Unit 1 : Self assessment-1 Success 1.
Which one of the following is a proposition?
How are you? What time is it?
C 4+x=5
2.
What is the negation of the statement "Salman sent more than 100 text messages every day"?
Salman sent more than 200 text messages every day.
Sairtiait seric less thair 100 text messages but not every day.
Salman did not send more than 100 text messages every day. Salman did not send any text message every day.
3.
The negation of the proposition "Michael's PC runs Linux" is
"Michael's PC does run Linux."
"Michael's PC only run Linux."
"Michael's PC does not run Linux."
"It is not the case Michael's PC does not run Linux." 4.
What is the negation of the statement "Sam is rich and happy"?
Sam is poor and unhappy.
Either Sam is poor or happy
Either Sam is poor or unhappy
Sam is not rich and happy. 5.
What will be Truth values of the statement (p \land q) \rightarrow (p \lor q) for the Truth values T,T,F,F of p and T,F,T,F of q?
O _{T, F,T,F}
C F, T,F,T
▼ T, T,T,T
F,F,F,F
o.
If: "You can use the wireless network in the airport,": "You pay the daily fee," and: "You are a subscriber to the service". Which is the right expression for the statement "To use the wireless network in the airport you must pay the daily fee unless you are a subscriber to the service".
O q Ar + p

 q v r → p p Λ (q v r) p Λ (q Λ r) 7.
Let Q(x, y) denote the statement "y is the capital of x." What are these truth values? i) Q(Punjab, Chandigarh), ii) Q(India, New Delhi) iii) Q(Rajasthan, Shimla), iv) Q(Nepal, Kathmandu)
 □ T,F,T,F □ T,T,F,F □ T,T,F,T □ T,T,T,T 8.
$(p \rightarrow q) \wedge (p \rightarrow r)$ is logically equivalent to
Let p and q be the propositions, p: It is below freezing, q: It is
Det p une q se the propositions, p It is selow freezing, q . It is
snowing. Write the proposition using p and q and logical connectives
snowing.Write the proposition using p and q and logical connectives
snowing. Write the proposition using p and q and logical connectives (including negations). "It is below freezing and snowing". $\begin{array}{cccccccccccccccccccccccccccccccccccc$
snowing. Write the proposition using p and q and logical connectives (including negations). "It is below freezing and snowing". $\begin{array}{cccccccccccccccccccccccccccccccccccc$
snowing.Write the proposition using p and q and logical connectives (including negations). "It is below freezing and snowing". $\begin{array}{ccccccccccccccccccccccccccccccccccc$

P V Q ∧¬R 11.
$ eg p \leftrightarrow q$ is logically equivalent to
Which one of the following is true for Biconditional statement $p \leftrightarrow q$
$p \leftrightarrow q$ is true when p is true and q is false $p \leftrightarrow q$ is true when p is false but q is true $p \leftrightarrow q$ is true when p is true and q is true $p \leftrightarrow q$ is false when p is false and q is false $p \leftrightarrow q$ is false when p is false and q is false
Which of the following statements is not correct for the biconditional
statement $p \leftrightarrow q$?
It is true when both p and q are true It is true when both p and q are false It is false when p is false and q is true It is true when p is false and q is true 14.
Which of the following statements is not correct for the biconditional
statement $p \leftrightarrow q$?
It is true when both p and q are true It is true when both p and q are false It is false when p is false and q is true It is true when p is false and q is true
The bi-conditional statement is represented by

$p \rightarrow q$
$p \equiv q$
None
Unit 2 : Self assessment-2
Success 1.
If $P(x)$ is "if $x<0$, then $x^2>x$ " and the domain consists of all real numbers then the truth value of $P(2)$ is:
If P(x) is if x<0, then x->x and the domain consists of all real numbers then the truth value of P(z) is.
• True
C False
It can be both True and False
question is not well defined.
2.
Which one of the following is the most appropriate logical formula to represent the statement? "Students who know Mathematical, coding skills are placed". The following notations are used: $M(x)$: x is knowing the Mathematical skills, $P(x)$: x is knowing the Coding skills, $P(x)$: x is placed
$\bullet \qquad \forall x((M(x) \lor C(x)) \rightarrow P(x))$
3.
Which of the following is correct?
\bigcirc $\neg \exists x P(x) \equiv \exists x \neg P(x)$
$\bigcirc \neg \forall x(x^2 > x) \equiv \forall x(x^2 \leq x)$
¬∃x(x^2=2)≡∀x(x^2≠2)
4.
According to proof by contraposition, which of the following is correct?
$\bigcirc p \rightarrow q \equiv q \rightarrow p$
 p + q = p / q p + q = ¬q + ¬p
$\bigcirc p + q \equiv \neg p + \neg q$
5.
Converse of the conditional statement p→q is
• q→p
$\bigcap_{\neg q \rightarrow \neg p}$
C ¬q→p

Identify the correct one that compound propositions p and q are logically equivalent if $P \mapsto Q$ is contradiction $P \mapsto Q$ is contingency $P \mapsto Q$ is contingency $P \mapsto Q$ is a tautology $P \mapsto Q$ is a tautology

This is a possible proposition of the following is correct? $P \mapsto Q$ is a tautology $P \mapsto Q$ is a tautolog

Find the equivalent statement of $\exists x \ P(x) \ \{Existential \ quantification\},$ where Domain $D = \{x1, x2, x3, ..., xn\}$

 $\begin{array}{c} & P(x1) \land P(x2) \land P(x3) \land \dots \land P(xn) \\ \hline \bullet & P(x1) \lor P(x2) \lor P(x3) \lor \dots \lor P(xn) \\ \hline \bullet & P(x1) \to P(x2) \to P(x3) \to \dots \to P(xn) \\ \hline & P(x1) \to P(x2) \to P(x3) \to \dots \to P(xn) \\ \hline \end{array}$

Which of the following is correct?

$$\neg \exists x P(x) \equiv \exists x \neg P(x)$$

$$\neg \forall x p(x) \equiv \forall x \neg P(x)$$

$$\neg \forall x (x^2 > x) \equiv \forall x (x^2 \le x)$$

$$\neg \exists x (x^2 = 2) \equiv \forall x (x^2 \ne 2)$$
10.

 $\neg \exists x(x^2=2) \equiv \forall x(x^2\neq 2)$

Suppose that the domain of propositional functions Q(x) is $D = \{0, 1, 2, 3, 4\}$. Expressed here the mentioned propositions with the help of

conjunction, disjunction and negation then which of the following is correct?

- $\exists x Q(x) \equiv Q(0) \land Q(1) \land Q(2) \lor Q(3) \lor Q(4)$
- $\forall x Q(x) \equiv Q(0) \land Q(1) \lor Q(2) \land Q(3) \lor Q(4)$
- $\exists x \neg Q(x) \equiv \neg Q(0) \lor \neg Q(1) \lor \neg Q(2) \lor \neg Q(3) \lor \neg Q(4)$
- $\forall \mathbf{x} \neg \mathbf{Q}(\mathbf{x}) \equiv \mathbf{Q}(0) \land \mathbf{Q}(1) \land \mathbf{Q}(2) \land \mathbf{Q}(3) \land \mathbf{Q}(4)$

Identify the correct statement of the following, where Q(x) is the propositional function with domain $D = \{-2, -1, 0, 1, 2\}$

- $\exists x Q(x) \equiv Q(-2) \land Q(-1) \land Q(0) \land Q(1) \land Q(2)$
- $\forall x Q(x) \equiv Q(-2) \lor Q(-1) \lor Q(0) \lor Q(1) \lor Q(2)$
- $\exists x \neg Q(x) \equiv \neg Q(-2) \land Q(-1) \land Q(0) \land Q(1) \land Q(2)$
- $\forall x \neg Q(x) \equiv \neg Q(-2) \land \neg Q(-1) \land \neg Q(0) \land \neg Q(1) \land \neg Q(2)$

What is the negation of the statement $\forall x (-2 \le x < 3)$?

- $\forall x (x < -2 \lor x \ge 3)$
- $\exists x(x < -2 \lor x \ge 3)$
- $\nabla \forall x (x < -2 \land x \ge 3)$
- $\exists x(x < -2 \land x \ge 3)$

The restricted universal quantification $\forall y \neq 0 (y^3 \neq 0)$ can also be written

as

- $\exists y(y \neq 0 \rightarrow y^3 \neq 0)$
- $\exists y (y \neq 0 \land y^3 \neq 0)$
- $\forall y(y \neq 0 \rightarrow y^3 \neq 0)$
- $\forall y(y \neq 0 \lor y^3 \neq 0)$

14

Let P(x): $x = x^2$, $x \in \mathbb{Z}$ then which is false?

- $\bigcirc -\forall x P(x)$
- $\forall x P(x)$
- $\supset \exists x P(x)$
- $\exists x P(x)$

Unit 3: Self assessment-3

Success

1

If (S, R) is such that S is the set of all people in the world and $(a, b) \in R$, where a and b are people, then a is taller than b......

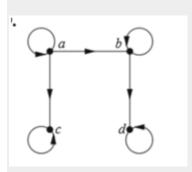
- Is not a poset
- Is a poset
- Is not transitive
- O Is symmetric

The set (Z, =) is

- Is not a poset
- Is a poset
- Is not transitive
- Is not symmetric

3

The following graph is



- a partial ordering
- Not antisymmetric
- Not transitive
- Not antisymmetric

4.

The two incomparable elements in the poset $(P(\{0,1,2\}),\subseteq)$ are

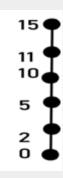
{5} and {1}, for instance
{0} and {1}, for instance
{2} and {6}, for instance
{10} and {10}, for instance

The lexicographic ordering of these n-tuples: (1,1,2), (1,2,1) are

- (1, 1, 3)<(1,3,1)
- (4, 1, 2) < (1,5,1)
- **(**1, 1, 2)<(1,2,1)
- (3, 1, 2)<(1,2,1)

6.

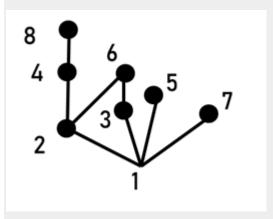
The following Hasse diagram for the "less than or equal to" relation is



- on {0,2,5,10,11,30}
- on {0,2,5,10,11,15}
- on {0,2,5,10,12,15}
- on {1,2,5,10,11,15}

7.

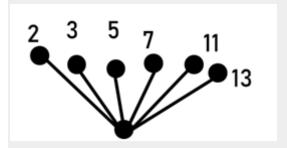
The following Hasse diagram for divisibility is



on the set {1,2,3,4,5,6,7,8}.

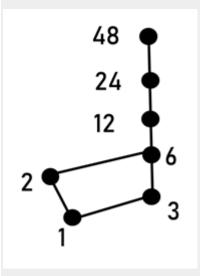
- on the set {1,2,3,4,5,6,7}. on the set {1,2,3,4,5,6,8}.
- on the set {0,2,3,4,5,6,7,8}.

The following Hasse diagram is on the set



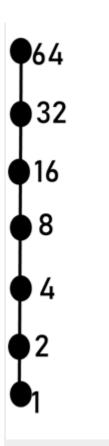
- {0,2,3,5,7,11,13}.
- {1,2,3,5,7,11,15}.
- {1,2,3,5,7,11,13}.
- {1,2,3,5,11,13}.

The following Hasse diagram is on the set



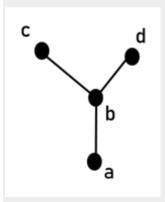
- {0,2,3,6,12,24,36,48}.
- {1,2,3,6,12,24,36,48}.
- {1,2,3,6,12,24,36,48,96}.
- {1,2,3,6,12,24,36}.

The following Hasse diagram is on the set



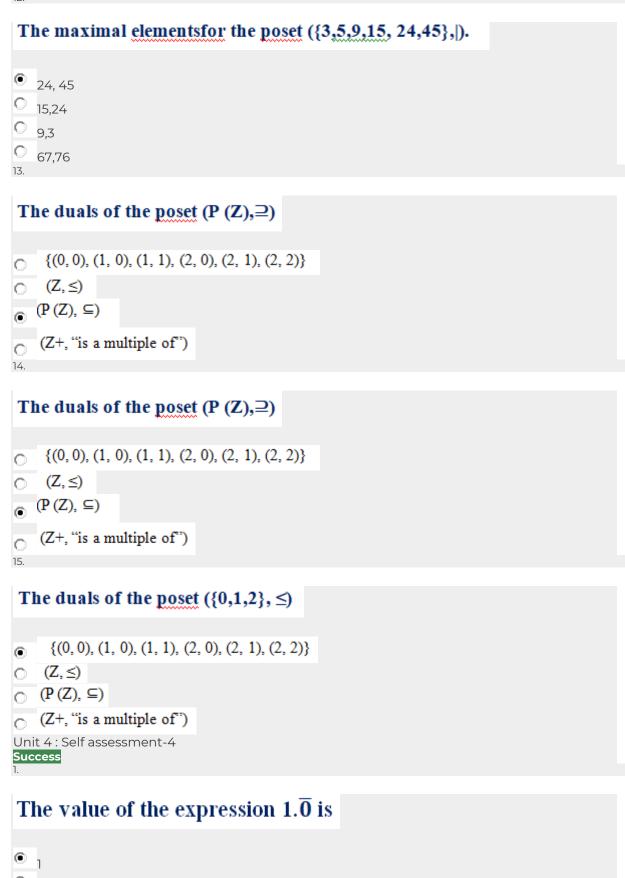
- **(1,2,4,8,16,32,64)**.
- {1,2,3,6,12,24,36,48}.
- **(**1,2,3,4,5,6,7,8).
- (0,2,3,4,5,6,7,8).

All ordered pairs in the partial ordering with the accompanying Hasse diagram is



- (a, c), (a, b), (a, d), (a, c), (b, a), (a, a), (b, b), (c, c), (d, d)
- (a, b), (a, c), (a, d), (b, c), (b, d), (a, a), (b, b), (c, c), (d, d)
- (a, b), (b, c), (e, d), (e, c), (b, d), (a, a), (c, b), (c, c), (d, d)
- (a, a), (a, c), (a, b), (b, c), (b, d), (b, a), (b, b), (d, c), (a, d)

O 1.0



O.1
The value of the expression $1+\overline{1}$
 ● 1 ○ 0 ● 1.0 ● 0.1 3.
The value of the expression $\overline{0}.0$
 ○ 1 ○ 0 ○ 1.0 ○ 0.1 4.
The value of the expression $\overline{1+0}$
 □ 1 • 0 □ 1.0 □ 0.1 5.
How many different Boolean functions of degree <i>n</i> are there?
What values of the Boolean variables x and y satisfy $xy = x + y$?
(0, 0) and (1, 1) (1, 0) and (1, 1) (0, 1) and (1, 1)

7.
That $x\overline{y} + y\overline{z} + \overline{x}z =$
$ \bar{x}y + \bar{y}z $ $ \bar{y}z + x\bar{z} $ $ \bar{x}y + x\bar{z} $ $ \bar{x}y + \bar{y}z + x\bar{z} $ 8.
The idempotent lawX+x=
 x 0 1 y 9.
The domination lawX+1=
 1 0 x y 10.
The associative <u>lawX</u> +(<u>v</u> +z) =
$(x,y) \cdot z$ $(x+y) + z$ $(x+y) \cdot z$ $X+(y+z)$ 11.
De Morgan's laws (\overline{xy}) =
$ \begin{array}{ccc} \bar{x}.\bar{y} \\ \bar{x}+\bar{y} \end{array} $ $ \begin{array}{ccc} x+y \end{array} $

0 x.y
The dual of the Boolean expression x +y is
 X.Y. X.X. X.X. X.X. x/y
The dual of the Boolean expression $\bar{x}\bar{y}$ is
$ \bar{x} + \bar{y} $ $ \bar{x} / \bar{y} $ $ x \cdot y $ $ x + y $ $ 14. $
The dual of the Boolean expression $xyz+\overline{x}\overline{y}\overline{z}$ is
$\begin{array}{ccc} & xyz+\bar{x}\bar{y}\bar{z} \\ \bigcirc & x+yz+\bar{x}\bar{y}\bar{z} \\ \bigcirc & xyz.\bar{x}\bar{y}\bar{z} \\ \bigcirc & (x+y+z).(\bar{x}+\bar{y}+\bar{z}) \\ 15. \end{array}$
The dual of the Boolean expression $x\overline{z}+x\cdot 0+\overline{x}\cdot 1$ is
$x\overline{z}.x \cdot 0 + \overline{x} \cdot 1$ $x\overline{z} + x + 0 + \overline{x} \cdot 1$ $x\overline{z} + x \cdot 0 + \overline{x} + 1$ $x\overline{z} + x \cdot 0 + \overline{x} + 1$ $x\overline{z} + x \cdot 1 \cdot x + 0$ Unit 5: Self assessment-5 Success 1.
A new company with just two employees, Sanchez and Patel, rents a floor of a building with 10 offices. How many ways are there to assign different offices to these two employees?
90 100 132

O 110 2.
A new company with just two employees, Sanchez and Patel, rents a floor of a building with 10 offices. How many ways are there to assign different offices to these two employees? 90 100 132 110 3.
A student can choose a computer project from one of three lists. The three lists contain 5, 10 and 15 possible projects, respectively. No project is on more than one list. How many possible projects are there to choose from? 50 40 30 10 4.
A new company with just two employees, Sachin and Parth, rents a floor of a building with 20 offices. How many ways are there to assign different offices to these two employees? 380 280 38 20 5.
A new company with just two employees, Sachin and Parth, rents a floor of a building with 20 offices. How many ways are there to assign different offices to these two employees? 380 280 38 20 6.
A computer company receives 350 applications from computer graduates for a job planning a line of new Web servers. Suppose that 210 of these applicants majored in computer science, 157 majored in business, and 51 majored both in computer science and in business. How many of these applicants majored neither in computer science nor in business? 34 44 50 20 7.

How many bit strings of length eight either start with a 0 bit or end with the two bits 11?

 ● 160 ○ 100 ○ 120 ○ 60 8.
How many bit strings of length eight either start with a 1 bit or end with the two bits 00?
 160 100 120 60 9.
The value of P(6,3) is
 675 987 120 876
10.
The value of each of the quantity P(6,5) is
 ○ 876 ○ 654 ○ 720 ○ 876 □ .
The value of each of the quantity P(8,8) is
 40,320 67,987 89,786 76,598 12.
The value of each of the quantity P(10,9) is
 7,689,560 6,754,637 76,543,220 3,628,800
The number of 5-permutations of a set with nine elements is

 □ 15,120 □ 16,786 □ 56,987 □ 67,890 □ 14. 	
How many ways are there for eight men and five women to stand in a line so that no two women stand next to each other? 609,638,400 675,987,098 786,987,600 786,987,600 15.	
Suppose that a department contains 10 men and 15 women. How many ways are there to form a committee with six members if it must have the same number of men and women? 89,765 87,987 54,600 65,897 16.	
A formula for the number of circular r-permutations of n people is n! / (r (n - r)!) n! n/ (n (n - n)!) n! n/ (n (r - r)!) nr! / (r (n - r)!) Unit 6: Self assessment-6 Success	
A woman has 11 close friends. In how many ways can she invite five of them to dinner? 456 462 450 451 2.	
A man has 11 close friends. In how many ways if two of the friends are married and will not attend separately? 210 222 223	

O 234 3.
A person has 11 close friends. In how many ways if two of them are not on speaking terms and will not attend together? 456 786 897 252 4.
A woman has 11 close friends of whom six are also women. In how many ways can she invite three or more of them if she wants the same number of men as women (including herself)? 325 360 400 480 5.
A student is to answer 10 out of 13 questions on an exam. How many choices has he? 567 456 786 286 6.
A student is to answer 10 out of 13 questions on an exam. How many if he must answer the first two questions? 897 890 165 987 7.
A student is to answer 10 out of 13 questions on an exam. How many if he must answer the first or second question but not both? 675 876 110 654 8.

A student is to answer 10 out of 13 questions on an exam. How many if he must answer exactly three out of the first five question?

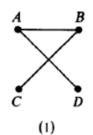
 ▶ 876 ▶ 80 ▶ 87 ▶ 90 9.
A student is to answer 10 out of 13 questions on an exam. How many if he must answer at least three of the five questions? 897 276 234 543 10.
The minimum number of students needed to guarantee that five of them belong to the same class (freshman, sophomore, junior, senior) Here the n=3 classes are the pigeonholes and k+1=7 so k=8. Thus, among any kn+1=14 student (pigeons), five of them belong to the same class. Here the n=4 classes are the pigeonholes and k+1=5 so k=4. Thus, among any kn+1=17 student (pigeons), five of them belong to the same class. Here the n=6 classes are the pigeonholes and k+1=50 so k=41. Thus, among any kn+1=107 student (pigeons), five of them belong to the same class. Here the n=24 classes are the pigeonholes and k+1=15 so k=4. Thus, among any kn+1=17 student (pigeons), five of them belong to the same class.
Let L be a list (not necessarily in alphabetical order) of the 26 letters in the english alphabet (which consists of 5 vowels,A,E,I,O,U and 21 consonants) then L has a sublist consisting
Let L be a list (not necessarily in alphabetical order) of the 26 letters in the english alphabet (which consists of 5 vowels,A,E,I,O,U and 21 consonants). Assuming L begins with a vowel, say A, then L has a sublist consisting

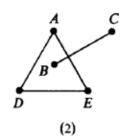
Show that a connected graph g with n vertices must have at least

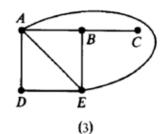
O a / admas
n-4 edges. n-3 edges.
n-2 edges.
n-1 edges.
The number of connected graphs with four vertices are
O 1
0 3
© 5 O 7
O ₇
Let G be a connected graph. If G contains a cycle C which contains an edge e, then
G + e is still connected
G − e is still connected
G – e is not connected
G - e is disconnected 4.
Consider the graph .All cycles, if any are
A B C B B C B B B C B B B B B B B B B B
AJBA, BEGB, CDHC
ABGA, BGEC, CDHC
AGBA, BLKB, CDHC
AGBA, BKLB, CHDC
Consider the graph Consider the graph all cut points, if any are

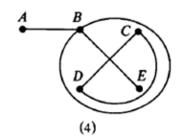


© B, E, H © C, E, G
O, E, A 6.
Suppose a graph G contains two distinct paths from vertex u to a vertex v.
Suppose a graph o contains two distinct patris norm vertex a to a vertex v.
then g has a cycle
then g has 3 cycles
then g has 4 cycles
then g has 5 cycles 7.
Suppose G is a finite cycle- free graph with a least one edge.
then G has at least two vertices of degree 2
then G has at least three vertices of degree 2
then G has at least two vertices of degree 1
then G has at least two vertices of degree 3
Let G be a connected graph. If $e = \{u, v\}$ is an edge such that $G - e$ is
disconnected, then u and v belong to different components of
disconnected, then u and v belong to different components of
disconnected, then u and v belong to different components of $G = G - e + I$
○ G+e. ○ G-e+l.
 ○ G+e. ○ G-e+l. ○ e -G.
○ G+e. ○ G-e+l.
 ○ G+e. ○ G-e+l. ○ e -G.
$ \begin{array}{ccc} G + e \\ G - e + 1 \\ e - G \\ \bullet & G - e \end{array} $
 G+e. G-e+1. e - G. G - e. Suppose G has V vertices and E edges. Let M and m denote, respectively, the maximum and minimum of the degrees of the vertices in G. then
○ $G+e$. ○ $G-e+l$. ○ $e-G$. ② $G-e$. 9. Suppose G has V vertices and E edges. Let M and m denote, respectively, the maximum and minimum of the degrees of the vertices in G. then
 G+e. G-e+l. e-G. G-e. Suppose G has V vertices and E edges. Let M and m denote, respectively, the maximum and minimum of the degrees of the vertices in G. then m ≥ 2E/V ≥ M m ≤ 2E/V ≤ M
 G+e. G-e+l. e-G. G-e. Suppose G has V vertices and E edges. Let M and m denote, respectively, the maximum and minimum of the degrees of the vertices in G. then m ≥ 2E/V ≥ M m ≤ 2E/V ≥ M m ≤ 2E/V ≥ M m ≤ 2E/V ≥ M
 G+e. G-e+l. e-G. G-e. Suppose G has V vertices and E edges. Let M and m denote, respectively, the maximum and minimum of the degrees of the vertices in G. then m ≥ 2E/V ≥ M m ≤ 2E/V ≤ M





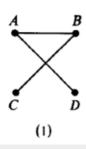


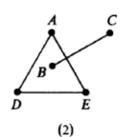


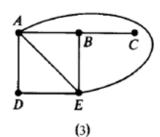
- Only (2) and (4) are connected
- Only (2) and (3) are connected
- Only (1) and (4) are connected
- Only (1) and (3) are connected

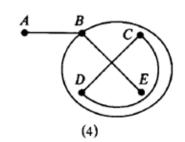
11.

Consider the multi graph which are cycle -free (without cycles).





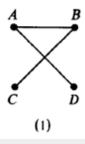


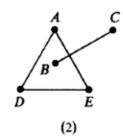


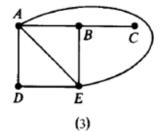
- Only (3) and (4) are cycle-free.
- Only (2) and (4) are cycle-free.
- Only (1) and (2) are cycle-free.
- Only (1) and (4) are cycle-free.

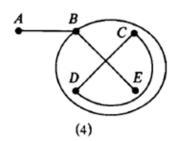
12.

Consider the multi graph, which are loop free (without loops)?





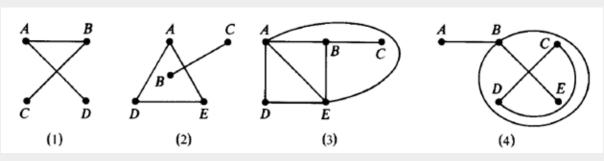




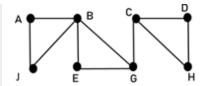
- Only (3) has a loop
- Only (1) has a loop
- Only (4) has a loop
- Only (2) has a loop

13.

Consider the multi graph, which are (simple) graphs?



- Only (1) and (3) are graphs.
- Only (2) and (3) are graphs.
- Only (1) and (4) are graphs.
- Only (1) and (2) are graphs.



Consider the graph. Find the subgraph H =

H(V', E') of G where V' equals: (a) $\{B,C,D,J,K\}$ (b) $\{A,C,J,L,M\}$

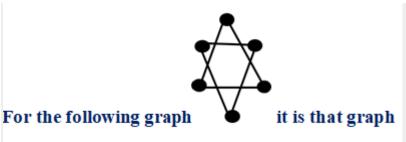
(c) {B,D, J,M} (d) {C,K, L,M}. Which of them are isomorphic?

- (b) and (c) are isomorphic,
- (a) and (c) are isomorphic,
- (a) and (d) are isomorphic,
- (a) and (b) are isomorphic,

Unit 8: Self assessment-8

Succes

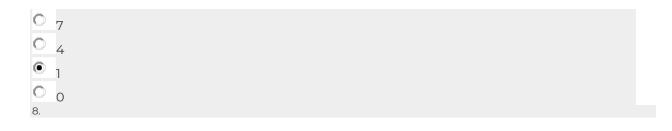
1



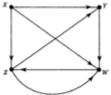
- is connected.
- is not connected
- has only one cycle

has no cycle	
What do the connected components of acquaintanceship graphs represent?	
Maximal sets of people with the property that for any three of them, we can find a string of acquaintances that takes us from one to the other Maximal sets of people with the property that for any two of them, we cannot find a string of acquaintances that takes us from one to the other Maximal sets of people with the property that for any two of them, we cannot find a string of acquaintances that takes us from one to the other Maximal sets of people with the property that for any four of them, we cannot find a string of acquaintances that takes us from one to the other Assimal sets of people with the property that for any four of them, we cannot find a string of acquaintances that takes us from one to the other	
The number of paths of length n between two different vertices in K ₄ if n is 2are 5 2 6 7 4.	
The number of paths of length n between two different vertices in K ₄ if n is3 are 7 9 8 6 5.	
The number of paths of length n between two different vertices in K ₄ if n is 4 are 60 90 20 10 6.	
The number of paths of length n between two different vertices in K ₄ if n is 5 are 71 61 23 41 7.	

The number of paths between c and d in the graph in Figure 2 of length (a) 2



Let G be the directed graph ,

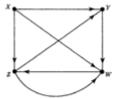


 J_w then total number cycles in G

are/is

- There is only one cycle in G, which is (Y, W, Z, Y).
- There 2 one cycles
- There 3 one cycles
- There 4 one cycles

9.

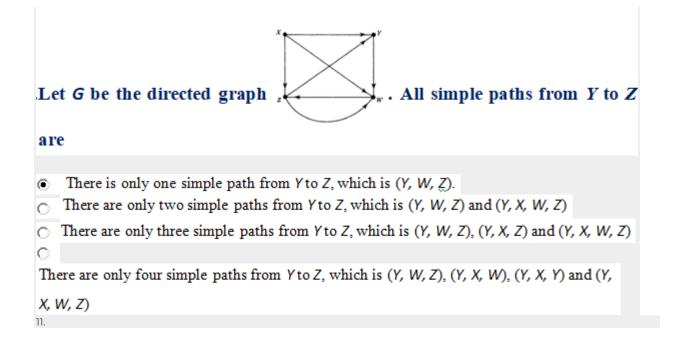


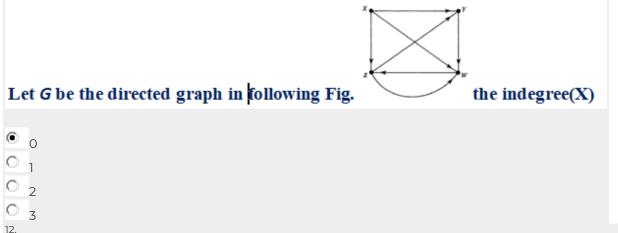
Let G be the directed graph

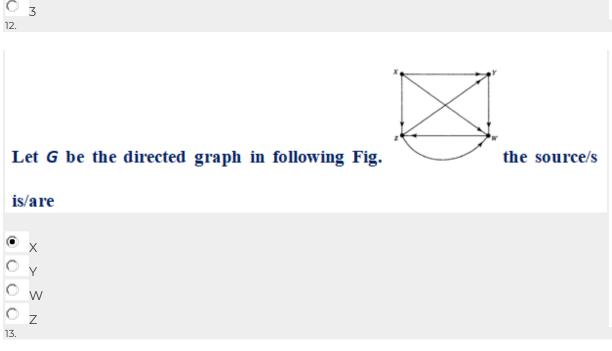
then all simple paths from X to

Z are

- There are three simple paths from X to Z, which are (X, Z), (X, W, Z), and (X, Y, W, Z).
- There are four simple paths from X to Z, which are (X, Z), (X, W, Z), and (X, Y, W, Z), (X, Y, W).
- There are two simple paths from X to Z, which are (X, Z), and (X, Y, W, Z).
- There isone simple paths from X to Z, which are (X, Z).









O X
O Y
O Z
O None

Let G be the directed graph with vertex set V (G) = (a, b, c, d, e, f, g) and edge set: $E(G) = \{(a, a), (b, e), (a, e), (e, b), (g, c), (a, e), (d, f), (d, b), (g, g)\}.$

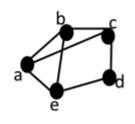
Then loops are

(g, g) (a, a),(b, e), (e, b) (a, a) (a, a) and (g, g)

Let G be the directed graph with vertex set V (G) = (a, b, c, d, e, f, g} and edge set: E(G) = {(a, a), (b, e), (a, e), (e, b), (g, c), (a, e), (d, f), (d, b), (g, g)}. Then parallel edges are

(g, g)
(b, e), (e, b)
(a, a)
(a, a) and (g, g)
Unit 9: Self assessment-9
Success

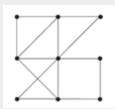
Following graph



- Neither has a Euler circuit nor has a Euler path
- has a Euler circuit
- has a Euler path
- has a Euler circuit and has a Euler Path

2

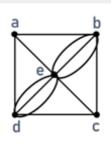
Following graph



- Neither has a Euler circuit nor has a Euler path
- has a Euler circuit
- has only an Euler path
- has a Euler circuit and but not Euler Path

Z

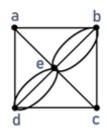
Following graph



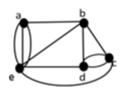
- Neither has a Euler circuit nor has a Euler path
- has a Euler circuit
- has a Euler path
- has a Euler circuit and has a Euler Path

4.

Following graph



- has a Euler path a, c, c, e, i, e, d, b, u, c, d
- has a Euler path a, e, c, e, b, e, d, b, a, c, d
- has a Euler path a, r, c, e, b, y, d, b, c, c, d
- has a Euler path a, o, c, e, b, e, u, b, a, c, d



Following graph

- a, b, e, d, c, f, d, b, e, a, h, a
- a, d, c, d, c, e, t, b, e, a, e, a
- a, b, c, d, c, e, d, b, e, a, e, a
- a, i, c, d, c, e, o, b, e,u,a, e, a

For which values of n do the graphs knhave a Euler path but no Euler

euler circuit is

circuit?

- n is odd
- n is even
- n is prime number
- n is a fractional number

7

For which values of n do the graphs $C_n have$ \underline{a} Euler path but no Euler

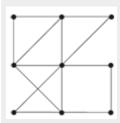
circuit?

- al
- 0 -

None 7
For which values of n do the graph Wnhave a Euler path but no Euler
circuit?
 All None 4 3 9.
For which values of n do the graphs Q_n have \underline{a} Euler path but no Euler
circuit?
 N=1 N=even N=odd N=prime N=prime
When can the centerlines of the streets in a city be painted without traveling a street more than once? (Assume that all the streets are two-way streets.)
• When the graph in which vertices represent intersections and edges streets has an Euler path
When the graph in which vertices does not represent intersections and edges streets has an Euler path
When the graph in which vertices represent intersections and edges streets does not have an Euler path
When the graph in which vertices represent intersections and edges streets have an Euler circuit.
The graph

\circ n	either has a Hamilton path nor a circuit.			
• h	as a Hamilton circuit.			
Od	oes nothave a Hamilton path.			
O d	oes nothave a Hamilton circuit.			
The g	raph			
O n	either has a Hamilton path nor a circuit.			
Od	O does nothave a Hamilton path.			
• h	• has a Hamilton circuit.			

The graph



has a Hamilton path and a circuit.

odes nothave a Hamilton circuit.

- does nothave a Hamilton path.
- has a Hamilton circuit.
- does not have a Hamilton circuit.

For which values of m and n does the complete bipartite graph $\mathbf{K}_{m,n}$ have a

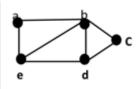
Hamilton circuit?

 $m = n \ge 3$

 $m = n \ge 12$

 $m = n \ge 2$

15.



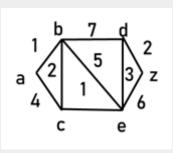
- has a Hamilton circuita, c, d, b, e, a.
- hasa Hamilton circuita, f, c, i, e, o.
- has a Hamilton circuita, f, c, u, e, o.
- has a Hamilton circuita, b, c, d, e, a.

Unit 10 : Self assessment-10

Success

1.

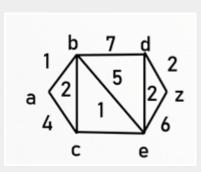
The shortest distance between sources a and destination z using Dijkstra 's



algorithm for following graph

- .
- □ 10
- O 11
- 0 12

The shortest distance between sources a and destination z using Dijkstra 's



algorithm for following graph

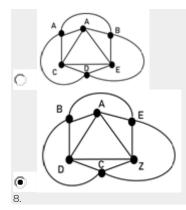
 8 10 11 12 3.
The shortest path between sources a and destination z using Dijkstra 's
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
algorithm for following graph
Therefore, shortest path between a and z =(a-b-c-d-e-z) Therefore, shortest path between a and z =(a-c-b-e-d-z) Therefore, shortest path between a and z =(a-b-c-e-d-z) Therefore, shortest path between a and z =(z-b-c-d-e-a) A.
The shortest path between sources a and destination z using Dijkstra 's
algorithm for following graph is
Therefore, shortest path between a and $z = (a-b-c-f-e-z)$
Therefore, shortest path between a and z =(a-c-b-e-f-z)
Therefore, shortest path between a and z =(a-b-c-e-f-z)
Therefore, shortest path between a and z =(z-b-c-f-e-a) 5.
The shortest path between sources a and destination z using Dijkstra 's

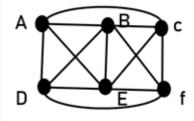


algorithm for following graph

is

Therefore, shortest path between a and z =(a-b-c-d-e-z) Therefore, shortest path between a and z =(a-c-b-e-d-z) • Therefore, shortest path between a and z =(a-b-c-e-d-z) Therefore, shortest path between a and z =(z-b-c-d-e-a) The shortest distance between sources a and destination z using Dijkstra 's algorithm for following graph A planar representation of

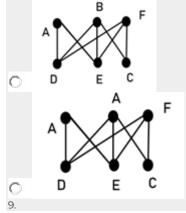


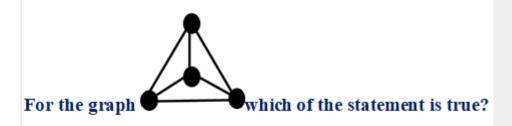


A planar representation of

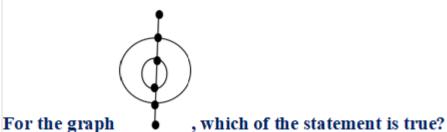
is that

- The graph has many planar representation
- The graph is nonplaner.

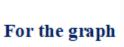




- V=4, E=6, R=0.Hence using euler 's formula V-E+R=4-6+4=2.Also d=2
- V=4, E=6, R=4.Hence using euler 's formulaV-E+R=4-6+4=2.Also d=3
- V=3, E=6, R=4.Hence using euler 's formula V-E+R=4-6+4=2.Also d=3
- V=9, E=6, R=4.Hence using euler 's formula V-E+R=4-6+4=9.Also d=3



- V=6, E=0, R=5; SO, V-E+R=6-9+5=2.Here d=6 since two edges are counted twice.
- V=6, E=3, R=5; SO, V-E+R=6-9+5=12.Here d=6 since two edges are counted twice.
- V=6, E=9, R=5; SO, V-E+R=6-9+5=62.Here d=6 since two edges are counted twice.
- V=6, E=9, R=5; SO, V-E+R=6-9+5=2.Here d=16 since two edges are counted twice.





, which of the statement is true?

- V=4, E=10, R=7.Henc V-E+R 5-10 +7=2.Here d=52
- V=6, E=10, R=7.Henc V-E+R 5-10 +7=2.Here d=2
- V=7, E=10, R=7.Henc V-E+R 5-10 +7=2.Here d=4
- V=5, E=10, R=7.Henc V-E+R 5-10 +7=2.Here d=5

The minimum number n of colors required to paint

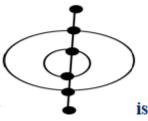


•	n=4
•	n=4

0 n=0

n=8

O n=7



The minimum number n of colors required to paint

- n=3
- 0 n=9
- n=6
- n=2

Find the minimum number n of colorsrequired to paint



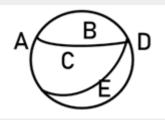
- only twelve colors are needed i.e, n=12
- only two colors are needed i.e, n=2
- only twenty two colors are needed i.e, n=22
- only one colors are needed i.e, n=1

Unit 11 : Self assessment-11

Success

1.

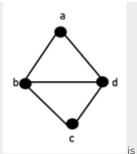
The number of colors needed to color the map so that no two adjacent



regions have the same color is.

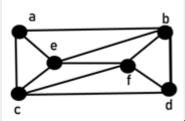
- Four colors
- Three colors
- Two colors

Five colors
The number of colors needed to color the map so that no two adjacent regions have the same color Three color Two colors One colors None of these 3.
The chromatic number of the given graph 2 7 1 3 4.
The chromatic number of the given graph



The chromatic number of the given graph

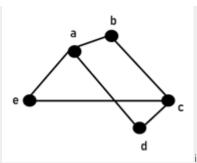




The chromatic number of the given graph



7



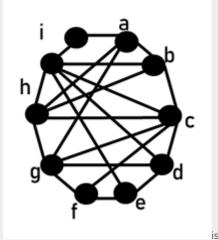
The chromatic number of the given graph

O 1

O 3

•

0 4



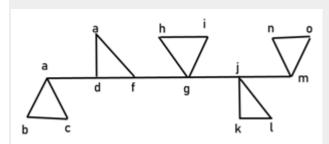
The chromatic number of the given graph

0

0 2

9

The chromatic number of the given graph is



ع ٥

Which graphs have a chromatic number of 1?

Graphswithnoedges

Graphswith2 edges

Graphswith 3 edges

Graphswith 4 edges

11.

What is the chromatic number of W_n ?

Oif n is even, 3 if n is odd I if n is even, 5 if n is odd I if n is even, 2 if n is odd I if n is even, 2 if n is odd I if n is even, 4 if n is odd I if n is even, 4 if n is odd
The chromatic number of the graph The chromatic number of the graph 1 2 3 4 13.
What is the chromatic number of K _n ? o n o n+1 o n-1 o n-2
The chromatic number of the complete bipartite graph K _{m, n} , where m and n are positive integersis
5 15.

What is the chromatic number of the graph Cn , where $n \ge 3$? (Recall that						
Cn is the cycle with n vertices.)						
 2 3 4 5 Unit 12: Self assessment-12 Success 1. 						
A tree with n vertices has						
 n-l edges n-2 edges n-3 edges n-4 edges 2. 						
A full m-ary tree with i internal vertices contains n =						
 mi +4 vertices. mi +3 vertices. mi +2 vertices. mi +1 vertices. 3. 						
A full m-ary tree with n vertices has						
 i = (n-1)/m internal vertices i = (n+1)/m internal vertices i = (n-2)/m internal vertices i = (n-3)/m internal vertices 4. 						
There are at most mh leaves in anm-ary tree of height						
 ○ h+2. ○ h+1. ○ h+3. ○ h. 						

Suppose that someone starts a chain letter. Each person who receives the letter is asked to send it on to four other people. Some people do this, but others do not send any letters. How many people have seen the letter, including the first person, if no one receives more than one letter and if the chain letter ends after there have been 100 people who read it but did not send it out? How many people sent out the letter?

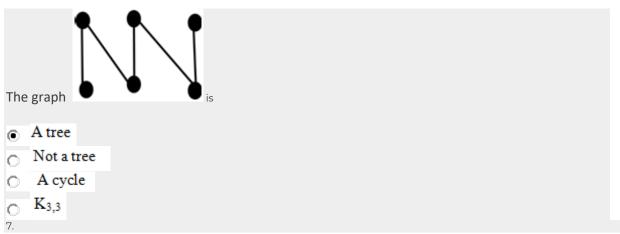
122 & 22

111 & 11

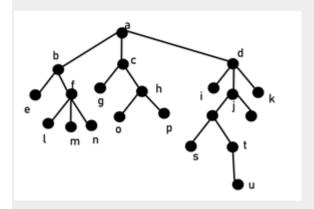
133 & 33

144 & 44

6.

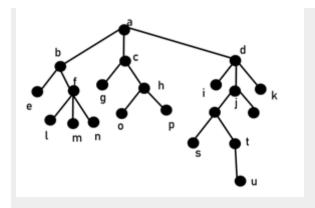


Answer these questions about the rooted tree



. Which vertex is the root?

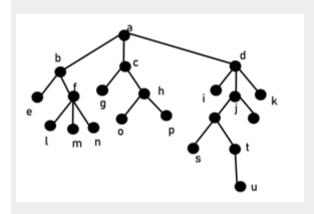




. Which vertices are internal?

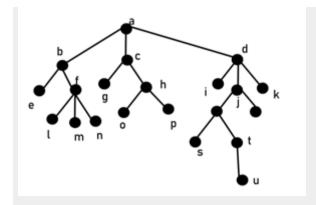
- a, b, c, d, f, h, j, q, t
- a, b, d, e, f, g, h, t, q, l, o
- a, b, f, d, f, k, j, m, t
- none of these

Answer these questions about the rooted tree



. Which vertices are leaves?

- e, a, i, k, l, b, j, o, l, r, s, a
- e, f, i, h, l, m, n, u, p, r, p, u
- e, g, i, k, l, m, n, o, p, r, s, u
- e, b, i, k, x, m, n, z, p, r, q, u



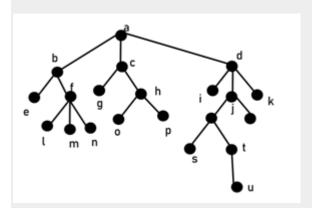
. Which vertices are children of j?

C t, r

O u, r

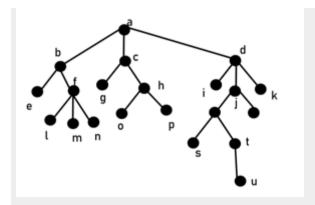
b, r

Answer these questions about the rooted tree



. Which vertex is the parent of h?

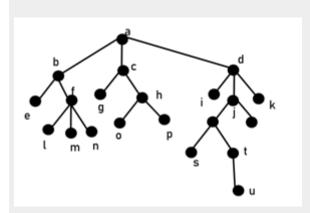




. Which vertices are siblings of o?

- 0 _M
- О с
- 13.

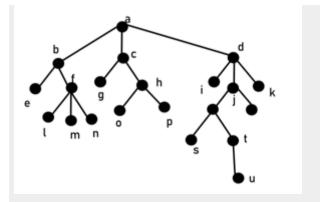
Answer these questions about the rooted tree



. Which vertices are ancestors of m?

- f, b, a
- O d, g, t
- O r, e, o
- **O** w, q, e

14.

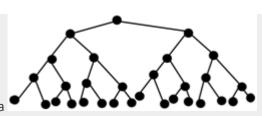


. Which vertices are descendants of b?

- e, V, I, m, n
- e, f, l, m, n
- e, Y, A, m, n
- None of these

 $How many edges does a full binary tree with 1000 in ternal vertices \ have?$

- 4000
- 1000
- 2000
- 500



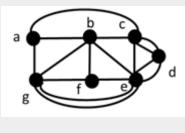
The following tree is a

- binary tree of height 7
- binary tree of height 6
- binary tree of height 5
- binary tree of height 4 Unit 13 : Self assessment-13

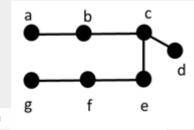
How many edges must be removed from a connected graph with n vertices and m edges to produce a spanning tree?

- m-n+1
- m-n+2
- m-n+3
- m-n+4

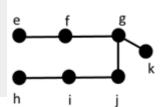
A spanning tree for the graph shown by removing edges in simple circuits.



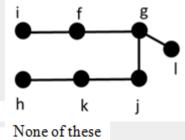
is



•

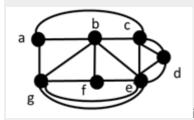


0

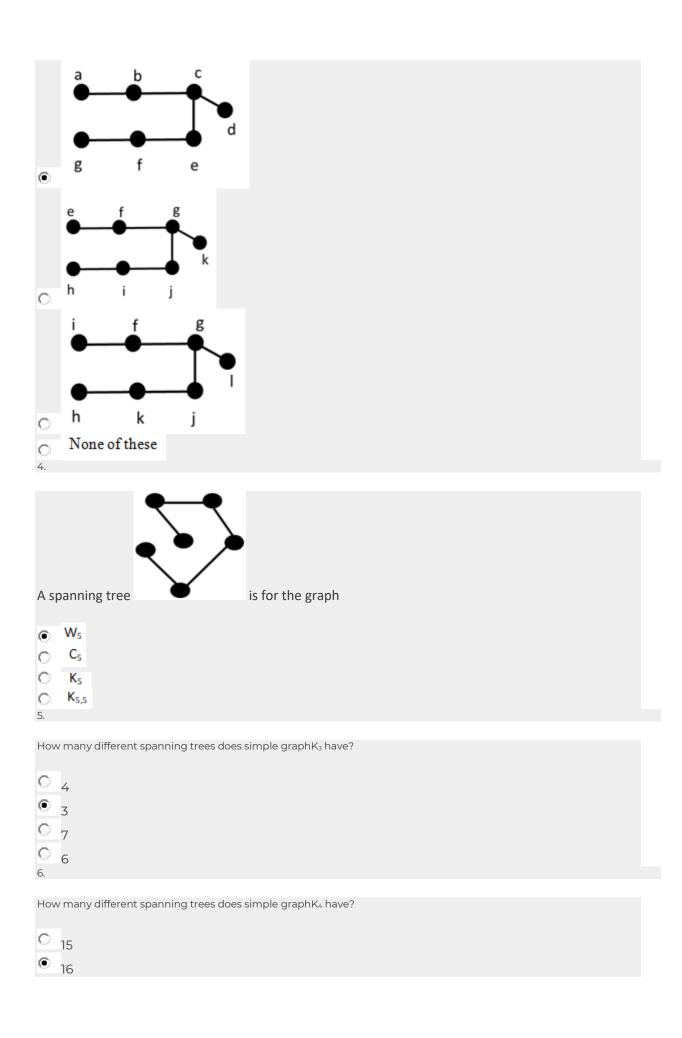


 \sim

A spanning tree for the graph shown by removing edges in simple circuits.



is



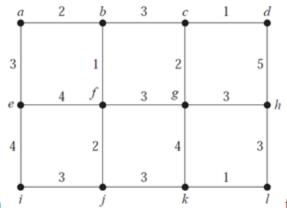
O 17					
O 18					
7.					
How many diffe	erent spanning	g trees does	simple gra	phsK _{2,2} have	?
O 6					
• 4					
0 5					
O 7 8.					
How many different spann	ing trees does simple	graphs Cahayo?			
riow many different spanin	rig trees does simple (grapins Cinave:			
0 9					
5					
0 8					
9.					
Heine Kanalaski	la alganithm	to design	41		
Using Kruskal'	s algorium	to design	the com	munications	network
			\$2000	Chicago	New York
	San Fr	ancisco	\$1200	\$1000	
		ancisco \$90	Denver	31000	<i>\$</i> /
			\$2200	\$1400	/
described	here				Atlanta
following is the	correct answer	r .			
O Kruskalla algerith		l			A+1+-

- Kruskal's algorithm will have us include first the links from Chicago to Atlanta, then Atlanta to New York, then Denver to San Francisco (the cheapest links). The next cheapest link, from Chicago to New York, cannot be included, since it would form a simple circuit. Therefore we next add the link from Chicago to San Francisco, and our network is complete.
- Kruskal's algorithm will have us include first the links from Atlanta to Chicago, then New York to Atlanta, then Denver to San Francisco (the cheapest links). The next cheapest link, from Chicago to New York, cannot be included, since it would form a simple circuit. Therefore we next add the link from Chicago to San Francisco, and our network is complete.
- Kruskal's algorithm will have us include first the links from Atlanta to Chicago, then Atlanta to New York, then Denver to San Francisco (the cheapest links). The next cheapest link, from Chicago to New York, cannot be included, since it would form a simple circuit. Therefore we next add the link from San Francisco to Chicago, and our network is complete.
- Kruskal's algorithm will have us include first the links from Atlanta to Chicago, then Atlanta to New York, then Denver to San Francisco (the cheapest links). The next cheapest link, from

Chicago to New York, cannot be included, since it would form a simple circuit. Therefore we next add the link from Chicago to San Francisco, and our network is complete.

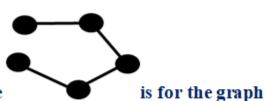
10.

Using Kruskal'salgorithmtoaminimumspanningtree for the weighted



graph in

- (e, k), {a, d}, {h, i}, {b, j}, {c, l}, {e, m}, {b, n}, {g, o}
- (e, f), {a, d}, {h, i}, {b, d}, {c, f}, {e, h}, {b, c}, {g, h}
- (e, p}, {q, d}, {s, i}, {v, d}, {d, f}, {e, h}, {b, c}, {g, h}
- e, p}, {q, j}, {s, i}, {v, d}, {d, f}, {e, h}, {b, c}, {g, h}



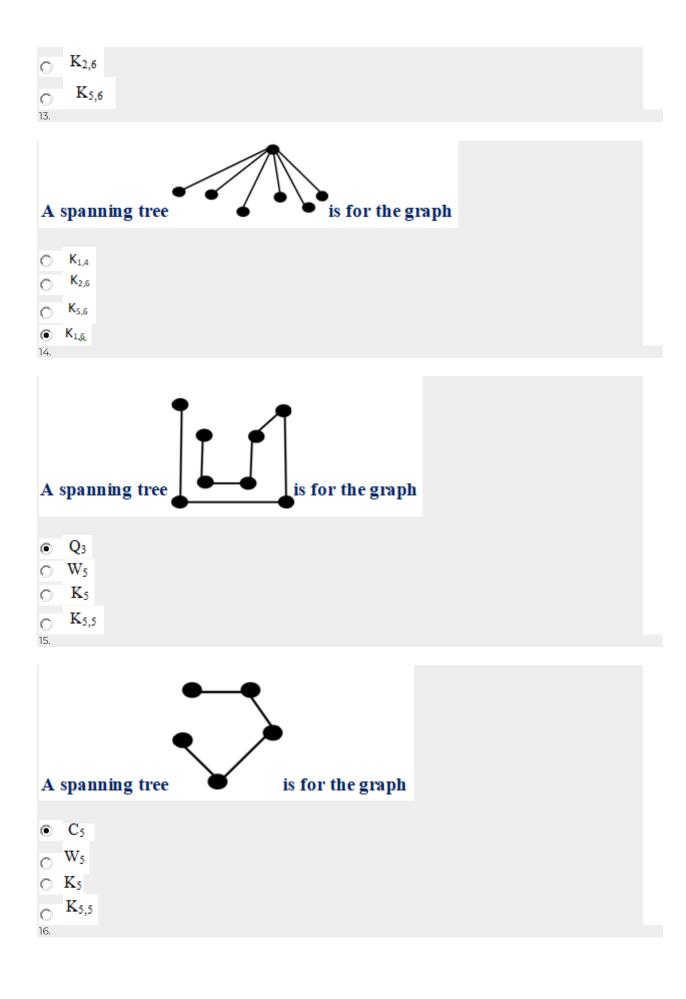
A spanning tree

- Q_3
- \circ W₅
- K_{5,5}

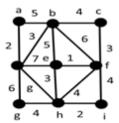
12.

A spanning tree is for the graph

- K_{1,4}



Using Prim's algorithm to find a minimum spanning tree for the given



weighted graph

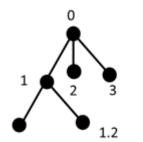
we get

- e, b}, {c, f}, {e, m}, {h, o}, {b, r}, {b, u}, {a, d}, {g, h}
- (e, c}, {c, i}, {e, k}, {h, p}, {b, s}, {b, v}, {a, d}, {g, h}
- e, d}, {c, j}, {e, l}, {h, q}, {b, t}, {b, w}, {a, d}, {g, h}
- (e, f}, {c, f}, {e, h}, {h, i}, {b, c}, {b, d}, {a, d}, {g, h}

Unit 14: Self assessment-14

Success

1.

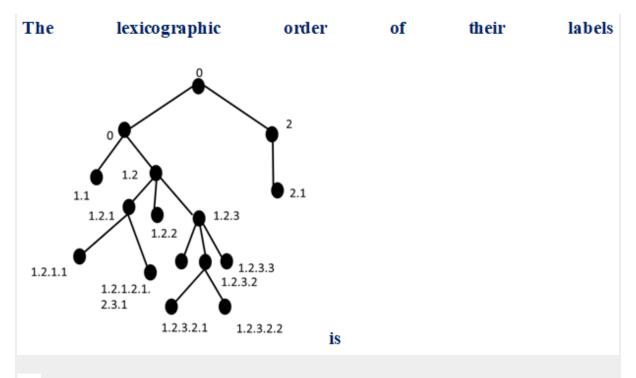


The lexicographic order of their labels 1.1

is

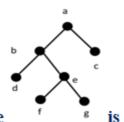
- the order is 1 < 1<1.1<1.2 < 2 < 3.
- the order is 0 < 1<1.1<1.2 < 2 < 3.
- the order is 1.1 < 1<1.1<1.2 < 2 < 3.
- the order is 0.1 < 1<1.1<1.2 < 2 < 3.

2.



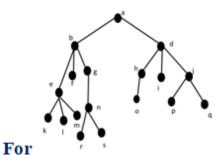
- 0 < 1 < 1.1 < 1.2 < 1.2.1 < 1.2.1.1 < 1.2.1.2 < 1.2.2 < 1.2.3 < 1.2.3.1 < 1.2.3.2 < 1.2.3.2 < 1.2.3.2.1 < 1.2.3.2.2 < 1.2.3.3 < 2 < 2.1.

 1 < 0 < 1.1 < 1.2 < 1.2.1 < 1.2.1.1 < 1.2.1.2 < 1.2.2 < 1.2.3 < 1.2.3.1 < 1.2.3.2 < 1.2.3.2 < 1.2.3.2.1 < 1.2.3.2.2 < 1.2.3.3 < 2 <
- 0 < 1 < 1.1 < 1.2.1 < 1.2.1 < 1.2.1.1 < 1.2.1.2 < 1.2.2 < 1.2.3 < 1.2.3.1 < 1.2.3.2 < 1.2.3.2.1 < 1.2.3.2.2 < 1.2.3.3 < 2 < 2.1.



The vertices of the given ordered rooted tree

- a, b, a, e, f, e, c
- a, b, d, e, f, g, c
- a, b, h, e, f, m, a
- a, h, k, e, f, l, c

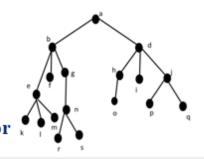


the order in which a preorder traversal visit

is

- a, b, e, k, o, m, f, g, n, g, s, c, p, h, o, i, j, p, q
- a, b, e, k, l, m, f, g, n, r, s, c, d, h, o, i, j, p, q
- a, b, e, k, l, m, j, g, n, k, s, c, d, l, o, i, j, m, q
- none of these

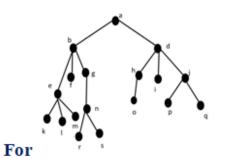
5.



the order in which ainorder traversal visit is

- j, n, o, a, f, c, g, k, h, p, l
- e, m, j, n, o, a, f, c, g, k, h, p, l
- d, b, i, e, m, j, n, o, a, f, c, g, k, h, p, l
- none of these

6.

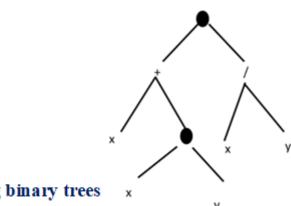


the order in which a postorder traversal visit

is

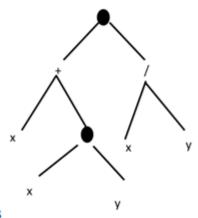
- k, j, i, e, f, r, s, n, g, b, c, o, h, i, p, q, j, d, a
- s, n, g, b, c, o, h, i, p, q, j, d, a

- k, l, m, e, f, r, s, n, g, b, c, o, h, i, p, q, j, d, a
- O None of these



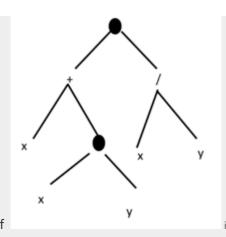
Using binary trees

the expression is



Using binary trees

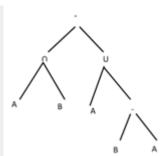
the expression is



Postfix notation of

- O xxy*+xy/*
- O x x y * + x y / =
- x x y * + x y / +
- O xxy*+xy/

0.

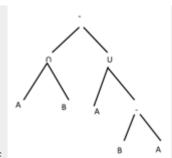


Using an ordered rooted tree

. Can be writtenas the this

- (A∩B) + (A∪ (B -A))
- (A∩B) * (A∪ (B -A))
- (A∩B) \ (A∪ (B -A))
- (A∩B) (A∪ (B -A))

11.



Prefix notation of

-) -∩ABUA-BA
- U) -∩BAUA-BA
- O) -∩CAUA-BA

) -∩BCUA-BA Postfix notation of AB∩ABA-u-AB∩CAA-u-AB∩AFA-u-BC∩ABA-u-Infix notation ((A∩B) -(A∪(B-A))) ((A∩B) -(A∪(B-A))) ((F∩B) -(c∪(B-A))) None of these The ordered rooted tree is such that whose preorder traversal is b, a, f, c, g, h, i, d, e, j, k, l, where a has four children, c has three children, j has two children, b and e have one child each, and all other vertices are leaves whose preorder traversal is a, b, f, c, g, h, i, d, e, j, k, l, where a has four children, c has three children, j has two children, b and e have one child each, and all other vertices are leaves whose preorder traversal is a, b, f, c, g, h, i, e, d, j, k, l, where a has four children, c has three children, j has two children, b and e have one child each, and all other vertices are leaves whose preorder traversal is a, b, f, c, g, h, i, d, e, j, l, k, where a has four children, c has three children, j has two children, b and e have one child each, and all other vertices are leaves