

# POLYMER AND COMPOSITE MATERIALS PROCESSING

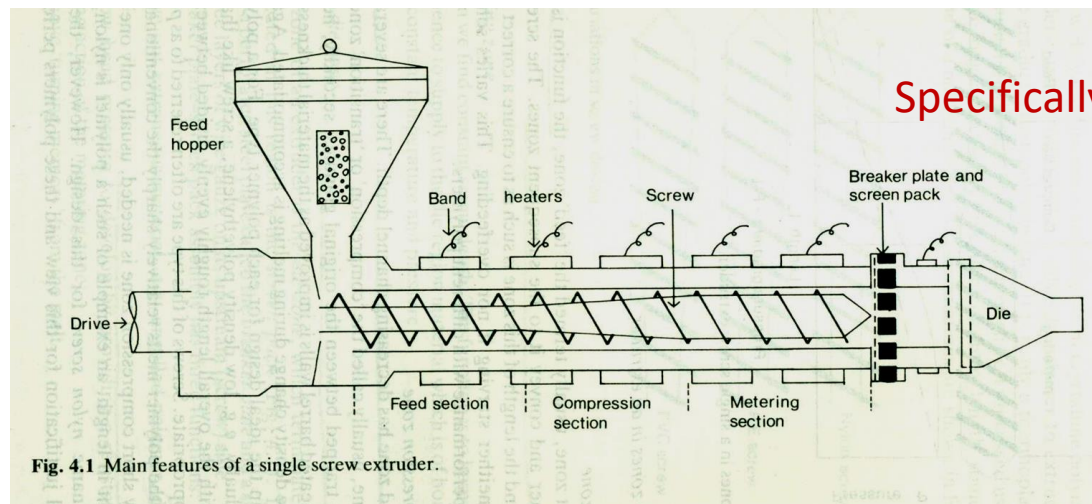
**Lecturer : Prof. Doojin Lee**

Department of Polymer Science and Engineering,  
Chonnam National University

# Ch. 4. EXTRUSION

## What is extrusion

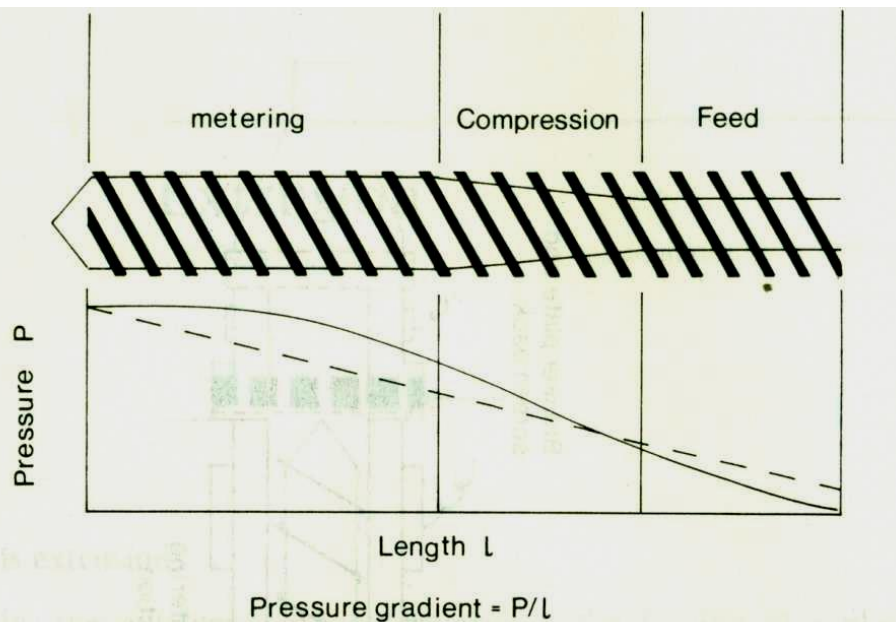
- The extrusion process comprises the forcing of a plastic or molten material through a shaped die by means of pressure.
- The most widely used type is the single screw machine.
- Twin screw extruders are also used where superior mixing or conveying is important.
- Solid polymer is fed in at one end and the profiled molten extrudate emerges from the other.
- Inside, the polymer melts and homogenizes.



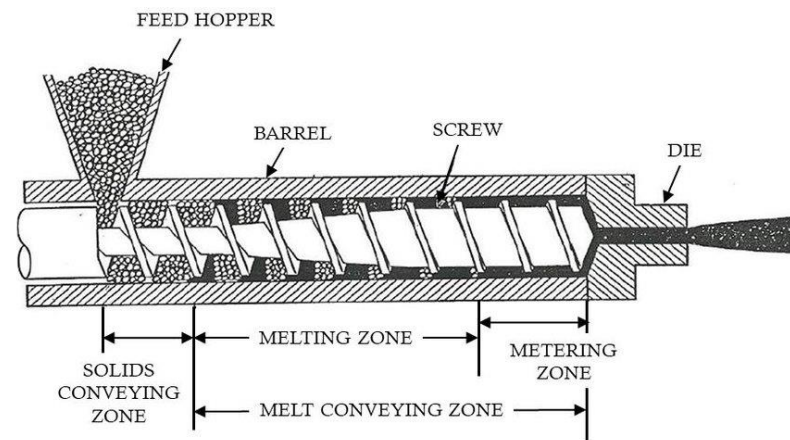
Specifically, blending or compounding?

# Features of a single screw extruder

- The screw of an extruder has one or two flights **spiralling along its length**.
  - The diameter to the outside : constant along the length to allow the close fit in the barrel.
  - **The root or core, however, is of varying diameter** and so the **spiralling channel varies in depth**.
  - A consequence of the decreasing channel depth : **increasing pressure along the extruder**.



**Fig. 4.2** Zones in a single screw extruder.



- The zones in an extruder

- 1) Feed zone

- Preheat the polymer and convey it to the subsequent zones.
    - The constant screw channel depth

- 2) Compression zone (transition zone)

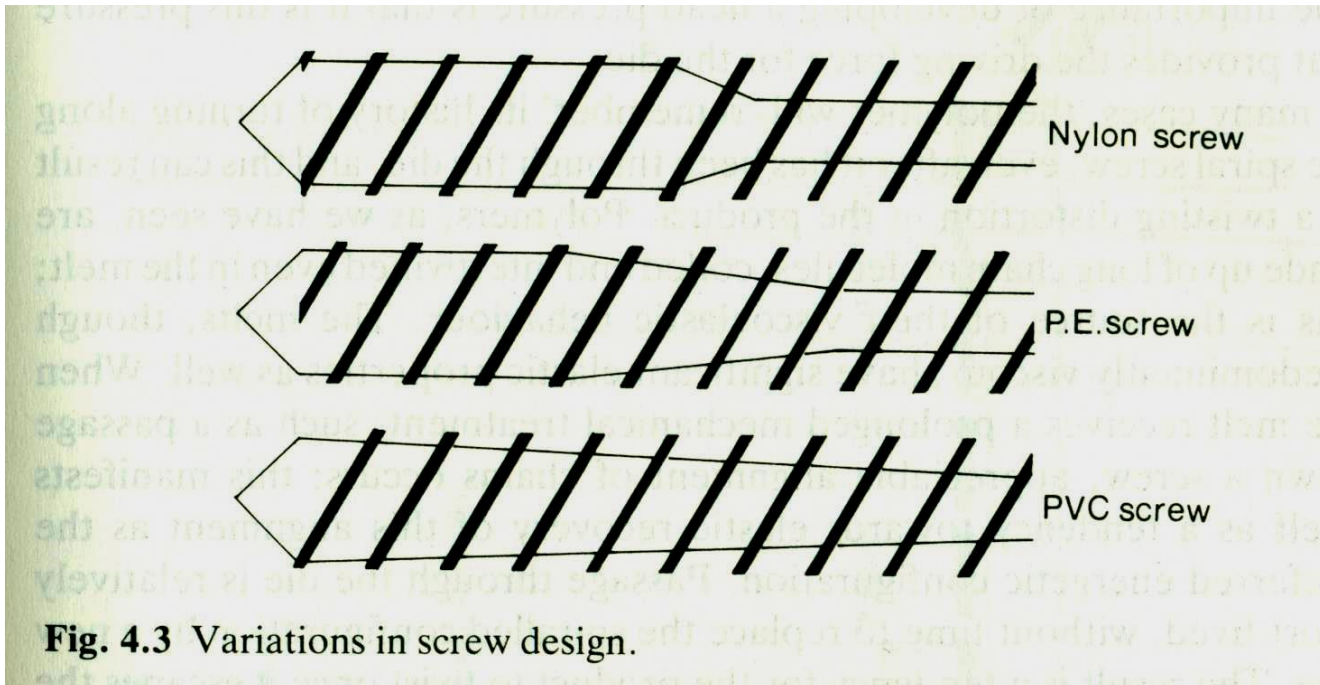
- The decreasing channel depth
    - The several functions
      - It expels air trapped between the original granules
      - Heat transfer from the heated barrel walls is improved as the material thickness decreases.
      - The density change (high packing of materials) during melting is accommodated.

- 3) Metering zone

- The constant screw depth (pressure stabilized)
    - The function is to homogenize the melt and hence to supply to the die region.

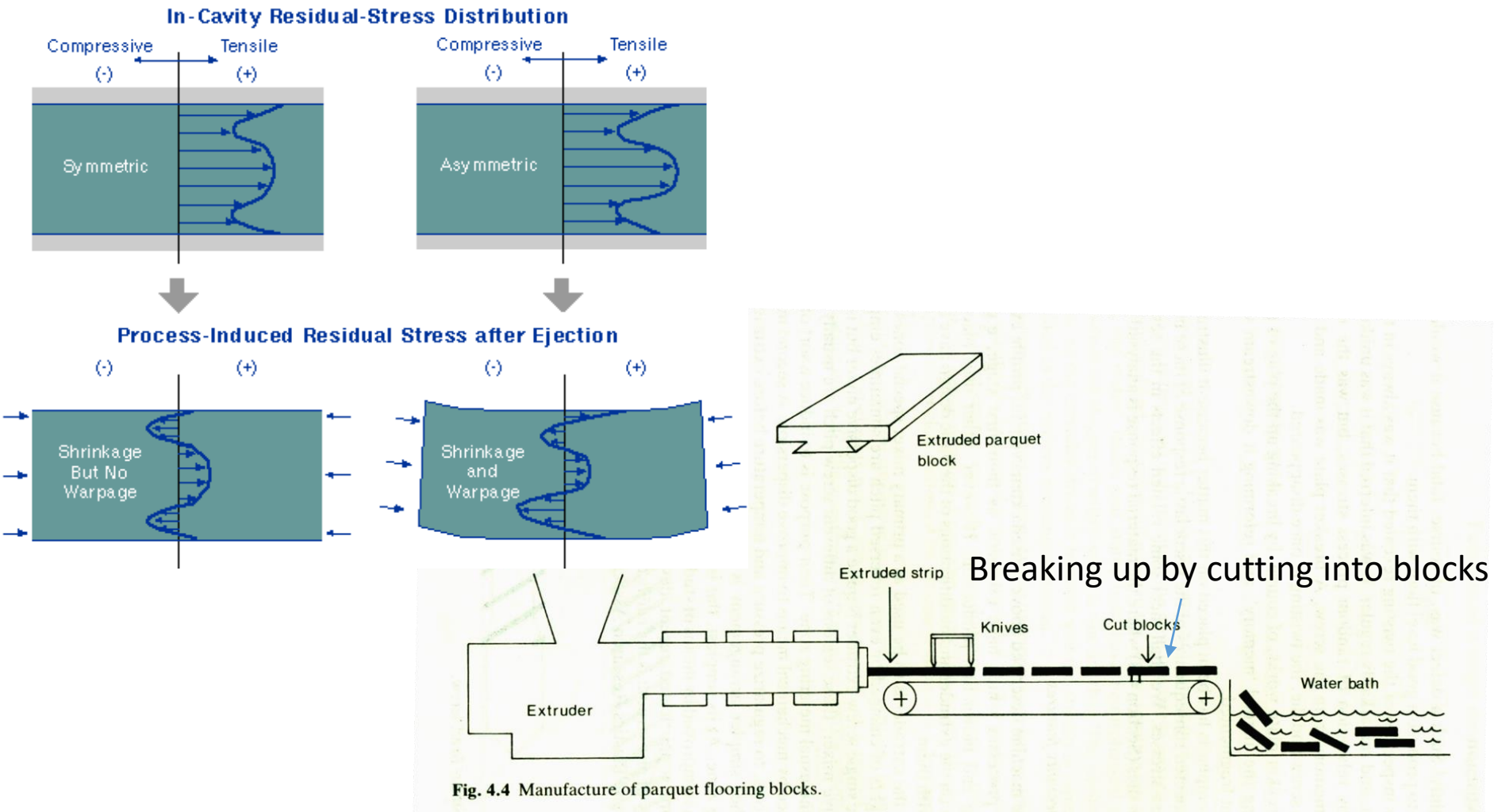
## 4) The die zone

- The final zone = die zone :
  - To sieve out extraneous material, e.g. ungelled polymer, dirt, foreign bodies
  - To allow head pressure to develop by providing a resistance for the pumping action of the metering zone
  - To remove 'turning memory' form the melt : this is due to the viscoelastic behavior of polymers.



**Fig. 4.3** Variations in screw design.

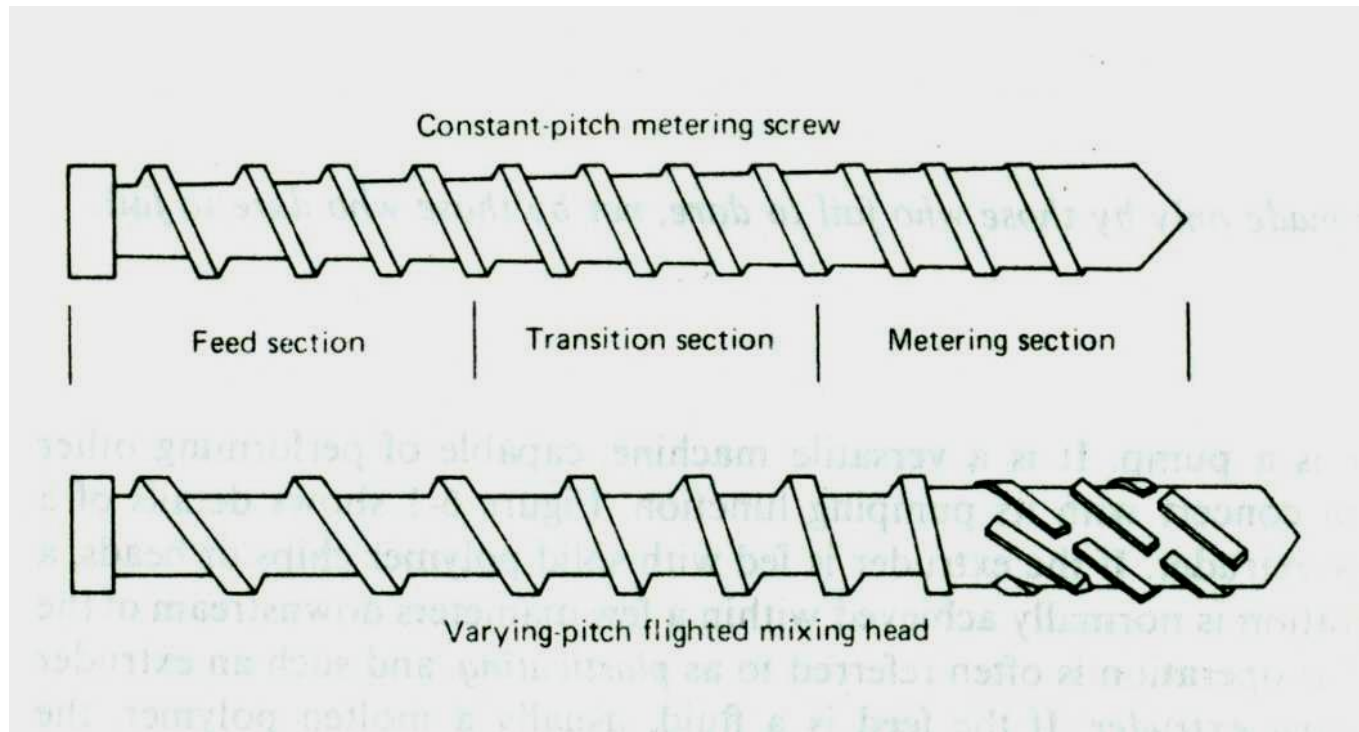
- An example of ‘**turning memory**’
  - When they were removed from the cooling bath, they were all twisted.
  - Why twisted? “**Residual stress**”



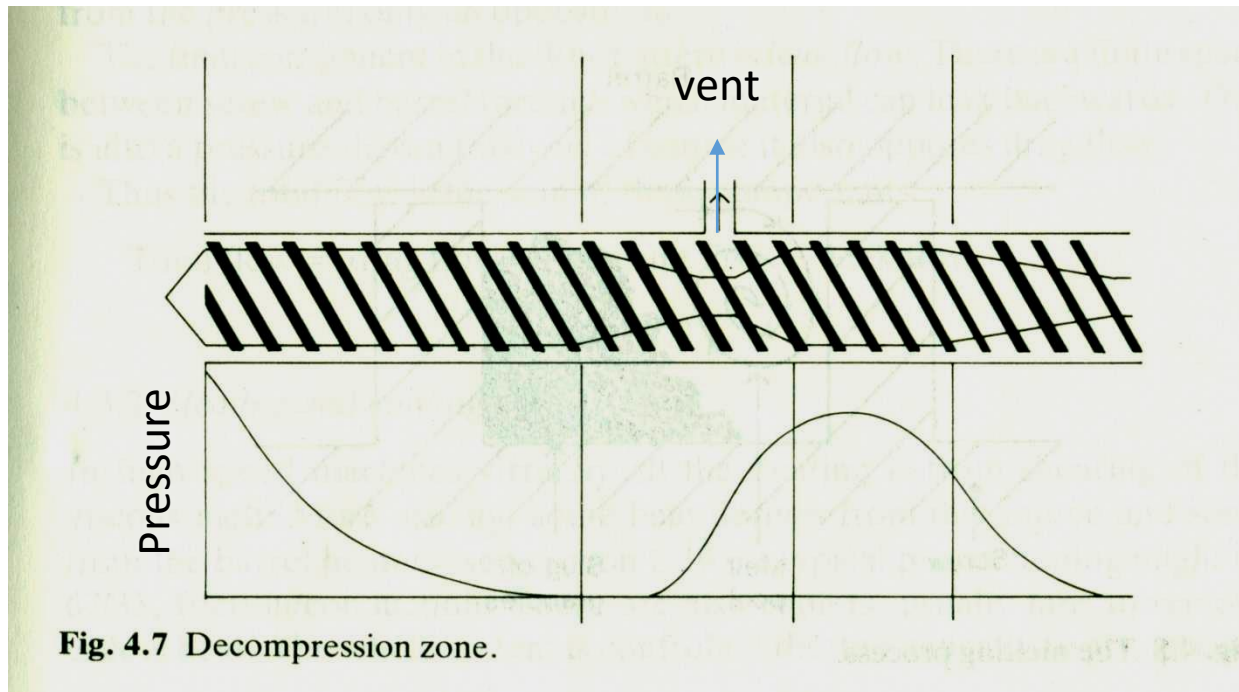


# • Specialty features

- The basic single screw extruder is quite a good dispersive mixer but is a poor distributive mixer.
- special zones having screw flights of changed or even reversed pitch : it achieves a good distribution.



- **Venting volatiles during extrusion:** The screw has a **decompression region**, followed by recompression and a further metering zone.





# Flow mechanisms

## 1) Melting

- As the polymer is conveyed along the screw, a thin film melts at the barrel wall.
- This is usually by means of conducted heat from the barrel heaters, but could be frictional.
- The molten polymer moves down the front face of the flight to the core and then sweeps up again to establish a **rotary motion in front of the leading edge of the flight**.

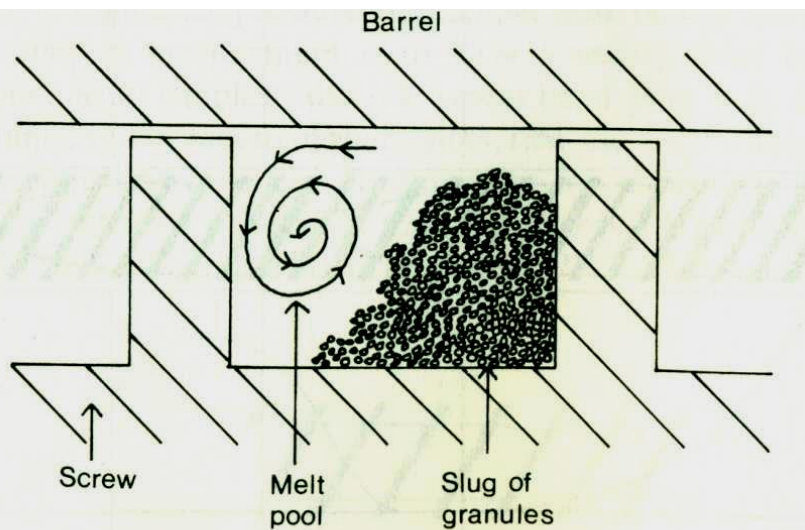
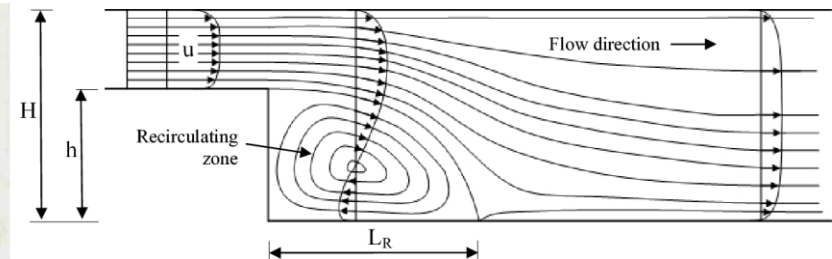


Fig. 4.8 The melting process.



## 2) Conveying (수지 이송)

- Two extreme cases : Poor dispersion and distribution
  - The material **sticks to the screw only and slips** on the barrel
    - The screw and material would simply rotate as a solid cylinder and **there would be no transport**.
  - The material **resists rotation in the barrel and slips** on the screw.
    - It will now tend to be **transported axially**.
- Drag flow
  - In practice, there is **friction with both screw and barrel**, and this leads to the **principal transport mechanism, drag flow**.
  - This is the equivalent to the **viscous drag** between stationary and moving plates separated by a viscous medium.

- Pressure flow
  - It is opposed by the pressure flow component, which is **caused by the pressure gradient** along the extruder
  - There is no actual flow resulting from the pressure.
- Leak flow
  - There is a **finite space between screw and barrel** through which material can **leak backwards (backflow)**.
  - This is also a pressure-driven flow and of course it also opposes drag flow.

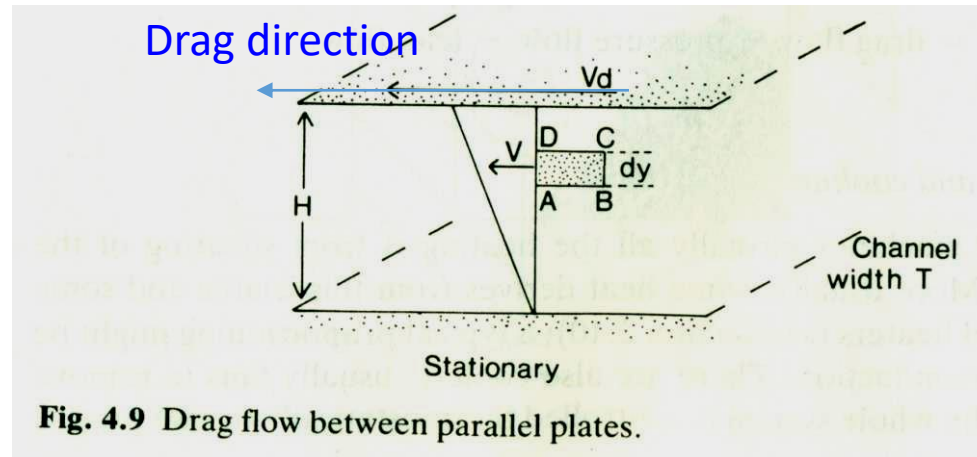
Total flow = Drag flow – Pressure flow – Leak flow

### 3) Heating and cooling

- More usually some heat derives from the **viscous heating** and some from the **barrel heater**.
  - A typical proportioning might be 67/33 , friction/conduction.
- There are also coolers, usually **fans to remove excess heat**. (cooling is not usual).
- Adiabatic ( $Q = 0$ ) and isothermal ( $T = \text{constant}$ )
  - The practical running condition may be regarded as lying between the extremes of adiabatic running, when **there would be only heat from viscous dissipation**, and isothermal running, when the **temperature at all points would be the same**, with **heat being supplied by heaters or removed by coolers to compensate for changes** in melt temperature.

# Analysis of flow

- Drag flow



- The volume flow rate for this element,  $dQ$

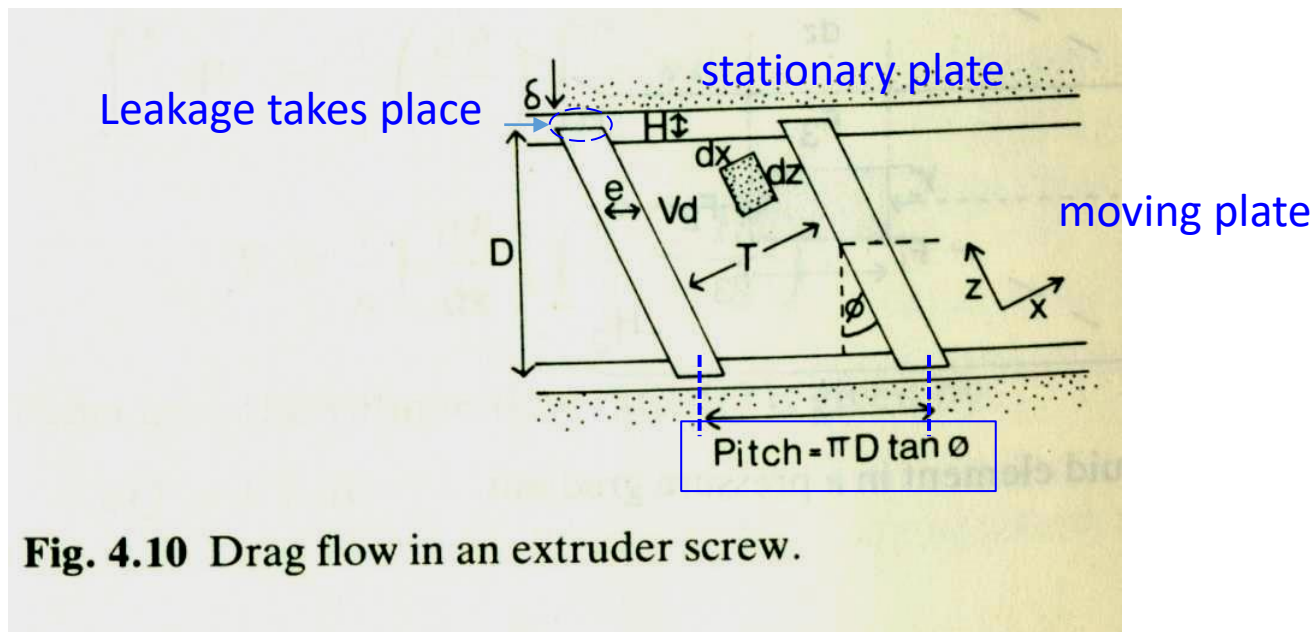
$$dQ = TVdy$$

- Assuming a linear velocity gradient,

$$V = \frac{V_d y}{H} \quad dQ = \frac{TV_d y dy}{H}$$

- Integrate the above equation over the channel depth,  $H$

$$Q_d = \int \frac{TV_d y dy}{H} = \underline{\underline{\frac{THV_d}{2}}}$$



- Application of the parallel plate to an extruder
  - The equivalent of the stationary plate is the barrel and of the moving plate is the rotating screw.

Drag velocity  $V_d = \pi D N \cos \phi$   $N$ : frequency of screw rotation (revolution/s)

Distance b/t screw  $T = \frac{(\pi D \tan \phi - e) \cos \phi}{\text{pitch}}$

Flow rate in drag flow  $Q_d = \frac{THV_d}{2} = \frac{(\pi D \tan \phi - e)(\pi D N \cos^2 \phi)H}{2} = \frac{\pi^2 D^2 N \sin \phi \cos \phi H}{2}$

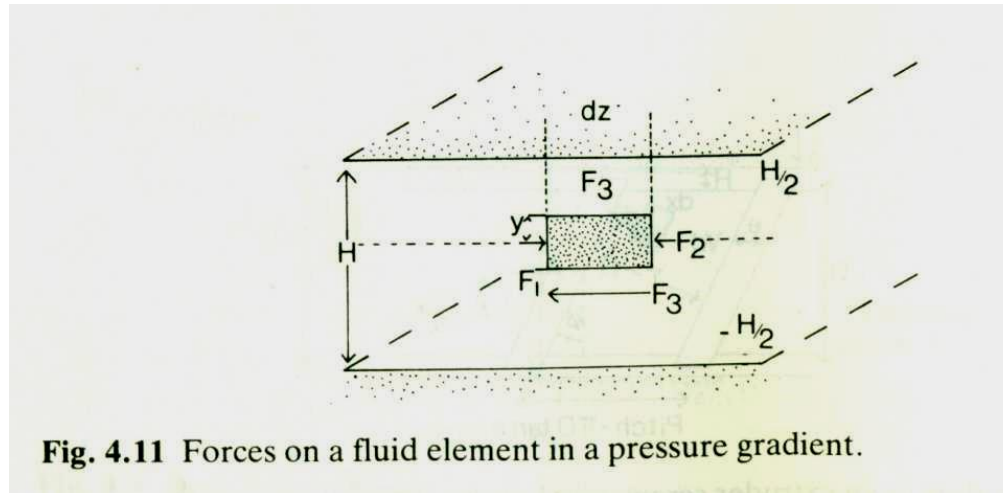
: Flow rate driven by drag flow in a extruder

→ function of  $D$ ,  $N$ ,  $H$ , angle



- Drag flow depends on
  - Screw diameter
  - Screw speed
  - Channel depth
  - Helix angle
- The helix angle is almost universally fixed at the square angle of  $17.66^\circ$ , i.e. one turn per diameter's length of screw.

- Pressure flow



- The forces acting on the fluid element are, for unit width

$$F_1 = \left( P + \frac{\partial P}{\partial z} dz \right) 2y$$

$$F_2 = P 2y \quad F_3 = \tau dz$$

- During steady flow, these are in equilibrium

$$F_1 = F_2 + 2F_3$$

- We reduce the following equation:

$$\tau = y \frac{\partial P}{\partial z}$$

- Assuming a Newtonian fluid,

$$\tau = \eta \dot{\gamma} = \eta \frac{dV}{dy}$$

- After combining the two equations,

$$\eta \frac{dV}{dy} = y \frac{dP}{dz} \qquad \frac{dV}{dy} = \frac{1}{\eta} \frac{dP}{dz} y$$

- Now, we can take the integration,

$$V = \int_0^V dV = \frac{1}{\eta} \left( \frac{dP}{dz} \right) \int_{H/2}^y y dy = \frac{1}{\eta} \left( \frac{dP}{dz} \right) \left( \frac{y^2}{2} - \frac{H^2}{8} \right)$$

$$dQ = VTdy = \frac{1}{\eta} \left( \frac{dP}{dz} \right) \left( \frac{y^2}{2} - \frac{H^2}{8} \right) T dy$$

$$Q_p = VT2y = 2 \int_0^{H/2} \frac{1}{\eta} \left( \frac{dP}{dz} \right) \left( \frac{y^2}{2} - \frac{H^2}{8} \right) T dy = \left( \frac{1}{12\eta} \right) \left( \frac{dP}{dz} \right) TH^3$$

- When applying this expression to an extruder screw channel,

$$T = \pi D \tan \phi \cos \phi$$

$$\sin \phi = \frac{dl}{dz}$$

- Then,  $\frac{dP}{dz} = \left( \frac{dP}{dl} \right) \sin \phi$

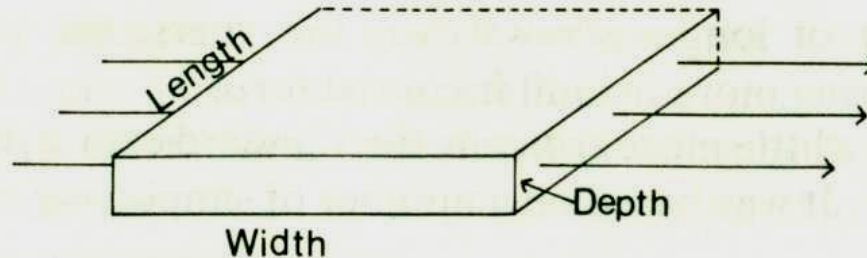
$$Q_p = \left( \frac{\pi D H^3 \sin^2 \phi}{12\eta} \right) \left( \frac{dP}{dl} \right) \leftarrow \sim P/l \text{ for linear change}$$

: Flow rate driven by pressure in a extruder

→ function of  $H$ ,  $D$ , viscosity, and pressure gradient  $dP/dl$

# • Leak flow

- Leak flow is **another pressure driven flow component**.
- The geometry is that of a wide slit;
  - $H = \delta$ , the depth of the slit
  - $T = \pi D / \cos \phi$ , the width of the slit
- Leak flow is **small compared with drag flow and pressure flow and may be neglected in finding total flow**.
- It only has **practical significance in badly worn machines** where the clearance between screw and barrel becomes large.



**Fig. 4.12** Leak flow through a wide slit.

- Total flow

$$Q = Q_d - Q_p = \frac{\pi^2 D^2 N H \sin \phi \cos \phi}{2} - \left( \frac{\pi D H^3 \sin^2 \phi P}{12 \eta l} \right)$$

- For practical purpose,

$$Q = \alpha N - \left( \frac{\beta P}{\eta} \right)$$

- The practical variables
  - Screw speed  $N$
  - Head pressure  $P$
  - Melt viscosity  $\eta$
  - Screw design  $\alpha, \beta = f(\phi, D, H)$



# • Influence of polymer properties

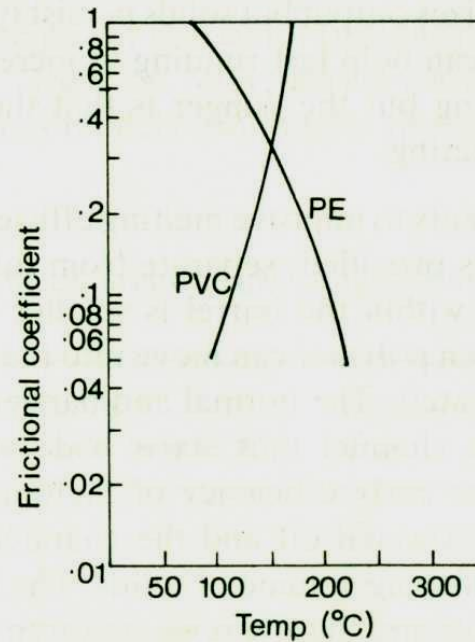
- The two important factors missing are (a) the **non-Newtonian rheology** of most polymer melts and (b) **their frictional properties**.
- The frictional drag at the barrel prevents the melt from simply rotating with the screw.
- In fact, the polymeric material must **slide on the surfaces and the sliding characteristics** are described by the relevant **coefficients of friction**.

**Table 4.1** Coefficients of friction, various countersurfaces

<i>Polymer</i>	<i>Coefficient of friction (<math>\lambda</math>)</i>
PTFE	0.04–0.15
LDPE	0.30–0.80
HDPE	0.08–0.20
PP	0.67
PS	0.33–0.50
PMMA	0.25–0.50
Nylon	0.15–0.40
PVC	0.20–0.90
SBR	0.50–3.0
NR	0.50–3.0

After Hall [4].

High friction ? → good drag flow (prevent simply rotating with the screw)



**Fig. 4.13** Comparison of frictional properties of polyethylene and PVC (after Jacobi).

- PVC is a polymer notorious for **thermal instability**.
  - Thus, it is a difficult polymer to run in a single screw extruder, is more often extruded in twin screw machine.
- This is the reason twin screw extruder is used for many polymer melts.

# Some aspects of screw design

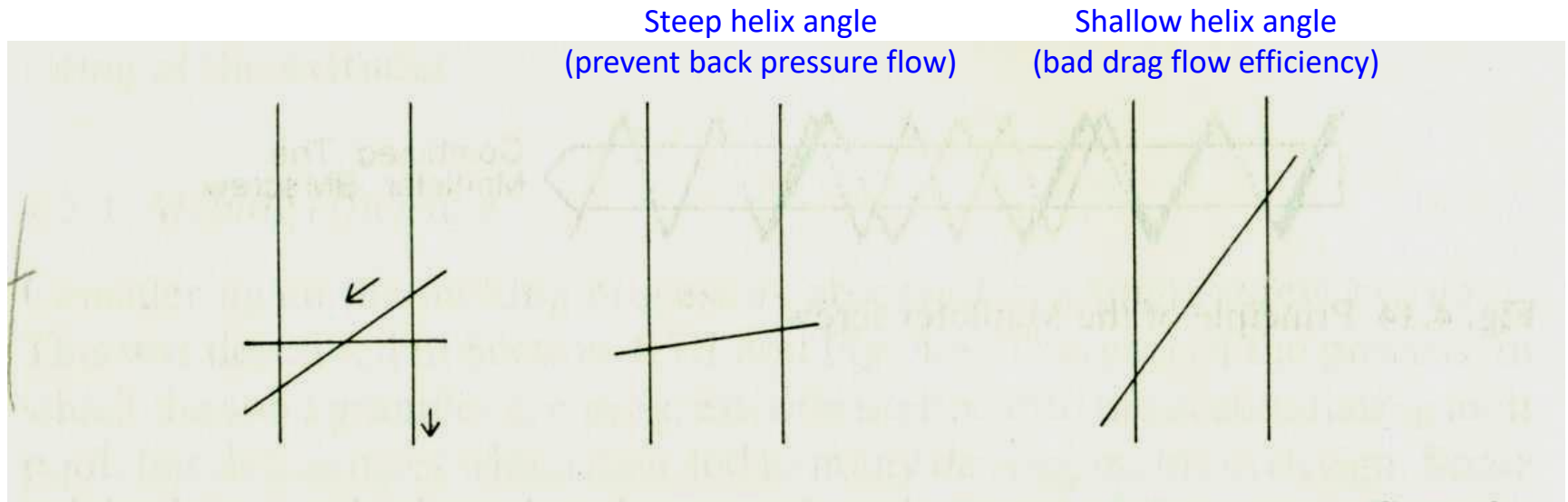
- Two important aspects
  - The **efficiency of melting** and **the output rating** of the extruder

- Melting efficiency

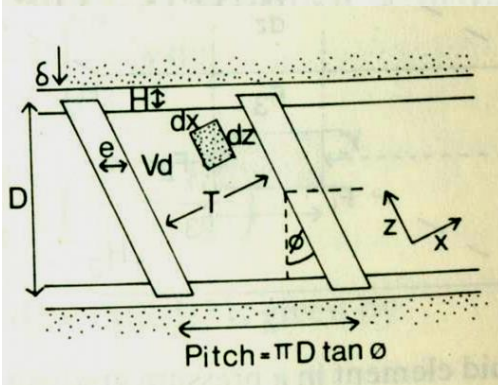
- Some variations in screw characteristics
  - Deeper channel
    - Conveys more material but takes longer to complete melting
  - Fast running
    - Maximizes output but solids persist further along the screw
  - Shallower channel
    - **Can help fast running to increase output** because of more efficient melting but the danger is that the **resultant high shear might lead to overheating**.

# • Optimum helix angle

- The competing requirements are a **steep angle to resist back pressure flow** and a **shallow angle to provide the least tortuous path for drag flow**.



**Fig. 4.15** Steep vs. shallow helix angle: the steep angle resists back pressure flow; the shallow angle provides least tortuous drag flow path.



Remember this angle  $\phi$  direction:

- Perpendicular to barrel :  $\phi = 0 \rightarrow$  blocked
- Parallel to barrel :  $\phi = 90 \rightarrow$  No head pressure

- The **volumetric efficiency**, at least of drag flow, **depends only on  $\phi$** .
- The 'ideal' axial velocity ( = velocity along the barrel direction)

$$V_a = \text{screw pitch} \times \text{screw speed} = \pi D \tan \phi \times N$$

- The velocity component parallel to the screw flight (screw 나사선 방향)

$$V_d = \frac{V_a}{\sin \phi} = \frac{\pi D N \tan \phi}{\sin \phi}$$

- The 'ideal' output (flow rate):  $Q_i = V_d \times \text{crosssection of channel}$

$$Q_i = \frac{\pi D N \tan \phi}{\sin \phi} (\pi D H \tan \phi) \cos \phi = \pi^2 D^2 H N \tan \phi$$

Maximum flow rate by drag flow we learned!

$$\therefore \text{Volumetric efficiency} = \frac{Q_{max}}{Q_i} = \frac{(\frac{1}{2})\pi^2 D^2 N \sin \phi \cos \phi H}{\pi^2 D^2 H N \tan \phi} = \frac{1}{2} \cos^2 \phi$$

e.g. Angle of  $17.66^\circ$  gives an efficiency of 45.4%.

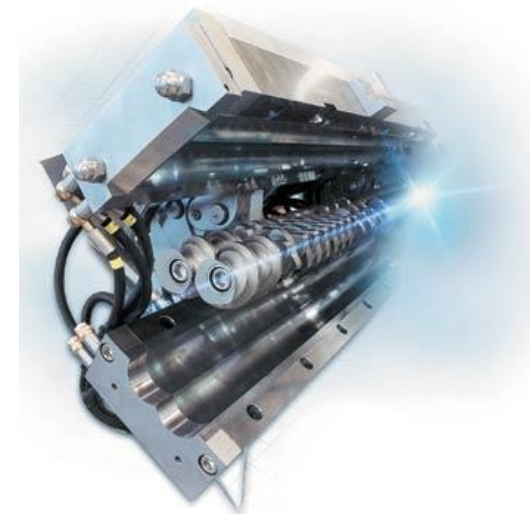
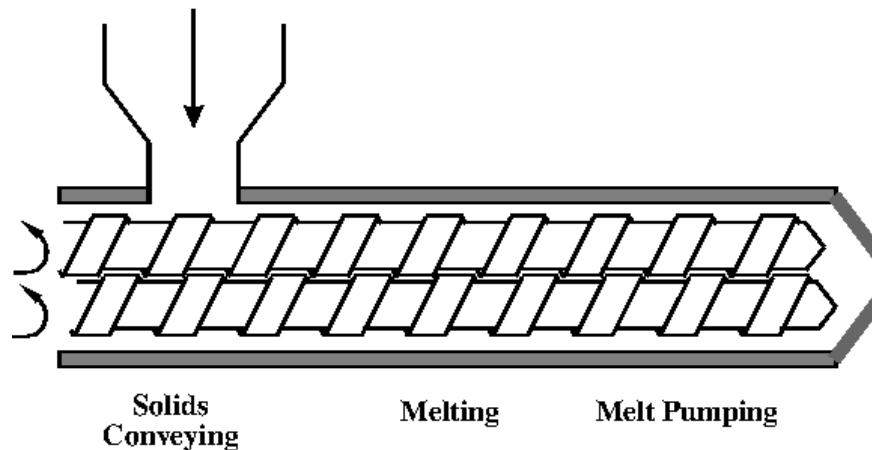
Angle of  $10^\circ$  gives rises to only 48.5%

→ Helix angle shouldn't be too steep!

→ Universally accepted value =  $17.66^\circ$

# Twin screw extruder

- PVC
  - Heat sensitive polymer
  - One of the applications is extrusion of window frames and associated products, e.g. frames for patio doors, main house doors, etc., in unplasticized or rigid PVC.





- Melt conveying in twin-screw extruders
  - Twin-screw extruders act as positive displacement pumps with **little dependence on friction**, and this is the main reason for their **choice for heat sensitive materials**.
- Categories of twin-screw extruders
  - The first division depending on the rotating direction
    - Co-rotating
    - Counter-rotating
  - The second division depending on whether the two screws mesh with each other or not
    - Meshing
    - Non-meshing
      - Double screws

# Extruder and die characteristics

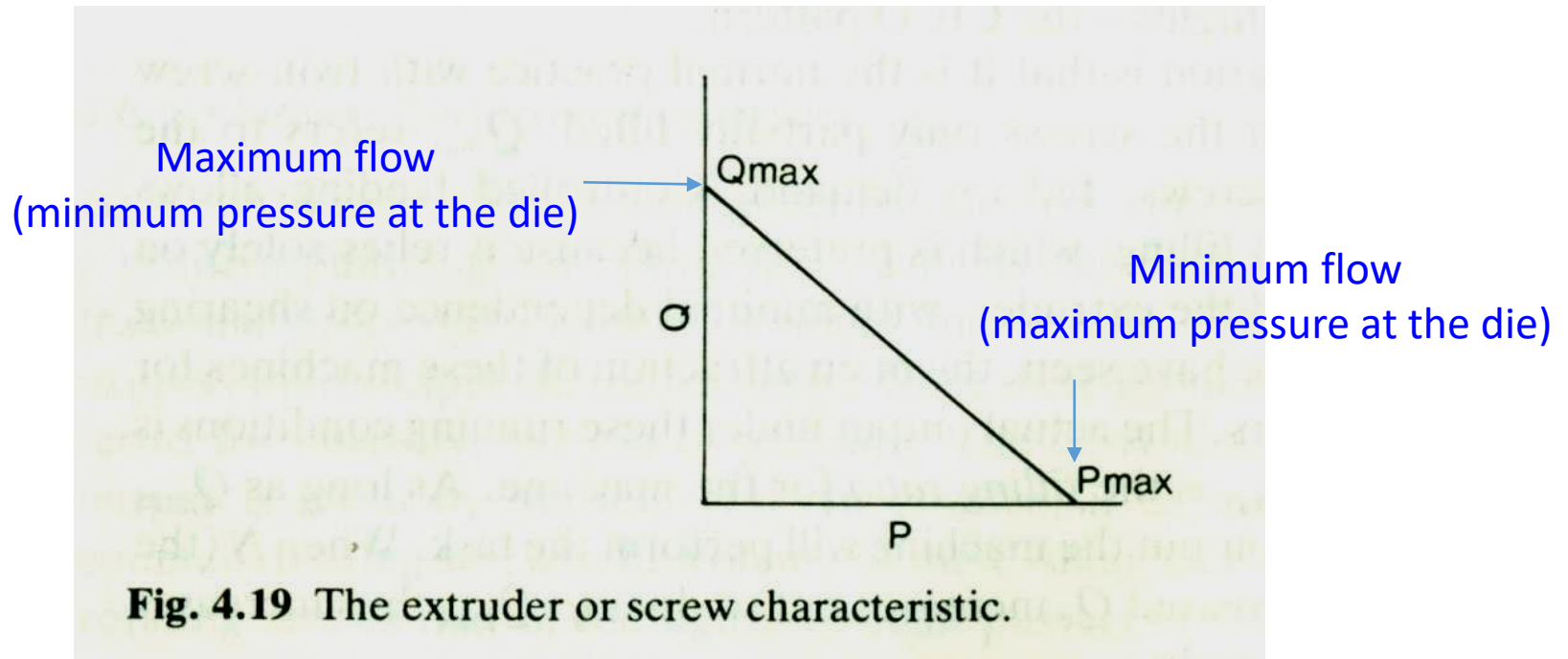
- The interaction of the extruder and its die can be understood by looking at their respective characteristics.
- If there were to be no pressure build-up, for example, no breaker plate or die, the output would be at its maximum.
  - We can use the drag flow ideal equation.

$$Q = Q_{\max} = \frac{\pi^2 D^2 N H \sin \phi \cos \phi}{2}$$

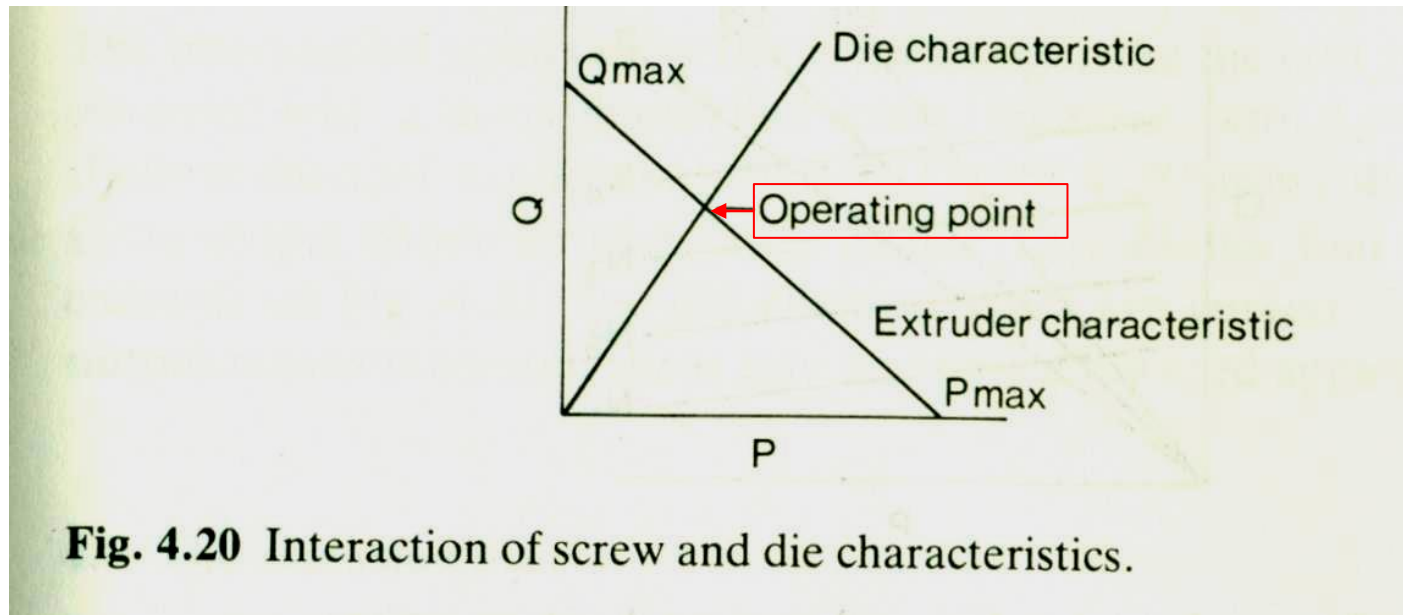
- If there is maximum resistance,  $Q = 0$  (Plugged case).

$$\frac{\pi^2 D^2 N H \sin \phi \cos \phi}{2} = \left( \frac{\pi D H^3 \sin^2 \phi P}{12 \eta l} \right)$$

$$P_{\max} = \frac{6 \pi D l N \eta}{H^2 \tan \phi}$$



- A die at the extruder outlet requires head pressure to function; the pressure is needed simply to force the melt through the die.
- The maximum output will result from minimum pressure.



**Fig. 4.20** Interaction of screw and die characteristics.

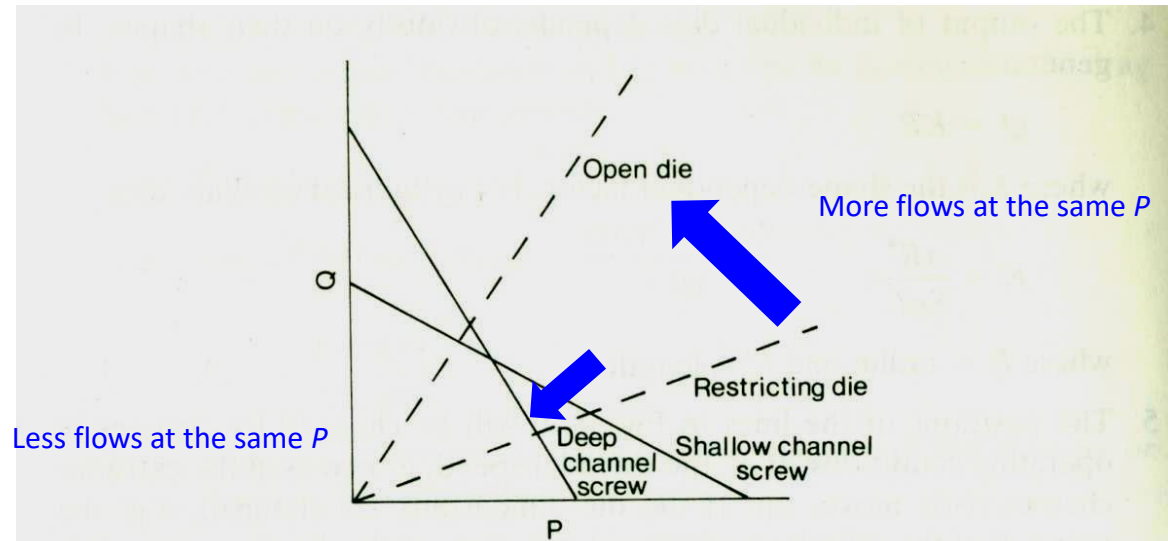
$$Q = KP \quad \text{Flow rate depends on die shape}$$

K is the shape-dependent factor. For cylindrical capillary dies,

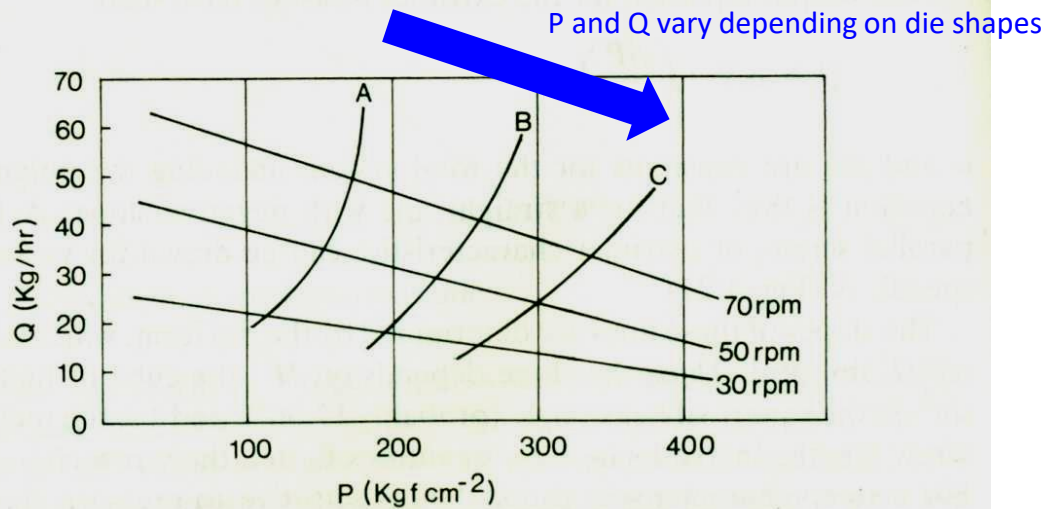
$$K = \frac{\pi R^4}{8\eta L}$$

- The output equation for the extruder is

$$Q = \alpha N - \left( \frac{\beta P}{\eta} \right)$$



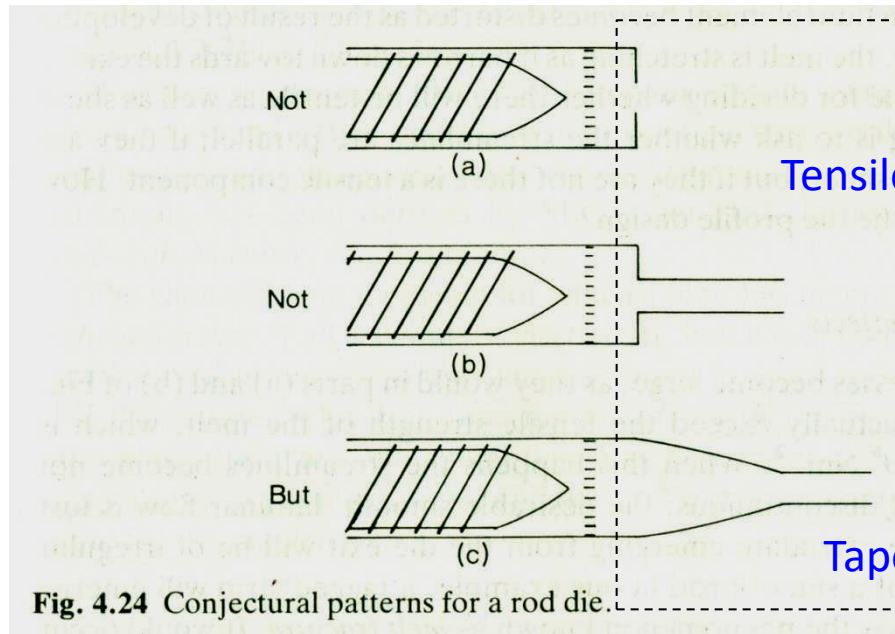
**Fig. 4.22** Different matches of screw and die characteristics.



**Fig. 4.23** Output characteristics for a 60 mm extruder (60 mm extruder, short compression screw, polyethylene, MFI 0.5, three different die characteristics).

# The extrusion die

- Basic flow patterns



Tensile stresses are high

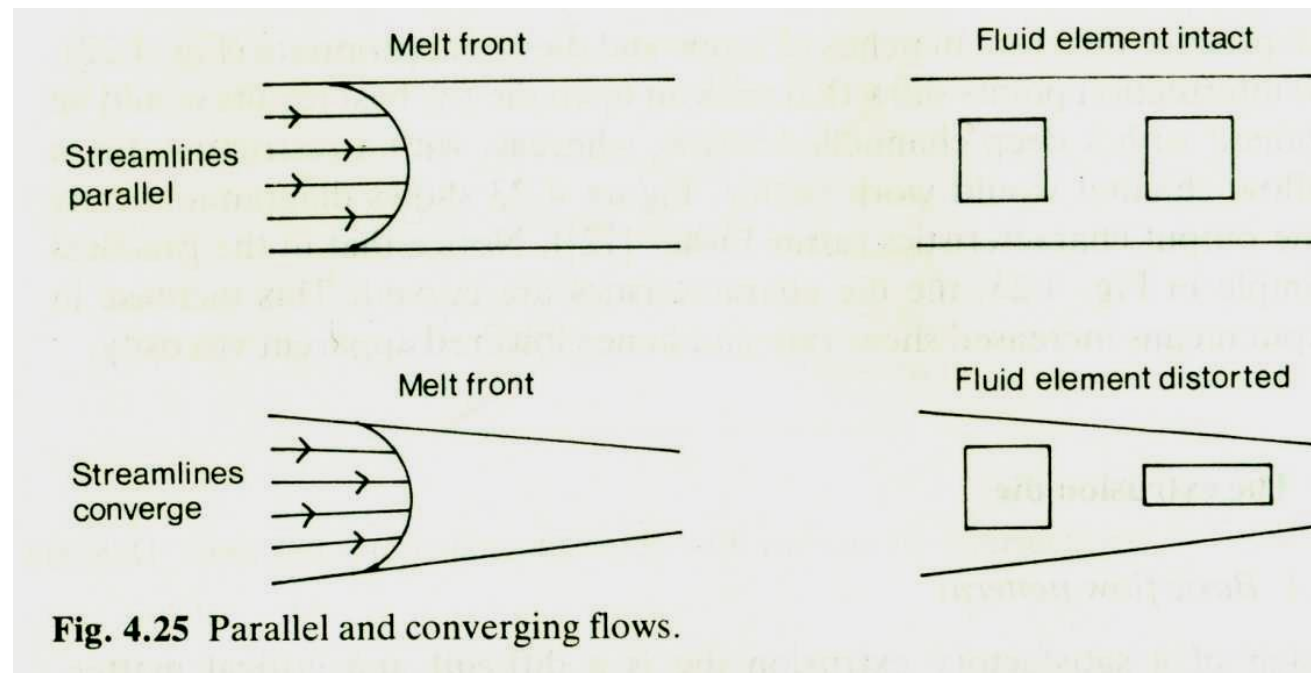
Tapered : tensile stress is low

- One needs to maintain for laminar flow in the melt.
- We have to prevent the occurrence of the dead spots where the melt circulates like a backwater and this leads to an extrudate with uneven heat and shear history.

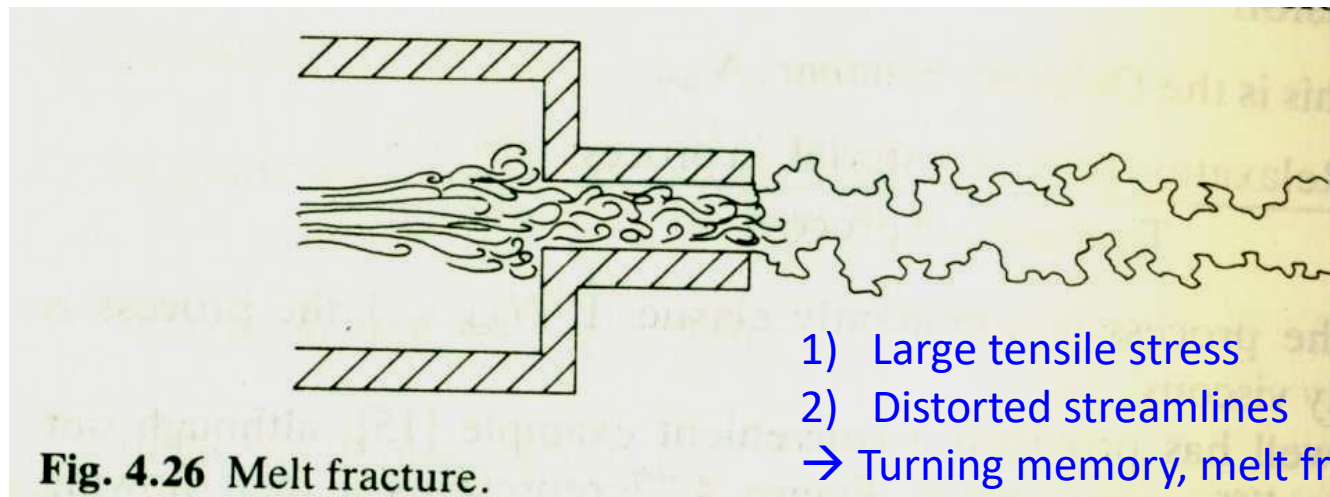
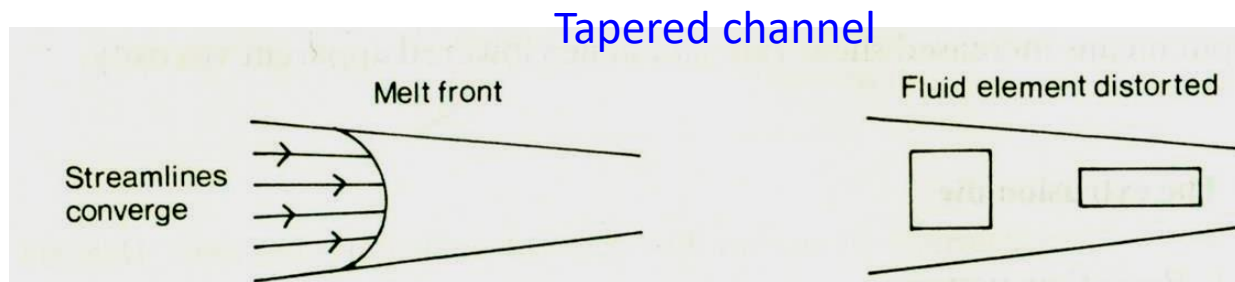


- Die entry effects

- If the tensile stresses become large (e.g. Fig. 4.24 (a) and (b)), they can actually exceed the tensile strength of the melt ( $\sim 10^6$  Pa).
- As a result, the streamlines become not only chaotic but discontinuous.



- The die entrance is **tapered**.
  - Eliminate the dead spots in the corners, hence maintaining a steady heat and shear history.
  - Minimize the development of tensile stresses, and hence **minimize distortion of the streamlines**
  - Extend the process time which helps to eliminate memory of earlier processing, e.g. the screw turning memory.



- Viscoelasticity
  - Old testament (Judge V): The song of [Deborah](#) and Barak  
“The mountains melted from before the Load”
  - Everything flows if you wait long enough!



- Deborah number, De
  - The ratio of a characteristic relaxation time of a material ( $\tau$ ) to a characteristic time of the process (T)
  - The relaxation time : its viscous and elastic responses to an applied stress.

$$\text{Relaxation time } (\lambda) = \frac{\text{viscosity}}{\text{elastic modulus}} = \frac{Pa \cdot s}{Pa} = s$$

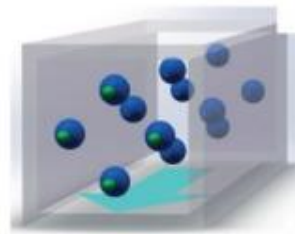
Higher Polymer concentration  $\rightarrow$  higher chain entanglement (resistance to motion)  
 $\rightarrow$  higher  $\lambda \rightarrow$  elastic response of the fluid

$$De = \frac{\text{Relaxation time of material, in process}}{\text{Timescale of process}}$$

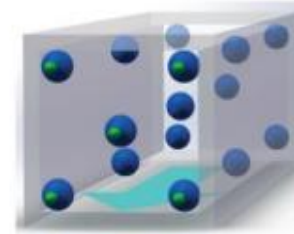
- If  $De \gg 1$ , the process is dominantly elastic.
- If  $De \sim 0$ , the process is dominantly viscous.

- At high  $De$  ( $Wi$ ) number

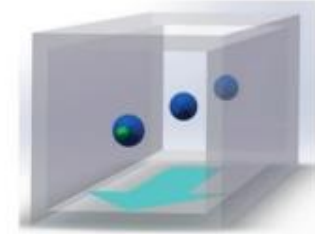
: particle focusing induced by normal forces of viscoelastic fluids under high  $De$  ( $Wi$ ) number



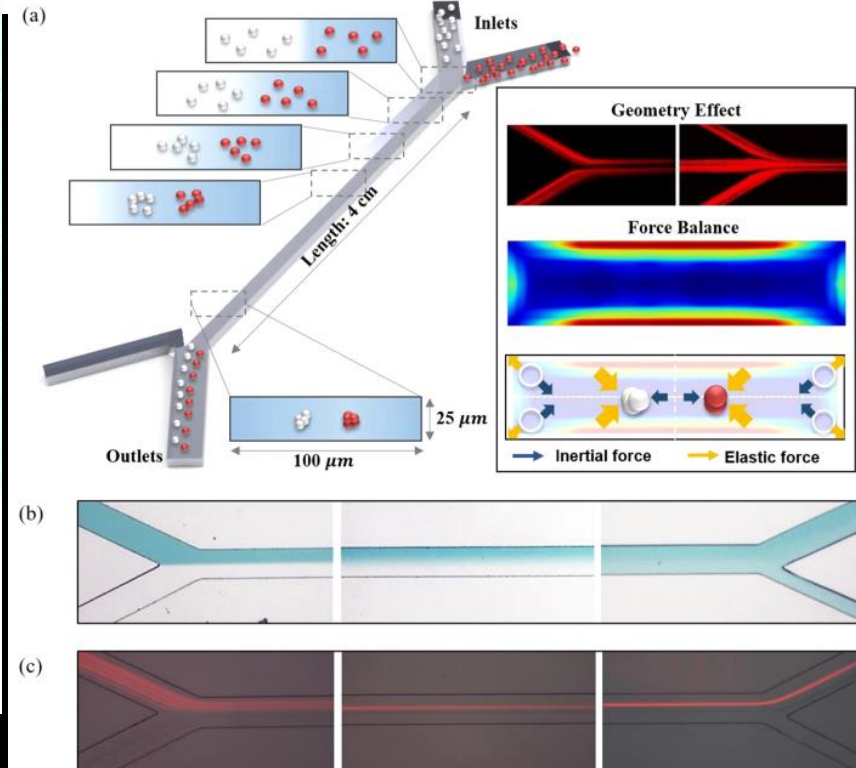
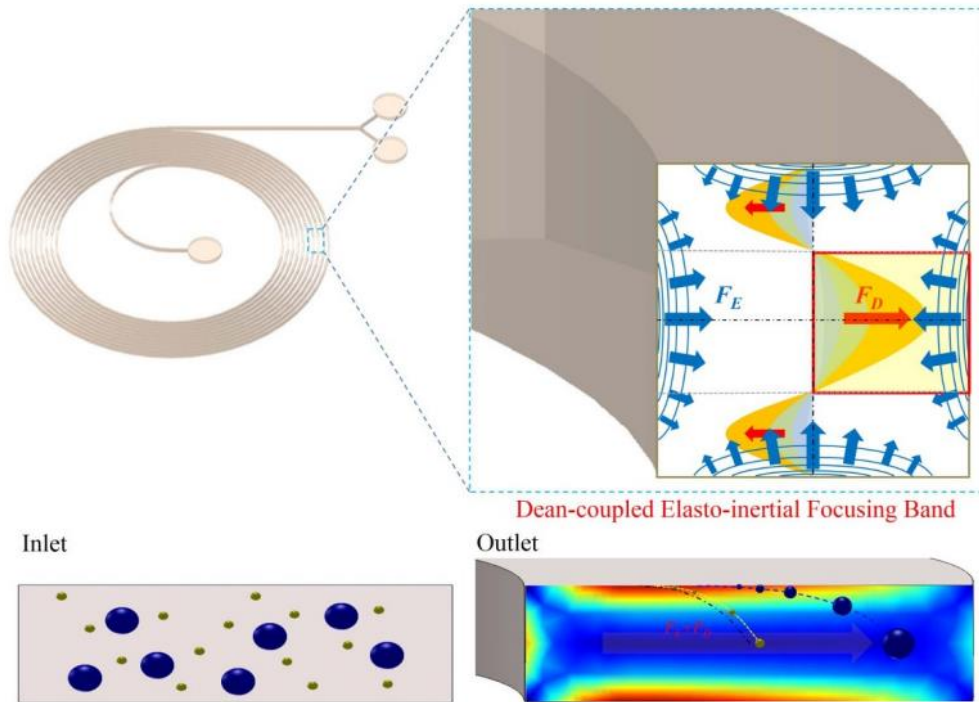
$Re > 0, Wi \approx 0$



$Re \approx 0, Wi > 0$

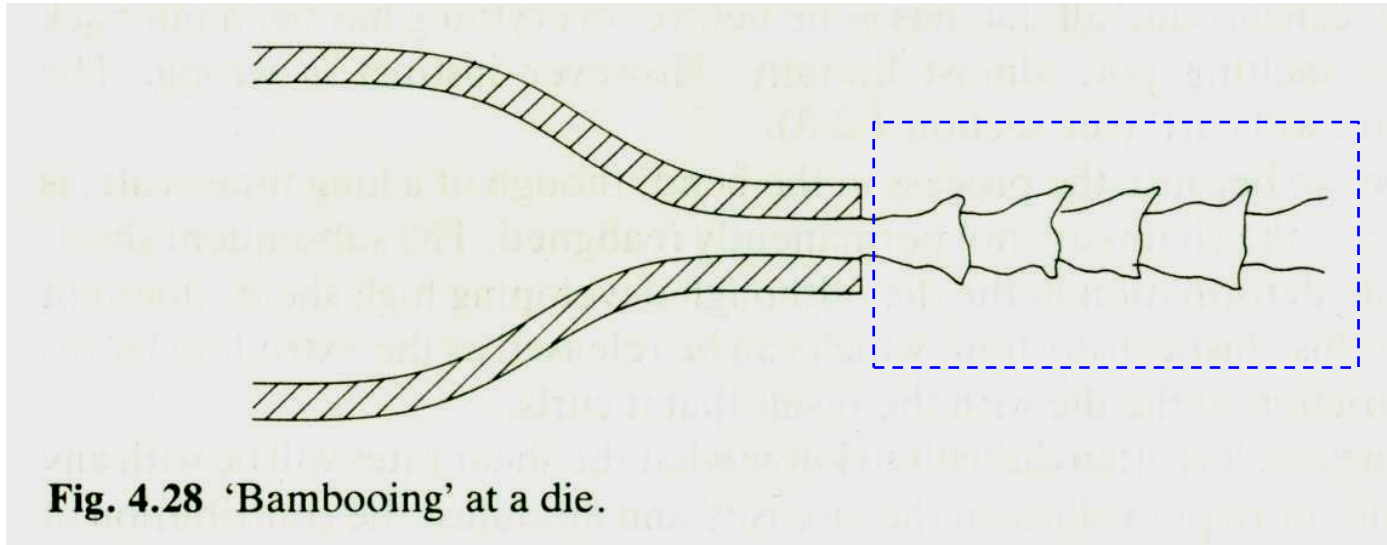


$Re > 0, Wi > 0$





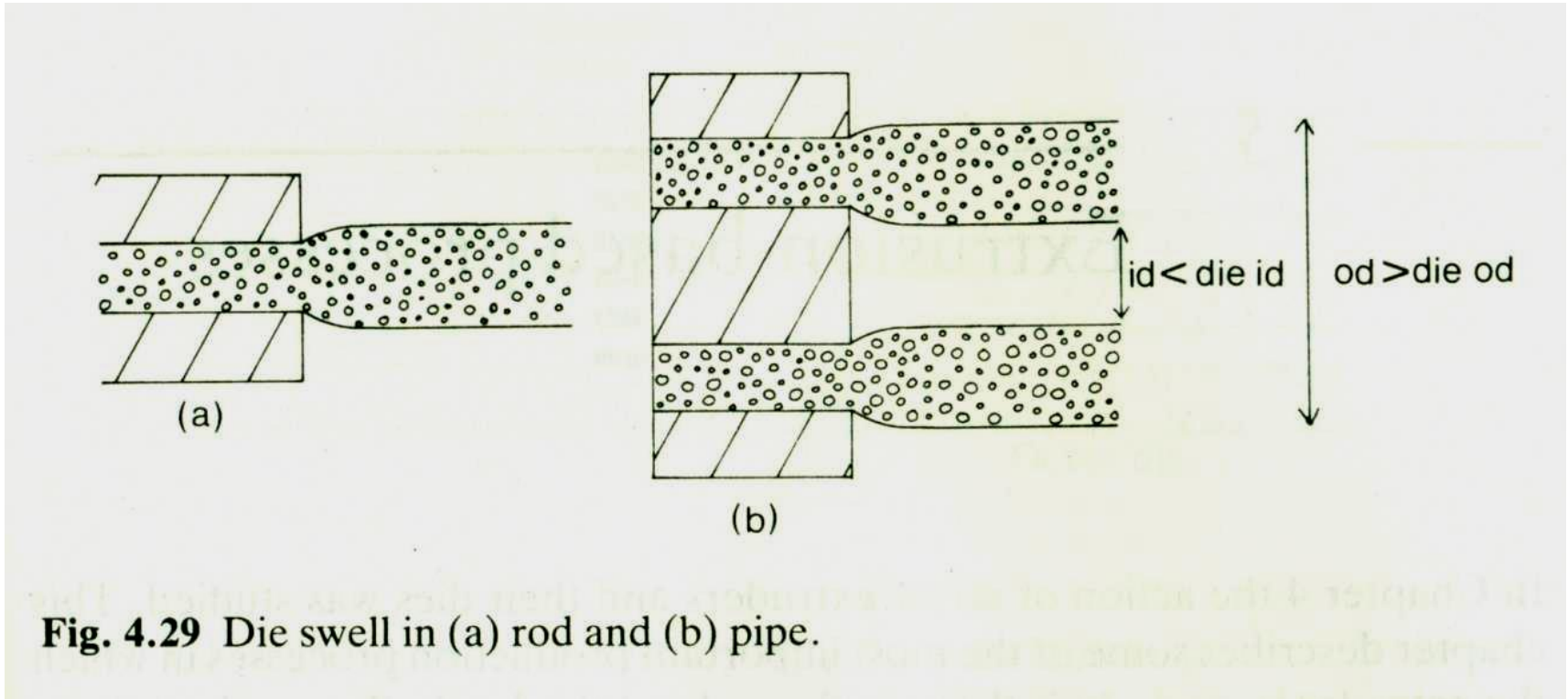
- Die exit **instabilities**
  - Shark skin → orange peel → bambooning at a die



- **Structured, highly filled, low elasticity materials** most easily show shark skin.
  - When the material leaves the die lip, the material at the wall has to **accelerate to the velocity** at which the extrudate is leaving the die.
  - This generates **tensile stress**, and, if the stress exceeds the tensile strength, the **surface ruptures causing the visual defect**.

- Die swell

- The die swell results from recovery of the elastic deformation as the extrudate leaves the constraint of the die channel and before it freezes.



Question ) Does die shrink exist? Why and under what condition?

→ Hint) Find out MWCNT nanocomposites