

**Moment** - Averages of the dataset, of different orders and centred at different points

- Moments are represented by the letter  **$\mu$**
- **$\mu_1$  First Moment** - The average of your samples (*average linear distance from 0*)
- **$\mu_2$  Second (Crude/Raw) Moment** - Squared average (*average squared distance from 0*)
  - Differentiates between datasets with different spreads but the same first moment
    - High numbers inflate the second moment more than low numbers deflate
      - A dataset with the same average but **higher spread** will have a **larger crude** moment
- **$\mu_2$  Second (Centred) Moment** - A squared average distance from the linear average
  - This means we have shifted the dataset so that **the first moment is 0**
  - This is also known as the **variance** (*average squared distance from average*)
  - The square root of this is the **standard deviation** (*average distance from average value*)
- **Crude/raw moments** - Centered at first distance = 0
  - have a ` to indicate they are crude, whereas centred moments don't
  - Crude moments take distances from 0
- **Crude/raw moments** - Centered from **first moment**  $\mu_1$ 
  - don't have a `
- **Higher Order Moments** - moments that are third or higher
- **Standardised moments** - moments that are adjusted for **first and second moment**
  - We can think of it as **normalised**
  - We **don't have to adjust for the third moment often**, because it's not included in the calculation of kurtosis (4th moment) or higher order moments
- **Adjusting moments for sampling** - when we take samples, and we apply the formulas for moments, we have to **adjust the formulas for the lower degree of freedom** as a result of taking a sample, not the whole population

## Sampling adjustments

1 
$$\frac{\sum x}{n}$$

2 
$$\frac{\sum (x - \mu)^2}{n} \longrightarrow \frac{\sum (x - \bar{x})^2}{n - 1}$$

3 
$$\frac{1}{n} \frac{\sum (x - \mu)^3}{\sigma^3} \longrightarrow \frac{n}{(n - 1)(n - 2)} \frac{\sum (x - \bar{x})^3}{s^3}$$

4 
$$\frac{1}{n} \frac{\sum (x - \mu)^4}{\sigma^4} \longrightarrow \frac{n(n + 1)}{(n - 1)(n - 2)(n - 3)} \frac{\sum (x - \bar{x})^4}{s^4} - \frac{3(n - 1)^2}{(n - 2)(n - 3)}$$