

TEST - Factoring & Transformations #3

K/U /13

A 12/16

TIP 10.5/15

C 5/1/Level

Knowledge and Understanding.

1. Evaluate: 2^{-3}

a) -8

b) -6

c) $-\frac{1}{8}$

d) $\frac{1}{4}$

e) $\frac{1}{8}$

2. Evaluate: $\left(\frac{2}{3}\right)^{-3}$

a) $-\frac{8}{27}$

b) $-\frac{8}{27}$

c) $\frac{8}{27}$

d) $\frac{27}{8}$

e) $\frac{35}{6}$

3. Expand and simplify: $(2x + 5y)(3x - 2y)$

a) $6x^2 - 11xy - 10y^2$

b) $6x^2 + 3xy - 10y^2$

c) $6x^2 + 4xy - 10y^2$

d) $6x^2 - 10y^2$

e) $6x^2 + 11xy - 10y^2$

4. Expand and simplify: $(3x + 4)^2$

a) $12x^2 + 12x + 16$

b) $12x^2 + 24x + 16$

c) $9x^2 + 24x + 16$

d) $9x^2 + 12x + 16$

e) $9x^2 + 24x + 8$

5. Expand and simplify: $(4x - 3y)^2$

a) $12x^2 - 12xy + 9y^2$

b) $8x^2 - 24xy + 9y^2$

c) $16x^2 - 24xy + 9y^2$

d) $16x^2 - 24xy - 9y^2$

e) $16x^2 - 12xy + 9y^2$

6. Factor: $x^2 + 7x + 12$

a) $(x + 4)(x + 3)$

b) $(x + 2)(x + 6)$

c) $(x + 12)(x + 1)$

d) $(x + 7)(x + 5)$

e) $(x - 4)(x - 3)$

7. Factor: $2x^2 + 13x - 15$

a) $(2x + 15)(x - 1)$

b) $(2x - 5)(x + 3)$

c) $(2x + 3)(x - 5)$

d) $(2x + 5)(x - 3)$

e) $(2x - 1)(x - 15)$

8. Factor: $9x^2 - 16y^2$

a) $(3x - 4y)(3x - 4y)$

b) $(9x + 16y)(x - y)$

c) $(9x - 16y)(x + y)$

d) $(3x + 4y)(3x - 4y)$

e) $x(9x - 16y)$

9. Factor completely: $8x^2 + 48x + 72$

a) $8(x + 3)^2$

b) $(8x + 24)(x + 3)$

c) $(2x + 6)(4x + 12)$

d) $8(x^2 + 6x + 9)$

e) $4(2x + 3)(x + 6)$

10. Factor: $x^4 - 12x^2y^2 + 36y^4$

a) $(x^2 - 6y^2)^2$

b) $(x^2 - 12y^2)^2$

c) $(x^4 - 6y^2)^2$

d) $(x^2 - 6y^4)^2$

e) $(x^4 - 6y^4)^2$

[3] 11. Complete the following table:

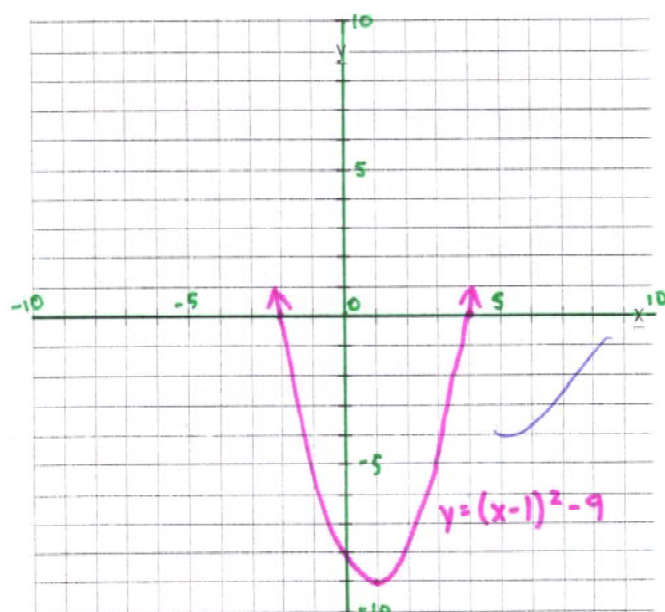
Equation	Vertex	Axis of symmetry	Vertical stretch or compression	Vertical movement	Horizontal movement	Max. or Min. value
$y = -2(x-3)^2 - 1$	$(3, -1)$	$x = 3$	vertical stretch by	1 unit down	3 units right	y max = -1
$y = \frac{1}{2}x^2 + 8$	$(-8, 0)$	$x = -8$	vertical compression by	8 units left	none	y min = 0

2.5

Applications.

[4] 12. The zeros of parabola are -2 and 4. The parabola is congruent to $y = x^2$. Find an equation in a factored form and graph it using zeros.

$$\textcircled{1} \quad y = (x+2)(x-4) \quad M = \frac{-2+4}{2} = 1$$



sub $x = 1$ into $\textcircled{1}$

$$\begin{aligned} y &= (1+2)(1-4) \\ &= 3 \times -3 \\ &= -9. \end{aligned}$$

vertex = $(1, -9)$

$$y = (x-1)^2 - 9$$

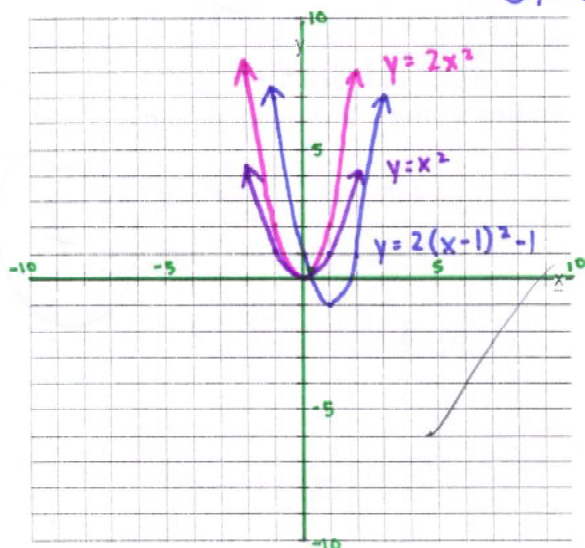
4

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[12] 13. Graph using transformations.

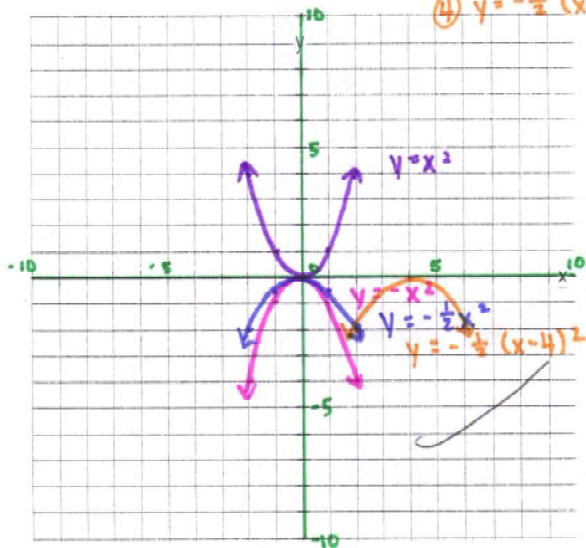
a) $y = 2(x-1)^2 - 1$

- ① $y = x^2$
- ② $y = 2x^2$
- ③ $y = 2(x-1)^2 - 1$



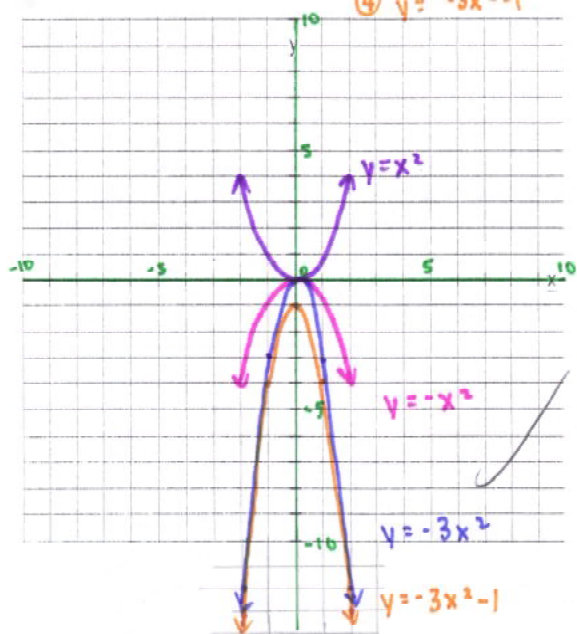
b) $y = -\frac{1}{2}(x-4)^2$

- ① $y = x^2$
- ② $y = -x^2$
- ③ $y = -\frac{1}{2}x^2$
- ④ $y = -\frac{1}{2}(x-4)^2$



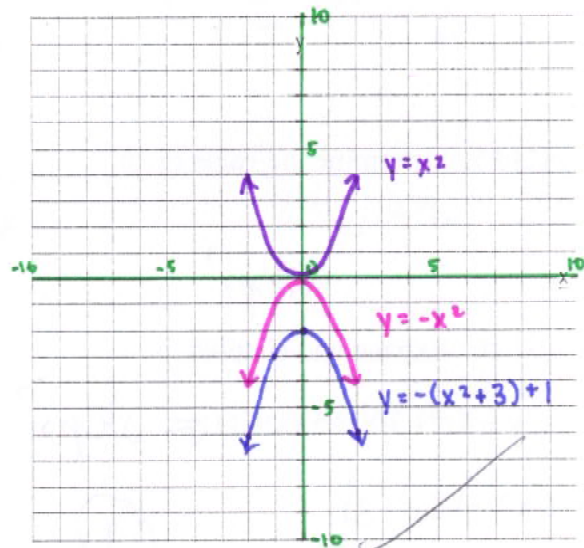
c) $y = -3x^2 - 1$

- ① $y = x^2$
- ② $y = -x^2$
- ③ $y = -3x^2$
- ④ $y = -3x^2 - 1$



d) $y = -(x^2 + 3) + 1$

- ① $y = x^2$
- ② $y = -x^2$
- ③ $y = -(x^2 + 3) + 1$



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Thinking. Inquiry. Problem Solving. [15]

[7] 14. Factor fully.

a) $mx - my - 5x + 5y$

$(x-y)(m-5)$ ✓

b) $5m^2 - 6m - 8$

$(m-2)(5m+4)$ ✓

c) $4x^2 - 28xy + 49y^2$

$(2x+7y)^2$ ✓

d) $3m^2 - 8m - 3$

$(m-3)(3m+1)$ ✓

e) $3x^3 - 3x^2 - 6x$

$3x(x-2)(x+1)$ ✓

f) $4a^2 - (2b+3)^2$

$(2a+2b+3)(2a-2b-3)$ ✓

g) $(x^2 - 3x)^2 - 2(x^2 - 3x) - 8$

$(x-4)(x+1)(x-2)(x-1)$ ✓

7

[2] 15. Determine the value of "n"

$-3^n = -\frac{1}{27}$

$n = -3$

5

Steps?

[3] 16. Expand and simplify.

$(3x+4)^2 - 3(x+5)(x-1)$ Steps?

$= 6x^2 - 12x + 31$

1

[3] 17. A parabola has zeros at -1 and 5 and passes through (0, -5). Write an equation in a standard form.

$M = \frac{-1+5}{2}$

$= 2$ ✓

$y = (x+1)(x-5)$

$y = x^2 - 4x - 5$

Steps

a=?

2

10.5