STAT 308 – Homework 4

For the problems in which calculations are needed, please include your R code with your answers, otherwise you will not be given full credit. Please upload your assignment by Thursday, September 22, 11:59 pm in a pdf file to Sakai.

• 1. Suppose we perform a simple linear regression where

$$n=50, \bar{x}=-0.208, \bar{y}=1.516, s_x=2.354, s_y=3.185$$

$$\hat{\beta}_0=1.745, \hat{\beta}_1=1.102, s_{Y|X}=1.868, s_{\hat{\beta}_0}=0.265, s_{\hat{\beta}_1}=0.113$$

- a. Calculate the sample correlation coefficient, r, and the r^2 .
- b. Calculate the estimate of the regression variance $s_{y|x}^2$. (Hint: Intuitively, this is the variance of Y that is not explained through the linear model with X.)
 - 2. Use the following incomplete ANOVA table to answer the following questions.

	$\mathrm{d}\mathrm{f}$	Sum Sq	Mean Sq	F value	Pr(>F)
Model	1	1.47		0.18	
Error					
Total	34				

- a. What is the mean squares for the model (MSM)?
- b. What is the mean squared error (MSE)?
- c. What are the error degrees of freedom?
- d. What is the sum of squared errors (SSE)?
- e. What is the p-value used to test for a significant linear relationship between X and Y?
 - 3. Reconsider the dataset AdRevenue.csv as well as our simple linear regression model of ad revenue (in millions of dollars) based on circulation (in millions).
- a. Obtain an ANOVA table for this model.
- b. Using the ANOVA table, perform a hypothesis test for a linear relationship between ad revenue and circulation. Be sure to properly state your hypotheses, your test statistic, p-value, and a decision and conclusion at $\alpha = 0.05$.
- c. What is the distribution the test statistic follows under H_0 ? In other words, what is the distribution we use to calculate the p-value?
- d. Using the ANOVA table, calculate the value of r^2 . Interpret this value in the context of the problem.