

Case Studies Nonlinear Optimization

Open Cast Mining

Final Presentation

July 09, 2016

InYoung Choi, Olivia Kaufmann, Martin Sperr, Florian Wuttke

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- 2 Physical Model
- 3 Parameter Identification: Physical Model
- 4 Parameter Identification: Black Box Model
- 5 Summary

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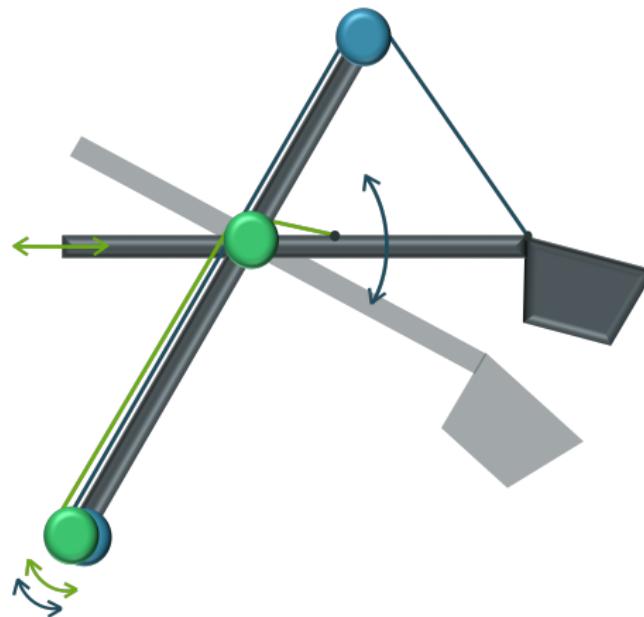
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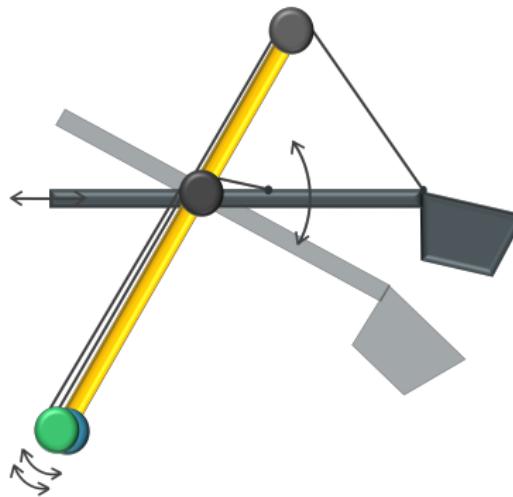
originally posted to Flickr by FAndrey at <http://flickr.com/photos/43301444@N06/4141786255>

- Goal: **Optimization of model parameters**
- Models of technical system = Physical properties + Control properties

Problem Setting

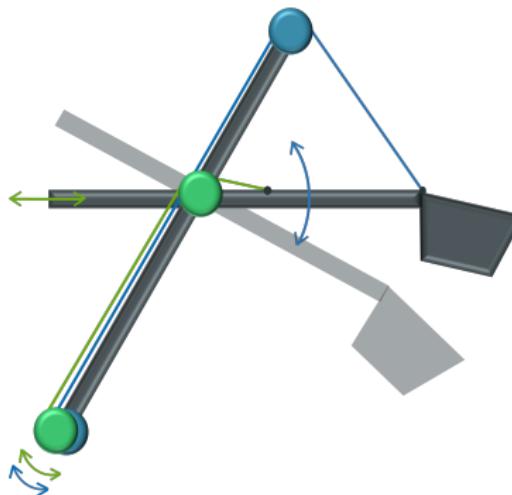


Problem Setting



- Arm element fixed to the base
- Cannot be moved w.r.t. the base

Problem Setting (include videos)



- Green: Shovel motion **back and forth**
- Blue: Shovel motion **up and down**

Procedure

Physical Model

- Rope properties
- Lagrange Formalism



Parameter Identification

Discretization

Procedure

Physical Model

- Rope properties
- Lagrange Formalism

vs

Blackbox Model

- Realistic model
- Confidential information



Parameter Identification

Discretization

Parameter Identification

Derivative-free optimization

Physical Modeling

Why?

Building an
accurate model



Good description of
the effects of control
and motion

Physical Modeling Cont'd

How?

To consider:

- Friction in cable reels
- Deformation of ropes
- Potential/Kinetic energy
- etc

Physical Modeling Cont'd

How?

To consider:

- Friction in cable reels
- Deformation of ropes
- Potential/Kinetic energy
- etc



Lagrange Formalism
(2nd order ODE)

Physical Modeling Visualization

Why is it important?

Performance videos of two different loads

Which color do we want to use?

TUMblue

TUMblue1

TUMblue2

TUMblue3

TUMblue4

TUMblue5

Parameter Identification

What are parameters?

- Friction coefficients
- Mass
- Inertia
- etc.

Parameter Identification

What are parameters?

- Friction coefficients
- Mass
- Inertia
- etc.

Why?

Accurate and
realistic parameters



Better prediction
and planning of
motion

Parameter Optimization Visualization

Two videos carrying the same load, but one with a random motion and the other with optimized parameters

Parameter Identification Two Ways

**Two independent models acquired,
two different computational approaches.**

Physical Model

- Rope properties
- Lagrange Formalism

vs

Blackbox Model

- Realistic model
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Parameter Identification

Discretization

Parameter Identification

Derivative-free optimization

Parameter Identification: Physical Model

Own Physical Model

Lagrange Formalism

$$A(x, p) \begin{pmatrix} \ddot{s} \\ \ddot{\theta} \end{pmatrix} = b(x, u, p)$$

↓

Parameter Identification

Discretization

$$\min_{x,p} \quad \frac{1}{2} \|\bar{x} - x\|^2$$

Parameter Identification: Physical Model

Own Physical Model

Lagrange Formalism

$$A(x, p) \begin{pmatrix} \ddot{s} \\ \ddot{\theta} \end{pmatrix} = b(x, u, p)$$

↓

Parameter Identification

Discretization

$$\min_{x,p} \quad \frac{1}{2} \|\bar{x} - x\|^2$$

- All the information needed for calibration is available
- Runge-Kutta method of different orders for discretization
- Parameter computation for a given control and motion

Parameter Identification: Blackbox Model

Siemens Blackbox Model

- **Input:** Joystick commands for up/down/back/forth
- **Output:** Position of the shovel



Parameter Identification

Particle Swarm, Pattern Search,
Genetic Algorithm, ...

Parameter Identification: Blackbox Model

- Almost no information is available except input/output
- Derivative-free optimization methods required
- As a real-life complex system, only a few parameters are studied here

Siemens Blackbox Model

- **Input:** Joystick commands for up/down/back/forth
- **Output:** Position of the shovel



Parameter Identification

Particle Swarm, Pattern Search, Genetic Algorithm, ...

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Lagrange Formalism

Method to describe dynamics of an accelerated system

T kinetic energy

V potentials

F non-conservative external forces

r points of actions of forces F

q free variables

Q generalized forces

Lagrange Formalism

Method to describe dynamics of an accelerated system

T kinetic energy

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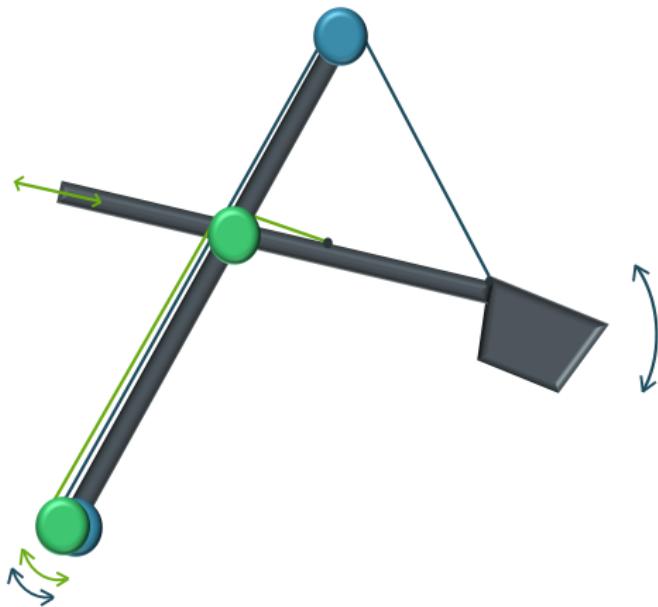
q free variables

Q generalized forces

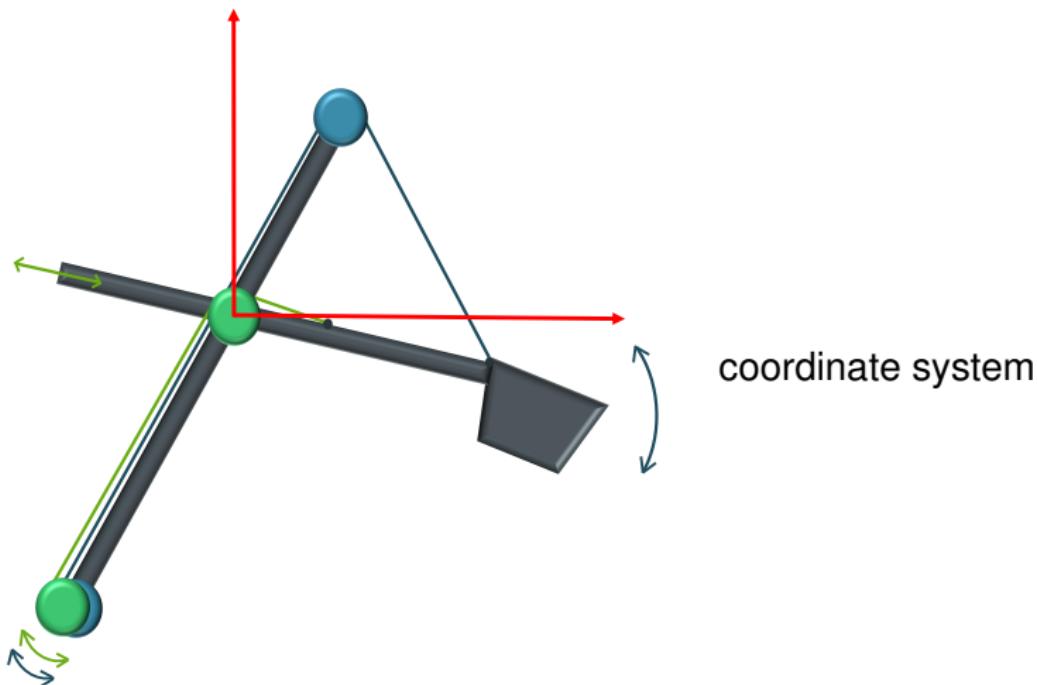
$$\frac{d}{dt} \left(\frac{\partial T}{\partial \dot{q}_i} \right) - \frac{\partial T}{\partial q_i} + \frac{\partial V}{\partial q_i} = Q_i$$

$$Q = \left(\frac{\partial r}{\partial q} \right)^T F$$

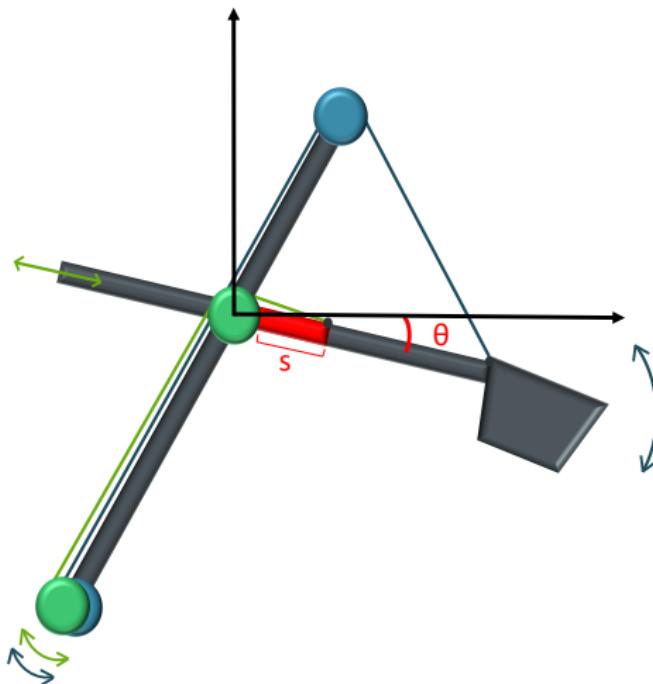
Physical Model of Excavator



Physical Model of Excavator



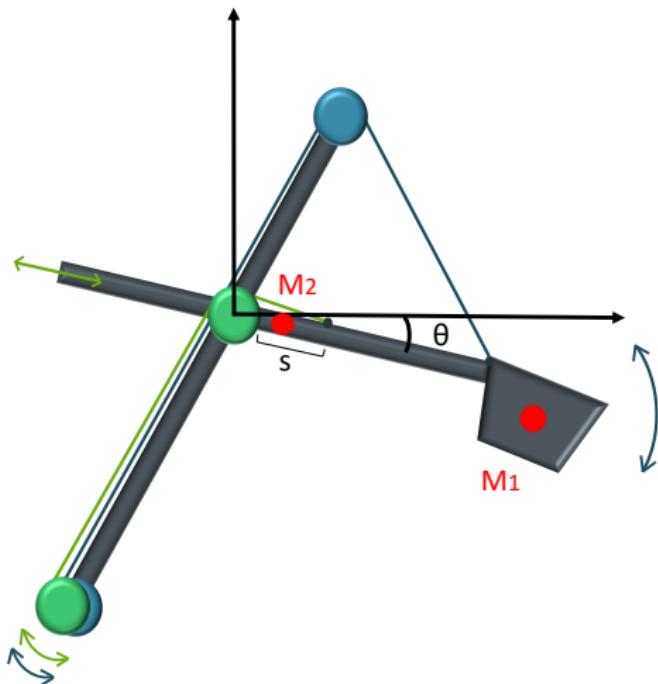
Physical Model of Excavator



degrees of freedom

- length s
- tilt angle θ

Physical Model of Excavator



movable centers of gravity of

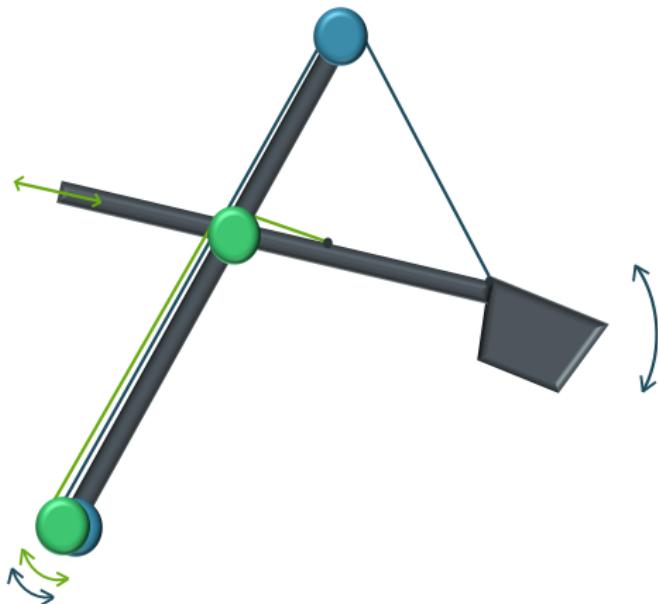
- shovel M_1
- arm M_2

Physical Model of Excavator

Assumptions to the model:

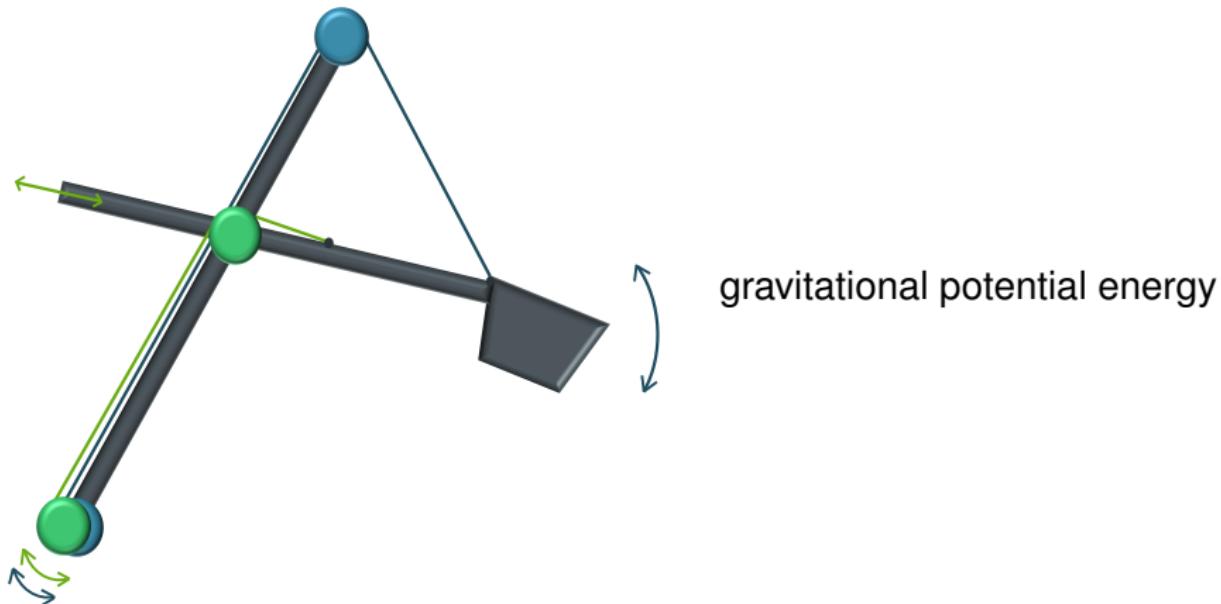
- no mass for the ropes
- shovel as point mass
- no slack/friction between ropes and cable reels

Kinetic Energy

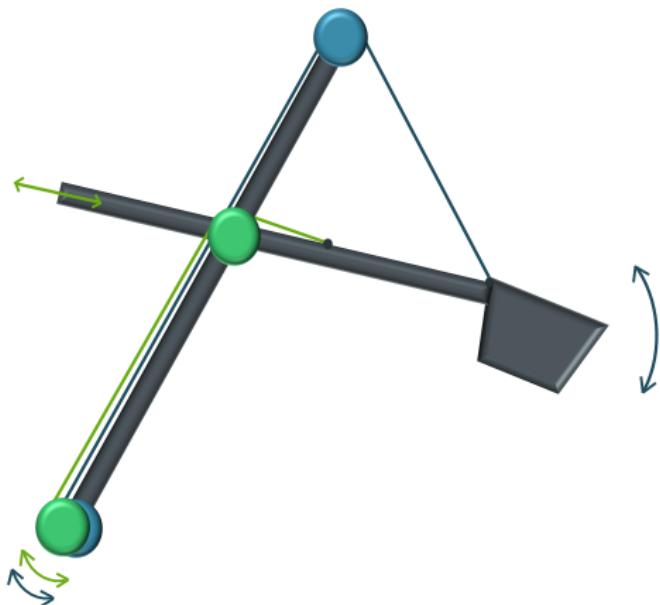


- movement of mass
- rotation of cable reel

Potential Energy



Generalized Forces



- torque on cable reel
- friction of cable reel

Lagrange Formalism

$$\frac{d}{dt} \left(\frac{\partial T}{\partial \dot{s}} \right) - \frac{\partial T}{\partial s} + \frac{\partial V}{\partial s} = Q_s$$

$$\frac{d}{dt} \left(\frac{\partial T}{\partial \dot{\theta}} \right) - \frac{\partial T}{\partial \theta} + \frac{\partial V}{\partial \theta} = Q_\theta$$

Resulting ODE

Second order ODE from Lagrange Formalism:

$$A(x, p) \begin{pmatrix} \ddot{s} \\ \ddot{\theta} \end{pmatrix} = b(x, u, p)$$

Transformed into first order ODE:

$$\frac{d}{dt} \begin{pmatrix} s \\ \theta \\ \dot{s} \\ \dot{\theta} \end{pmatrix} = \begin{pmatrix} \dot{s} \\ \dot{\theta} \\ A^{-1}(x, p)b(x, u, p) \end{pmatrix} = f(x, u, p)$$

state $x = (s, \theta, \dot{s}, \dot{\theta})^T$

control $u = (\tau_1, \tau_2)^T$

parameters $p = (p_1, \dots, p_k)^T$

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Discretization of the ODE

Discretize time interval:

$$[0, T] \rightarrow \{0 = t_0, t_1, \dots, t_{m-1}, t_m = T\}$$

Discretize state and control:

$$x_n = x(t_n)$$

$$u_n = u(t_n)$$

Discretization of the ODE

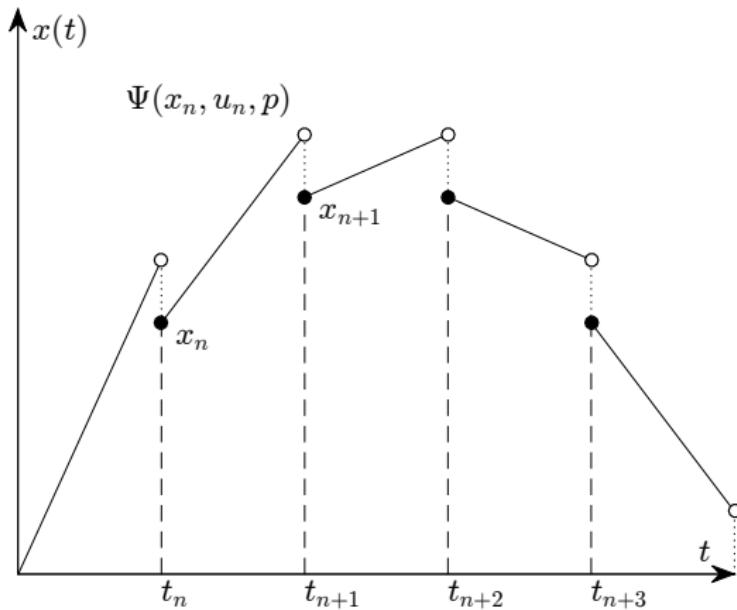
Explicit Euler for every time step $h_n = t_{n+1} - t_n$:

$$\Psi(x_n, u_n, p) = x_n + h_n f(x_n, u_n, p)$$

Discrete constraint:

$$0 = x_{n+1} - \Psi(x_n, u_n, p) =: \Phi_n(x, u, p) \quad \forall n = 0, \dots, m-1$$

Discretization of the ODE



Problem Formulation

Natural approach: Optimal Control Problem

$$\begin{aligned} \min_{x,p} \quad & \frac{1}{2} \|\bar{x} - x\|^2 \\ \text{s. t.} \quad & \Phi(x, \bar{u}, p) = 0 \\ & p \geq 0 \end{aligned}$$

state	$x = (s, \theta, \dot{s}, \dot{\theta})^T$
parameters	$p = (p_1, \dots, p_k)^T$
control	$\bar{u} = (\tau_1, \tau_2)^T$
desired motion	\bar{x}

Problem Formulation

Original Problem

$$\begin{aligned} \min_{x,p} \quad & \frac{1}{2} \|\bar{x} - x\|^2 \\ \text{s. t.} \quad & \Phi(x, \bar{u}, p) = 0 \\ & p \geq 0 \end{aligned}$$

Problem Formulation

Original Problem

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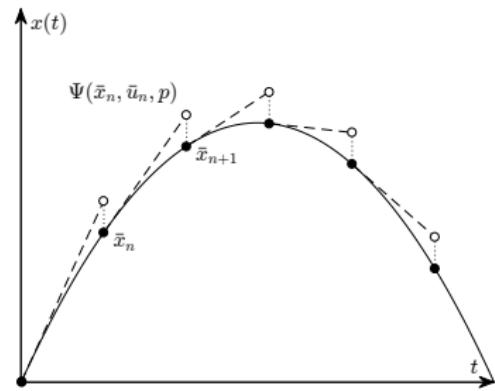
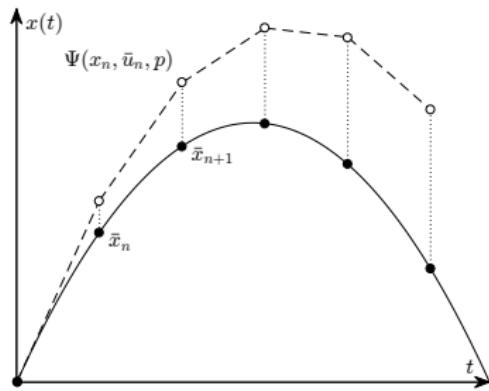
Reinterpreted Problem

$$\begin{aligned} \min_p \quad & \frac{1}{2} \|\Phi(\bar{x}, \bar{u}, p)\|^2 \\ \text{s. t.} \quad & p \geq 0 \end{aligned}$$

$$\begin{aligned} \min_p \quad & \frac{1}{2} \|\Phi(\bar{x}, \bar{u}, p)\|^2 \\ \text{s. t.} \quad & p \geq 0 \end{aligned}$$

- \bar{x} solves ODE
- $\Phi(\bar{x}, \bar{u}, \bar{p}) \rightarrow 0$ for discretization $m \rightarrow \infty$
- Problem dimension fixed for $m \rightarrow \infty$

Comparison of the Approaches

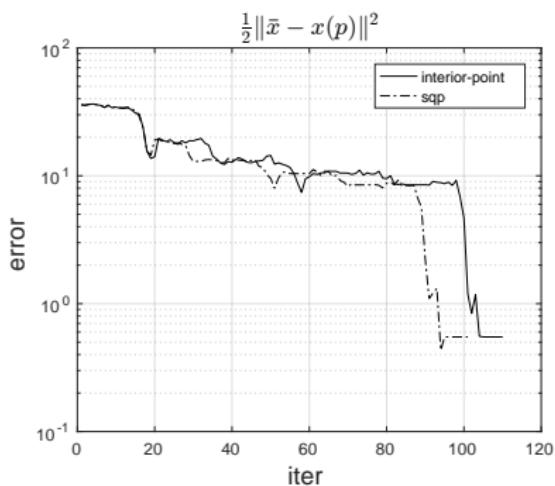
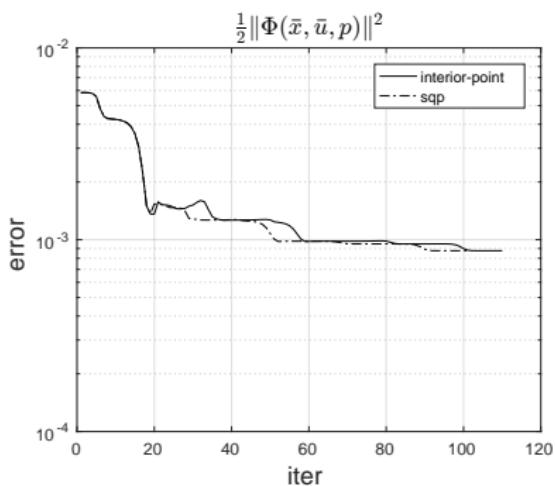


continuous vs. stepwise Approximation

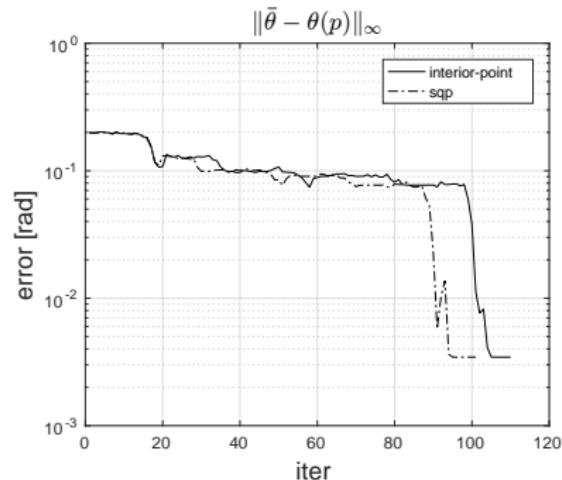
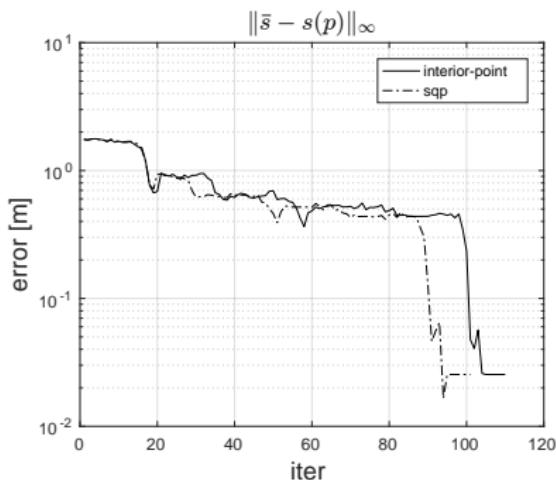
Example Instance

- $[0, T] = [0, 14s]$
- 1500 time steps
- $p_0 \in [0.8\bar{p}, 1.2\bar{p}]$
- $x(p)$ solution of ODE for given p

Results



Results



Exact up to 3cm

Results

movies: reference and optimizes trajectory

Results

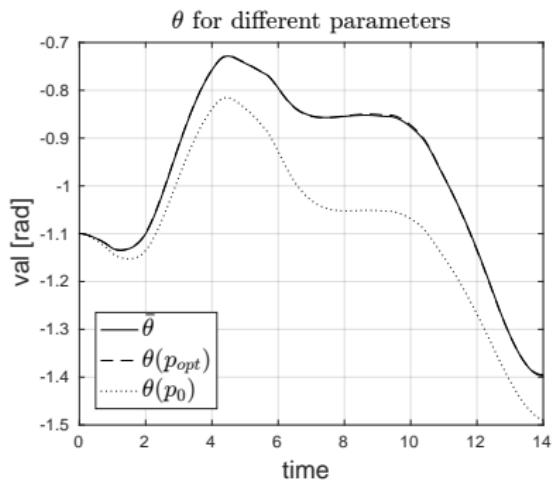
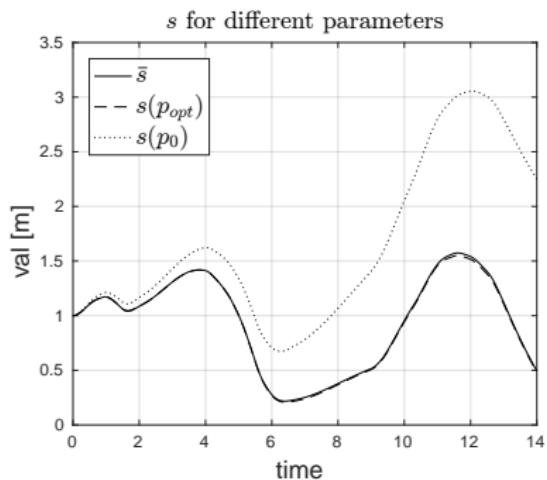


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Examples

- Friction coefficients
- Masses
- Inertia

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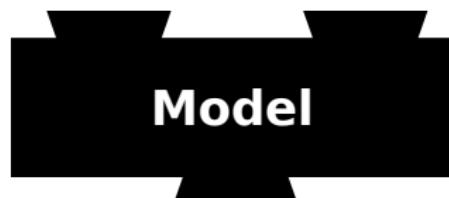
Black box model

- Realistic model from Siemens
- Confidential information

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Black box model

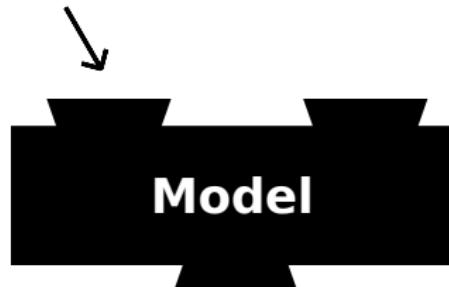
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Control



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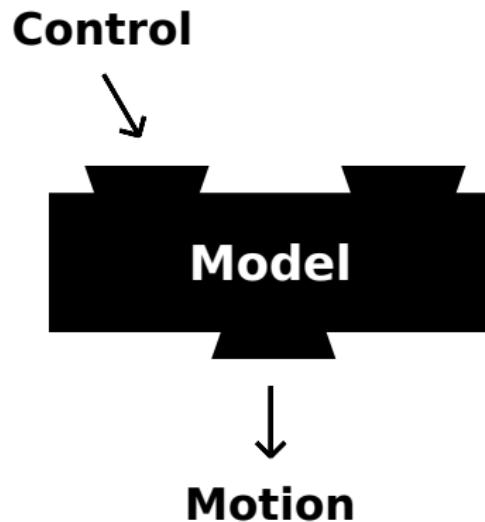
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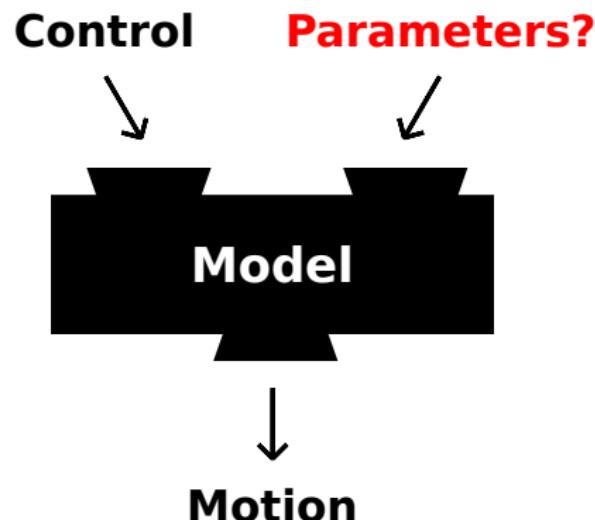
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Trajectories

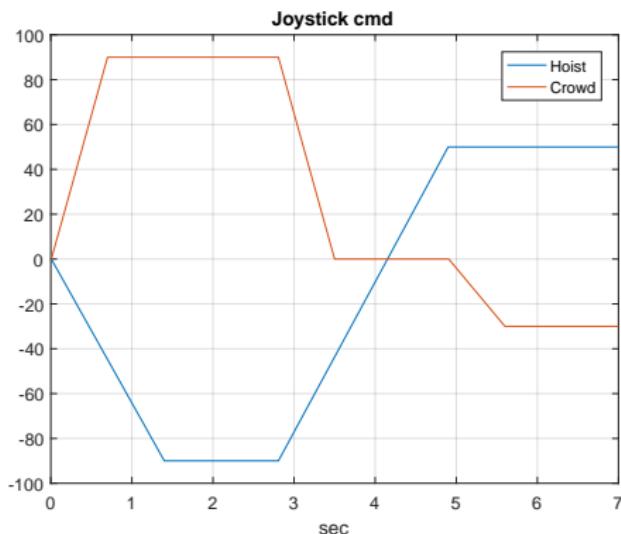
Input: Joystick commands for Up/Down and Forth/Back

Output: Position of the shovel

Trajectories

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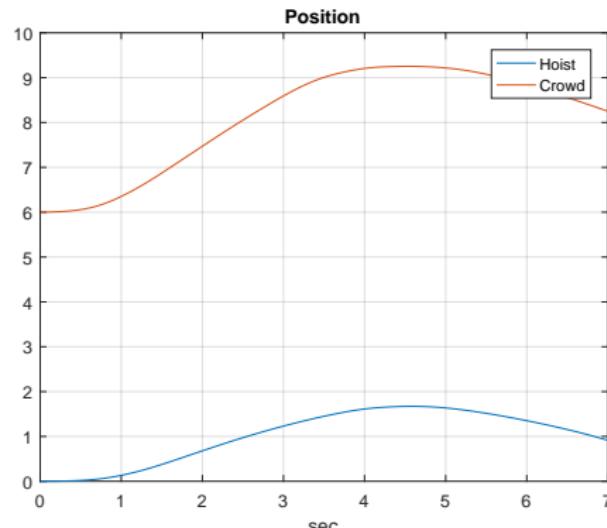
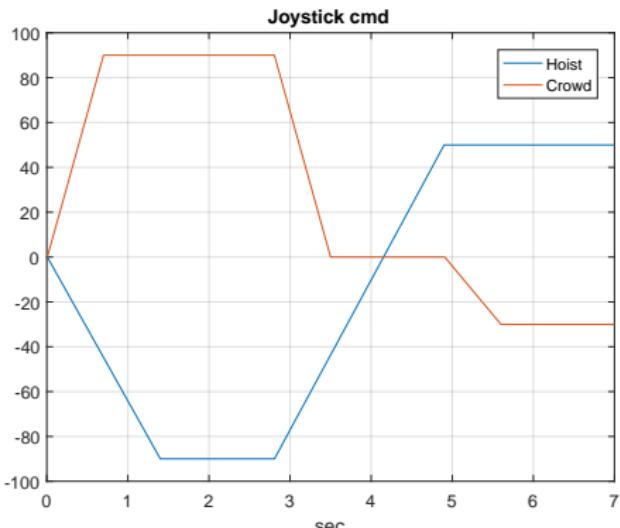
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Trajectories

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Output: Position of the shovel



Objective Function

Optimized Parameters:

- Inertia (Engine)
- Inertia (Arm)
- Friction
- Mass

Objective Function

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Penalty Term:

$$\|\bar{X}_i - X_i(p)\|^2$$

Objective Function

Optimized Parameters:

- Inertia (Engine)
- Inertia (Arm)
- Friction
- Mass

Penalty Term:

$$\frac{\|\bar{X}_i - X_i(p)\|^2}{\|\bar{X}_i\|^2}$$

Objective Function

Optimized Parameters:

- Inertia (Engine)
- Inertia (Arm)
- Friction
- Mass

Penalty Term:

$$\frac{\|\bar{X}_i - X_i(p)\|^2}{\|\bar{X}_i\|^2} + \frac{\|\bar{Y}_i - Y_i(p)\|^2}{\|\bar{Y}_i\|^2}$$

\bar{X}_i, \bar{Y}_i reference trajectories

Objective Function

Optimized Parameters:

- Inertia (Engine)
- Inertia (Arm)
- Friction
- Mass

Penalty Term:

$$\frac{1}{n} \cdot \sum_{i=1}^n \left(\frac{\|\bar{X}_i - X_i(p)\|^2}{\|\bar{X}_i\|^2} + \frac{\|\bar{Y}_i - Y_i(p)\|^2}{\|\bar{Y}_i\|^2} \right)$$

\bar{X}_i, \bar{Y}_i reference trajectories

Objective Function

Optimized Parameters:

- Inertia (Engine)
- Inertia (Arm)
- Friction
- Mass

Penalty Term:

$$\min_{p \in \mathbb{R}^4} f(p) = \frac{1}{n} \cdot \sum_{i=1}^n \left(\frac{\|\bar{X}_i - X_i(p)\|^2}{\|\bar{X}_i\|^2} + \frac{\|\bar{Y}_i - Y_i(p)\|^2}{\|\bar{Y}_i\|^2} \right)$$

s. t.

$$p_j \geq 0$$

\bar{X}_i, \bar{Y}_i reference trajectories

Influence of the Parameters

10% parameter deviation:

- Inertia (Engine): $1 \cdot 10^{-3}$
- Inertia (Arm): $3 \cdot 10^{-3}$
- Friction: $8 \cdot 10^{-11}$
- Mass: $5 \cdot 10^{-2}$

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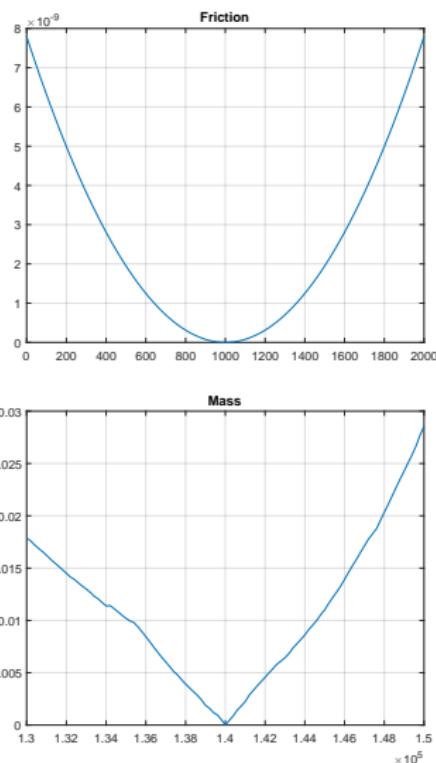
Big parameter changes \Rightarrow Small effects

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Optimizers

- Derivative free optimization
- Deterministic or stochastic
- Decrease function value by evaluating systematically

Optimizers

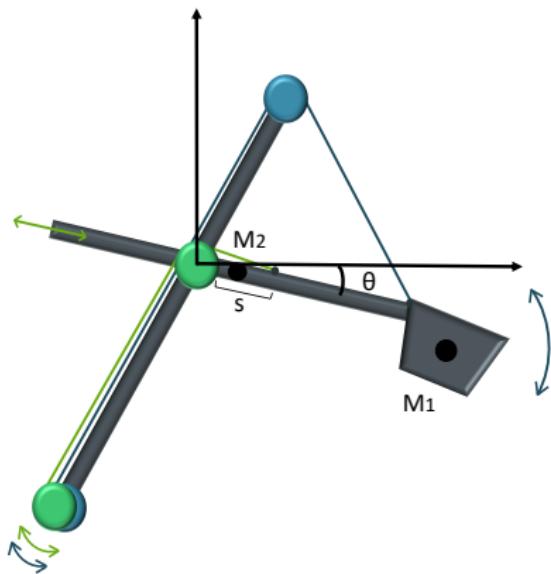
- Derivative free optimization
- Deterministic or stochastic
- Decrease function value by evaluating systematically

	value	evaluations	time	dev_{\max}	dev_{mean}
Particle Swarm	10^{-12}	2200	6 min	$10^{-1.0}$	$10^{-3.8}$
Pattern Search	10^{-11}	6500	17 min	$10^{-1.3}$	$10^{-3.7}$
Genetic Algorithm	10^{-4}	5500	14 min	$10^{-0.5}$	$10^{-1.0}$
Simulated Annealing	10^{-3}	4200	11 min	$10^{-0.3}$	$10^{-0.6}$

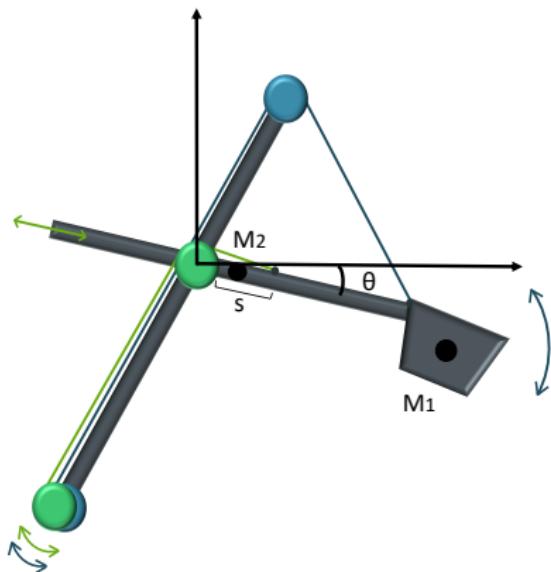
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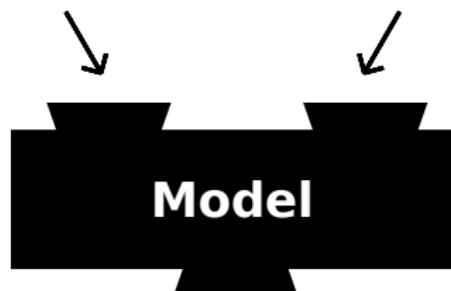
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Summary



Control **Parameters?**



Motion