

SUPPORTING INFORMATION

# **Learning from Correlations Based on Local Structure: Rare-earth Nickelates Revisited**

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# Scatter Matrices

Scatter plots of the amplitude and ordering temperatures from the experiment and DFT structure data sets.

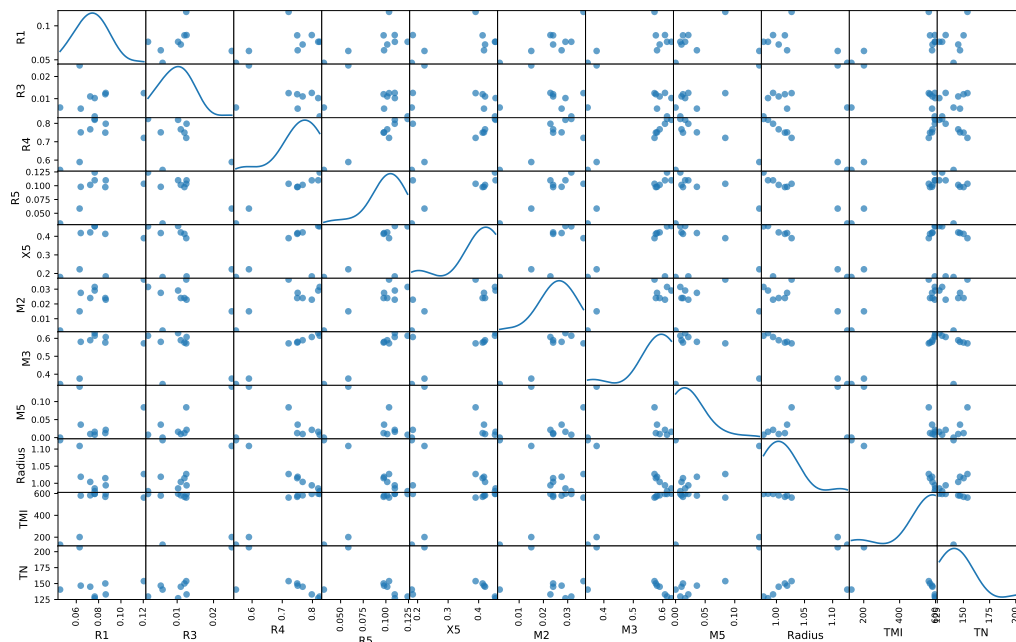


Figure S1: Scatter plot matrix from experiment using distortion-mode amplitudes. The diagonal elements are kernel density estimations for each variable.

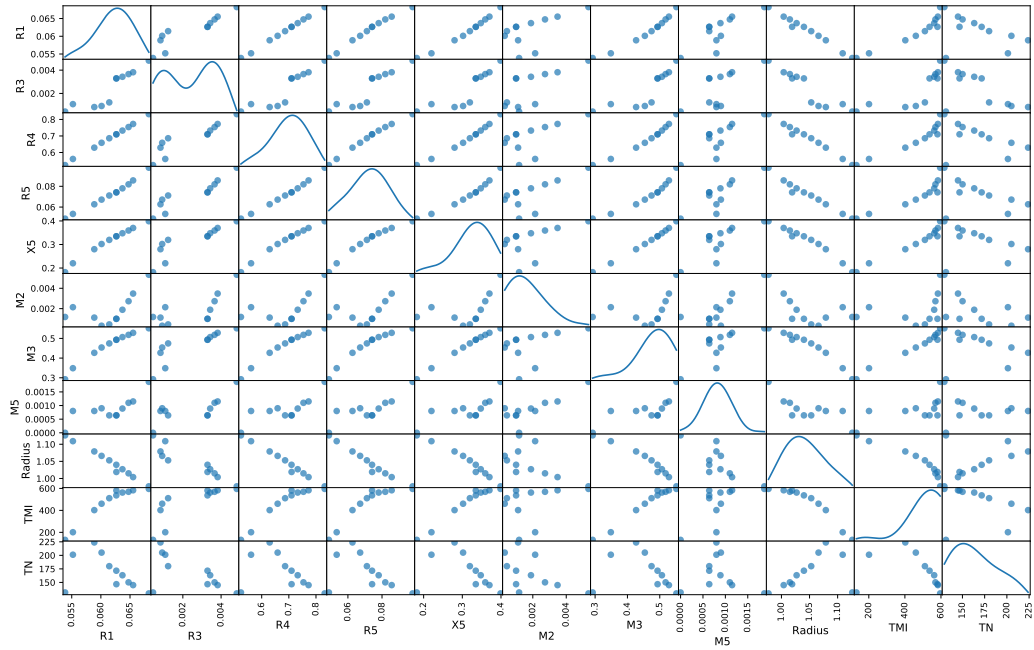


Figure S2: Scatter plot matrix from DFT using distortion-mode amplitudes. The diagonal elements are kernel density estimations for each variable.

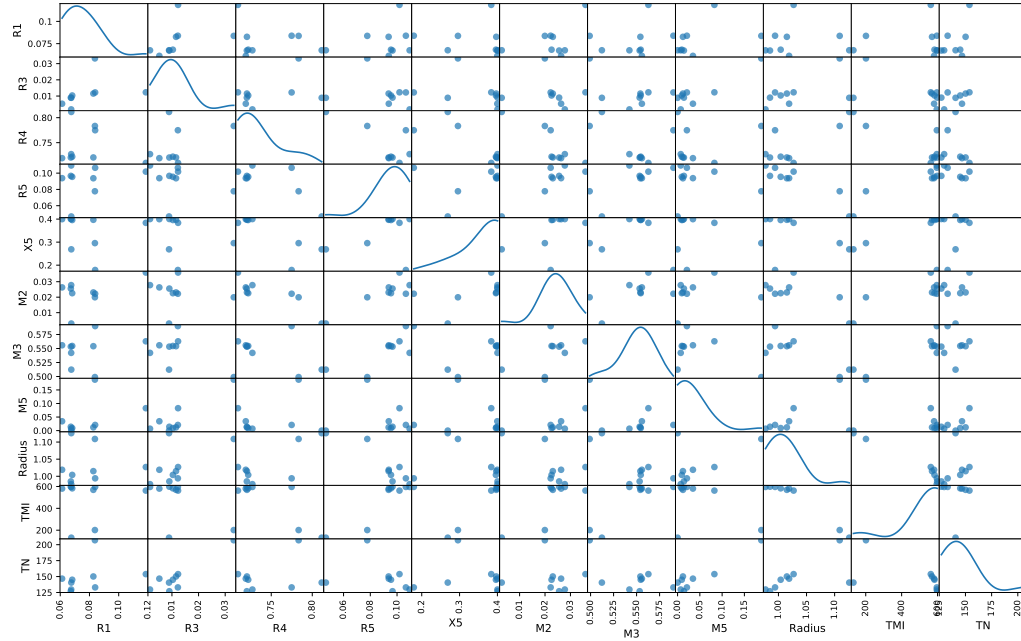


Figure S3: Scatter plot matrix from experiment using normalized distortion-mode amplitudes. The diagonal elements are kernel density estimations for each variable.

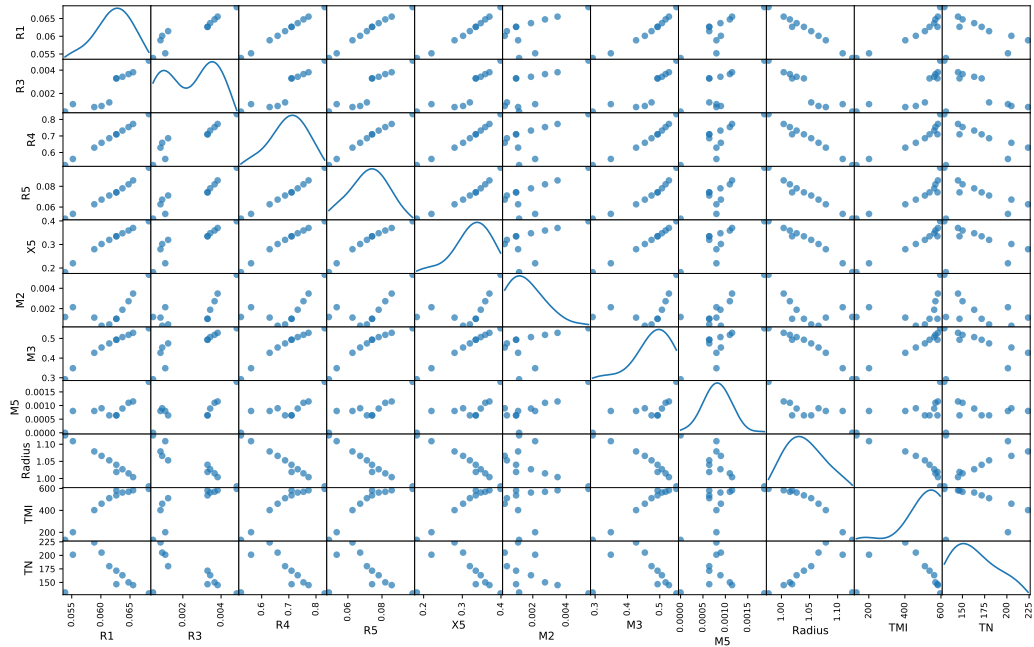


Figure S4: Scatter plot matrix from DFT using normalized distortion-mode amplitudes. The diagonal elements are kernel density estimations for each variable.

## Normalized Correlation-Coefficient-Heat Map for Experimental Structures

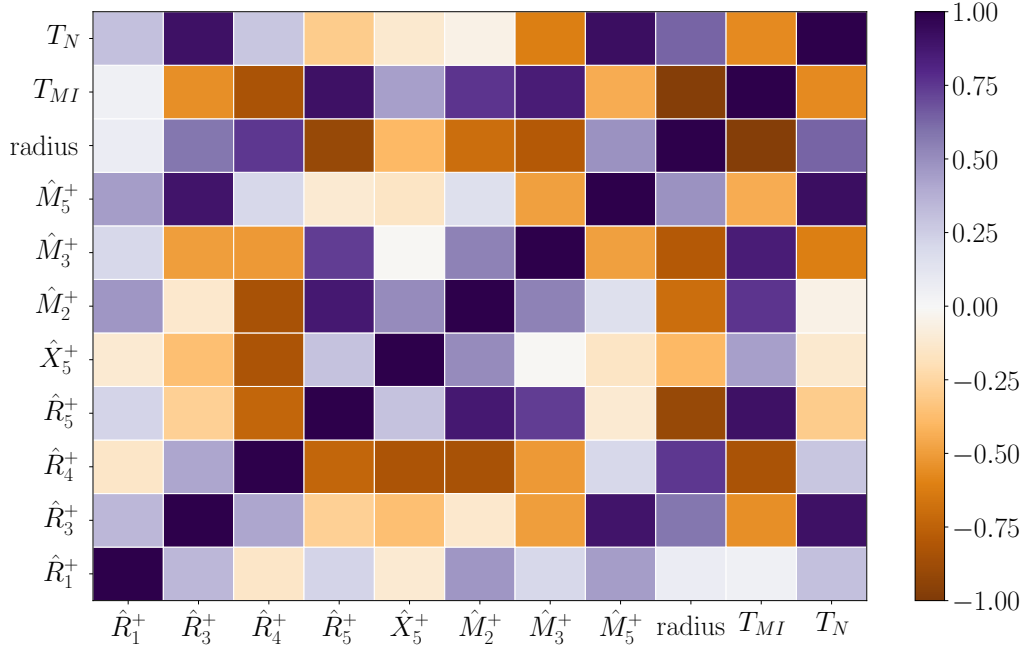


Figure S5: Normalized correlation-coefficient-heat maps ( $n$ CCHMs) calculated from the experimentally published crystal structures. Normalization is indicated by a 'hat' on the irrep label and is based on the Euclidean norm of the total mode vector mapping  $Pm\bar{3}m \rightarrow P2_1/c$ . All ordering temperatures correspond to values from experiment.

## Distortion Modes for NdNiO<sub>3</sub>

Table S1 provides the distortion mode amplitudes given with respect to the  $Pm\bar{3}m$  aristo-type based on the experimental and our DFT calculated  $P2_1/c$  NdNiO<sub>3</sub> structures. We also provide the metric,  $\xi$ , defined as the ratio between the DFT and experimental amplitude of each irreducible representation (irrep) in the correct antiferromagnetic  $E'$  (AFM- $E'$ ) spin order. The breathing ( $R_1^+$ ),  $a$ -type Jahn-Teller ( $R_3^+$ ), and rumpling ( $M_5^+$ ) distortions responsible for the  $Pnma \rightarrow P2_1/c$  symmetry lowering transition are shown in bold. The physical representation of each distortion mode is presented in Fig. 1 of the main text.

Table S1: Distortion modes for the theoretical (DFT) and experimental low temperature phase of NdNiO<sub>3</sub> (in units of Å).

NdNiO <sub>3</sub>	<b><math>R_1^+</math></b>	<b><math>R_3^+</math></b>	$R_4^+$	$R_5^+$	$M_2^+$	$M_3^+$	<b><math>M_5^+</math></b>	$X_5^+$
AFM- $E'$ (DFT)	<b>0.062</b>	<b>0.001</b>	0.581	0.057	0.002	0.366	<b>0.0004</b>	0.237
Experiment (Ref. 1)	<b>0.063</b>	<b>0.025</b>	0.589	0.059	0.015	0.375	<b>0.141</b>	0.222
$\xi$	<b>0.98</b>	<b>0.04</b>	0.99	0.97	0.13	0.98	<b>0.003</b>	1.07

Table S2 provides the distortion mode amplitudes given with respect to the  $Pm\bar{3}m$  aristotype based on the the experimental  $Pnma$   $\text{NdNiO}_3$  structures reported at 293K. For each mode, we provide the coefficient of variation, which is defined as the standard deviation divided by the mean.

Table S2: Distortion modes for the experimental high temperature phase of  $\text{NdNiO}_3$  (in units of Å) and the coefficient of variation (last column) for five different ICSD reports specified by collection code (CC) in the first row.

Mode	CC:164562	CC:78319	CC:24875	CC:69788	CC:67725	Coeff. of Var.
$R_4^+$	0.537	0.503	0.685	0.53557	0.554	0.113
$R_5^+$	0.047	0.091	0.143	0.04614	0.038	0.544
$X_5^+$	0.193	0.353	0.263	0.197	0.189	0.264
$M_2^+$	0.038	0.024	0.011	0.010	0.0043	0.690
$M_3^+$	0.371	0.342	0.441	0.398	0.373	0.087

## References

- (1) Garcia-Muñoz, J. L.; Aranda, M. A. G.; Alonso, J. A.; Martinez-Lope, M. J. Structure and Charge Order in the Antiferromagnetic Band-Insulating Phase of  $\text{NdNiO}_3$ . *Phys. Rev. B* **2009**, 79, 134432.