**Series -** a sum of a list (*usually* never ending) of never-ending terms written as  $\sum_{n=i}^k a_n$ 

- Infinite Series A series that is a sum of an infinite sequence of terms (there is no final term)
- Divergent Series An infinite series that doesn't have a finite limit (every term, the sum always increases)
- Infinite Divergent Series A series of infinite terms that doesn't have a final limit
  - Harmonic Series an example of divergent infinite series  $\sum_{n=1}^{\infty} \frac{1}{n} = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} + \cdots$
- Example Power Series  $\sum_{n=0}^{\infty} C_n X^n$ 
  - We can represent the power series with a function of x,  $f(x) = c_0 + c_1x + c_2x^2 + ...$

## Taylor Series - A series that estimates what a function looks like

- A power series that tells us what a function looks like when centered at some point a
- A Taylor series is saying that we can approximate a function f(x) at x = a, with some Taylor series t(x) at x = a, where t(x) is a series (a sum of terms) of polynomials that approximate f(x) at x = a
  - Taylor Series is for using polynomial functions to approximate non-polynomial functions
    - Polynomials tend to be easier to compute, differentiate, etc.
- Maclaurin Series a special kind of Taylor series, where we look at a function centered at 0, i.e. a = 0