Chapter 16 - Message Passing

Message-Passing Algorithm - an algorithm performed on a network/graph, where information is passed locally among nodes, **iteratively**, using **simple operations**, to eventually **solve a global problem**

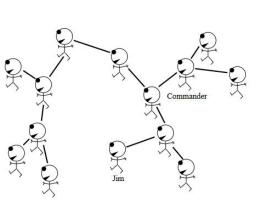
16.1 Counting

Naive approaches are expensive

$$Q \xrightarrow{1} Q \xrightarrow{2} Q \xrightarrow{3} Q \xrightarrow{4} Q$$

Line Graph

- You need soldiers to shout their name to the commander and the commander must be able to hear all of them and add up all of the numbers
- Message Passing each soldier adds 1 to the number whispered from behind or from in front, then pass it in the same direction, and the commander adds the front and back numbers together and adds 1
- The above doesn't work in a graph with a cycle, as you can't split the total two 3 numbers that can be computed separately



- 1. Count your number of neighbours, N.
- 2. Keep count of the number of messages you have received from your neighbours, m, and of the values v_1, v_2, \ldots, v_N of each of those messages. Let V be the running total of the messages you have received.
- 3. If the number of messages you have received, m, is equal to N-1, then identify the neighbour who has not sent you a message and tell them the number V+1.
- 4. If the number of messages you have received is equal to N, then:
 - (a) the number V+1 is the required total.
 - (b) for each neighbour n { say to neighbour n the number $V+1-v_n$. }

- Tree
- We can modify our line graph solution to work for a tree