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BinarySearch.pd
                                                                             2/15/2006
// Example of implementing a binary search algorithm.
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final class Table of X
require X has total operator (arg) end
abstract
         var members: seq of X;
         // Invariant states that the members are in a non-decreasing order
        invariant members.isndec;
interface
         // Find the index of the first element that ranks with or below the
        parameter
         function search(x: X): nat
                  satisfy result <= #members,</pre>
                           forall z::0..<result :- x > members[z],
                           forall z::result..<#members :- ~(x > members[z])
                 via
                           // Implement with a binary search
                          var i: nat != 0;
                           loop
                                   var k: int != #members;
                                   change i
                                   keep
                                            0 <= i',
                                            i' <= k',
                                            k' <= #members,
                                            forall z::0..<i':-x> members[z],
                                            forall z::k'...<\#members :- \sim (x >
                                            members[z])
                                   until i' = k'

decrease k' - i';

// Start of loop body...

// Set up the partition value
                                   let p = (i + k)/2;
assert i <= p < k;
                                   if
                                    [x > members[p]]:
                                            i! = >p;
                                            // If x ranks above members[p] then
                                            // move i to >p
                                    []:
                                            // If x ranks with or below members[p]
                                            // then move k to p
                                   fi
                           end;
                          value i;
                  end;
         // Count operator
         operator #: nat
^= #members;
         // Index operator to access the members of the list
         operator [] (index: nat): X
                  pre index < #self</pre>
                   = members[index];
         // Build from a set
         build{mem: set of X}
                 post members! = mem.permndec;
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end;