

Machine Learning 101

➤ Supervised Learning

"right answers" given

task: estimate more "right answers"

[Regression Problem: continuous value answer

[Classification Problem: discrete valued output

➤ Unsupervised Learning

no "right answer"

can find structure in data

→ clusters

➤ Linear Regression

Notation

- Training set \leadsto dataset for given problem
- $m \leadsto$ number of examples in training set
- x 's \leadsto "input" variables
- y 's \leadsto "output" / "target" variable
- $(x^{(i)}, y^{(i)}) \leadsto$ i -th training example
- hypothesis \leadsto function given by learning algorithm
 - \hookrightarrow maps from x 's to y 's

Cost Function

given: $h_{\theta}(x) = \theta_0 + \theta_1 x$

\rightarrow input

\hookrightarrow hypothesis

\hookrightarrow parameters

$$\hookrightarrow J(\theta) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 \quad \left. \vphantom{\sum} \right\} \begin{array}{l} \text{minimize this:} \\ \text{get } \theta \text{ values that "cost less"} \\ \therefore \text{fit data best} \end{array}$$

➤ Gradient Descent

* Can reach different local min depending on starting parameters
 \hookrightarrow works best in cases in which there is only one min point
(elliptic paraboloid)

Algorithm:

while !convergence \hookrightarrow learning rate

$$\theta_j := \theta_j - \alpha \frac{\partial J(\theta_0, \theta_1)}{\partial \theta_j} \quad \hookrightarrow \text{univariate case}$$

} * Simultaneous ~~update~~ update \circ in literal algorithm, next state must be calculated and stored into temp values all at once, then updated all at once or well

→ Learning Rate (α)

too small: gradient descent is too slow

too big: "big steps", may lead to overshooting and failure to converge

→ Gradient Descent for Linear Regression

model $\begin{cases} h_\theta(x) = \theta_0 + \theta_1 x \\ J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2 \end{cases} \rightarrow$ apply GD to get lowest cost parameters

$$\theta_j := \theta_j - \alpha \left[\frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1) \right] \rightarrow j=0 \rightarrow \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\rightarrow j=1 \rightarrow \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) \cdot x^{(i)}$$

$$\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x^{(i)}$$

* "Batch" Gradient Descent:
each iteration goes through
the entire training set