

# RSA-CRT Fault Attack

Let  $(e, N)$  be the RSA public key and  $(p, q, |d|_p, |d|_q, |q^{-1}|_p)$  the RSA private key for use with Chinese Remainder Theorem (CRT). Furthermore, assume that the signer produced a faulty signature  $f$ , whereby the fault affected only the partial signature modulo  $p$  (i.e.  $s_1$  according to the RFC), and later discovered that the signature was invalid and recomputed the signature  $s$ , this time without errors.

We know from PKCS #1 that there exist  $s_1, s_2$  s.t.  $s = s_2 + q \cdot |(s_1 - s_2) \cdot |q^{-1}|_p|_p$  and similarly some  $f_1$  exists s.t.  $f = s_2 + q \cdot |(f_1 - s_2) \cdot |q^{-1}|_p|_p$ .

From that follows that  $s - f = q \cdot |(s_1 - f_1) \cdot |q^{-1}|_p|_p$ , which means  $q$  divides  $s - f$ .

Since  $q$  is prime, it follows that  $q = \gcd(s - f, N)$ .

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## References:

- <https://crypto.stanford.edu/~dabo/abstracts/faults.html>

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