Trajectories

Input

- Joystick commands: `cmd_hst_pt`, `cmd_crd_pt`

Output

- Torques: `u_hst`, `u_crd`
- Positions: `y_hst`, `y_crd`

Currently we have:

- `n_tra` different trajectories of size `n_sim`
- `n_tra = 9; n_sim = 1000`
- each of them is a matrix of size `(n_sim, n_tra)`

Objective Function

Parameters that are optimized:

`hst_inertia_engine, inertia_yy, hst_friction, crd_mass`

$$\begin{aligned} \min_{p \in \mathbb{R}^4} f(p) = \quad & \frac{1}{n_{\text{tra}}} \cdot \left(\alpha_1 \cdot \| \overline{U}_{\text{hst}} - U_{\text{hst}}(p) \|_{\text{F}}^2 + \ldots \right) \\ \text{s.t.} \quad & p_i \geq 0 \end{aligned}$$

where

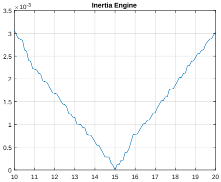
$$\alpha_1 = \frac{1}{\|\overline{U}_{\text{hst}}\|_{\text{F}}^2} \qquad \|\overline{U}_{i,j}\|_{\text{F}}^2 = \sum_{j=1}^{n_{\text{tra}}} \sum_{i=1}^{n_{\text{sim}}} |\overline{U}_{i,j}|^2$$

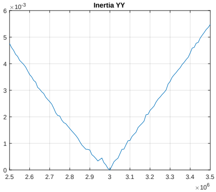
$\| \cdot \|_{\text{F}}$ is the Frobenius norm

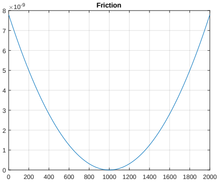
Influence of the Parameters

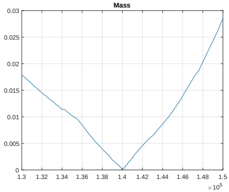
10% deviation of parameter . . . cause in the objective function:

- `hst_inertia_engine` $1 \cdot 10^{-3}$ linear
- `inertia_yy` $3.3 \cdot 10^{-3}$ linear
- `hst_friction` $7.8 \cdot 10^{-11}$ quadratic
- `crd_mass` $52 \cdot 10^{-3}$ linear









Solvers

Conditions:

- Starting values: $X \sim \mathrm{N}\left(\bar{x}, \bar{x}/2\right)$, where $\bar{x}$ is the given value
- Smarm Size: 10
- Function Tolerance: 10^{-9}
- Time Limit: 15 min
- Max Iterations: ∞

	penalty	evaluations	time
Particle Swarm	10^{-13}	2500	3 min
Pattern Search	10^{-3}	6000	8 min
Genetic Algorithm	10^{-2}	7500	15 min (time limit)
Simulated Annealing	10^{-1}	3000	4 min

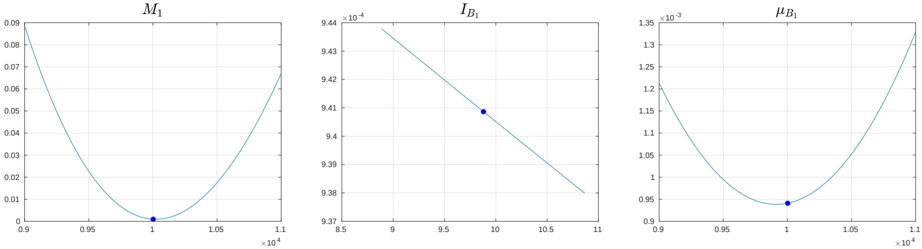
Optimization Problem

$$\min_{p\in\mathbb{R}^{10}} f(p) = \frac{1}{2}\|x_{\mathsf{ref}} - x(p)\|^2$$
$$\text{s. t.} \quad p_i \geq 0$$

- state $x = (s, \theta, \dot{s}, \dot{\theta})^T$
- x_{ref} reference trajectory
- $x(p)$ approximation using Runge-Kutta methods of Order 1/2/3/4

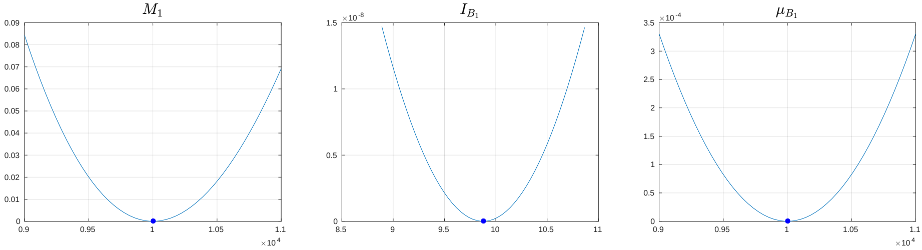
Influence of the Parameters

Using $x_{\text{ref}} = x_{\text{real}}$, the real trajectory:



Influence of the Parameters

Using $x_{\text{ref}} = x(p_{\text{real}})$, the approximation from the real parameters:



Solvers

Conditions:

- Supporting Points: 100
- Runge-Kutta Order: 1
- Reference Trajectory: x_{real}
- $\frac{1}{2}\|x_{\text{real}} - x(p_{\text{real}})\|^2 = 9.4 \cdot 10^{-4}$
- Optimality Tolerance: 10^{-10}

	iterations	$\frac{1}{2}\|x_{\text{real}} - x(p)\|$	$\frac{1}{2}\|x(p_{\text{real}}) - x(p)\|$
SQP	177	$1.8 \cdot 10^{-4}$	$7.6 \cdot 10^{-4}$
Interior Point	186	$1.8 \cdot 10^{-4}$	$7.6 \cdot 10^{-4}$
Trust Region	12	$1.8 \cdot 10^{-4}$	$7.6 \cdot 10^{-4}$
Active Set	17	$1.9 \cdot 10^{-2}$	$2.6 \cdot 10^{-2}$

Solvers

Conditions:

- Supporting Points: 100
- Runge-Kutta Order: 4
- Reference Trajectory: x_{real}
- $\frac{1}{2}\|x_{\text{real}} - x(p_{\text{real}})\|^2 = 9.4 \cdot 10^{-5}$
- Optimality Tolerance: 10^{-10}

	iterations	$\frac{1}{2}\|x_{\text{real}} - x(p)\|$	$\frac{1}{2}\|x(p_{\text{real}}) - x(p)\|$
SQP	193	$8.9 \cdot 10^{-5}$	$5.3 \cdot 10^{-6}$
Interior Point	206	$8.9 \cdot 10^{-5}$	$5.3 \cdot 10^{-6}$
Trust Region	19	$8.9 \cdot 10^{-5}$	$5.2 \cdot 10^{-6}$
Active Set	17	$1.9 \cdot 10^{-2}$	$1.9 \cdot 10^{-2}$