Singletons and You

Justin Le https://blog.jle.im (justin@jle.im)

Lambdaconf 2017, May 27, 2017

Preface

Slide available at https://mstksg.github.io/talks/lambdaconf-2017/singletons/singleton-slides.html.

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GHC extensions (potentially) used:

import Data.Singletons

```
{-# LANGUAGE GADTs
                                   #-}
                                   #-}
{-# LANGUAGE KindSignatures
                                   #-}
{-# LANGUAGE LambdaCase
{-# LANGUAGE RankNTypes
                                   #-}
                                   #-}
{-# LANGUAGE RankNTypes
{-# LANGUAGE ScopedTypeVariables
                                   #-}
                                   #-}
{-# LANGUAGE TemplateHaskell
{-# LANGUAGE TypeFamilies
                                   #-}
{-# LANGUAGE TypeInType
                                   #-}
{-# LANGUAGE TypeOperators
                                   #-}
{-# LANGUAGE UndecidableInstances #-}
import Data.Kind
                        -- to get type Type = *
```

Safety with Phantom Types

```
data DoorState = Opened | Closed | Locked
  deriving (Show, Eq)

data Door (s :: DoorState) = UnsafeMkDoor

-- alternatively
data Door :: DoorState -> Type where
  UnsafeMkDoor :: Door s
```

Other similar examples

- State machines (socket connections, file handles, opened/closed)
- Refinement types
- "Tagged" types (santized/unsantized strings)

```
closeDoor :: Door 'Opened -> Door 'Closed
closeDoor UnsafeMkDoor = UnsafeMkDoor
```

```
closeDoor :: Door 'Opened -> Door 'Closed
closeDoor UnsafeMkDoor = UnsafeMkDoor

openDoor :: Door 'Closed -> Door 'Opened
openDoor UnsafeMkDoor = UnsafeMkDoor
```

```
doorStatus :: Door s -> DoorState
doorStatus = -- ????
```

We have a problem.

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```
doorStatus :: Door s -> DoorState
doorStatus UnsafeMkDoor = -- s ????
```

More Problems

```
initalizeDoor :: DoorStatus -> Door s
initializeDoor = \case
    Opened -> UnsafeMkDoor
    Closed -> UnsafeMkDoor
    Locked -> UnsafeMkDoor
```

More Problems

```
initalizeDoor :: DoorStatus -> Door s
initializeDoor = \case
    Opened -> UnsafeMkDoor
    Closed -> UnsafeMkDoor
    Locked -> UnsafeMkDoor
```

Neat, but does this work?

More Problems

```
ghci> :t initializeDoor Opened :: Door 'Closed
initializeDoor Opened :: Door 'Closed
Oops.
```

▶ In Haskell, types only exist at *compile-time*. They are **erased** at runtime.

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- In Haskell, types only exist at compile-time. They are erased at runtime.
- ➤ This is a good thing for performance! Types incur no runtime overhead!
- But it makes functions like doorStatus fundamentally unwritable without fancy typeclasses.
- ▶ ...or does it?

```
data SingDS :: DoorStatus -> Type where
   SOpened :: SingDS 'Opened
   SClosed :: SingDS 'Closed
   SLocked :: SingDS 'Locked
```

Creates three constructors:

```
SOpened :: SingDS 'Opened
SClosed :: SingDS 'Closed
SLocked :: SingDS 'Locked
```

▶ A **singleton** is a type that has exactly one inhabited value.

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- ► A **singleton** is a type that has exactly one inhabited value.
- ► There is only one value of type SingDS 'Opened, and only one value of type SingDS 'Closed.
- ▶ The constructor that a SingDS s uses reveals to us what s is.

With our new singletons, we can essentially **pattern match** on types:

```
showSingDS :: SingDS s -> String
showSingDS = \case
    SOpened -> "Opened"
    SClosed -> "Closed"
    SLocked -> "Locked"
```

With our new singletons, we can essentially **pattern match** on types:

```
showSingDS :: SingDS s -> String
showSingDS = \case
    SOpened -> "Opened"
    SClosed -> "Closed"
    SLocked -> "Locked"
```

Alone like this, it's a bit boring. We didn't need GADTs for this.

Door Status

```
doorStatus' :: SingDS s -> Door s -> DoorState
doorStatus' = \case
    SOpened -> \_ -> "Door is opened"
    SClosed -> \_ -> "Door is closed"
    SLocked -> \_ -> "Door is locked"
```

► GADT-ness allows us to enforce that the s in SingDS s is the same as the s in our Door.

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- ► GADT-ness allows us to enforce that the s in SingDS s is the same as the s in our Door.
- Singleton property means that SingDS s has a one-to-one correspondence with its constructors.

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- ► GADT-ness allows us to enforce that the s in SingDS s is the same as the s in our Door.
- Singleton property means that SingDS s has a one-to-one correspondence with its constructors.
- Pattern matching on that single constructor reveals to us the type of Door.

Implicit Passing

class SingDSI s where

```
singDS :: SingDSI s

instance SingDSI 'Opened where
    singDS = SOpened

instance SingDSI 'Closed where
    singDS = SClosed

instance SingDSI 'Locked where
    singDS = SLocked
```

Implicit Passing

```
class SingDSI s where
    singDS :: SingDSI s
instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
doorStatus :: SingDSI s => Door s -> DoorState
doorStatus = doorStatus' singDS
```

Implicit Passing

```
class SingDSI s where
    singDS :: SingDSI s
instance SingDSI 'Opened where
    singDS = SOpened
instance SingDSI 'Closed where
    singDS = SClosed
instance SingDSI 'Locked where
    singDS = SLocked
doorStatus :: SingDSI s => Door s -> DoorState
doorStatus = doorStatus' singDS
ghci> doorStatus (UnsafeMkDoor :: Door 'Locked)
Door is locked!
```

Initialize Door

```
initializeDoor' :: Sing s -> Door s
initializeDoor' _ _ = UnsafeMkDoor
```

Initialize Door

```
initializeDoor' :: Sing s -> Door s
initializeDoor' _ = UnsafeMkDoor

ghci> :t initializeDoor' SOpened
initializeDoor SOpened :: Door 'Opened
ghci> :t initializeDoor' SClosed
initializeDoor SOpened :: Door 'Closed
```

Initialize Door

Implicit passing style:

```
initializeDoor :: SingDSI s => Door s
initializeDoor = initializeDoor' singDS
```

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- ► The two are the same way of providing the same information to the compiler, and at runtime.
- We can use the two styles interchangebly.
- One is explicitly passing the type, the other is explicitly passing the type.

Ditching the phantom

Sometimes we don't care about what the status of our door is, and we want the type system to relax.

Ditching the phantom

Sometimes we don't care about what the status of our door is, and we want the type system to relax.

This is essentially the same as saying that the status of our door is a runtime property that we do not want to (or sometimes can't) check at compile-time.

Ditching the phantom

```
data SomeDoor :: Type where
```

MkSomeDoor :: SingDS s => Door s -> SomeDoor

Ditching the phantom

```
data SomeDoor :: Type where
    MkSomeDoor :: SingDS s => Door s -> SomeDoor

ghci> let myDoor = MkSomeDoor (initializeDoor SOpened)
ghci> :t myDoor
myDoor :: SomeDoor
ghci> case myDoor of MkSomeDoor d -> doorStatus d
Door is opened.
```

Runtime-deferred types

```
initializeSomeDoor :: DoorStatus -> SomeDoor
initializeSomeDoor = \case
    Opened -> SomeDoor (initialiseDoor' SOpened)
    Closed -> SomeDoor (initialiseDoor' SClosed)
    Locked -> SomeDoor (initialiseDoor' SLocked)
```

Runtime-deferred types

```
initializeSomeDoor :: DoorStatus -> SomeDoor
initializeSomeDoor = \case
    Opened -> SomeDoor (initialiseDoor' SOpened)
    Closed -> SomeDoor (initialiseDoor' SClosed)
    Locked -> SomeDoor (initialiseDoor' SLocked)
ghci> let myDoor = initializeSomeDoor Locked
ghci> :t myDoor
myDoor :: SomeDoor
ghci> case myDoor of MkSomeDoor d -> doorStatus d
Door is locked.
```

The Singletons Library

The singletons library provides a unified framework for creating and working with singletons for different types (not just DoorStatus), and also for functions on those types.

http://hackage.haskell.org/package/singletons

```
$(singletons [d|
  data DoorState = Opened | Closed | Locked
  deriving (Show, Eq)
|])
```

```
$(singletons [d|
  data DoorState = Opened | Closed | Locked
    deriving (Show, Eq)
  11)
This creates three types and three constructors:
data Sing :: DoorState -> Type where
    SOpened :: Sing 'Opened
    SClosed :: Sing 'Closed
    SLocked :: Sing 'Locked
```

And also

```
instance SingI 'Opened where
    sing = SOpened
instance SingI 'Closed where
    sing = SClosed
instance SingI 'Locked where
    sing = SLocked
```

And some more stuff too.

```
STrue :: Sing 'True

SJust SFalse :: Sing ('Just 'True)

SOpened `SCons` SClosed `SCons` SNil :: Sing '[ 'Opened, 'Opened']
```

SingI is a poly-kinded typeclass.

Sing is a poly-kinded type constructor (family):

Some more stuff

Some other convenient features:

Non-trivial type dependencies

```
knock :: Door s -> IO () knock = -- ??
```

We want to allow the user to knock on a closed or locked door, but not an opened door.

Non-trivial type dependencies

```
knock :: Door s -> IO ()
knock = -- ??
```

We want to allow the user to knock on a closed or locked door, but not an opened door.

We can do this simple case using pattern matching, but it's not always feasible or scalable. We want to define a type relationship that can be used by potentially many functions.

```
$(singletons [d|
  canKnock :: DoorState -> Bool
  canKnock Opened = False
  canKnock Closed = True
  canKnock Locked = True
  [])
```

```
$(singletons [d|
  canKnock :: DoorState -> Bool
  canKnock Opened = False
  canKnock Closed = True
  canKnock Locked = True
  |])

knock :: (CanKnock s ~ True) => Door s -> IO ()
knock _ = putStrLn "knock knock!"
```

```
$(singletons [d|
  canKnock :: DoorState -> Bool
  canKnock Opened = False
  canKnock Closed = True
  canKnock Locked = True
  11)
knock :: (CanKnock s ~ True) => Door s -> IO ()
knock = putStrLn "knock knock!"
ghci> knock (initializeDoor SOpened)
Compile Error!!!!
ghci> knock (initializeDoor SClosed)
knock knock!
```

```
tryKnock' :: Sing s -> Door s -> IO ()
tryKnock' s = case sCanKnock s of
   STrue -> knock
   SFalse -> \_ -> putStrLn "Cannot knock door!"
tryKnock :: SingI s => Door s -> IO ()
tryKnock = tryKnock' sing
```

```
tryKnock' :: Sing s -> Door s -> IO ()
tryKnock' s = case sCanKnock s of
    STrue -> knock
    SFalse -> \  -> putStrLn "Cannot knock door!"
tryKnock :: SingI s => Door s -> IO ()
tryKnock = tryKnock' sing
ghci> tryKnock (initializeDoor SOpened)
Cannot knock door!
ghci> tryKnock (initializeDoor SClosed)
knock knock!
```

Vectors

```
$(singletons [d|
  data N = Z | S N
  |])

data Vec :: N -> Type -> Type where
    VNil :: Vec Z a
    (:*) :: a -> Vec n a -> Vec (S n) a

infixr 5 :*
```

The Types demand it

```
replicateV'
    :: Sing n
    -> a
    -> Vec n a
replicateV' = \case
    SZ    -> \_ -> VNil
    SS n   -> \x    -> x    :* replicateV' n x
```

The Types demand it

```
replicateV'
    :: Sing n
    -> a
    -> Vec n a
replicateV' = \case
    SZ -> \ -> VNil
    SS n \rightarrow \x \rightarrow x :* replicateV' n x
replicateV
    :: SingI n
    => a
    -> Vec n a
replicateV = replicateV' sing
```

Thank you!

Further confusion: https://blog.jle.im/entry/verified-instances-in-haskell.html