Singletons and You

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Preface

Slide available at https://mstksg.github.io/talks/lambdaconf-2017/singletons/singleton-slides.html.

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GHC extensions (potentially) used:

```
{-# LANGUAGE GADTs
                                   #-}
{-# LANGUAGE KindSignatures
                                   #-}
{-# LANGUAGE LambdaCase
                                   #-}
{-# LANGUAGE RankNTypes
                                   #-}
{-# LANGUAGE RankNTypes
                                   #-}
{-# LANGUAGE ScopedTypeVariables
                                   #-}
{-# LANGUAGE TemplateHaskell
                                   #-}
{-# LANGUAGE TypeFamilies
                                   #-}
{-# LANGUAGE TypeInType
                                   #-}
{-# LANGUAGE TypeOperators
                                   #-}
{-# LANGUAGE UndecidableInstances #-}
```

Safety with Phantom Types

```
data DoorState = Opened | Closed | Locked
  deriving (Show, Eq)

data Door (s :: DoorState) = UnsafeMkDoor

-- alternatively
data Door :: DoorState -> Type where
  UnsafeMkDoor :: Door s
```

Other similar examples

- State machines (socket connections, file handles, opened/closed)
- Refinement types
- "Tagged" types (santized/unsantized strings)

```
closeDoor :: Door 'Opened -> Door 'Closed
closeDoor UnsafeMkDoor = UnsafeMkDoor
```

```
closeDoor :: Door 'Opened -> Door 'Closed
closeDoor UnsafeMkDoor = UnsafeMkDoor

openDoor :: Door 'Closed -> Door 'Opened
openDoor UnsafeMkDoor = UnsafeMkDoor
```

```
doorStatus :: Door s -> DoorState
doorStatus = -- ?????
```

We have a problem.

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doorStatus :: Door s -> DoorState
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```

More Problems

```
initalizeDoor :: DoorStatus -> Door s
initializeDoor = \case
    Opened -> UnsafeMkDoor
    Closed -> UnsafeMkDoor
    Locked -> UnsafeMkDoor
```

More Problems

```
initalizeDoor :: DoorStatus -> Door s
initializeDoor = \case
    Opened -> UnsafeMkDoor
    Closed -> UnsafeMkDoor
    Locked -> UnsafeMkDoor
```

Neat, but does this work?

More Problems

```
ghci> :t initializeDoor Opened :: Door 'Closed
initializeDoor Opened :: Door 'Closed
Oops.
```

► In Haskell, types only exist at *compile-time*. They are **erased** at runtime.

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- ▶ In Haskell, types only exist at *compile-time*. They are **erased** at runtime.
- ► This is a good thing for performance! Types incur no runtime overhead!
- But it makes functions like doorStatus fundamentally unwritable without fancy typeclasses.
- ▶ ...or does it?

```
data SingDS :: DoorStatus -> Type where
```

SOpened :: SingDS 'Opened SClosed :: SingDS 'Closed SLocked :: SingDS 'Locked

Creates three constructors:

SOpened :: SingDS 'Opened SClosed :: SingDS 'Closed SLocked :: SingDS 'Locked

▶ A **singleton** is a type that has exactly one inhabited value.

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- ▶ A **singleton** is a type that has exactly one inhabited value.
- There is only one value of type SingDS 'Opened, and only one value of type SingDS 'Closed.
- ▶ The constructor that a SingDS s uses reveals to us what s is.

With our new singletons, we can essentially **pattern match** on types:

```
showSingDS :: SingDS s -> String
showSingDS = \case
    SOpened -> "Opened"
    SClosed -> "Closed"
    SLocked -> "Locked"
```

With our new singletons, we can essentially **pattern match** on types:

```
showSingDS :: SingDS s -> String
showSingDS = \case
    SOpened -> "Opened"
    SClosed -> "Closed"
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```

Alone like this, it's a bit boring. We didn't need GADTs for this.

Door Status

```
doorStatus' :: SingDS s -> Door s -> DoorState
doorStatus' = \case
    SOpened -> \_ -> "Door is opened"
    SClosed -> \_ -> "Door is closed"
    SLocked -> \_ -> "Door is locked"
```

► GADT-ness allows us to enforce that the s in SingDS s is the same as the s in our Door.

Door Status

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doorStatus' :: SingDS s -> Door s -> DoorState
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- Singleton property means that SingDS s has a one-to-one correspondence with its constructors.

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- ► GADT-ness allows us to enforce that the s in SingDS s is the same as the s in our Door.
- Singleton property means that SingDS s has a one-to-one correspondence with its constructors.
- Pattern matching on that single constructor reveals to us the type of Door.

Implicit Passing

class SingDSI s where

```
singDS :: SingDSI s

instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
```

Implicit Passing

```
class SingDSI s where
    singDS :: SingDSI s
instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
doorStatus :: SingDSI s => Door s -> DoorState
doorStatus = doorStatus' singDS
```

Implicit Passing

```
class SingDSI s where
    singDS :: SingDSI s
instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
doorStatus :: SingDSI s => Door s -> DoorState
doorStatus = doorStatus' singDS
ghci> doorStatus (UnsafeMkDoor :: Door 'Locked)
Door is locked!
```

Initialize Door

```
initializeDoor' :: SingDS s -> Door s
initializeDoor' _ _ = UnsafeMkDoor
```

Initialize Door

```
initializeDoor' :: SingDS s -> Door s
initializeDoor' _ _ = UnsafeMkDoor
ghci> :t initializeDoor' SOpened
initializeDoor SOpened :: Door 'Opened
ghci> :t initializeDoor' SClosed
initializeDoor SClosed :: Door 'Closed
```

Initialize Door

Implicit passing style:

```
initializeDoor :: SingDSI s => Door s
initializeDoor = initializeDoor' singDS
```

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- ▶ Really, SingDS s → is the same as SingDSI s ⇒
- ► The two are the same way of providing the same information to the compiler, and at runtime.
- ▶ We can use the two styles interchangebly.
- One is explicitly passing the type, the other is explicitly passing the type.

Ditching the phantom

Sometimes we don't care about what the status of our door is, and we want the type system to relax.

Ditching the phantom

Sometimes we don't care about what the status of our door is, and we want the type system to relax.

This is essentially the same as saying that the status of our door is a runtime property that we do not want to (or sometimes can't) check at compile-time.

Ditching the phantom

```
data SomeDoor :: Type where
```

MkSomeDoor :: SingDS s => Door s -> SomeDoor

Ditching the phantom

```
data SomeDoor :: Type where
    MkSomeDoor :: SingDS s => Door s -> SomeDoor

ghci> let myDoor = MkSomeDoor (initializeDoor SOpened)
ghci> :t myDoor
myDoor :: SomeDoor
ghci> case myDoor of MkSomeDoor d -> doorStatus d
Door is opened.
```

Runtime-deferred types

```
initializeSomeDoor :: DoorStatus -> SomeDoor
initializeSomeDoor = \case
    Opened -> SomeDoor (initialiseDoor' SOpened)
    Closed -> SomeDoor (initialiseDoor' SClosed)
    Locked -> SomeDoor (initialiseDoor' SLocked)
```

Runtime-deferred types

```
initializeSomeDoor :: DoorStatus -> SomeDoor
initializeSomeDoor = \case
    Opened -> SomeDoor (initialiseDoor' SOpened)
    Closed -> SomeDoor (initialiseDoor' SClosed)
    Locked -> SomeDoor (initialiseDoor' SLocked)
ghci> let myDoor = initializeSomeDoor Locked
ghci> :t myDoor
myDoor :: SomeDoor
ghci> case myDoor of MkSomeDoor d -> doorStatus d
Door is locked.
```

The Singletons Library

The singletons library provides a unified framework for creating and working with singletons for different types (not just DoorStatus), and also for functions on those types.

http://hackage.haskell.org/package/singletons

The singletons way

```
$(singletons [d|
  data DoorState = Opened | Closed | Locked
  deriving (Show, Eq)
|])
```

The singletons way

```
$(singletons [d]
  data DoorState = Opened | Closed | Locked
    deriving (Show, Eq)
  11)
This creates three types and three constructors:
-- not the actual code, but essentially what happens
data Sing :: DoorState -> Type where
    SOpened :: Sing 'Opened
    SClosed :: Sing 'Closed
    SLocked :: Sing 'Locked
Sing is a poly-kinded type constructor (family):
```

The singletons way

```
And also

instance SingI 'Opened where
    sing = SOpened

instance SingI 'Closed where
    sing = SClosed

instance SingI 'Locked where
    sing = SLocked

(SingI is a poly-kinded typeclass)
```

Examples

```
STrue :: Sing 'True

SJust SFalse :: Sing ('Just 'True)

SOpened `SCons` SClosed `SCons` SNil :: Sing '[ 'Opened, 'Opened, 'Opened' Strue'

STrue
```

Other stuff created from the library

```
Some other convenient features:
ghci> fromSing SOpened
Opened
ghci> let s = toSing Opened
ghci> :t s
s :: SomeSing DoorStatus
ghci> case s of
        SomeSing SOpened -> "Opened."
        SomeSing SClosed -> "SClosed."
        SomeSing SLocked -> "SLocked."
```

Non-trivial type logic

```
knock :: Door s -> IO ()
knock = -- ??
```

We want to allow the user to knock on a closed or locked door, but not an opened door.

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```
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knock = -- ??
```

We want to allow the user to knock on a closed or locked door, but not an opened door.

We can do this simple case using pattern matching, but it's not always feasible or scalable. We want to define a type relationship that can be used by potentially many functions.

```
$(singletons [d|
  canKnock :: DoorState -> Bool
  canKnock Opened = False
  canKnock Closed = True
  canKnock Locked = True
  [])
```

```
$(singletons [d|
   canKnock :: DoorState -> Bool
   canKnock Opened = False
   canKnock Closed = True
   canKnock Locked = True
   |])
knock :: (CanKnock s ~ True) => Door s -> IO ()
knock _ = putStrLn "knock knock!"
```

```
$(singletons [d|
  canKnock :: DoorState -> Bool
  canKnock Opened = False
  canKnock Closed = True
  canKnock Locked = True
  11)
knock :: (CanKnock s ~ True) => Door s -> IO ()
knock = putStrLn "knock knock!"
ghci> knock (initializeDoor SOpened)
Compile Error!!!!
ghci> knock (initializeDoor SClosed)
knock knock!
```

```
tryKnock' :: Sing s -> Door s -> IO ()
tryKnock' s = case sCanKnock s of
   STrue -> knock
   SFalse -> \_ -> putStrLn "Cannot knock door!"
tryKnock :: SingI s => Door s -> IO ()
tryKnock = tryKnock' sing
```

```
tryKnock' :: Sing s -> Door s -> IO ()
tryKnock' s = case sCanKnock s of
    STrue -> knock
   SFalse -> \ -> putStrLn "Cannot knock door!"
tryKnock :: SingI s => Door s -> IO ()
tryKnock = tryKnock' sing
ghci> tryKnock (initializeDoor SOpened)
Cannot knock door!
ghci> tryKnock (initializeDoor SClosed)
knock knock!
```

Vectors

```
$(singletons [d|
  data N = Z | S N
  |])

data Vec :: N -> Type -> Type where
    VNil :: Vec Z a
    (:*) :: a -> Vec n a -> Vec (S n) a

infixr 5 :*
```

The Types demand it

```
replicateV'
    :: Sing n
    -> a
    -> Vec n a
replicateV' = \case
    SZ    -> \_ -> VNil
    SS n   -> \x    -> x    :* replicateV' n x
```

The Types demand it

```
replicateV'
    :: Sing n
    -> a
    -> Vec n a
replicateV' = \case
    SZ -> \ -> VNil
    SS n \rightarrow \x \rightarrow x :* replicateV' n x
replicateV
    :: SingI n
    => a
    -> Vec n a
replicateV = replicateV' sing
```

Thank you!

Further confusion: https://blog.jle.im/entry/verified-instances-in-haskell.html