proc(paramA::integer)

  local alpha,res,i:

  alpha := paramA:
  res := BBVAN([alpha,seq(alphaB[i],i=2..n)]):

  return res:
end proc:
=
> GETDEGREE := proc(paramA::procedure)

  local BB,alpha,gK,k,m,yK,vK,mEval:

  BB := paramA:
  gK := 0:
  k := 0:
  m := 1:
  while true do:
    alpha := rand():
    mEval := eval(m,x=alpha):
    while mEval=0 do:
      alpha := rand():
      mEval := eval(m,x=alpha):
    od:
    yK := BB(alpha):
    vK := ((yK-eval(gK,x=alpha))/mEval):
    if vK=0 then:
      return gK:
    fi:
  end while:
end proc:

```

```

    gK := gK+(vK*m):
    m := expand(m*(x-alpha)):
    k := k+1:

```

```

od:
end proc:

```

```

> res := GETDEGREE(BZ):
res;

```

$$-2x^3 + 18x^2 - 52x + 48 \quad (3)$$

```

> res := eval(diff(res,x),x=alphaB[1]):
res;

```

$$-22 \quad (4)$$

```

> mapRes := eval(diff(Determinant(vanMat),x[1]),[seq(x[i]=alphaB
[i],i=1..n)]):
mapRes;

```

$$-22 \quad (5)$$

```

> sumEval := expand(sum(8*k-2,k=1..d+2));

```

$$sumEval := 4d^2 + 18d + 20 \quad (6)$$