Package 'groupTesting'

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array.gt.simulation Simulating Array-Based Group Testing Data

Description

This function simulates two-dimensional array-based group testing data.

Usage

```
array.gt.simulation(
   N,
   p = 0.1,
   protocol = c("A2", "A2M"),
   n,
   Se,
   Sp,
   assayID,
   Yt = NULL
)
```

Arguments

| N | The number of individuals to be tested. |
|----------|--|
| р | A vector of length N consisting of individual disease probabilities. |
| protocol | Either "A2" or "A2M", where "A2" ("A2M") refers to the two-dimensional array without (with) testing the members of an array as a single pooled sample. |
| n | The row (or column) size of the arrays. |
| Se | A vector of assay sensitivities. |
| Sp | A vector of assay specificities. |
| assayID | A vector of assay identification numbers. |
| Yt | A vector of individual true disease statuses. |

Details

We consider the array testing protocol outlined in Kim et al. (2007). Under this protocol, N individuals are assigned to m non-overlapping n-by-n matrices such that $N=mn^2$. From each matrix, n pools are formed using the row specimens and another n pools are formed using the column specimens. In stage 1, the 2n pools are tested. In stage 2, individual testing is used for case identification according to the strategy described in Kim et al. (2007). This is a 2-stage protocol called $Square\ Array\ without\ Master\ Pool\ Testing\ and\ denoted\ by\ A2(<math>n:1$) in Kim et al. (2007). A variant (3-stage protocol) is also presented in Kim et al. (2007) which employs testing the n^2 array members together as an initial pooled unit before implementing the 2-stage array. If the initial pooled test is negative, the procedure stops (i.e., the 2-stage array is not needed). However, if the pooled test is positive, the 2-stage protocol is used as before. This 3-stage approach is called $Square\ Array\ with\ Master\ Pool\ Testing\ and\ is\ denoted\ by\ A2(<math>n^2:n:1$). See Kim et al. (2007) for more details.

N should be divisible by n^2 , the number of individuals assigned to each array. If not divisible, the remainder pool is not tested.

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p is a vector of individual disease probabilities. When all individuals have the same probability of disease, say, 0.10, p can be specified as rep(0.10, N) or p=0.10.

```
For "A2" and "A2M", the pool sizes used are c(n,1) and c(n^2,n,1), respectively.
```

For "A2", Se is c(Se1,Se2), where Se1 is the sensitivity of the assay used for both row and column pools, and Se2 is the sensitivity of the assay used for individual testing. For "A2M", Se is c(Se1,Se2,Se3), where Se1 is for the initial array pool, Se2 is for the row and column pools, and Se3 is for individual testing. Sp is specified in the same manner.

For "A2", assayID is c(1,1) when the same assay is used for row/column pool testing as well as for individual testing, and assayID is c(1,2) when assay 1 is used for row/column pool testing and assay 2 is used for individual testing. In the same manner, assayID is specified for "A2M" as c(1,1,1), c(1,2,3), and in many other ways.

When available, the individual true disease statuses (1 for positive and 0 for negative) can be used in simulating the group testing data through argument Yt. When an input is entered for Yt, argument p will be ignored.

When N is not divisible by the array size n^2 , the remainder individuals are tested one by one.

Value

A list with components:

```
gtData The simulated group testing data.
```

testsExp The number of tests expended in the simulation.

References

Kim HY, Hudgens M, Dreyfuss J, Westreich D, and Pilcher C (2007). Comparison of Group Testing Algorithms for Case Identification in the Presence of Testing Error. *Biometrics*, 63(4), 1152–1163.

See Also

hier.gt.simulation for simulation of the hierarchical group testing data.

```
## Not run:
## Example 1: Square Array without Master Pool Testing (i.e., 2-Stage Array)
N <- 48
                  # Sample size
protocol <- "A2"</pre>
                     # 2-stage array
n <- 4
                     # Row/column size
Se <- c(0.95, 0.95) # Sensitivities in stages 1-2
Sp <- c(0.98, 0.98) # Specificities in stages 1-2
assayID <- c(1, 1) # The same assay in both stages
# (a) Homogeneous population
pHom <- 0.10
                     # Overall prevalence
array.gt.simulation (N=N,p=pHom,protocol=protocol,n=n,Se=Se,Sp=Sp,assayID) \\
# Alternatively, the individual true statuses can be used as:
yt <- rbinom( N, size=1, prob=0.1 )</pre>
array.gt.simulation(N=N,protocol=protocol,n=n,Se=Se,Sp=Sp,assayID=assayID,Yt=yt)
# (b) Heterogeneous population (regression)
```

```
param <- c(-3,2,1)
x1 <- rnorm(N, mean=0, sd=.75)
x2 <- rbinom(N, size=1, prob=0.5)</pre>
X \leftarrow cbind(1, x1, x2)
pReg <- exp(X%*%param)/(1+exp(X%*%param)) # Logit
array.gt.simulation(N=N,p=pReg,protocol=protocol,n=n,Se=Se,Sp=Sp,assayID)
# The above examples with different assays
Se <- c(0.95, 0.98)
Sp < -c(0.97, 0.99)
assayID <- c(1, 2)
array.gt.simulation(N,pHom,protocol,n,Se,Sp,assayID)
array.gt.simulation(N,pReg,protocol,n,Se,Sp,assayID)
## Example 2: Square Array with Master Pool Testing (i.e., 3-Stage Array)
N <- 48
protocol <- "A2M"</pre>
n <- 4
Se <- c(0.95, 0.95, 0.95)
Sp <- c(0.98, 0.98, 0.98)
assayID <- c(1, 1, 1) # The same assay in 3 stages
# (a) Homogeneous population
pHom <- 0.10
array.gt.simulation(N,pHom,protocol,n,Se,Sp,assayID)
# (b) Heterogeneous population (regression)
param <- c(-3,2,1)
x1 <- rnorm(N, mean=0, sd=.75)
x2 <- rbinom(N, size=1, prob=0.5)</pre>
X \leftarrow cbind(1, x1, x2)
pReg <- exp(X%*%param)/(1+exp(X%*%param)) # Logit
array.gt.simulation(N,pReg,protocol,n,Se,Sp,assayID)
# The above examples with different assays:
Se <- c(0.95, 0.98, 0.98)
Sp \leftarrow c(0.97, 0.98, 0.92)
assayID <- 1:3
array.gt.simulation(N,pHom,protocol,n,Se,Sp,assayID)
array.gt.simulation(N,pReg,protocol,n,Se,Sp,assayID)
## End(Not run)
```

glm.gt

EM Algorithm for Fitting Regression Models to Group Testing Data

Description

This function implements an expectation-maximization (EM) algorithm to fit regression models to group testing data, where pooled responses are related to individual covariates through a link function in the generalized linear model (GLM) family. The EM algorithm finds the maximum likelihood estimate (MLE) for the vector of regression coefficients, **beta**. The EM algorithm can model

pooling data observed from **any** group testing protocol used in practice, including hierarchical and array testing (Kim et al., 2007).

Usage

```
glm.gt(
  beta0,
  gtData,
  Χ,
  g,
  dg = NULL,
  d2g = NULL,
  grdMethod = c("central", "forward", "backward"),
  covariance = FALSE,
  nburn = 2000,
  ngit = 5000,
  maxit = 200,
  tol = 0.001,
  tracing = TRUE,
  conf.level = 0.95,
)
```

Arguments

| beta0 | An initial value for the regression coefficients. |
|------------|--|
| gtData | A matrix or data.frame consisting of the pooled test outcomes and other information from a group testing application. Needs to be specified as shown in the example below. |
| Χ | The design matrix. |
| g | An inverse link function in the GLM family. |
| dg | The first derivate of g. When NULL, a finite-difference approximation will be used. |
| d2g | The second derivate of g. When NULL, a finite-difference approximation will be used. |
| grdMethod | The finite-difference approximation method to be used for \mbox{dg} and $\mbox{d2g}$. See 'Details'. |
| covariance | When TRUE, the covariance matrix is calculated at the MLE. |
| nburn | The number of initial Gibbs iterates to be discarded. |
| ngit | The number of Gibbs iterates to be used in the E-step after discarding nburn iterates as a burn-in period. |
| maxit | The maximum number of EM steps (iterations) allowed in the EM algorithm. |
| tol | Convergence tolerance used in the EM algorithm. |
| tracing | When TRUE, progress in the EM algorithm is displayed. |
| conf.level | Confidence level to be used for the Wald confidence interval. |
| | Further arguments to be passed to optim. See 'Details'. |
| | |

Details

gtData must be specified as follows. Columns 1-5 consist of the pooled test outcomes (0 for negative and 1 for positive), pool sizes, pool-specific sensitivities, pool-specific specificities, and assay identification (ID) numbers, respectively. From column 6 onward, the pool member ID numbers need to be specified. Note that the ID numbers must start with 1 and increase consecutively up to N, the total number of individuals tested. For smaller pools, incomplete ID numbers must be filled out by -9 or any non-positive numbers as shown in the example below. The design matrix X consists of invidual covariate information, such as age, sex, and symptoms, of the pool members located in column 6 onward.

| | Z | psz | Se | Sp | Assay | Mem1 | Mem2 | Mem3 | Mem4 | Mem5 | Mem6 |
|--------|---|-----|------|------|-------|------|------|------|------|------|------|
| Pool:1 | 1 | 6 | 0.90 | 0.92 | 1 | 1 | 2 | 3 | 4 | 5 | 6 |
| Pool:2 | 0 | 6 | 0.90 | 0.92 | 1 | 7 | 8 | 9 | 10 | 11 | 12 |
| Pool:3 | 1 | 2 | 0.95 | 0.96 | 2 | 1 | 2 | -9 | -9 | -9 | -9 |
| Pool:4 | 0 | 2 | 0.95 | 0.96 | 2 | 3 | 4 | -9 | -9 | -9 | -9 |
| Pool:5 | 1 | 2 | 0.95 | 0.96 | 2 | 5 | 6 | -9 | -9 | -9 | -9 |
| Pool:6 | 0 | 1 | 0.92 | 0.90 | 3 | 1 | -9 | -9 | -9 | -9 | -9 |
| Pool:7 | 1 | 1 | 0.92 | 0.90 | 3 | 2 | -9 | -9 | -9 | -9 | -9 |
| Pool:8 | 0 | 1 | 0.92 | 0.90 | 3 | 5 | -9 | -9 | -9 | -9 | -9 |
| Pool:9 | 0 | 1 | 0.92 | 0.90 | 3 | 6 | -9 | -9 | -9 | -9 | -9 |

This is an example of gtData, where 12 individuals are assigned to 2 non-overlapping initial pools and then tested based on the 3-stage hierarchical protocol. The test outcomes, Z, from 9 pools are in column 1. In three stages, different pool sizes (6, 2, and 1), sensitivities, specificities, and assays are used. The ID numbers of the pool members are shown in columns 6-11. The row names and column names are not required. Note that the EM algorithm can accommodate any group testing data including those described in Kim et al. (2007). For individual testing data, the pool size in column 2 is 1 for all pools.

X is an Nxk design matrix, where each column represents a vector of individual covariate values. For an intercept model, the first column values must be 1. The column (covariate) names of X, such as "age" and "sex", will be displayed in the estimation summary. When column names are missing (NULL), the names that will be displayed by default are "Intercept", "x1", "x2", and so on.

The EM algorithm implements a Gibbs sampler to approximate the expectation in the E-step. Under each EM iteration, ngit Gibbs samples are retained for these purposes after discarding the initial nburn samples.

g relates the pooled responses Z (column 1 in gtData) to X. dg and d2g can be specified analogously. These characteristics can be obtained from glmLink for the common links: logit, probit, and complementary log-log.

grdMethod is used only when dg and d2g are NULL, where a finite-difference approximation is implemented by the function fderiv from the package pracma.

The optimization routine optim is used to complete the M-step with the default method "Nelder-Mead". The argument ... allows the user to change the default method as well as other arguments in optim.

The covariance matrix is calculated by an appeal to the missing data principle and the method outlined in Louis (1982).

Value

A list with components:

param The MLE of the regression coefficients.

covariance Estimated covariance matrix for the regression coefficients.

iterUsed The number of EM iterations needed for convergence.

convergence 0 if the EM algorithm converges successfully and 1 if the iteration limit maxit

has been reached.

summary Estimation summary with Wald confidence interval.

References

Kim HY, Hudgens M, Dreyfuss J, Westreich D, and Pilcher C. (2007). Comparison of Group Testing Algorithms for Case Identification in the Presence of Testing Error. *Biometrics*, 63:1152-1163.

Louis T. (1982). Finding the Observed Information Matrix when Using the EM algorithm. *Journal of the Royal Statistical Society: Series B*, 44:226-233.

Vansteelandt S, Goetghebeur E, and Verstraeten T. (2000). Regression Models for Disease Prevalence with Diagnostic Tests on Pools of Serum Samples. *Biometrics*, 56:1126-1133.

See Also

hier.gt.simulation and array.gt.simulation for group testing data simulation, and prop.gt for estimation of a disease prevalence from group testing data.

```
## Not run:
library("groupTesting")
## To illustrate 'glm.gt', we use data simulated
## by the functions 'hier.gt.simulation' and 'array.gt.simulation'.
## Note: The simulated data-structures are consistent
## with the data-structure required for 'gtData'.
## Example 1: MLE from 3-stage hierarchical group testing data.
## The data used is simulated by 'hier.gt.simulation'.
N <- 1200
                      # Sample size
S <- 3
                      # 3-stage hierarchical testing
psz < -c(6,2,1)
                      # Pool sizes used in stages 1-3
Se <- c(.95,.95,.98) # Sensitivities in stages 1-3
Sp \leftarrow c(.95,.98,.96) # Specificities in stages 1-3
assayID \leftarrow c(1,2,3)
                     # Assays used in stages 1-3
param.t <- c(-3,2,1) # The TRUE parameter to be estimated
# Simulating covariates:
set.seed(123)
x1 <- rnorm(N, mean=0, sd=0.75)
x2 <- rbinom(N, size=1, prob=0.5)</pre>
X \leftarrow cbind(1, x1, x2)
colnames( X ) <- c("Intercept", "Predictor 1", "Predictor 2")</pre>
# Note: Because the 1st column of X is 1, intercept model will be fit.
# Specifying logit inverse link:
```

```
g <- function(t){exp(t)/(1+exp(t))}</pre>
pReg <- g(X%*%param.t)</pre>
# Simulating test responses:
gtOut <- hier.gt.simulation(N,pReg,S,psz,Se,Sp,assayID)$gtData</pre>
# Fitting the model (with intercept):
param0 <- param.t + 0.2 # Initial value</pre>
res <- glm.gt(beta0=param0,gtData=gtOut,X=X,</pre>
              g=g,dg=NULL,d2g=NULL,
              grdMethod="central",covariance=TRUE,
              nburn=2000, ngit=5000, maxit=200,
              tol=1e-03,tracing=TRUE,conf.level=0.95)
# Note: Because dg and d2g are NULL (i.e., the exact derivatives
        are not given), numerical derivatives are used.
# Estimation results:
# > res
# $param
# [1] -3.0521378 1.9967745 0.9296381
# $covariance
              [,1]
                                         [,3]
                           [,2]
# [1,] 0.04501087 -0.022290818 -0.034408283
# [2,] -0.02229082 0.031942459 0.007639122
# [3,] -0.03440828  0.007639122  0.048313159
# $iterUsed
# [1] 5
# $convergence
# [1] 0
# $summary
              Estimate Std.Err 95%lower 95%upper
                -3.052 0.212 -3.468 -2.636
# Intercept
                        0.179
# Predictor 1
                 1.997
                                  1.646
                                            2.347
# Predictor 2
                 0.930 0.220
                                   0.499
                                           1.360
## Example 2: MLE from two-dimensional array testing data.
## The data used is simulated by 'array.gt.simulation'.
N <- 1000
                     # Sample size
protocol <- "A2"</pre>
                     # 2-stage array without testing initial master pool
n <- 5
                     # Row/column size
Se < c(0.95, 0.95) # Sensitivities
Sp \leftarrow c(0.98, 0.98) # Specificities
assayID <- c(1, 1) # The same assay in both stages
param <- c(-4,1,1) # The TRUE parameter to be estimated
# Simulating data:
set.seed(123)
x1 \leftarrow runif(N)
```

```
x2 <- rnorm(N, mean=0, sd=0.5)
x3 <- rbinom(N, size=1, prob=0.5)
X \leftarrow cbind(x1, x2, x3)
# Note: Because the 1st column of X is not 1,
        the model without intercept will be fit.
# Finding g, dg, and d2g from the function 'glmLink':
res0 <- glmLink(fn.name="logit")</pre>
g <- res0$g
                       # Logit inverse link g()
dg <- res0$dg
                      # The exact first derivate of g
d2g <- res0$d2g
                     # The exact second derivate of g
pReg <- g(X%*%param) # Individual probabilities</pre>
gtOut <- array.gt.simulation(N,pReg,protocol,n,Se,Sp,assayID)$gtData</pre>
# Fitting the model (without intercept):
param0 <- param + 0.2
res <- glm.gt(beta0=param0,gtData=gtOut,X=X,g=g,</pre>
              dg=dg,d2g=d2g,covariance=TRUE,
              nburn=2000, ngit=5000, maxit=200,
              tol=1e-03, tracing=TRUE, conf.level=0.95)
print(res)
## Example 3: MLE from non-overlapping initial pooled responses.
## The data used is simulated by 'hier.gt.simulation'.
## Note: With initial pooled responses, our MLE is equivalent
## to the MLE in Vansteelandt et al. (2000).
N <- 1000
                     # Sample size
psz <- 5
                    # Pool size
S <- 1
                    # 1-stage testing
Se <- 0.95
                    # Sensitivity
Sp <- 0.99
                    # Specificity
               # Assay used for all pools
assayID <- 1
param <- c(-3,2,1) # The TRUE parameter to be estimated
# Simulating data:
set.seed(123)
x1 <- rnorm(N, mean=0, sd=0.75)
x2 <- rbinom(N, size=1, prob=0.5)</pre>
X \leftarrow cbind(1, x1, x2)
# Finding g, dg, and d2g by the function 'glmLink':
res0 <- glmLink(fn.name="probit") # Probit link</pre>
g <- res0$g
dg <- res0$dg
d2g <- res0$d2g
pReg <- g(X%*%param)</pre>
gtOut <- hier.gt.simulation(N,pReg,S,psz,Se,Sp,assayID)$gtData</pre>
# Fitting the model:
param0 <- param + 0.2
res <- glm.gt(beta0=param0,gtData=gtOut,X=X,g=g,</pre>
                 dg=dg,d2g=d2g,covariance=TRUE,
                 nburn=2000, ngit=5000, maxit=200,
                 tol=1e-03, tracing=TRUE, conf.level=0.95)
```

```
print(res)
## Example 4: MLE from individual (one-by-one) testing data.
## The data used is simulated by 'hier.gt.simulation'.
N <- 1000
                       # Sample size
                      # Pool size 1 (i.e., individual testing)
psz <- 1
S <- 1
                     # 1-stage testing
Se <- 0.95
                     # Sensitivity
Sp <- 0.99
                     # Specificity
assayID <- 1
                    # Assay used for all pools
param <- c(-3,2,1) # The TRUE parameter to be estimated
# Simulating data:
set.seed(123)
x1 <- rnorm(N, mean=0, sd=0.75)
x2 \leftarrow rbinom(N, size=1, prob=0.5)
X \leftarrow cbind(1, x1, x2)
g \leftarrow function(t){exp(t)/(1+exp(t))} # Inverse logit
pReg <- g(X%*%param)</pre>
gtOut <- hier.gt.simulation(N,pReg,S,psz,Se,Sp,assayID)$gtData</pre>
# Fitting the model:
param0 <- param + 0.2
res <- glm.gt(beta0=param0,gtData=gtOut,</pre>
              X=X,g=g,dg=NULL,d2g=NULL,
              grdMethod="central",covariance=TRUE,
              nburn=2000, ngit=5000, maxit=200,
              tol=1e-03,tracing=TRUE,conf.level=0.95)
print(res)
## Example 5: Using pooled testing data.
# Pooled test outcomes:
Z \leftarrow c(1, 0, 1, 0, 1, 0, 1, 0, 0)
# Design matrix, X:
x1 \leftarrow c(0.8, 1.2, 0.4, 1.5, 1.8, 1.8, 0.1, 1.6, 0.2, 0.2, 1.8, 0.2)
x2 \leftarrow c(31,56,45,64,26,47,22,60,35,41,32,41)
X \leftarrow cbind(x1, x2)
# Pool sizes used:
psz <- c(6, 6, 2, 2, 2, 1, 1, 1, 1)
# Pool-specific Se & Sp:
Se <- c(.90, .90, .95, .95, .95, .92, .92, .92, .92)
Sp <- c(.92, .92, .96, .96, .96, .90, .90, .90)
# Assays used:
Assay \leftarrow c(1, 1, 2, 2, 2, 3, 3, 3, 3)
# Pool members:
Memb <- rbind(</pre>
  c(1, 2, 3, 4, 5, 6),
   c(7, 8, 9, 10, 11, 12),
```

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```
c(1, 2, -9, -9, -9, -9),
   c(3, 4, -9, -9, -9, -9),
   c(5, 6, -9, -9, -9),
   c(1,-9, -9, -9, -9, -9),
   c(2,-9, -9, -9, -9, -9),
   c(5,-9, -9, -9, -9, -9),
   c(6,-9, -9, -9, -9, -9)
)
# The data-structure suited for 'gtData':
gtOut <- cbind(Z, psz, Se, Sp, Assay, Memb)</pre>
# Fitting the model with logit link:
g \leftarrow function(t) \{ exp(t)/(1+exp(t)) \}
param0 <- c(0, 0)
res <- glm.gt(beta0=param0,gtData=gtOut,X=X,</pre>
               g=g,dg=NULL,d2g=NULL,
               grdMethod="central",covariance=TRUE,
               nburn=2000, ngit=5000, maxit=200,
               tol=1e-03, tracing=TRUE, conf.level=0.95)
print(res)
## End(Not run)
```

 ${\tt glmLink}$

Link Functions in the Class of Generalized Linear Models

Description

This function provides characteristics of common link functions (logit, probit, and comlementary log-log). Specifically, based on the link name, the function with its inverse, first derivative, and second derivative is provided.

Usage

```
glmLink(fn.name = c("logit", "probit", "cloglog"))
```

Arguments

```
fn.name One of the three: "logit", "probit", and "cloglog".
```

Value

A list with components:

```
g The link function corresponding to "logit", "probit", or "cloglog".

dg The first derivative of g.

d2g The second derivative of g.

gInv The inverse of g.
```

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Examples

```
## Try:
glmLink("logit")
```

hier.gt.simulation

Simulating Hierarchical Group Testing Data

Description

This function simulates hierarchical group testing data with any number of hierarchical stages.

Usage

```
hier.gt.simulation(N, p = 0.1, S, psz, Se, Sp, assayID, Yt = NULL)
```

Arguments

| N | The number of individuals to be tested. |
|---------|--|
| р | A vector of length N consisting of individual disease probabilities. |
| S | The number of stages used in testing, where $S \ge 1$. |
| psz | A vector of pool sizes in stages 1-S. |
| Se | A vector of assay sensitivities in stages 1-S. |
| Sp | A vector of assay specificities in stages 1-S. |
| assayID | A vector of the identification numbers of the assays used in stages 1-S. |
| Yt | A vector of individual true disease statuses. |

Details

We consider the S-stage hierarchical testing protocol outlined in Kim et al. (2007). Under this protocol, N individual specimens are first assigned to m non-overlapping pools, where each initial pool size is c; i.e., N=mc. The initial pools are tested in stage 1. If a pooled test is negative, all members in the pool are diagnosed as negative. However, if a pooled test is positive, the pool members are split into non-overlapping subpools to be tested in the next stage. This procedure is continued. Note that individual testing is used in the final stage, S, for case identification.

N should to be divisible by the initial pool size c. If not divisible, the remainder pool is not tested.

p is a vector of individual disease probabilities. When all individuals have the same probability of disease, say, 0.10, p can be specified as p=rep(0.10, N) or p=0.10.

S is a positive integer, $S \ge 1$. When S=1, only the initial pools in stage 1 are tested.

psz is a vector of length S, where the first element is the stage-1 pool size, the second element is the stage-2 pool size, and so on. Pool size at any stage must be divisible by the pool size used at the next stage. For example, psz can be specified as c(12,3,1) but not as c(12,5,1).

When psz is a vector of length 1, test responses are simulated only from the initial pools.

Se is a vector of length S, where the first element is the sensitivity of the assay used in stage 1, the second element is sensitivity of the assay in stage 2, and so on.

Sp is a vector of length S, where the first element is the specificity of the assay used in stage 1, the second element is specificity of the assay in stage 2, and so on.

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assayID is a vector of length S, where the first element is the ID of the assay in stage 1, the second element is the ID of the assay in stage 2, and so on.

When available, the individual true disease statuses (1 for positive and 0 for negative) can be used in simulating the group testing data through argument Yt. When an input is entered for Yt, argument p will be ignored.

When N is not divisible by c (the initial pool size), we implement the following policy to test the remainder individuals: (1) a smaller remainder pool is used for the initial pooled testing protocol (i.e., when S=1); (2) a smaller remainder pool with 2-stage testing is used for the multistage hierarchical protocol (i.e., when S > 1).

Value

A list with components:

```
gtData The simulated group testing data.
testsExp The number of tests expended.
```

References

Kim HY, Hudgens M, Dreyfuss J, Westreich D, and Pilcher C (2007). Comparison of Group Testing Algorithms for Case Identification in the Presence of Testing Error. *Biometrics*, 63(4), 1152–1163.

See Also

array.gt.simulation for simulation of the array-based group testing data.

```
## Not run:
## Example 1: Two-stage hierarchical (Dorfman) pooling data
N <- 50 # Sample size
psz <- c(5, 1) # Pool sizes used in stages 1 and 2
S <- 2
                   # The number of stages
Se <- c(0.95, 0.95) # Sensitivities in stages 1-2
Sp <- c(0.98, 0.98) # Specificities in stages 1-2
assayID <- c(1, 1) # The same assay in both stages
# (a) Homogeneous population
pHom <- 0.10 # Overall prevalence
hier.gt.simulation(N=N,p=pHom,S=S,psz=psz,Se=Se,Sp=Sp,assayID=assayID)
# Alternatively, the individual true statuses can be used as:
yt <- rbinom( N, size=1, prob=0.1 )
hier.gt.simulation(N=N,S=S,psz=psz,Se=Se,Sp=Sp,assayID=assayID,Yt=yt)
# (b) Heterogeneous population (regression)
param <- c(-3,2,1)
x1 <- rnorm(N, mean=0, sd=.75)
x2 <- rbinom(N, size=1, prob=0.5)</pre>
X \leftarrow cbind(1, x1, x2)
pReg <- exp(X%*%param)/(1+exp(X%*%param)) # Logit</pre>
\label{lem:hier.gt.simulation(N=N,p=pReg,S=S,psz=psz,Se=Se,Sp=Sp,assayID=assayID)} \\
```

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```
## Example 2: Initial (1-stage) pooled testing data
N <- 50
S <- 1
Se <- 0.95
Sp <- 0.98
assayID <- 1
# (a) Homogeneous population
pHom <- 0.10 # Overall prevalence
# a(i) Pooled testing
psz <- 5
               # pool size
hier.gt.simulation(N,pHom,S,psz,Se,Sp,assayID)
# a(ii) Inidividual testing
psz <- 1
             # pool size
hier.gt.simulation(N,pHom,S,psz,Se,Sp,assayID)
# (b) Heterogeneous population (regression)
param <- c(-3,2,1)
x1 <- rnorm(N, mean=0, sd=.75)
x2 <- rbinom(N, size=1, prob=0.5)
X \leftarrow cbind(1, x1, x2)
pReg <- exp(X%*%param)/(1+exp(X%*%param)) # Logit</pre>
# b(i) Pooled testing
psz <- 5
hier.gt.simulation(N,pReg,S,psz,Se,Sp,assayID)
# b(ii) Individual testing
psz <- 1
hier.gt.simulation(N,pReg,S,psz,Se,Sp,assayID)
## Example 3: Data with other configurations
N <- 48
p < -0.10
Se <- c(.90, .95, .92, .90, .99)
Sp \leftarrow c(.96, .96, .90, .92, .95)
Assay <- 1:5
# Initial pooled testing, using the first element of Se, Sp & Assay
pszH1 <- 4
hier.gt.simulation(N=N,p=p,S=1,psz=pszH1,Se=Se,Sp=Sp,assayID=Assay)
                      # Two-stage, using first 2 elements of Se, Sp & Assay
pszH2 < - c(4,1)
hier.gt.simulation(N=N,p=p,S=2,psz=pszH2,Se=Se,Sp=Sp,assayID=Assay)
pszH4 \leftarrow c(16,8,2,1) # Four-stage, using first 4 elements of Se, Sp & Assay
hier.gt.simulation(N=N,p=p,S=4,psz=pszH4,Se=Se,Sp=Sp,assayID=Assay)
pszH3 < - c(12,2,1)
                      # Three-stage, using first 3 elements of Se, Sp & Assay
Assay3 <- c(2,1,3) # Array ID numbers do not need to be in order
hier.gt.simulation(N=N,p=p,S=3,psz=pszH3,Se=Se,Sp=Sp,assayID=Assay3)
# Works but discards the remainder pool of 2 individuals
N <- 50
```

```
psz <- c(12,2,1)
hier.gt.simulation(N=N,p=p,S=3,psz=psz,Se=Se,Sp=Sp,assayID=Assay)
## End(Not run)</pre>
```

prop.gt

EM Algorithm to Estimate the Prevalence of a Disease from Group Testing Data

Description

This function implements an expectation-maximization (EM) algorithm to find the maximum likelihood estimate (MLE) of a disease prevalence, p, based on group testing data. The EM algorithm can model pooling data observed from **any** group testing protocol used in practice, including hierarchical and array testing (Kim et al., 2007).

Usage

```
prop.gt(
  p0,
  gtData,
  covariance = FALSE,
  nburn = 2000,
  ngit = 5000,
  maxit = 200,
  tol = 0.001,
  tracing = TRUE,
  conf.level = 0.95
)
```

Arguments

| p0 | An initial value of the prevalence. |
|------------|--|
| gtData | A matrix or data frame consisting of the pooled test outcomes and other information from a group testing application. Needs to be specified as shown in the example below. |
| covariance | When TRUE, the variance is calculated at the MLE. |
| nburn | The number of initial Gibbs iterates to be discarded. |
| ngit | The number of Gibbs iterates to be used in the E-step after discarding the initial iterates as a burn-in period. |
| maxit | The maximum number of EM steps (iterations) allowed in the EM algorithm. |
| tol | Convergence tolerance used in the EM algorithm. |
| tracing | When TRUE, progress in the EM algorithm is displayed. |
| conf.level | Confidence level to be used for the Wald confidence interval. |

Details

gtData must be specified as follows. Columns 1-5 consist of the pooled test outcomes (0 for negative and 1 for positive), pool sizes, pool-specific sensitivities, pool-specific specificities, and assay ID numbers, respectively. From column 6 onward, the pool member ID numbers need to be specified. Note that the ID numbers must start with 1 and increase consecutively up to N, the total number of individuals tested. For smaller pools, incomplete ID numbers must be filled out by -9 or any non-positive numbers as shown in the example below.

| | Z | psz | Se | Sp | Assay | Mem1 | Mem2 | Mem3 | Mem4 | Mem5 | Mem6 |
|--------|---|-----|------|------|-------|------|------|------|------|------|------|
| Pool:1 | 1 | 6 | 0.90 | 0.92 | 1 | 1 | 2 | 3 | 4 | 5 | 6 |
| Pool:2 | 0 | 6 | 0.90 | 0.92 | 1 | 7 | 8 | 9 | 10 | 11 | 12 |
| Pool:3 | 1 | 2 | 0.95 | 0.96 | 2 | 1 | 2 | -9 | -9 | -9 | -9 |
| Pool:4 | 0 | 2 | 0.95 | 0.96 | 2 | 3 | 4 | -9 | -9 | -9 | -9 |
| Pool:5 | 1 | 2 | 0.95 | 0.96 | 2 | 5 | 6 | -9 | -9 | -9 | -9 |
| Pool:6 | 0 | 1 | 0.92 | 0.90 | 3 | 1 | -9 | -9 | -9 | -9 | -9 |
| Pool:7 | 1 | 1 | 0.92 | 0.90 | 3 | 2 | -9 | -9 | -9 | -9 | -9 |
| Pool:8 | 0 | 1 | 0.92 | 0.90 | 3 | 5 | -9 | -9 | -9 | -9 | -9 |
| Pool:9 | 0 | 1 | 0.92 | 0.90 | 3 | 6 | -9 | -9 | -9 | -9 | -9 |

This is an example of gtData, where 12 individuals are assigned to 2 non-overlapping initial pools and then tested based on the 3-stage hierarchical protocol. The test outcomes, Z, from 9 pools are in column 1. In three stages, different pool sizes (6, 2, and 1), sensitivities, specificities, and assays are used. The ID numbers of the pool members are shown in columns 6-11. The row names and column names are not required. Note that the EM algorithm can accommodate any group testing data including those described in Kim et al. (2007). For individual testing data, the pool size in column 2 is 1 for all pools.

The EM algorithm implements a Gibbs sampler to approximate quantities required to complete the E-step. Under each EM iteration, ngit Gibbs samples are retained for these purposes after discarding the initial nburn samples.

The variance of the MLE is calculated by an appeal to the missing data principle and the method outlined in Louis (1982).

Value

A list with components:

param The MLE of the disease prevalence.

covariance Estimated variance for the disease prevalence.

iterUsed The number of EM iterations used for convergence.

convergence 0 if the EM algorithm converges successfully and 1 if the iteration limit maxit

has been reached.

summary Estimation summary with Wald confidence interval.

References

Kim HY, Hudgens M, Dreyfuss J, Westreich D, and Pilcher C. (2007). Comparison of Group Testing Algorithms for Case Identification in the Presence of Testing Error. *Biometrics*, 63:1152-1163.

Litvak E, Tu X, and Pagano M. (1994). Screening for the Presence of a Disease by Pooling Sera Samples. *Journal of the American Statistical Association*, 89:424-434.

Liu A, Liu C, Zhang Z, and Albert P. (2012). Optimality of Group Testing in the Presence of Misclassification. *Biometrika*, 99:245-251.

Louis T. (1982). Finding the Observed Information Matrix when Using the EM algorithm. *Journal of the Royal Statistical Society: Series B*, 44:226-233.

See Also

hier.gt.simulation and array.gt.simulation for group testing data simulation, and glm.gt for group testing regression models.

```
## Not run:
library("groupTesting")
\#\# To illustrate 'prop.gt', we use data simulated
## by the R functions 'hier.gt.simulation' and 'array.gt.simulation'.
## The simulated data-structures are consistent
## with the data-structure required for 'gtData'.
## Example 1: MLE from 3-stage hierarchical group testing data.
## The data used is simulated by 'hier.gt.simulation'.
N <- 1200
                      # Sample size
S <- 3
                      # 3-stage hierarchical testing
psz <- c(6,2,1)
                  # Pool sizes used in stages 1-3
Se <- c(.95,.95,.98) # Sensitivities in stages 1-3
Sp \leftarrow c(.95,.98,.96) # Specificities in stages 1-3
assayID <- c(1,2,3) # Assays used in stages 1-3
p.t <- 0.05
                      # The TRUE parameter to be estimated
# Simulating data:
set.seed(123)
gtOut <- hier.gt.simulation(N,p.t,S,psz,Se,Sp,assayID)$gtData</pre>
# Running the EM algorithm:
pStart <- p.t + 0.2 # Initial value
res <- prop.gt(p0=pStart,gtData=gtOut,covariance=TRUE,</pre>
               nburn=2000, ngit=5000, maxit=200, tol=1e-03,
               tracing=TRUE,conf.level=0.95)
# Estimation results:
# > res
# $param
# [1] 0.04865533
# $covariance
               [,1]
# [1,] 4.374172e-05
# $iterUsed
# [1] 4
```

```
# $convergence
# [1] 0
# $summary
# Estimate StdErr 95%lower 95%upper
# prop 0.049 0.007 0.036 0.062
## Example 2: MLE from two-dimensional array testing data.
## The data used is simulated by 'array.gt.simulation'.
N <- 1000
                    # Sample size
protocol <- "A2"  # 2-stage array without testing the initial master pool</pre>
n <- 5
                    # Row/column size
Se <- c(0.95, 0.95) # Sensitivities
Sp \leftarrow c(0.98, 0.98) # Specificities
assayID <- c(1, 1) # The same assay in both stages
p.true <- 0.05
                    # The TRUE parameter to be estimated
# Simulating data:
set.seed(123)
gtOut <- array.gt.simulation(N,p.true,protocol,n,Se,Sp,assayID)$gtData</pre>
# Fitting the model:
pStart <- p.true + 0.2 # Initial value
res <- prop.gt(p0=pStart,gtData=gtOut,covariance=TRUE)</pre>
print(res)
## Example 3: MLE from non-overlapping initial pooled responses.
## The data used is simulated by 'hier.gt.simulation'.
## Note: With initial pooled responses, our MLE is equivalent
## to the MLE in Litvak et al. (1994) and Liu et al. (2012).
                     # Sample size
N <- 1000
psz <- 5
                    # Pool size
S <- 1
                    # 1-stage testing
                    # Sensitivity
Se <- 0.95
Sp <- 0.99
                     # Specificity
assayID <- 1
                     # Assay used for all pools
p.true <- 0.05
                     # True parameter
set.seed(123)
gtOut <- hier.gt.simulation(N,p.true,S,psz,Se,Sp,assayID)$gtData</pre>
pStart <- p.true + 0.2 # Initial value
res <- prop.gt(p0=pStart,gtData=gtOut,</pre>
               covariance=TRUE, nburn=2000, ngit=5000,
               maxit=200,tol=1e-03,tracing=TRUE)
print(res)
## Example 4: MLE from individual (one-by-one) testing data.
## The data used is simulated by 'hier.gt.simulation'.
```

```
N <- 1000
                     # Sample size
                     # Pool size 1 (i.e., individual testing)
psz <- 1
                    # 1-stage testing
S <- 1
Se <- 0.95
                    # Sensitivity
Sp <- 0.99
                     # Specificity
assayID <- 1
                    # Assay used for all pools
p.true <- 0.05
                    # True parameter
set.seed(123)
gtOut <- hier.gt.simulation(N,p.true,S,psz,Se,Sp,assayID)$gtData</pre>
pStart <- p.true + 0.2 # Initial value
res <- prop.gt(p0=pStart,gtData=gtOut,</pre>
               covariance=TRUE, nburn=2000,
               ngit=5000, maxit=200,
               tol=1e-03, tracing=TRUE)
print(res)
## Example 5: Using pooled testing data.
# Pooled test outcomes:
Z \leftarrow c(1, 0, 1, 0, 1, 0, 1, 0, 0)
# Pool sizes used:
psz <- c(6, 6, 2, 2, 2, 1, 1, 1, 1)
# Pool-specific Se & Sp:
Se <- c(.90, .90, .95, .95, .95, .92, .92, .92, .92)
Sp \leftarrow c(.92, .92, .96, .96, .96, .90, .90, .90, .90)
# Assays used:
Assay \leftarrow c(1, 1, 2, 2, 2, 3, 3, 3, 3)
# Pool members:
Memb <- rbind(</pre>
  c(1, 2, 3, 4, 5, 6),
  c(7, 8, 9, 10, 11, 12),
  c(1, 2, -9, -9, -9),
  c(3, 4, -9, -9, -9, -9),
  c(5, 6, -9, -9, -9),
  c(1,-9, -9, -9, -9),
  c(2,-9, -9, -9, -9),
   c(5,-9, -9, -9, -9, -9),
   c(6,-9, -9, -9, -9, -9)
# The data-structure suited for 'gtData':
gtOut <- cbind(Z, psz, Se, Sp, Assay, Memb)</pre>
# Fitting the model:
pStart <- 0.10
res <- prop.gt(p0=pStart,gtData=gtOut,</pre>
               covariance=TRUE, nburn=2000,
               ngit=5000, maxit=200,
               tol=1e-03,tracing=TRUE)
print(res)
```

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```
## End(Not run)
```

waldTest

Wald Chi-Square Test

Description

This function implements the Wald *chi-square* test on a Kx1 parameter vector **theta**. The test assumes that **thetaHat**, a consistent estimator of **theta** such as MLE, is asymptotically normal with mean **theta** and covariance matrix **Sigma**. The function can implement 1 test on **theta** as well as multiple, \mathbf{Q} , tests jointly on **theta**.

Usage

```
waldTest(R, thetaHat, Sigma, r = 0, L = NULL)
```

Arguments

R A QxK matrix of known coefficients depending on how the test is to be carried

out.

thetaHat An estimate of **theta**.

Sigma An estimated covariance matrix for thetaHat.

r A Qx1 matrix of hypothesized values.

L A character string to be used as a name of the test. When NULL, "L" will be

used.

Details

Suppose that Q tests are to be performed jointly on the K by 1 parameter vector **theta**. Let R be a QxK matrix of known coefficients such as 0, 1, and -1, and r be a Qx1 matrix of hypothesized values. The hypotheses are $H0: R\theta = r$ vs. $H1: R\theta != r$. The test statistic has a chi-square distribution with Q degrees of freedom (Buse, 1982; Agresti, 2002).

Value

A data frame object of the Wald test results.

References

Agresti A. (2002). Categorical Data Analysis (2nd ed.). Wiley. ISBN 0471360937.

Buse A. (1982). The Likelihood Ratio, Wald, and Lagrange Multiplier Tests: An Expository Note. *The American Statistician*, 36:153-157.

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```
## Example 1
# Parameter: p (proportion)
MLE <- 0.42
Var <- 0.016
# (a) Test H0: p = 0.50 vs. H1: p != 0.50
R <- matrix(1, nrow=1, ncol=1)</pre>
p0 <- 0.50
waldTest( R=R, thetaHat=MLE, r=p0, Sigma=Var )
## Example 2
# Parameter: beta = (beta1, beta2), regression coefficients
MLE <- c(1.09, 2.95)
Cov <- rbind(c(0.21, -0.27),
             c(-0.27, 0.66))
# (a) Test H0: beta1 = beta2 vs. H1: beta1 != beta2
R \leftarrow rbind(c(1,-1))
waldTest( R=R, thetaHat=MLE, r=0, Sigma=Cov, L="1 vs 2" )
# (b) Test H0: beta1 = 0 vs. H1: beta1 != 0
R \leftarrow rbind(c(1,0))
waldTest( R=R, thetaHat=MLE, r=0, Sigma=Cov )
## Example 3
# Parameter: beta = (beta0, beta1, beta2)
MLE <- c(-3.05, 1.99, 0.93)
Cov <- rbind(c( 0.045, -0.022, -0.034),
             c(-0.022, 0.032, 0.008),
c(-0.034, 0.008, 0.048))
# Performing simultaneous test:
# H0: beta0 = -3, H0: beta1 = 2, H0: beta2 = 1
# H1: beta0 != -3, H1: beta1 != 2, H1: beta2 != 1
R < - rbind(c(1,0,0),
           c(0,1,0),
           c(0,0,1))
r <- matrix( c(-3,2,1), nrow=3 )
waldTest( R=R, thetaHat=MLE, r=r, Sigma=Cov)
```

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