

11.5
K/U /13TEST - Factoring & Transformations #3
A 12+4/16 TIP 10.5/15

C 10/15 /Level 4

Knowledge and Understanding.

1. Evaluate:
- 2^{-3}

- a) -8 b) -6 c)
- $-\frac{1}{8}$
- d)
- $\frac{1}{4}$

e) $\frac{1}{8}$

2. Evaluate:
- $\left(\frac{2}{3}\right)^{-3}$

- a)
- $-\frac{8}{3}$
- b)
- $-\frac{8}{27}$
- c)
- $\frac{8}{27}$

d) $\frac{27}{8}$

e) $\frac{35}{6}$

3. Expand and simplify:
- $(2x + 5y)(3x - 2y)$

- a)
- $6x^2 - 11xy - 10y^2$
- b)
- $6x^2 + 3xy - 10y^2$
- c)
- $6x^2 + 4xy - 10y^2$
-
- d)
- $6x^2 - 10y^2$
- e)
- $6x^2 + 11xy - 10y^2$

4. Expand and simplify:
- $(3x + 4)^2$

- a)
- $12x^2 + 12x + 16$
- b)
- $12x^2 + 24x + 16$
- c)
- $9x^2 + 24x + 16$
- d)
- $9x^2 + 12x + 16$
- e)
- $9x^2 + 24x + 8$

5. Expand and simplify:
- $(4x - 3y)^2$

- a)
- $12x^2 - 12xy + 9y^2$
- b)
- $8x^2 - 24xy + 9y^2$
- c)
- $16x^2 - 24xy + 9y^2$
-
- d)
- $16x^2 - 24xy - 9y^2$
- e)
- $16x^2 - 12xy + 9y^2$

6. Factor:
- $x^2 + 7x + 12$

- a)
- $(x + 4)(x + 3)$
- b)
- $(x + 2)(x + 6)$
- c)
- $(x + 12)(x + 1)$
- d)
- $(x + 7)(x + 5)$
- e)
- $(x - 4)(x - 3)$

7. Factor:
- $2x^2 + 13x - 15$

- a)
- $(2x + 15)(x - 1)$
- b)
- $(2x - 5)(x + 3)$
- c)
- $(2x + 3)(x - 5)$
- d)
- $(2x + 5)(x - 3)$
- e)
- $(2x - 1)(x - 15)$

8. Factor:
- $9x^2 - 16y^2$

- a)
- $(3x - 4y)(3x + 4y)$
- b)
- $(9x + 16y)(x - y)$
- c)
- $(9x - 16y)(x + y)$
-
- d)
- $(3x + 4y)(3x - 4y)$
- e)
- $x(9x - 16y)$

9. Factor completely:
- $8x^2 + 48x + 72$

- a)
- $8(x + 3)^2$
- b)
- $(8x + 24)(x + 3)$
- c)
- $(2x + 6)(4x + 12)$
-
- d)
- $8(x^2 + 6x + 9)$
- e)
- $4(2x + 3)(x + 6)$

10. Factor:
- $x^4 - 12x^2y^2 + 36y^4$

- a)
- $(x^2 - 6y^2)^2$
- b)
- $(x^2 - 12y^2)^2$
- c)
- $(x^4 - 6y^2)^2$
- d)
- $(x^2 - 6y^4)^2$
- e)
- $(x^4 - 6y^4)^2$

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9.1 Intro to Parabolas

[3] 11. Complete the following table:

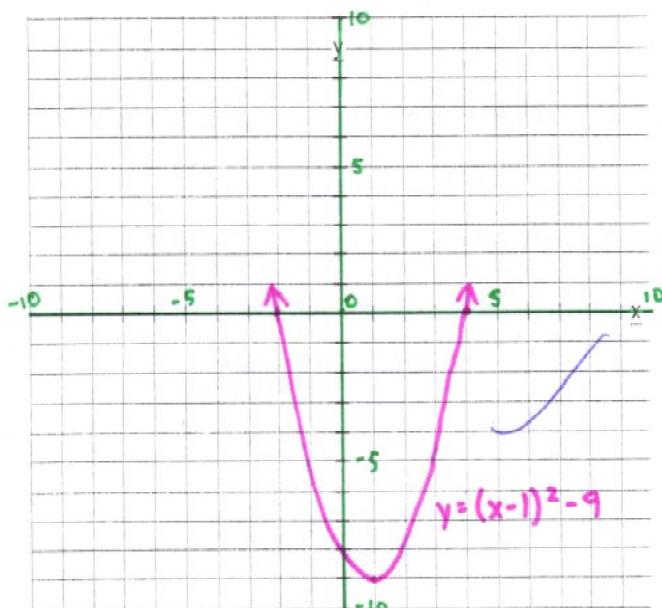
Equation	Vertex	Axis of symmetry	Vertical stretch or compression	Vertical movement	Horizontal movement	Max. or Min. value
$y = -2(x-3)^2 - 1$	(3, -1)	$x = 3$	vertical stretch by 2	1 unit down	3 units right	$y_{\max} = -1$
$y = \frac{1}{2}x^2 + 8$	(-8, 0)	$x = -8$	vertical compression by $\frac{1}{2}$	8 units left	none	$y_{\min} = 0$

2.5

Applications.

[4] 12. The zeros of parabola are -2 and 4. The parabola is congruent to $y = x^2$. Find an equation in a factored form and graph it using zeros.

$$\textcircled{1} \quad y = (x+2)(x-4) \quad M = \frac{-2+4}{2} \\ = 1$$



sub $x = 1$ into $\textcircled{1}$

$$y = (1+2)(1-4)$$

$$= 3 \times -3 \\ = -9.$$

$$\text{vertex} = (1, -9)$$

$$y = (x-1)^2 - 9$$

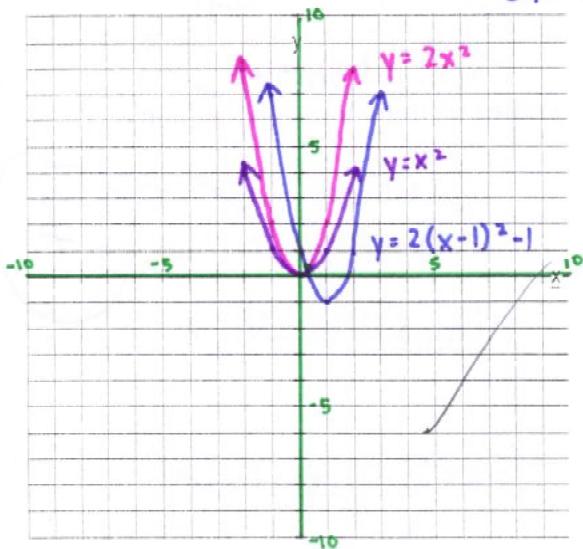
⑨

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[12] 13. Graph using transformations.

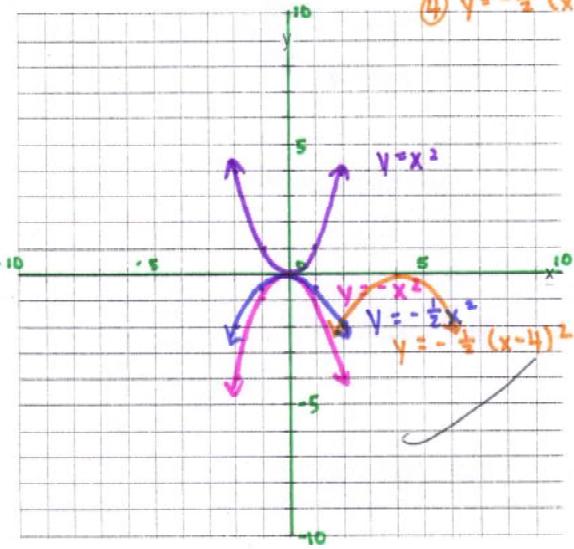
a) $y = 2(x - 1)^2 - 1$

- ① $y = x^2$
- ② $y = 2x^2$
- ③ $y = 2(x - 1)^2 - 1$



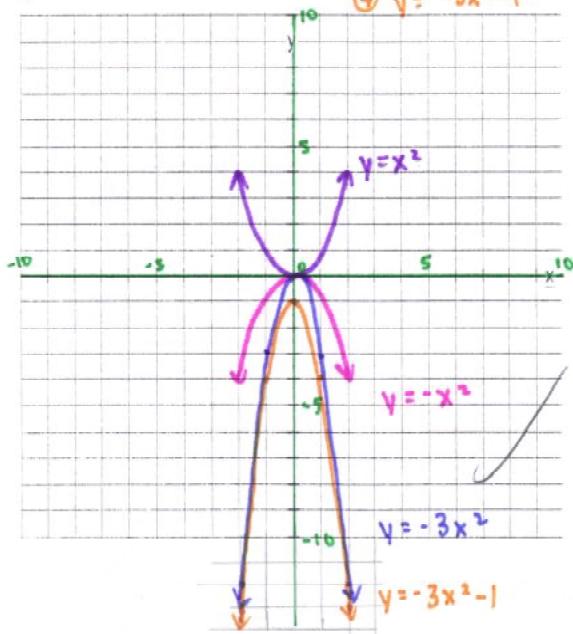
b) $y = -\frac{1}{2}(x - 4)^2$

- ① $y = x^2$
- ② $y = -x^2$
- ③ $y = -\frac{1}{2}x^2$
- ④ $y = -\frac{1}{2}(x - 4)^2$



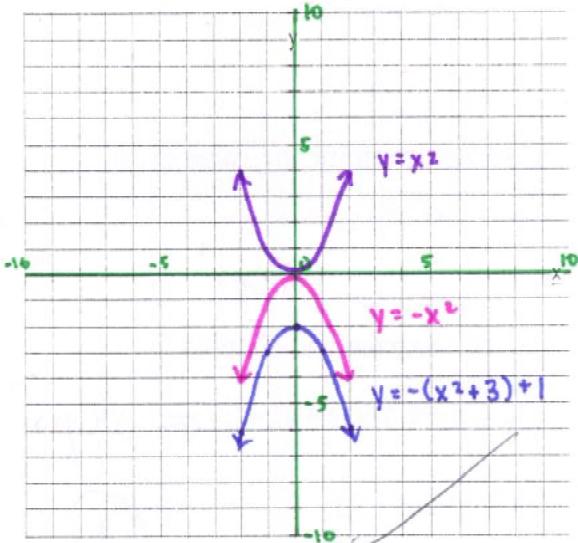
c) $y = -3x^2 - 1$

- ① $y = x^2$
- ② $y = -x^2$
- ③ $y = -3x^2$
- ④ $y = -3x^2 - 1$



d) $y = -(x^2 + 3) + 1$

- ① $y = x^2$
- ② $y = -x^2$
- ③ $y = -(x^2 + 3) + 1$



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Thinking, Inquiry, Problem Solving. [15]

[7] 14. Factor fully.

a) $mx - my - 5x + 5y$

$$(x-y)(m-5)$$

b) $5m^2 - 6m - 8$

$$(m-2)(5m+4)$$

c) $4x^2 - 28xy + 49y^2$

$$(2x-7y)^2$$

d) $3m^2 - 8m - 3$

$$(m-3)(3m+1)$$

e) $3x^3 - 3x^2 - 6x$

$$3x(x-2)(x+1)$$

f) $4a^2 - (2b+3)^2$

$$(2a+2b+3)(2a-2b+3)$$

g) $(x^2 - 3x)^2 - 2(x^2 - 3x) - 8$

$$(x-4)(x+1)(x-2)(x-1)$$

[2] 15. Determine the value of "n"

$$-3^n = -\frac{1}{27}$$

Steps? $n = -3$ (5)

[3] 16. Expand and simplify.

$$(3x+4)^2 - 3(x+5)(x-1)$$

Steps?

$$= 6x^2 - 12x + 31$$

(1)

[3] 17. A parabola has zeros at -1 and 5 and passes through (0, -5). Write an equation in standard form.

$$M = \frac{-1+5}{2}$$

$$y = (x+1)(x-5)$$

$$= 2$$

$$y = x^2 - 4x - 5$$

Steps?

$$a = ?$$

(2)

10.5