

# Chapter 4

## Urban Mobility



Laura Alessandretti<sup>1b</sup> and Michael Szell<sup>1b</sup>

**Abstract** In this chapter, we discuss urban mobility from a complexity science perspective. First, we give an overview of the datasets that enable this approach, such as mobile phone records, location-based social network traces, or GPS trajectories from sensors installed on vehicles. We then review the empirical and theoretical understanding of the properties of human movements, including the distribution of travel distances and times, the entropy of trajectories, and the interplay between exploration and exploitation of locations. Next, we explain generative and predictive models of individual mobility, and their limitations due to intrinsic limits of predictability. Finally, we discuss urban transport from a systemic perspective, including system-wide challenges like ridesharing, multimodality, and sustainable transport.

### 4.1 Introduction and History of Quantitative Mobility Studies

From commuting to work, running errands, to going on a leisure trip, mobility is an integral part of our daily lives. Humans allocate a significant amount of time, money and energy to travel, with the average US household spending on mobility a non-negligibly high fraction of around 16% of its budget [1], and with commuting accounting on average for around 56 minutes per day [2]. Mobility underlies some of the most critical challenges of our times, including the design of sustainable urban transportation and the containment of epidemics. For example, a badly designed transport system can drive critical problems such as congestion, road deaths, and pollution. Transportation is estimated to account for around 27% of greenhouse gas emissions in the US, out of which around 57% comes from light-duty on-road

---

L. Alessandretti

DTU Compute, Technical University of Denmark, Lyngby, Denmark

e-mail: [lauale@dtu.dk](mailto:lauale@dtu.dk)

M. Szell (✉)

NEtwoRks, Data, and Society (NERDS), ITU Copenhagen, Copenhagen, Denmark

e-mail: [misz@itu.dk](mailto:misz@itu.dk)

vehicles (cars, motorbikes, vans) [3]. People on the move drive social mixing which in turn can facilitate the spread of infectious diseases [4]. Important societal issues are deeply intertwined with mobility patterns, and it has become critical to quantify and understand human movements. Understanding human mobility is important not only from a theoretical standpoint but also crucial to inform policy makers on how to improve urban transport and infrastructure, with the ultimate goal to invest into policies that improve the movement of people or that reduce the need for movement in the first place.

The study of human movements has a long history. The first rigorous approaches to quantify human movement patterns can be traced back to the 19th century, for example to Eduard Lill [5], statistician and chief inspector of the imperial-royal Austrian north-west railway company, who noticed that the number of people traveling from a place decreases as a hyperbola with distance, eventually giving rise to the gravity laws of travel discussed in Chap. 6. From this statistical perspective, the aggregate of many people can be described via simple mathematical laws, despite each individual having their individual, unique reasons for movement. This perspective is taken to the extreme in statistical physics, where large numbers of particles are easily described via their emergent properties, for example the temperature and pressure of a gas. This reductionist Ansatz, and the corresponding tools developed in statistical physics, are powerful ways to understand large numbers of interacting or moving entities *statistically*, whether they are particles or humans [6].

From these early studies on human mobility, we have come a long way. As an empirical science, the availability of high-resolution data has been crucial to drive evidence-based understanding. Such data have started to become available at the start of the 21st century, with first the diffusion of mobile phones, smartcards, and GPS positioning systems installed on vehicles, then smartphones and wearable devices. Concurrently with the development of increasingly powerful computational tools, the data revolution has enabled a richer and richer understanding of human mobility patterns. First, scientists could shift focus from the collective to the individual level, by studying single trajectories that have increasingly high temporal and spatial resolution, to the point that we can now trace actual route choices. Second, we are achieving a better and better understanding of the mechanisms underlying mobility behavior, through enriching mobility data with additional information, such as the features of the visited locations, individuals' social interactions, environmental and weather data, and features of the built environment [7].

In this chapter, we give an overview on how the field of complex systems, shaped considerably by statistical physicists, makes use of and adapts their tools in the context of urban mobility. Our chapter does not claim completeness but is an introductory overview of the fundamental concepts with hand-picked highlights; for a comprehensive review see, e.g., Barbosa et al. [8]. We outline the main aspects of the field by following largely the historical co-evolution of data and research. In Sect. 4.2 we discuss sources of data and issues of data quality. In Sect. 4.3 we introduce metrics and descriptive results about the statistical properties of individual empirical trajectories. In Sect. 4.4 we summarize the main statistical and mechanistic models about urban mobility patterns. Although we explicitly do not cover other approaches

to urban mobility, for example from transport engineering, we follow up with an outlook in Sect. 4.5 on sustainable transport and urban livability due to the urgency of this topic in the context of the climate crisis, asking to which extent some of the long-range or high-speed movements in cities of today are actually necessary and how they could be avoided. Finally, we provide a list of important tools and further materials in Sect. 4.6 and end with conclusions in Sect. 4.7.

## 4.2 Data Sources

Since the early 2000s, the development and widespread adoption of technologies that record the positions of individuals over time has driven a rapid growth of the field of human mobility, through enabling access to data [7]. Here, we describe some of the most widely used data sources.

### 4.2.1 *Data from Mobile Network Operators*

Mobile network operators gather location data for billing and operational purposes, through monitoring the cell towers that user devices connect to. These data have been widely used for human mobility research. Data collected by network operators has inherently limited spatial resolution, because the coverage of cell towers is quite wide, ranging from some tens of meters in urban areas up to tens of kilometers in rural areas. In terms of temporal resolution, there has been a rapid evolution over the last 20 years. Before the diffusion of smartphones, research was largely based on Call Detail Records (CDR), which captures the closest cell tower to individuals as they issue or receive calls or SMS. More recently, researchers have gained access to higher-frequency data. eXtended Detail Records (XDR) are collected when users explicitly request an http address or when the phone downloads content from the Internet (e.g., emails, messages, app updates). Control Plane Records (CPRs) are network-triggered (e.g., assigning a new antenna, connecting new devices) and are used to monitor the cellphone network status. CDR, XDR, and CPR vary significantly in their time granularity and data sparsity [9].

### 4.2.2 *Data from Smartphone Applications*

Other useful data sources are represented by services that collect Global Positioning System (GPS) positions through smartphone applications or services. In the early years of human mobility research, these data would mostly be collected by Location Based Social Networks (LSBN) services, such as Foursquare or Twitter (now “X”), which would gather location data only when individuals used the service.

Nowadays, other applications, including navigation apps or apps that perform targeted advertising, collect GPS positions from user devices at higher frequency. In turn, these applications are often equipped with software development kits (SDK) that can send the GPS data from the user's device to the company that produced the SDK. Through using several smartphone applications, SDK companies can thus collect comprehensive geolocation data. Especially since the COVID-19 pandemic, SDK data has become widely used for mobility research [10, 11].

### 4.2.3 *Transport and Mobile Sensor Data*

The digitization of private and public transport services now allows tracking of citizens in the public transportation system, such as through public transport travel card, and analyzing/visualizing entire taxi systems and transportation fleets. Further, detailed records are being generated by novel mobility sharing systems, from car and bicycle sharing to e-scooter and ride sharing. Custom sensors, installed on vehicles, can provide the potential to sense ecological urban variables and the sentiments of city dwellers in unprecedented detail.

Most data sources come with a wide range of biases and measurement problems, such as missing (sub)trajectories, zigzagging, or GPS jitter. Mobility data usually originate from applications that were not developed for research purposes, leading to typically low data quality. Any serious movement data analysis therefore has to account for adequate data preprocessing, including assessment and mitigation of data quality issues, which is often an extensive task [12]. Further, stop and home detection are not trivial [13, 14]. For example, several factors are crucial in the correct estimation of home locations, such as spatial aggregation or localization errors.

## 4.3 **Statistical Properties of Individual Trajectories**

Characterizing the statistical properties of individual trajectories is necessary to understand the underlying dynamics of human mobility and to design reliable predictive models. Generally, one can think of the movements of an individual as a trajectory consisting of *displacements* between locations and *pauses* at locations where the individual stops and spends time. Depending on the sampling frequency, the availability of spatio-temporal details, and the goal or scope of the analysis, trajectories can be studied either as sequences of locations, as sequences of locations embedded in space and time, or as high-frequency trajectories. In this section, we review some of the fundamental metrics that have been used in the literature to characterize individual trajectories and the resulting empirical findings. We will introduce richer and richer representations of individual trajectories. The entropy measures that

we introduce here swiftly can be well motivated from statistical mechanics, and can be extended or applied to many additional questions in urban science, see Chap. 12.

### 4.3.1 Trajectories as Sequences of Locations

In the simplest form, a trajectory can be represented as a sequence of locations, discarding aspects related to the position of locations in physical space. A large stream of literature has focused on the characteristics of these sequences of places.

One first key question is: How predictable are these sequences of locations? Or, in other words, to what extent is human mobility repetitive? This question is important for modeling purposes, to understand how simple we can make our models, and for privacy considerations. A key metric to address these questions is entropy, which can be thought of as a measure of uncertainty.

The most naive way of assessing predictability of an individual  $i$  is by examining their visited number of unique locations  $N_i$ . In the trivial case  $N_i = 1$  there is no uncertainty about the individual's location and it is fully predictable. However, the larger  $N_i$  gets, the more uncertain the location and the less predictable the individual becomes. A measure for the uncertainty of an individual's location which considers only  $N_i$  was introduced by Song et al. [15] as the *random entropy*

$$S_i^{\text{rand}} = \log_2 N_i$$

of an individual  $i$ 's trajectory, given their visited number of unique locations  $N_i$ . For example, a person 1 who visited 2 locations has  $S_1^{\text{rand}} = \log_2 N_1 = \log_2 2 = 1$ , a person 2 who has visited 4 locations has  $S_2^{\text{rand}} = \log_2 N_2 = \log_2 4 = 2$ .

Coming from thermodynamics and statistical physics, entropy more formally measures the degree to which the probability of a system is spread out over different possible microstates. In information theory it is called *Shannon entropy*

$$H(X) = - \sum p(x) \log_2 p(x)$$

of a discrete random variable  $X$ , where  $\sum$  denotes the sum over all possible values  $x$  of  $X$ . In mobility research, the Shannon entropy of an individual  $i$ 's trajectory has been called *temporal-uncorrelated entropy* [15]

$$S_i^{\text{unc}} = - \sum_{j=1}^{N_i} p_i(j) \log_2 p_i(j),$$

where  $p_i(j)$  denotes the fraction of individual  $i$ 's visits to location  $j$ .

As an example, consider a person 1 who visited a location A 270 times and a location B 30 times. Then  $p_1(A) = 0.9$ ,  $p_1(B) = 0.1$ , and

$$\begin{aligned}
S_1^{\text{unc}} &= - \sum_{j=1}^{N_1} p_1(j) \log_2 p_1(j) \\
&= -(p_1(A) \log_2 p_1(A) + p_1(B) \log_2 p_1(B)) \\
&= -(0.9 \log_2 0.9 + 0.1 \log_2 0.1) \\
&\approx 0.47.
\end{aligned}$$

In another example, imagine person 2 visited location A 200 times, location B 300 times, location C 300 times, location D 200 times, meaning  $p_2(A) = 0.2$ ,  $p_2(B) = 0.3$ ,  $p_2(C) = 0.2$ , and  $p_2(D) = 0.2$ . Then  $S_2^{\text{unc}} \approx 1.97$ .

The random and temporal-uncorrelated entropies of an individual are identical,  $S^{\text{rand}} = S^{\text{unc}}$ , when all locations are visited with equal probability. However,  $S^{\text{unc}}$  becomes smaller the more unequal, or skewed, the distribution probabilities of different locations are. From the examples above,  $S_2^{\text{rand}} = 2$  which is almost the same as  $S_2^{\text{unc}} = 1.97$  because all four locations were visited with similar frequency. However, for individual 1,  $S_1^{\text{rand}} = 1$  is much larger than  $S_1^{\text{unc}} = 0.47$  because in this case the visitation frequencies were much more skewed, 270 to 30. These two concepts of entropy, random and temporal-uncorrelated, are thus useful to assess how much the skew in visiting probabilities affects the uncertainty of locations.

Extending the concept of entropy one step further adds the aspect of ordering, asking: How heterogeneous are visitations not only across locations but also in their time-ordering? The *real entropy*  $S_i^{\text{real}}$  of an individual  $i$ 's trajectory is given by

$$S_i^{\text{real}} = - \sum_{T'_i \subset T_i} P(T'_i) \log_2 P(T'_i),$$

where  $P(T'_i)$  is the probability of finding a particular time-ordered subsequence  $T'_i$  in the trajectory  $T_i$  [15]. Thus, an individual with a trajectory of repeating or regular patterns, such as ABACDCABACDCABACDC will have a much lower real entropy than an individual who has an identical number and visitation distribution of locations but a less regular order of visitations, for example ABCDACABACDCABACACD. Similarly as  $S^{\text{rand}}$  was an upper limit for  $S^{\text{unc}}$ , here  $S^{\text{unc}}$  is an upper limit for  $S^{\text{real}}$ . The identity  $S^{\text{unc}} = S^{\text{real}}$  is given when the order of locations in the trajectory is randomized, thereby destroying all time-correlated information.

A measure associated to the entropy  $S$  is the predictability  $\Pi$ , derived from information theory [15], which is the probability that an optimal predictive algorithm can predict correctly the individual's future whereabouts. Every type of entropy has a respective predictability measure, for which the inequality relation between entropies  $S^{\text{rand}} \geq S^{\text{unc}} \geq S^{\text{real}}$  is inverted to  $\Pi^{\text{rand}} \leq \Pi^{\text{unc}} \leq \Pi^{\text{real}}$ . The more uncertainty, the less predictability. As Song et al. [15] have shown, a significant share of predictability is encoded in the time ordering which make the trips of most individuals highly predictable.

This high predictability of human trajectories has strong privacy implications. For example, it was shown that for the trajectories of 1.5 million individuals, with

hourly sampling and spatial aggregation to 6,500 cell phone towers, only 4 random spatio-temporal points are needed to identify 95% of individuals [16]. Such insights have profound legal and ethical consequences on the sharing and tracking of micro-mobility data, and have spurred research on privacy-enhancement techniques such as cloaking, suppression, aggregation, swapping, or differential privacy [17].

While the statistical characterization of trajectories, either individually or in aggregate, is crucial for fundamental predictability and privacy considerations, two important practical questions remain: 1) What are those regular sequences of locations, and 2) What is the relation with other people's movements in the city? The first question can be tackled via motif analysis, where the most common trips of individuals are interpreted as a network of trips between locations [18]. Motifs in complex networks are generally small subgraphs that appear with significantly higher than expected probability [19]. Analyzing both surveys and mobile phone data in different cities, Schneider et al. [18] found that half of the daily mobility networks are just described by two trivial motifs, consisting of one node (no movement) or of two nodes (back and forth movement, typically home-work). The vast majority of all other daily movements are described by remaining 15 motifs. The second question—the relation with other people's movements—has been investigated for example in the context of bus transit patterns of 5 million individuals in Singapore [20]. Due to the striking regularity of daily commutes, the emergence of “familiar strangers” in a tight-knit contact network was observed, with crucial consequences on the impact of human behavior on diffusion/spreading processes. More recent studies have compared explicitly social relations with mobility behavior [21, 22]. For example, the Copenhagen network study [21] has found striking differences in geospatial versus social entropy in a population of 1,000 university students, uncovering “party nights” that are characterized by geospatial exploration but conservative social behavior.

The reason why sequences of human locations are highly predictable is rooted in the high level of regularity of day-to-day routines, with mobility highly dominated by home-work commuting. Moreover, the way humans visit places and allocate time among them is characterized by universal properties, as shown by several empirical studies. Some notable properties include:

*Heterogeneous distribution of visits.* Humans allocate their time in a heterogeneous way across places, implying they spend most of their time within a small set of favorite locations. Ranking locations from the most visited to the least visited, the number of visits for a location with rank  $L$  follows a power-law  $P \sim L^{-\alpha}$  with exponent  $\alpha \sim 1.2$  [23, 24].

*Sublinear exploration.* The number of distinct locations  $S$  visited by an individual grows over time ( $t$ ) as  $S(t) \sim t^\beta$ , with  $\beta \sim 0.6$ , implying that there is a decreasing tendency to explore new locations [23].

*Periodicity.* The probability to return to a location visited  $n$  hours before is characterized by peaks at 24 h, 48 h and 72 h, due to the recurrence and temporal periodicity inherent to human mobility, which is driven by circadian and weekly patterns. [23]

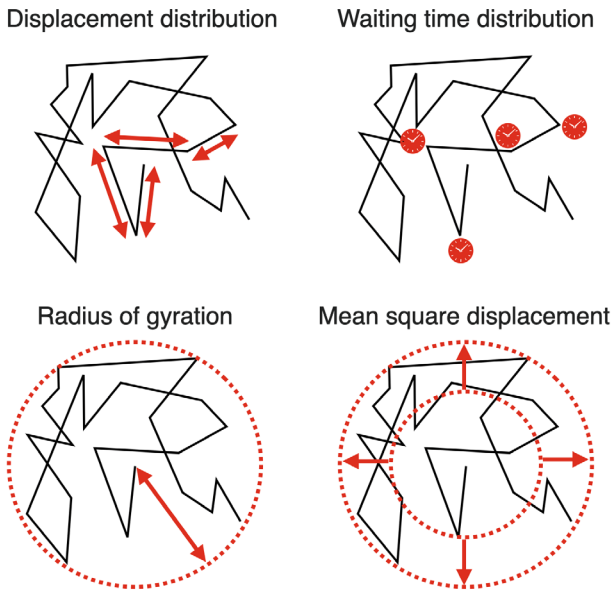
*Conservation of the number of visited places.* It was shown that, despite the fact that our routines change and evolve over long time-scales, some properties of the set

of visited locations, including its size, remain approximately conserved at the level of the single individual [24].

### 4.3.2 Trajectories in Space and Time

If the data are available, realism can be increased by considering trajectories as sequences of locations embedded in space and time. Two key properties that characterize these sequences are the waiting time and the displacement distributions, see Fig. 4.1.

The *waiting time distribution*  $P(\Delta t)$  describes probabilistically the time  $\Delta t$  that an individual pauses after a move. The *displacement distribution*  $P(\Delta r)$  describes probabilistically the distance  $\Delta r$  that an individual moves after a pause. The distribution of waiting times (or pause durations),  $\Delta t$ , between movements and the distribution of distances,  $\Delta r$ , travelled between pauses are useful to quantitatively assess the dynamics of human mobility. For example, specific probability distributions of distances and waiting times characterise different types of diffusion processes.



**Fig. 4.1** To quantitatively study the movements of humans, the field of complex systems adapts the random walk approach from statistical physics originally developed for describing particle movements, with metrics such as displacement distribution, waiting time distribution, radius of gyration, mean square displacement. The black connected line segments denote a trajectory starting in the center, the red markers illustrate the different metrics



Thanks to the recent availability of data used as proxy for human trajectories, the characteristic distributions of distances and waiting times between consecutive locations have been widely investigated. There is no agreement, however, on which distribution best describes these empirical datasets. Pioneer studies, based on CDR [23, 25] and banknote records [26], found that the distribution of displacement  $\Delta r$  is well approximated by a power-law,  $P(\Delta r) \sim (\Delta r)^{-\beta}$ , (or “Lévy distribution” [27], typically with  $1 < \beta < 3$ ), and that an exponential cut-off in the distribution may control boundary effects [25]. These findings were confirmed by studies based on GPS trajectories of individuals [28–30] and vehicles [31, 32], as well as online social networks data [33–35]. It has been noted, however, that power-law behaviour may fail to describe intra-urban displacements [36]. Other analyses, based on online social network data [37–39] and GPS trajectories [40–43] showed that the distribution of displacements is well fitted by an exponential curve,  $P(\Delta r) \sim e^{-\lambda \Delta r}$ , in particular at short distances. Finally, analyses based on Taxi GPS [44, 45] suggested that displacements may also obey log-normal distributions,  $P(\Delta r) \sim (1/\Delta r) \cdot e^{-(\log \Delta r - \mu)^2 / 2\sigma^2}$ . Another study found that this is the case also for single-transportation trips [29].

Fewer studies have explored the distribution of waiting times between displacements,  $\Delta t$ , as trajectory sampling is often uneven; e.g., in CDR data location is recorded only when the phone user makes a call or sends an SMS, and LBSN data include the positions of individuals who actively “check-in” at specific places. Analyses based on evenly sampled trajectories from mobile phone call records [18, 23], and individuals GPS trajectories [28, 30] found that the distribution of waiting times can also be approximated by a power-law. A recent study based on GPS trajectories of vehicles, however, suggests that for waiting times larger than 4 hours, this distribution is best approximated by a log-normal function [46]. Several studies have highlighted the presence of natural temporal scales in individual routines. Distributions of waiting times display peaks that correspond to the typical times spent home on a typical day (around 14 hours) and at work (3–4 hours for a part-time job and 8–9 hours for a full-time job) [18, 47, 48].

The datasets considered have different *spatial resolution and coverage*, and few studies have so far considered the whole range of displacements occurring between  $10^1$  m and  $10^7$  m (10, 000 km). Another issue for comparability concerns the *temporal sampling* in the datasets analysed so far. Uneven sampling typical of CDR and LBSN data (i) does not allow to distinguish phases of *displacement* and *pause*, since individuals could be active also while transiting between locations, and (ii) may fail to capture patterns other than regular ones [49, 50], because individuals’ voice-call/SMS/data activity may be higher in certain preferred locations. Finally, studies focusing on displacements effectuated using one or several *specific transportation modalities* (private car [46, 51], taxi [43], public transportation [52], or walking [30]) capture only a specific aspect of human mobility behaviour.

Nevertheless, an aggregate measure of diffusion over many individuals, which describes how fast an area is explored, is given by the *mean square displacement*  $MSD(t)$ , see Fig. 4.1. It measures the deviation of the position of  $N$  individuals from a reference position over a timespan  $t$  as an (ensemble) average over all the individuals  $j$ ,

$$\text{MSD}(t) = \langle \mathbf{r}_j(t) - \mathbf{r}_j(0) \rangle = \frac{1}{N} \sum_{j=1}^N \left( \mathbf{r}_j(t) - \mathbf{r}_j(0) \right)^2 ,$$

where  $\mathbf{r}_j(t)$  is the position of individual  $j$  at time  $t$  and  $\mathbf{r}_j(0)$  is their initial reference position. The mean squared displacement is a measure introduced in statistical mechanics to study diffusion processes, and can be thought of as measuring the portion of the system “explored” by an ensemble of individuals. Empirical research has shown that human mobility patterns follows a slow diffusion process, in which the MSD grows logarithmically [23].

To distinguish whether individuals all sample from the same displacement or waiting time distributions, or whether individuals have different movement behaviors, it is useful to define the *radius of gyration*, see Fig. 4.1. It is the typical distance travelled by an individual over a fixed timespan  $t$ ,

$$r_g = \sqrt{\frac{1}{n} \sum_{i=1}^n |\mathbf{r}_i - \mathbf{r}_{\text{cm}}|^2} ,$$

where  $n$  is the number of jumps within timespan  $t$ ,  $\mathbf{r}_i$  represents the position at step  $i$ , and  $\mathbf{r}_{\text{cm}} = \frac{1}{n} \sum_{i=1}^n \mathbf{r}_i$  is the center of mass of the trajectory. Gonzalez et al. [25] have introduced this metric to human mobility studies, showing that individuals have different typical travel distances. In particular, it has been shown that the distribution of the radius of gyration across individuals is broad and can be well described by a truncated power-law [25].

## 4.4 Modeling Urban Mobility Patterns

To study the movements of humans, the field of complex systems adapts models from statistical physics, which studies the movements of particles. Central to this approach is the concept of *random walk*, see Fig. 4.1. A random walk describes the random, Brownian motion of particles suspended in a liquid or gas, and can be taken as the simplest model for a moving individual. Generally defined, a random walk is a random process describing a path of random steps on a mathematical space. For example, a random walk on the integer number line  $\mathbb{Z}$  could start at 0 and at each step move  $-1$  or  $+1$  with equal probability, decided by a coin flip. Thus, after two coin flips, the following outcomes are possible:

- $-2$ , after  $0 - 1 - 1$
- $0$ , after  $0 - 1 + 1$  or  $0 + 1 - 1$
- $2$ , after  $0 + 1 + 1$

In the above example, the random walk describes a trajectory on  $\mathbb{Z}$  with a fixed jump distance of 1 and an arbitrary waiting time—for repeated coin flipping this could be for example 3 seconds. Further, this random walk is memoryless, as the coin flip is a random process independent of previous outcomes. There are several ways to extend the behavior of random walkers, adding complexity to more realistically model human mobility. For example, in continuous-time random walk (CTRW) models, jump lengths and waiting times can follow arbitrary distributions. This model was suggested as one of the first models able to capture the probability distributions of displacements and waiting times, where the step-lengths and waiting times were calibrated from heavy-tailed probability distributions observed in human mobility [26].

However, human mobility is not completely random, and researchers quickly realized that more realistic mechanisms were needed to capture the properties of human trajectories. An ingredient to make trajectories more realistic is memory, i.e. individuals can remember and be influenced by visits to previous places. In 2010, Song et al. [23] proposed an agent-based model with memory that could capture many of the observed properties of mobility.

The *Exploration and Preferential Return* model (EPR) proposes that whenever individuals visit a location, they either (i) explore with probability  $P_{\text{new}} = S^{-\gamma}$ , where  $S$  is the number of distinct locations previously visited, or (ii) return to a previously visited location with complimentary probability  $P_{\text{ret}} = 1 - P_{\text{new}}$  [23]. When returning to a previously visited location, the probability  $p_i$  to visit location  $i$  is proportional to the number of visits the individual previously had to that location, an effect known as preferential return. Several variations of the EPR model have been proposed to account for other aspects of human mobility including more memory and recency effects [24, 53, 54], social interactions [55], and heterogeneities across individuals [56].

An important development of the EPR model is the *Preferential Exploration and Preferential Return* (PEPR) model, developed by Schl pfer et al. [55]. This model couples the movements of agents, so that, when exploring new locations, they are preferentially attracted towards highly frequented areas, which can be seen as a manifestation of Central Place Theory. Importantly, this model is able not only to reproduce the individual mobility, but also collective patterns of mobility, thus linking the literature streams on individual and collective mobility (collective mobility is covered in Chap. 5). In particular, the PEPR model accounts for an important empirical discovery made by Schl pfer et al. [55], related to the frequency at which individuals visit different locations. By studying mobility traces extracted from phones the authors had found that the number of users who visit a location at distance  $r$ , exactly  $n$  times in a period of length  $T$ , decreases as  $N \sim r^{-2} f^{-2}$ , where  $f = n/T$ .

While capturing many properties of human movements, preferential return models are still unable to explain the power-law distribution of displacements in mobility data. The observation that mobility patterns are captured by power-law distributions seemed to show that human mobility is scale-free in a truly fundamental sense. But concurrently, it was known that the natural and built environment is rich in spatial scales, from neighbourhoods, to cities, regions, countries and continents [57].

The notion of scale is fundamental within the fields of geography and spatial cognition, because we think of space in a hierarchical fashion characterized by typical scales [58]. In this sense, there appeared to be an important schism between traditional geography and the data-driven work on human mobility. This divide got explicitly addressed in 2020 by Alessandretti et al. [59] working with a very large dataset of GPS traces. This study showed that typical scales are indeed embedded within the same type of scale-free trajectories analyzed by previous researchers. The explanation is that scales manifest as containers of mobility behavior. Neighborhoods have typical sizes, but the distance between the neighborhoods a certain individual visits is unrelated to the size of neighborhoods (it is rather set by the city scale). Similarly with cities which also tend to have a typical geographical size, but the cities a certain individual tends to visit may be close—or located in opposite ends of their home country. A similar logic is true for scales across neighborhoods, cities, regions, countries, continents, and the entire world. The authors use a model-based approach to infer the typical sizes of these containers across millions of individuals.

Based on these ideas, the *container model* models physical space as a hierarchy of  $L$  levels, ordered from the smallest to largest (e.g. individual locations to countries). At any level  $l$ , space is partitioned into compact containers with a characteristic size. Each geographical location  $k$  can be identified as a sequence of nested containers,  $k = (k_1, \dots, k_l, \dots, k_L)$  that contains it. The *level-distance*  $d(j, k)$  between locations  $j$  and  $k$  is defined as the highest index at which the two sequences of containers describing  $j$  and  $k$  differ. For an agent located in  $j$ , the probability of moving to  $k$  is the product of two factors  $P(j \rightarrow k) = p_{d(j,k), d(j,h)} \prod_{l \leq d(j,k)} a(k_l)$ . The first factor,  $p_{d(j,k)}$ , is the probability of traveling at level-distance  $d(j, k)$ . The second factor  $\prod_{l \leq d(j,k)} a(k_l)$  is the probability of choosing a specific location  $k$  at that level-distance, where  $a(k_l)$  is the attractiveness of a container at level  $l$  including location  $k$ .

## 4.5 Improving Urban Transport Systems

The research described so far focuses mostly on understanding where and when people move, statistically describing individual trajectories or emerging aggregate patterns. The question of how people get to their destinations—which transport mode they use, which route they take and why, and the role of the underlying transport system—has remained largely uncharted from a quantitative perspective, also due to the limited availability of data with high enough resolution. For example, how individuals choose routes through balancing the interplay between public and private forms of transportation such as walking, driving and cycling remains poorly characterized. The existing empirical research using a *systemic* and *long-term* view on urban transport systems, including shared travel, multimodal travel, or system dynamics like induced demand is thus quite limited [60]. In this section we review first on the one hand some microscopic and mode-specific wayfinding mechanisms, on the other hand more systems-level approaches of how to think about the dynamics

of urban transport systems with the aim to improve them. We discuss the importance of different urban transport modes, to help designing more efficient and sustainable urban transportation.

### 4.5.1 Wayfinding

Apart from a statistical, quantitative description of human mobility, it is important to understand the mechanisms of how humans are navigating in cities to find their ways. While pathfinding on a graph (such as a street network) is a solved problem in computer science via Dijkstra's shortest path algorithm and its modern replacements [61], the implementation of routing on multimodal networks can be challenging [62, 63], and an array of cognitive peculiarities (see also Chapter 1) have to be accounted for such as upbringing [64], vector-based navigation [65], information overload [66], or mode-specific travel behavior [67]. Recent findings have established that pedestrians, cyclists, and motorists do not tend to follow optimal routes, and are instead influenced by urban features and goal distance and direction [65, 68–70].

### 4.5.2 Shareability Networks

Existing urban transport systems are highly inefficient, such as the individualized transport mode of taxis. In New York City, for example, a large fleet of around 13,500 taxicabs serves individualized mobility needs, but with a high fraction of idle or low occupation runs. To quantify how much such a localized fleet could be improved, Santi et al. [71] introduced the concept of shareability network in 2014 using methods from network science.

The idea of shareability networks is to view a vehicle fleet from a global perspective and to optimize for the whole system with global knowledge instead of locally. For example, instead of having two taxis deliver two individuals in parallel from the same starting point to the same end point, the routes of the two passengers could have been bundled with just one taxi with small inconvenience to both. Taking this idea to the extreme, towards  $k$ -sharing with  $k > 2$ , would lead to a system of dynamically routed “taxi buses”. As Santi et al. [71] showed, in New York City indeed a large fraction of trips could be shared with relatively low discomfort, with cumulative trip length cut by 40% or more.

Trip-sharing systems were introduced later by UBER (called UBERPool), and by similar ride hailing companies, leading to a claimed short-term reduction of driven kilometers [72]. However, in total, companies like UBER have later shown to have generated more traffic and congestion due to rebound effects and their competition with public transport [73–75]. This example shows how long-term systems thinking is necessary to understand the full impact and possible unintended consequences of short-term optimization, see Sect. 4.5.3.

The research on shareability networks was later expanded with a focus on fleet size and vehicle-sharing networks [76], finding a potential to reduce the New York City taxi fleet size by 30%. Such a potential reduction follows directly from a reorganization of taxi dispatching that could be implemented with a mobile phone app and does not assume ride sharing, nor requires changes to regulations, business models, or human attitudes towards mobility to become effective. Finally, further research uncovered scaling effects in ride-sharing [77, 78].

### ***4.5.3 Sustainable, Multimodal Transport and Systems Thinking***

Understanding urban mobility is impossible without understanding its history and the complex socio-technical system it is part of. This history shows a transition towards car-centricity in the 20th century for most cities, entailing critical consequences on the whole system. For example, over 1.3 Mio. people die on the road every year [79], vehicular pollution causes millions of more yearly deaths [80], and vehicular traffic noise has shown to cause dementia-related diseases on a large scale [81]. Further, cars come with massive inefficiencies due to their skewed space requirements and usage patterns [82]. Apart from empirical evidence that this is unsustainable [83], also mathematical models from complexity science show that cities as (car-centric) transport monocultures are not sustainable [84, 85], and that a mere replacement of fossil fuel cars with electric vehicles is not an adequate solution [86–89], especially when much more efficient and economic solutions such as mass transit or bicycles are available.

To fix such monocultures, the biggest question in urban transport is how to reverse car dependency [90], i.e. how to best replace unsustainable modes of transport and to prioritize more sustainable ones. In particular, active travel such as walking and cycling has the highest societal benefits [91]. Cost-benefit analysis which accounts for the environment and public health reveals that each kilometer walked or cycled in the European Union provides €0.37 or €0.18 to society, respectively, while each kilometer driven by car incurs a cost of €0.11 [92]. Overcoming transportation monocultures is also possible with a focus on more multimodal transport, i.e. the combination of multiple transport modes promising all of their benefits while avoiding their weaknesses. For an overview of state of the art complex systems based approaches to multimodal mobility see Alessandretti et al. [60].

Systems thinking is the appropriate method of understanding how (un)sustainable urban mobility emerges over time [93]. There is a complex co-evolution between urban transport infrastructure, land use, and socio-political/cultural factors with long-term feedback loops. Complex systems dynamics are crucially dependent on the *interactions* between its parts and not just on the parts themselves. For example, increased traffic volume creates pressure to invest into road infrastructure, which drives more traffic volume. This is the well-known phenomenon of *induced*

*demand* [93]. Due to increased roadway capacities, catchment areas increase, leading to urban sprawl, which in turn increases traffic volume and erodes active modes of transport due to increased distances and lack of adequate transport infrastructure. In particular cultures such as in the US, this phenomenon has sometimes lead to extreme sprawl, which makes it all the harder to reverse car-dependence. This situation is also an example for path dependency and lock-in effects common in complex systems, where the more the system evolves towards a certain path, the harder it is to reverse.

The general phenomenon of car-dependence can be thought of as a dynamic reinforced through different socio-technical systems such as the automotive industry, land use, or car culture [94]. Therefore, long-term urban planning cannot detach transport planning from the planning of land-use, housing, parking [95], etc., but the whole system must be understood as being shaped by strong, non-linear, long-term interactions. Although the opposite of systems thinking, namely short-term engineering thinking, has its use cases, it is inadequate to apply to most problems in complex systems, because the optimization or control of sub-systems can lead to unintended consequences (such as induced demand or urban sprawl) [93]. Using short-term traffic engineering thinking has lead to the outdated “predict and provide” logic, where e.g. traffic volumes are predicted from past flows and the role of policy makers is to react by providing a short-term solution. On the contrary, following systems thinking, this logic is replaced with the more adequate “decide and provide” principle, which aims to pro-actively shape the future [96]. It acknowledges that e.g. the choice to drive a car is not solely the result of people’s individual preferences, i.e. exogenous to the system, but determined largely by transport and urban systems organised around car driving, which can be changed with appropriate policies.

Such policies can leverage long-term systems dynamics, allowing to re-shape transport systems for the better [93]. For example, the reversal of induced demand, namely disappearing traffic, happens when public space is reallocated from private cars to space-efficient modes of transport. As research shows [90, 97], significant reductions in overall traffic levels can occur in the right conditions, because mode choice is more elastic than commonly believed: Many individuals are willing to give up traveling by car if there are appropriate alternatives. To succeed, it is also important to consider the right communication strategies and the strong psychological aspect of car attachment [98]. Apart from policies to develop multimodal networks and street redesign, a large array of further policies can address a variety of system dynamics, from market-based instruments such as carbon-prices, road pricing, to abolishing minimum parking requirements, or financial support to increase the attractiveness of micromobility [93]. For all these policies, it is important to prioritize correctly, for example following an “avoid-shift-improve” approach [99, 100]. First, focus on avoiding the need for mobility, for example through planning for proximity such as the 15-minute city [101]. Second, aim for a shift from unsustainable to more sustainable modes of transport. Only as a last third step aim to improve existing components of the system such as making vehicle technology more efficient.

## 4.6 Tools

Over the years, computational tools have become more and more important for studying urban systems and human mobility. For an overview of the available tools in geographic analysis and transport planning see Lovelace [102]. Here we focus on open-source tools as they allow fully reproducible research or analysis. There is a plethora of tools specialized on various purposes, including network analysis (single-layer or multilayer), routing and access (unimodal or multimodal), or mobility analysis. We classify these computational tools into three groups.

### 4.6.1 Transport and Mobility Tools

We first describe the most general tools for mobility and transport analysis.

To work with public transportation data, the Python library *transitfeed* [103] is suited to parse, validate and build General Transit Feed Specification (GTFS) files, which is a data specification that allows public transit agencies to publish their transit data in a usable form. This tool is particularly useful to those interested in the manipulation of the raw data. However, to convert the data into a network, some additional steps are needed, such as using *Peartree* (see below).

*Movingpandas* [104] is a Python package that provides trajectory data structures and functions for the analysis and visualisation of mobility data. In a similar sense, and also developed in Python, *scikit-mobility* [105] is a library that implements a framework for analyzing statistical patterns and modeling mobility, including functions for estimating movement between zones using spatial interaction models, and tools to assess privacy risks related to the analysis of mobility datasets.

### 4.6.2 Transport Network Tools

In this section we cover tools for studying transportation networks.

Multiple tools were developed to obtain data on transportation and multimodal infrastructures. One of the best known is *OSMnx* [106], a Python package that downloads street networks from OpenStreetMap into Python objects. *OSMnx* can further be used to download other transportation networks, and to build its multimodal transport networks.

Another reliable Python library to read data from OpenStreetMap and extract transportation networks is *Pyrosm* [107]. Differently from *OSMnx*, *Pyrosm* reads the data directly from OpenStreetMap's Protocol Buffer Format files (\*.osm.pbf), while *OSMnx* downloads the data from the Overpass API [108]. For this reason *Pyrosm* is a particularly good alternative when working with large urban areas, states, and



even countries, while *OSMnx* typically offers a more precise way to collect data from specific points in a city.

Finally, an alternative to *transitfeed*'s functionality of reading GTFS feeds is *Peartree* [109], a Python library allowing to convert GTFS feed schedules into the corresponding directed network graph.

### 4.6.3 Tools for Routing or Access on Transport Networks

In this section we cover tools that can be used for routing and navigation.

On one hand there are established general, high-performance tools for unimodal routing such as *graphhopper* [110] and *OSRM* [111]. These tools were developed for routing on one network type but could in principle be extended to multimodal routing. Explicit multimodal routing is provided by *OpenTripPlanner (OTP)* [112] and *R5* [113]. Both tools exist as fast R implementations, *r5r* [114] and *OTP for R* [115]; the Python implementation of *R5* is *R5py* [116]. The R package *dodgr* [117], thanks to an efficient algorithm for computing distances between pairs of nodes in a street network, further enables the aggregation of flows on network links from a set of origin and destination points, a matrix of pairwise flow densities, and the underlying street network.

Finally, several open source packages focus on computing accessibility metrics, e.g. the ease by which people can reach points of interests, such as those offering employment, shopping, medical care or recreation [118]. *Pandana* [119, 120] is a Python library that enables to compute the accessibility of places by retrieving points of interest and street network data from OpenStreetMap [121] and by efficiently computing shortest paths along the street network. *Access* [122] is a Python library that computes a wide range of spatial accessibility metrics from a set of origins and destinations, and travel times or distances between them. Built on top of *Pandana*, *UrbanAccess* [123] integrates the creation of multi-modal transport networks (transit and pedestrian) using GTFS data and the computation of accessibility metrics. Similar functionalities are offered in R and Python by *r5r* [114] and *R5py* [116], respectively.

## 4.7 Conclusions

Modelling urban mobility patterns is critical to address a wide range of societal challenges, from managing public health, to planning urban infrastructure and transportation. By gaining insights into how people move, we can make informed decisions towards developing transportation systems that are efficient and inclusive, reducing carbon emissions, and enhancing public safety.

The scientific study of human mobility dates back to the late 19th century and has been extensively studied in Transportation Science and Human Geography throughout the 20th century. Over the past few decades, the field has made significant

advances, facilitated by the availability of large datasets and the development of Complexity Science, which has brought together methods for understanding inter-connected, non-linear systems.

In this chapter, we provided a brief, introductory overview of recent developments, including hand-picked highlights. We started with a short history of the field, focusing on the complexity science perspective. We then described the wide range of data sources used in mobility studies and the empirical findings these data have enabled. We also presented a variety of modelling approaches developed to capture different aspects of individual movements and discuss how these models can be used to study urban transportation networks. Finally, we presented a set of computational open-source tools that can be used for urban mobility analysis and research.

Notwithstanding the important discoveries made thus far, many challenges remain. For example, issues surround the understanding of causal mechanisms underlying human spatial behavior in urban contexts. While research using passively collected data has suggested some potential mechanisms, integrating experimental or quasi-experimental approaches may be necessary to shed light on how the cognitive and behavioral mechanisms identified in laboratory settings drive real-world behavior and validate hypotheses brought forward by the field of Human Mobility.

Other challenges include the availability and quality of data, including misrepresentation, spatial and temporal resolution differences, and data skews. These problems can affect insights derived from the data, and the literature is still sparse on how to address them, partly due to the lack of ground-truth data. Additionally, mobility datasets are sensitive because they contain detailed information regarding people's whereabouts and behavioral patterns, making it critical that this data is handled in safe and ethical ways. The difficulties of obtaining informed consent for data use and enabling result reproducibility do not have clear solutions yet.

Finally, from an applications perspective, new challenges surround the understanding of emerging technologies for urban mobility, from micro-mobility, to autonomous vehicles, route recommendation engines, vehicle-to-vehicle communication, and vehicle-to-infrastructure communication. Efforts are needed to understand the impact of these developing technologies on travel behaviour and to comprehensively integrate widely diverse travel modes into a unified framework.

All in all, our chapter could serve as a basis for teaching the topic to an advanced audience (master level or higher); much of the discussed material is covered in open teaching resources available at <https://github.com/mszell/geospatialdatascience>.

## References

1. *Transportation Economic Trends: Transportation spending—average household*. <https://data.bts.gov/stories/s/Transportation-Economic-Trends-Transportation-Spen/ida7-k95k/>
2. C. Burd, M. Burrows, B. McKenzie, Travel time to work in the united states: 2019, in *American Community Survey Reports, United States Census Bureau 2* (2021), p. 2021. <http://large.stanford.edu/courses/2022/ph240/schutt2/docs/acs-47.pdf>
3. <https://www.epa.gov/ghgemissions/sources-greenhouse-gas-emissions>

4. L. Alessandretti, What human mobility data tell us about COVID-19 spread. *Nature Reviews Physics* **4**(1), 12–13 (2022). <https://doi.org/10.1038/s42254-021-00407-1>
5. E. Lill, *Die Grundgesetze des Personenverkehrs: Eine Studie* (Hartleben's Verlag, Vienna, 1889)
6. P. Ball, The physical modelling of human social systems. *Complexus* **1**(4), 190–206 (2003). <https://doi.org/10.1159/000082449>
7. B. Resch, M. Szell, Human-Centric Data Science for Urban Studies, in *ISPRS International Journal of Geo-Information* 8.584 (2019). <https://doi.org/10.3390/ijgi8120584>
8. H. Barbosa et al., Human mobility: Models and applications. *Physics Reports* **734**, 1–74 (2018). <https://doi.org/10.1016/j.physrep.2018.01.001>
9. L. Pappalardo et al., Evaluation of home detection algorithms on mobile phone data using individual-level ground truth, in *EPJ data science* 10.1 (2021), p. 29. <https://doi.org/10.1140/epjds/s13688-021-00284-9>
10. A. Aleta et al., Modelling the impact of testing, contact tracing and household quarantine on second waves of COVID-19. *Nature Human Behaviour* **4**(9), 964–971 (2020). <https://doi.org/10.1016/j.tra.2010.08.003>
11. S. Chang et al., Mobility network models of COVID-19 explain inequities and inform reopening. *Nature* **589**(7840), 82–87 (2021). <https://doi.org/10.1038/s41586-020-2923-3>
12. G. Andrienko, N. Andrienko, G. Fuchs, Understanding movement data quality. *Journal of location Based services* **10**(1), 31–46 (2016). <https://doi.org/10.1080/17489725.2016.1169322>
13. F. Calabrese et al., Understanding individual mobility patterns from urban sensing data: A mobile phone trace example. *Transportation research part C: emerging technologies* **26**, 301–313 (2013). <https://doi.org/10.1016/j.trc.2012.09.009>
14. L. Pappalardo et al., scikit-mobility: A Python Library for the Analysis, Generation, and Risk Assessment of Mobility Data, in *Journal of Statistical Software* 103.4 (2022), pp. 1–38. <https://doi.org/10.18637/jss.v103.i04>. <https://www.jstatsoft.org/index.php/jss/article/view/v103i04>
15. C. Song et al., Limits of predictability in human mobility. *Science* **327**(5968), 1018–1021 (2010). <https://doi.org/10.1126/science.1177170>
16. Y.-A. De Montjoye et al., Unique in the crowd: The privacy bounds of human mobility. *Scientific reports* **3**(1), 1–5 (2013). <https://doi.org/10.1038/srep01376>
17. M. Fiore et al., Privacy in trajectory micro-data publishing: a survey, in *Transactions on Data Privacy* 13 (2020), pp. 91–149. <https://orbit.dtu.dk/en/publications/privacy-in-trajectory-micro-data-publishing-a-survey>
18. C.M. Schneider et al., Unravelling daily human mobility motifs, in *Journal of The Royal Society Interface* 10.84 (2013), p. 20130246. <https://doi.org/10.1098/rsif.2013.0246>
19. R. Milo et al., Network motifs: simple building blocks of complex networks. *Science* **298**(5594), 824–827 (2002). <https://doi.org/10.1126/science.298.5594.824>
20. L. Sun et al., Understanding metropolitan patterns of daily encounters. *Proceedings of the National Academy of Sciences* **110**(34), 13774–13779 (2013). <https://doi.org/10.1073/pnas.1306440110>
21. V. Sekara, A. Stopczynski, S. Lehmann, Fundamental structures of dynamic social networks. *Proceedings of the national academy of sciences* **113**(36), 9977–9982 (2016). <https://doi.org/10.1073/pnas.1602803113>
22. Z. Chen et al., Contrasting social and non-social sources of predictability in human mobility. *Nature communications* **13**(1), 1–9 (2022). <https://doi.org/10.1038/s41467-022-29592-y>
23. C. Song et al., Modelling the scaling properties of human mobility. *Nature Physics* **6**(10), 818–823 (2010). <https://doi.org/10.1038/nphys1760>
24. L. Alessandretti et al., Evidence for a conserved quantity in human mobility. *Nature human behaviour* **2**(7), 485–491 (2018). <https://doi.org/10.1038/s41562-018-0364-x>
25. M.C. Gonzalez, C.A. Hidalgo, A.-L. Barabasi, Understanding individual human mobility patterns. *Nature* **453**(7196), 779–782 (2008). <https://doi.org/10.1038/nature07850>
26. D. Brockmann, L. Hufnagel, T. Geisel, The scaling laws of human travel. *Nature* **439**(7075), 462–465 (2006). <https://doi.org/10.1038/nature04292>

27. A. Baronchelli, F. Radicchi, Lévy flights in human behavior and cognition. *Chaos, Solitons & Fractals* **56**, 101–105 (2013). <https://doi.org/10.1016/j.chaos.2013.07.013>
28. X.-W. Wang, X.-P. Han, B.-H. Wang, Correlations and scaling laws in human mobility, in *PloS one* 9.1 (2014), e84954. <https://doi.org/10.1371/journal.pone.0084954>
29. K. Zhao et al., Explaining the power-law distribution of human mobility through transportation modality decomposition, in *Scientific reports* 5 (2015). <https://doi.org/10.1038/srep09136>
30. I. Rhee et al., On the levy-walk nature of human mobility. *IEEE/ACM transactions on networking (TON)* **19**(3), 630–643 (2011). <https://doi.org/10.1109/tnet.2011.2120618>
31. B. Jiang, J. Yin, S. Zhao, Characterizing the human mobility pattern in a large street network, in *Physical Review E* 80.2 (2009), p. 021136. <https://doi.org/10.1103/physreve.80.021136>
32. Y. Liu et al., Understanding intra-urban trip patterns from taxi trajectory data. *Journal of geographical systems* **14**(4), 463–483 (2012). <https://doi.org/10.1007/s10109-012-0166-z>
33. M.G. Beiró et al., Predicting human mobility through the assimilation of social media traces into mobility models, in *arXiv preprint arXiv:1601.04560* (2016). <https://doi.org/10.1140/epjds/s13688-016-0092-2>
34. Z. Cheng et al., Exploring Millions of Footprints in Location Sharing Services”. *ICWSM* **2011**, 81–88 (2011). <https://doi.org/10.1609/icwsml.v5i1.14109>
35. B. Hawelka et al., Geo-located Twitter as proxy for global mobility patterns. *Cartography and Geographic Information Science* **41**(3), 260–271 (2014). <https://doi.org/10.1080/15230406.2014.890072>
36. A. Noulas et al., A tale of many cities: universal patterns in human urban mobility, in *PloS one* 7.5 (2012), e37027. <https://doi.org/10.1371/journal.pone.0037027>
37. L. Wu et al., Intra-urban human mobility and activity transition: evidence from social media check-in data, in *PloS one* 9.5 (2014), e97010. <https://doi.org/10.1371/journal.pone.0097010>
38. Y. Liu et al., Uncovering patterns of inter-urban trip and spatial interaction from social media check-in data, in *PloS one* 9.1 (2014), e86026. <https://doi.org/10.1371/journal.pone.0086026>
39. R. Jurdak et al., Understanding human mobility from Twitter, in *PloS one* 10.7 (2015), e0131469. <https://doi.org/10.1371/journal.pone.0131469>
40. H. Liu, Y.-H. Chen, J.-S. Lih, Crossover from exponential to power-law scaling for human mobility pattern in urban, suburban and rural areas. *The European Physical Journal B* **88**(5), 1–7 (2015). <https://doi.org/10.1140/epjb/e2015-60232-1>
41. X. Liang et al., The scaling of human mobility by taxis is exponential. *Physica A: Statistical Mechanics and its Applications* **391**(5), 2135–2144 (2012). <https://doi.org/10.1016/j.physa.2011.11.035>
42. L. Gong et al., Inferring trip purposes and uncovering travel patterns from taxi trajectory data. *Cartography and Geographic Information Science* **43**(2), 103–114 (2016). <https://doi.org/10.1080/15230406.2015.1014424>
43. K. Zhao, M.P. Chinnasamy, S. Tarkoma, Automatic City Region Analysis for Urban Routing, in *2015 IEEE International Conference on Data Mining Workshop (ICDMW)*. IEEE, 2015, pp. 1136–1142. <https://doi.org/10.1109/icdmw.2015.176>
44. W. Wang et al., A comparative analysis of intra-city human mobility by taxi. *Physica A: Statistical Mechanics and its Applications* **420**, 134–147 (2015). <https://doi.org/10.1016/j.physa.2014.10.085>
45. J. Tang et al., Uncovering urban human mobility from large scale taxi GPS data. *Physica A: Statistical Mechanics and its Applications* **438**, 140–153 (2015). <https://doi.org/10.1016/j.physa.2015.06.032>
46. R. Gallotti et al., A stochastic model of randomly accelerated walkers for human mobility, in *Nature Communications* 7 (2016), p. 12600. <https://doi.org/10.1038/ncomms12600>
47. S. Hasan et al., Spatiotemporal patterns of urban human mobility. *Journal of Statistical Physics* **151**(1–2), 304–318 (2013). <https://doi.org/10.1007/s10955-012-0645-0>
48. A. Bazzani et al., Statistical laws in urban mobility from microscopic GPS data in the area of Florence, in *Journal of Statistical Mechanics: Theory and Experiment* 2010.05 (2010), P05001. <https://doi.org/10.1088/1742-5468/2010/05/p05001>

49. S. Çolak et al., Analyzing cell phone location data for urban travel: current methods, limitations, and opportunities. *Transportation Research Record* **2526**(1), 126–135 (2015). <https://doi.org/10.3141/2526-14>
50. G. Ranjan et al., Are call detail records biased for sampling human mobility? In: *ACM SIGMOBILE Mobile Computing and Communications Review* 16.3 (2012), pp. 33–44. <https://doi.org/10.1145/2412096.2412101>
51. R. Gallotti, A. Bazzani, S. Rambaldi, Understanding the variability of daily travel-time expenditures using GPS trajectory data, in *EPJ Data Science* 4.1 (2015), p. 1. <https://doi.org/10.1140/epjds/s13688-015-0055-z>
52. C. Roth et al., Structure of urban movements: polycentric activity and entangled hierarchical flows, in *PloS one* 6.1 (2011), e15923. <https://doi.org/10.1371/journal.pone.0015923>
53. M. Szell et al., Understanding mobility in a social petri dish. *Scientific reports* **2**(1), 1–6 (2012). <https://doi.org/10.1038/srep00457>
54. H. Barbosa et al., The effect of recency to human mobility. *EPJ Data Science* **4**(1), 1–14 (2015). <https://doi.org/10.1140/epjds/s13688-015-0059-8>
55. M. Schlöpfer et al., The universal visitation law of human mobility. *Nature* **593**(7860), 522–527 (2021). <https://doi.org/10.1038/s41586-021-03480-9>
56. L. Pappalardo et al., Returners and explorers dichotomy in human mobility. *Nature communications* **6**(1), 1–8 (2015). <https://doi.org/10.1038/ncomms9166>
57. D. Pumain, *Hierarchy in natural and social sciences*. Springer (2006). <https://doi.org/10.1007/1-4020-4127-6>
58. S. Grauwin et al., Identifying and modeling the structural discontinuities of human interactions, in *Scientific Reports* 7.46677 (2017). <https://doi.org/10.1038/srep46677>
59. L. Alessandretti, U. Aslak, S. Lehmann, The scales of human mobility. *Nature* **587**(7834), 402–407 (2020). <https://doi.org/10.1038/s41586-020-2909-1>
60. L. Alessandretti et al., Multimodal urban mobility and multilayer transport networks. *Environment and Planning B: Urban Analytics and City Science*, 1–33 (2022). <https://doi.org/10.1177/23998083221108190>
61. D. Delling et al., Engineering route planning algorithms, in *Algorithmics of large and complex networks*. Springer, 2009, pp. 117–139. [https://doi.org/10.1007/978-3-642-02094-0\\_7](https://doi.org/10.1007/978-3-642-02094-0_7)
62. F. Poletti et al., Public transit route mapping for large-scale multimodal networks, in *ISPRS International Journal of Geo-Information* 6.9 (2017), p. 268. <https://doi.org/10.3390/ijgi6090268>
63. J.-Q. Li et al., A multimodal trip planning system with real-time traffic and transit information. *Journal of Intelligent Transportation Systems* **16**(2), 60–69 (2012). <https://doi.org/10.1080/15472450.2012.671708>
64. A. Coutrot et al., Entropy of city street networks linked to future spatial navigation ability. *Nature* **604**(7904), 104–110 (2022). <https://doi.org/10.1101/2020.01.23.917211>
65. C. Bongiorno et al., Vector-based pedestrian navigation in cities. *Nature Computational Science* **1**(10), 678–685 (2021). <https://doi.org/10.1038/s43588-021-00130-y>
66. R. Gallotti, M.A. Porter, M. Barthelemy, Lost in transportation: Information measures and cognitive limits in multilayer navigation, in *Science advances* 2.2 (2016), e1500445. <https://doi.org/10.1126/sciadv.1500445>
67. J. Broach, J. Dill, J. Gliebe, Where do cyclists ride? A route choice model developed with revealed preference GPS data, in *Transportation Research Part A: Policy and Practice* **46**(10), 1730–1740 (2012). <https://doi.org/10.1016/j.tra.2012.07.005>
68. E.J. Manley, J.D. Addison, T. Cheng, Shortest path or anchor-based route choice: a large-scale empirical analysis of minicab routing in London”. en. In: *Journal of Transport Geography* 43 (Feb. 2015), pp. 123–139. ISSN: 0966-6923. <https://doi.org/10.1016/j.jtrangeo.2015.01.006>
69. N. Malleon et al., The characteristics of asymmetric pedestrian behavior: A preliminary study using passive smartphone location data”. en. In: *Transactions in GIS* 22.2 (2018), pp. 616–634. ISSN: 1467-9671. <https://doi.org/10.1111/tgis.12336>
70. A. Lima et al., Understanding individual routing behaviour, in *Journal of The Royal Society Interface* 13.116 (2016), p. 20160021. <https://doi.org/10.1098/rsif.2016.0021>

71. P. Santi et al., Quantifying the benefits of vehicle pooling with shareability networks. *Proceedings of the National Academy of Sciences* **111**(37), 13290–13294 (2014). <https://doi.org/10.1073/pnas.1403657111>
72. U. Editor, *Earth Day is Sunday. And every day.* — *uber.com*. <https://www.uber.com/blog/earth-day-2018/>. [Accessed 06-Oct-2022]. 2018
73. A. Henao, W.E. Marshall, The impact of ride-hailing on vehicle miles traveled. *Transportation* **46**(6), 2173–2194 (2019). <https://doi.org/10.1007/s11116-018-9923-2>
74. A. Tirachini, Ride-hailing, travel behaviour and sustainable mobility: an international review. *Transportation* **47**(4), 2011–2047 (2020). <https://doi.org/10.1007/s11116-019-10070-2>
75. M. Diao, H. Kong, J. Zhao, Impacts of transportation network companies on urban mobility. *Nature Sustainability* **4**(6), 494–500 (2021). <https://doi.org/10.1038/s41893-020-00678-z>
76. M.M. Vazifeh et al., Addressing the minimum fleet problem in on-demand urban mobility. *Nature* **557**(7706), 534–538 (2018). <https://doi.org/10.1038/s41586-018-0095-1>
77. R. Tachet et al., Scaling law of urban ride sharing, in *Scientific Reports* **7**, 42868 (2017). <https://doi.org/10.1038/srep42868>
78. N. Molkenthin, M. Schröder, M. Timme, Scaling laws of collective ride-sharing dynamics, in *Physical Review Letters* **125**, 24 (2020), p. 248302. <https://doi.org/10.1103/physrevlett.125.248302>
79. World Health Organization, Global status report on road safety, in (2018)
80. F. Caiazzo et al., Air pollution and early deaths in the United States. Part I: Quantifying the impact of major sectors in 2005, in *Atmospheric Environment* **79** (2013), pp. 198–208. <https://doi.org/10.1016/j.atmosenv.2013.05.081>
81. M. Lech Cantuaria et al., Residential exposure to transportation noise in Denmark and incidence of dementia: national cohort study, in *bmj* **374** (2021). <https://doi.org/10.1136/bmj.n1954>
82. M. Szell, Crowdsourced quantification and visualization of urban mobility space inequality, in *Urban Planning* **3** (2018), pp. 1–20. <https://doi.org/10.17645/up.v3i1.1209>
83. D. Banister, *Unsustainable transport: city transport in the new century*. Routledge (2005). <https://doi.org/10.4324/9780203003886>
84. R. Louf, M. Barthélemy, Modeling the polycentric transition of cities, in *Physical review letters* **111**, 19 (2013), p. 198702. <https://doi.org/10.1103/physrevlett.111.198702>
85. R. Prieto Curiel et al., A paradox of traffic and extra cars in a city as a collective behaviour, in *Royal Society Open Science* **8** (201808 2021). <https://doi.org/10.1098/rsos.201808>
86. F. Creutzig et al., Transport: A roadblock to climate change mitigation?" In: *Science* **350**, 6263 (2015), pp. 911–912. <https://doi.org/10.1126/science.aac8033>
87. A. Milovanoff, I.D. Posen, H.L. MacLean, Electrification of light-duty vehicle fleet alone will not meet mitigation targets. *Nature Climate Change* **10**(12), 1102–1107 (2020). <https://doi.org/10.1038/s41558-020-00921-7>
88. C. Brand et al., The climate change mitigation effects of daily active travel in cities, in *Transportation Research Part D: Transport and Environment* **93** (2021), p. 102764. <https://doi.org/10.21203/rs.3.rs-39219/v2>
89. J. Henderson, EVs are not the answer: a mobility justice critique of electric vehicle transitions. *Annals of the American Association of Geographers* **110**(6), 1993–2010 (2020). <https://doi.org/10.1080/24694452.2020.1744422>
90. International Transport Forum. *Reversing Car Dependency*. 2021, p. 41. <https://doi.org/10.1787/bebe3b6e-en>
91. Walking and Cycling, *latest evidence to support policy-making and practice* (WHO, Tech. rep, 2022)
92. S. Gössling et al., The social cost of automobility, cycling and walking in the European Union. *Ecological Economics* **158**, 65–74 (2019). <https://doi.org/10.1016/j.ecolecon.2018.12.016>
93. *Transport Strategies for Net-Zero Systems by Design*. Tech. rep. (OECD Publishing, 2021)
94. G. Mattioli et al., The political economy of car dependence: A systems of provision approach, in *Energy Research & Social Science* **66** (2020), p. 101486. <https://doi.org/10.1016/j.erss.2020.101486>



95. D.C. Shoup, *The high cost of free parking*. (Routledge, 2021)
96. G. Lyons, C. Davidson, Guidance for transport planning and policymaking in the face of an uncertain future. *Transportation Research Part A: Policy and Practice* **88**, 104–116 (2016). <https://doi.org/10.1016/j.tra.2016.03.012>
97. S. Cairns, S. Atkins, P. Goodwin, Disappearing traffic? The story so far, in *Proceedings of the Institution of Civil Engineers-Municipal Engineer*. Vol. 151. 1. Thomas Telford Ltd. 2002, pp. 13–22. <https://doi.org/10.1680/muen.151.1.13.38856>
98. S. Gössling, Why cities need to take road space from cars-and how this could be done. *Journal of Urban Design* **25**(4), 443–448 (2020). <https://doi.org/10.1080/13574809.2020.1727318>
99. D. Bongardt et al., Sustainable Urban Transport: Avoid-Shift-Improve (ASI), in *Transformative Urban Mobility Initiative* (2019)
100. E. Holden et al., Grand Narratives for sustainable mobility: A conceptual review, in *Energy Research & Social Science* **65** (2020), p. 101454. <https://doi.org/10.1016/j.erss.2020.101454>
101. C. Moreno et al., Introducing the “15-Minute City”: Sustainability, resilience and place identity in future post-pandemic cities. *Smart Cities* **4**(1), 93–111 (2021). <https://doi.org/10.3390/smartcities4010006>
102. R. Lovelace, Open Source Tools for Geographic Analysis in Transport Planning, in *Journal of Geographical Systems* (Jan. 2021). ISSN: 1435-5949. <https://doi.org/10.1007/s10109-020-00342-2>
103. Google, *transitfeed*. V.1.2.16 <https://github.com/google/transitfeed>. 2018. <https://github.com/google/transitfeed>
104. A. Graser, MovingPandas: efficient structures for movement data in Python. *GIForum* **1**, 54–68 (2019). [https://doi.org/10.1553/giscience2019\\_01\\_s54](https://doi.org/10.1553/giscience2019_01_s54)
105. L. Pappalardo et al., *scikit-mobility: a Python library for the analysis, generation and risk assessment of mobility data*. 2021. [arXiv: 1907.07062](https://arxiv.org/abs/1907.07062) [physics.soc-ph]
106. G. Boeing, OSMnx: New methods for acquiring, constructing, analyzing, and visualizing complex street networks, in *Computers, Environment and Urban Systems* **65** (Sept. 2017), pp. 126–139. ISSN: 01989715. <https://doi.org/10.1016/j.compenvurbysys.2017.05.004>
107. H. Tenkanen, *pyrosm*. V.0.5.0 <https://github.com/HTenkanen/pyrosm>. May 2020. <https://doi.org/10.5281/ZENODO.3818244>. <https://github.com/HTenkanen/pyrosm>
108. OpenStreetMap contributors, *Overpass API*. <https://overpass-api.de/>. (2017)
109. K. Butts, *Peartree*. Peartree, V0.6.4, <https://github.com/kuanb/peartree/releases/tag/0.6.4> (2021)
110. GraphHopper, *GraphHopper*. <https://www.graphhopper.com/> (2022)
111. OSRM, *Open source routing machine*. <http://project-osrm.org/> (2021)
112. OTP, *OpenTripPlanner*. <http://www.opentripplanner.org/> (2022)
113. M. Wigginton Conway, A. Byrd, M. van der Linden, Evidence-based transit and land use sketch planning using interactive accessibility methods on combined schedule and headway-based networks, in *Transportation Research Record* **2653.1** (2017), pp. 45–53. <https://doi.org/10.3141/2653-06>
114. R.H.M. Pereira et al., r5r: Rapid realistic routing on multimodal transport networks with R5 in R, in *Findings* (2021), p. 21262. <https://doi.org/10.32866/001c.21262>
115. M. Morgan et al., OpenTripPlanner for R, in *Journal of Open Source Software* **4.44** (2019), p. 1926. <https://doi.org/10.21105/joss.01926>
116. C. Fink et al., *r5py: Rapid Realistic Routing with R5 in Python*. 2022. <https://doi.org/10.5281/zenodo.7060437>
117. M. Padgham, Dodgr: An r package for network flow aggregation, in *Findings* (2019), p. 6945. <https://doi.org/10.32866/6945>
118. P. Rietveld, The accessibility of railway stations: the role of the bicycle in The Netherlands. *Transportation Research Part D: Transport and Environment* **5**(1), 71–75 (2000). [https://doi.org/10.1016/S1361-9209\(99\)00019-X](https://doi.org/10.1016/S1361-9209(99)00019-X)
119. F. Foti, P. Waddell, D. Luxen, A generalized computational framework for accessibility: from the pedestrian to the metropolitan scale, in *Proceedings of the 4th TRB Conference on Innovations in Travel Modeling*. Transportation Research Board (2012)

120. Pandana, *Pandana*. V.0.6.1 2021. <https://github.com/UDST/pandana>
121. OpenStreetMap contributors, *Planet dump retrieved from* <https://planet.osm.org>. <https://www.openstreetmap.org> (2017)
122. J. Saxon et al., An open software environment to make spatial access metrics more accessible, in *Journal of Computational Social Science* (2021), pp. 1–20. <https://doi.org/10.1007/s42001-021-00126-8>
123. S.D. Blanchard, P. Waddell, Urbanaccess: generalized methodology for measuring regional accessibility with an integrated pedestrian and transit network. *Transportation research record* **2653**(1), 35–44 (2017). <https://doi.org/10.3141/2653-05>