

Tree Colors: color schemes for tree structured data

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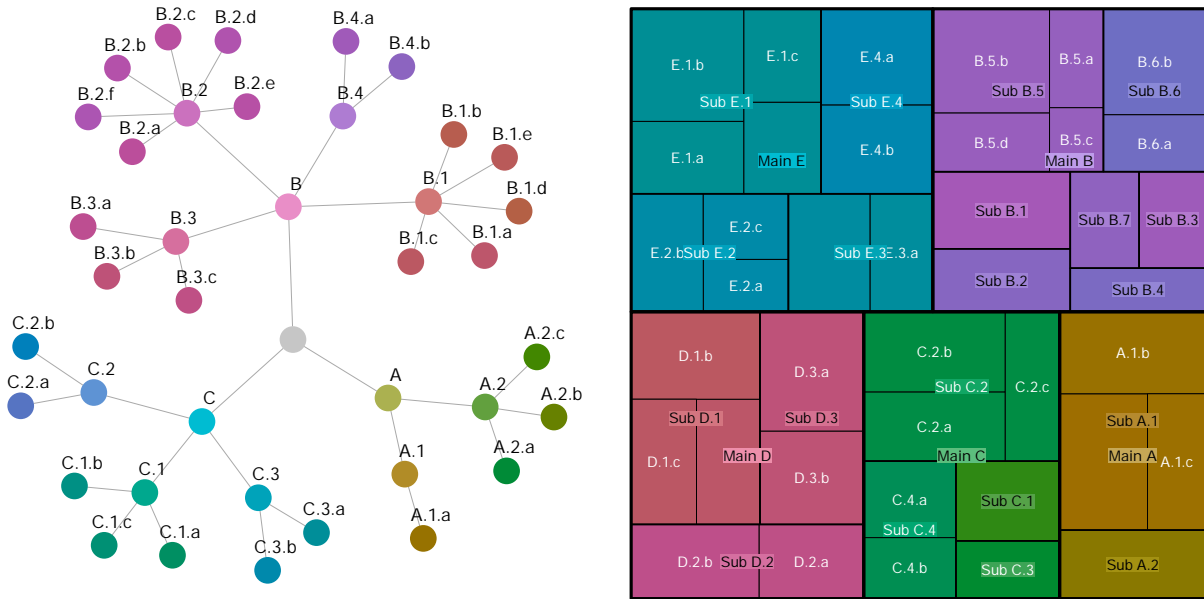


Fig. 1. Tree Colors applied to a node-link diagram (left) and a treemap (right).

Abstract— We present a method to map tree structures to colors from the Hue-Chroma-Luminance color model, which is known for its well balanced perceptual properties. The Tree Colors method can be tuned with several parameters, whose effect on the resulting color schemes is discussed in detail. We provide a free and open source implementation with sensible parameter defaults. Categorical data are very common in statistical graphics, and often these categories form a classification tree. We evaluate applying Tree Colors to tree structured data with a survey on a large group of users from a national statistical institute. *Our user study suggests that tree color schemes are useful, not only for improving node-link diagrams, but also for unveiling tree structure in non-hierarchical visualizations. Remarkably we find that Tree Colors do not improve detection of parent-child relations in treemaps in comparison to a standard qualitative color scheme.*

Index Terms—Color schemes, statistical graphics, hierarchical data.

1 INTRODUCTION

Data are often hierarchically structured. For example business data are typically broken down by economic activity and demographic data by geographic region. Several visual exploration methods of such data use the underlying hierarchical structure, for instance treemaps [25, 29]. Color schemes reflecting the hierarchical structure would be very useful in supporting their visual analysis. Such color schemes could clarify the chosen layout by emphasizing the tree structure of the data. For node-link diagrams, this makes it possible to relax its tree layout, having more space to place the nodes and labels.

Assigning colors to categories is far from trivial. On the one hand, qualitative colors should be distinct, but on the other hand they should minimize perceptual bias by preventing the suggestion of non-existent order or proximity. The selection of color schemes for categorical data first depends on the type of data. For nominal data, such as gender or

nationality, qualitative color schemes are used, while for ordinal data, such as level of urbanization, sequential or diverging color schemes are used [4, 34]. However, for hierarchical categories there are no specific guidelines for selecting color schemes, to the best of our knowledge.

We have designed a hierarchical color scheme with the following properties in mind. First it is a qualitative color scheme that assigns a unique and distinct color to each node of the tree with no perceived order in nodes [4, 34]. Second, to encode parent-child relations, the color of each node is similar to its parent. Third and last, the depth of a node is reflected in the color of a node. By transitivity the last two properties result in similar colors for siblings.

The color schemes that are generated by our proposed method are called Tree Colors. To ensure well balanced perceptual properties, we use the Hue-Chroma-Luminance (HCL) space, a transformation of the CIELUV color space, that is designed with the aim to control human color perception [13]. Colors with different hue values are perceptually uniform in colorfulness and brightness, which does not hold for the popular Hue-Saturation-Value (HSV) and HSL color spaces [34].

We evaluated the Tree Colors method with a user study by comparing it to a color scheme with a distinct colors for each main branch of the tree. The results of this study indicate that Tree Colors can be effective in tree visualizations, especially in tree structured node-link diagrams. However, the results for treemaps are mixed, and therefore

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additional research in this area is needed

This paper is outlined as follows. In Section 3 we describe the proposed method. We provide several applications of statistical graphics that use Tree Colors in Section 5. The conducted user study is described in Section 6. We conclude with a discussion in Section 7.

2 RELATED WORK

Several websites contain examples of visualizations that use color to encode tree structure. For example `newsmap.jp` [31] aggregates news and presents a tree map of news to its users. The color of each news item indicates one of seven news types. Although a treemap the `newsmap.jp` color scheme is not hierarchical. Each news type has a fixed hue value, and the colors within a news type differ in chroma and luminance to make the rectangles more distinct and attractive. In contrast when using Tree Colors sibling nodes have different hues but equal luminance and chroma. IBM’s Many Eyes [12] uses HSV color schemes for treemaps that take groups into account. The colors vary in hue but all have equal saturation and value. Nodes within a group have similar hue values. This is comparable to Tree Colors, but the Many Eyes color scheme is restricted to one grouping and thus not hierarchical. Furthermore instead of HSV Tree Colors uses the perception based HCL color space model, keeping Chroma and Luminance for sibling nodes equal. While there seems to be a need for tree color schemes, to the best of our knowledge no guidelines or description are given in literature for constructing such color schemes.

Most tree visualizations proposed in literature [24] use color to a small extent. A visualization technique that uses color as a major attribute is InterRing [33], a navigation tool with a radial layout. The leaf nodes are assigned different hue values. The color of a parent node is derived by averaging the colors of its children, where larger branches have more weight. An implicit effect of this method is that colors of higher hierarchical levels are less saturated, except for one-child-per-parent branches. Hierarchical color schemes are also applied to the Hyperbolic Wheel [18], an exploration tool for hierarchical data. These color schemes are abstracted from the Hue-Saturation-Lightness (HSL) space, where brightness decreases proportional from root to leaf nodes, and where child nodes inherit the hue values from their parent nodes and add small hue values to distinct them from their siblings. However, hue values of nodes in the same hierarchical layer may be overlapping.

3 METHOD

Our method maps a tree structure on colors in HCL space, which is a transformation of the CIELUV color space, such that it reflects the hierarchical properties of the tree. We use the hue parameter H , with range $[0, 360]$, for the tree structure, where the hue of each child node resembles the hue of its parent. The chroma and luminance parameters C and L , both with range $[0, 100]$, are used to discriminate the different hierarchical levels.

An example of Tree Colors applied to a tree drawn with a radial layout is shown in Figure 2. Although other layouts may be more suitable to highlight tree structure, for instance the Fruchterman-Reingold algorithm [11] applied in the node-link diagram in Figure 1, the applied radial Reingold-Tilford layout [22] preserves the original order of nodes in each hierarchical layer, which is in this case purely alphabetical. This layout helps to illustrate the assignment of Tree Colors to the node of a tree.

3.1 Hue values

Hue values are selected using the following recursive algorithm that assigns to each node v of a tree structure a hue value H_v . The inputs for the algorithm are a hue range r , a hue fraction f , a boolean permutation flag `perm` and a boolean reverse flag `rev`. The root of a tree starts with hue range $r = [H_{start} = 0, H_{end} = 360]$:

AssignHue($v, r, f, \text{perm}, \text{rev}$)

1. Select the middle hue value in r as the hue value of node v , which is H_v ¹.

¹The root node itself is colored grey, so its hue is irrelevant.

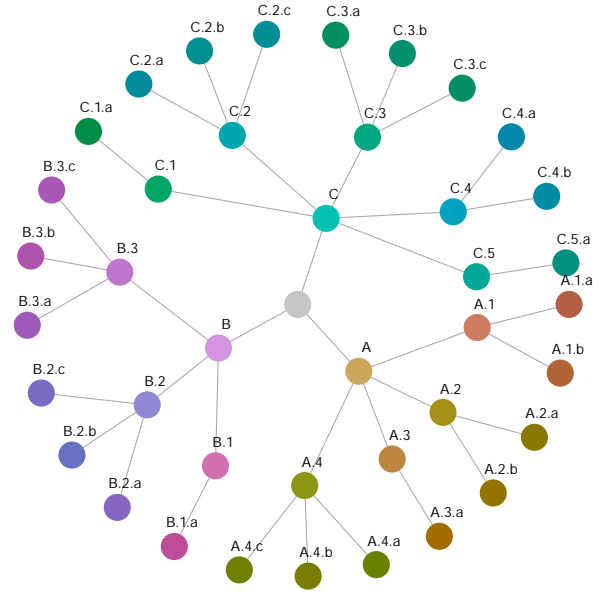


Fig. 2. Radial layout of a tree colored with Tree Colors.

2. Let N be the number of child nodes of v . If $N > 0$:
 - i divide r in N equal parts r_i with $i = 1, \dots, N$;
 - ii if `perm` then permute the r_i 's;
 - iii if `rev` then reverse the even-numbered r_i 's;
 - iv reduce each r_i by keeping its middle fraction f ;
 - v for each child node v_i DO **AssignHue**($v_i, r_i, f, \text{perm}, \text{rev}$).

This algorithm is illustrated in Figure 3. In (a) the full hue range (for a constant $C = 60$ and $L = 70$) is split in three equal parts, since the root node has three children. Of each part, only the middle fractions (f , with a default value of 0.75) are kept in (b) and assigned to A, B, and C. For example, from the part between 0 to 120 degrees, only the $120 \cdot 0.75 = 90$ degrees in the middle, so from 15 to 105 degrees, are kept and assigned to A. In (c) and (d) these steps are recursively taken for the deepest two hierarchical layers.

3.1.1 Hue permutations and reversals

In most hierarchical structures, there is no order between siblings. When the nodes in such structure are plotted in a linear or radial layout, the colors of the siblings should not introduce a perceptual order. Therefore, the assigned hue ranges are by default (`perm=true`) permuted among the siblings.

The used permutation order is based on the five-elements-permutation $[1, 3, 5, 2, 4]$. The permuted order is determined by equally spreading the siblings on a circle in the original order, and to pick the siblings at angles of 0 modulo 144 degrees. Notice that the difference of any two adjacent siblings in $[1, 3, 5, 2, 4]$ is exactly $2/5 \cdot 360 = 144$ degrees, also between the last and the first sibling. For the cases where the number of siblings is not a multiple of five, the modulo angle is rounded down to the next sibling. It may occur that a sibling is picked twice while others have not yet been picked, for instance when 360 is a multiple of the rounded modulo angle. In these cases, the next sibling is picked and the process continues with the same picking angle. To illustrate this method, consider six siblings that are placed at 60 degrees from each other on a circle. The modulo angle will be rounded down to 120. Since this is a multiple of 360, the fourth sibling is picked at an angle of 60 instead of 0 degrees. Hence the picking angles in this case will be 0, 120, 240, 60, 180 and 300 degrees. For the three and four siblings case we use the permutations $[1, 3, 2]$ and $[1, 3, 2, 4]$ respectively to prevent a perceptual order of the siblings in these cases.

The permutations for three to twelve siblings for a hue range between 120 (green) and 240 (blue) are depicted in Figure 4. Note that

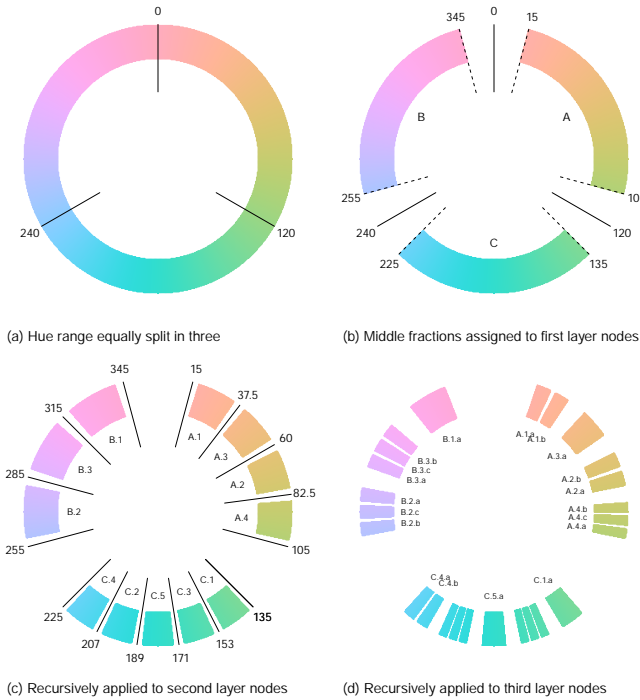


Fig. 3. Assignment of hue values.

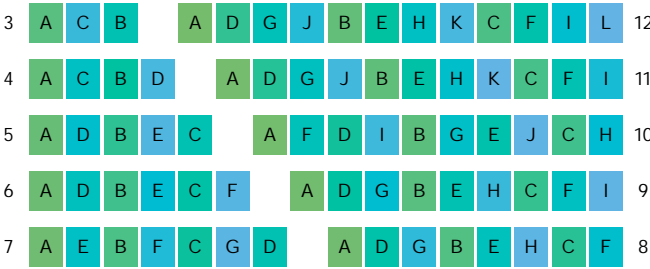


Fig. 4. Permutations of siblings.

the order of the five-siblings case, which is [1, 3, 5, 2, 4], is the position of the siblings A, B, C, D, and E respectively. Therefore, the permutation of them is A, D, B, E, and C.

Furthermore, adjacent leaf nodes with a different parent should have dissimilar colors in order to differentiate between branches. Therefore, the permuted color ranges within even numbered branches are by default reversed (`rev=true`). This is needed because the first category is always mapped to the lowest hue value, and the last category to a higher hue value. In Figure 4, category A has the most greenish color in all shown cases, while the last categories are cyan or blue. To reverse the hue ranges in an alternating way, so only the even-numbered, the hue distance between any two adjacent nodes with different parents will increase, and thus easier to tell apart.

Note that the labeling in Figure 3 shows that the assignment of colors is permuted and also reversed for even-numbered branches. The three top-layer hue ranges [0, 120], [120, 240], and [240, 360] are permuted and therefore assigned to A, C, and B respectively. Since branches A and C are odd-numbered, their hue ranges are permuted but not reversed. The permutations of these branches are [A.1, A.3, A.2, A.4], and [C.1, C.3, C.5, C.2, C.4]. Since branch B is odd-numbered, its hue ranges are not only permuted, but also reversed: [B.2, B.3, B.1].

The result of these permutations is that siblings are better discriminated in each subsequent hierarchical layer, which is illustrated in

Figure 2. For comparison, the permutation is turned off in the node-link diagrams shown in Figure 5. In the left diagram, the hue values form a gradual hue circle with only small hue gaps between branches, which are caused by hue fraction f (see Subsection 3.1.2). In the right diagram the even-numbered branches are reversed. The leaf nodes of branch B are now more distinct from the other leaf nodes. However, the distinction between branches of the second hierarchical layer is still less than with permutation enabled (Figure 2).

The permutations and reversals of hue ranges is developed particularly for visualization methods in which sibling nodes are arranged linearly or radially. However, when sibling nodes are arranged differently, for instance in treemaps, the coloring of sibling nodes may appear random. Therefore, adjacent nodes might get indistinguishable colors in such visualizations.

3.1.2 Hue fraction

The fraction f is needed to introduce a ‘hue gap’ between nodes with a different parent. This choice is a trade-off between discriminating different main branches and discriminating different leaf nodes. If $f = 0$, the hue ranges are diminished to single hue points, which implies that each main branch is assigned a constant hue. On the other end of the extreme, if $f = 1$, the full hue range is available at each hierarchical layer, which makes leaf nodes easier to distinguish, but harder to take apart leaf nodes of different branches. However for a radial or linear layout this can be alleviated by using permutation and reversal.

The choice of f depends on several aspects, such as the application, the size and dimensions of the hierarchical data, and on the used visualization method. In Figures 6 a node-link diagram with a Fruchterman-Reingold layout [11] is shown with different values of f . For such explicit tree visualizations, high values of f can be chosen to discriminate the leaf nodes without losing touch of the global tree structure which is clearly visible, also without Tree Colors. Even values of (or close to) 1.00 are appropriate here. To be on the save side, we suggest $f = 0.75$ for explicit tree visualizations as a guideline.

For implicit tree visualizations where the tree structure is not clearly visible without colors, lower values of f are more suitable. This is illustrated with a treemap and different values of f in Figure 7. We applied the ordered treemap layout [1] for these treemaps. For $f = 0.75$ and especially $f = 1.00$, it is difficult to quickly see the global tree structure; the main categories A and C are hard to take apart as well as the categories B and D. Therefore we suggest $f = 0.50$ as a rule of thumb for implicit tree visualizations.

3.2 Chroma and luminance values

There are basically two methods to encode hierarchical depth in the colors of the nodes. Either brightness increases or decreases with depth. If brightness increases, leaf nodes will be brighter but also less saturated than nodes high in the tree. We refer to this method as the additive color method, since by metaphor, the leaf node colors can be

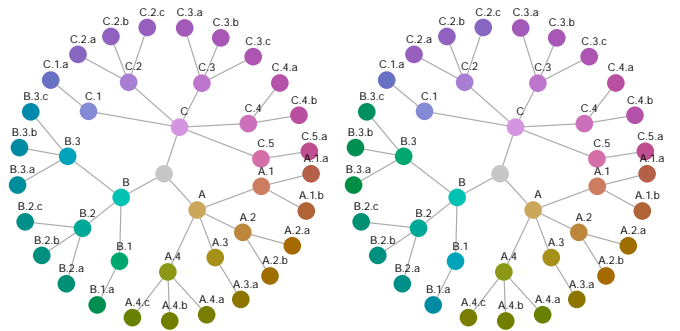


Fig. 5. Node-link diagrams with permutation disabled. Reversal of even-numbered branches is disabled on the left, and enabled on the right.

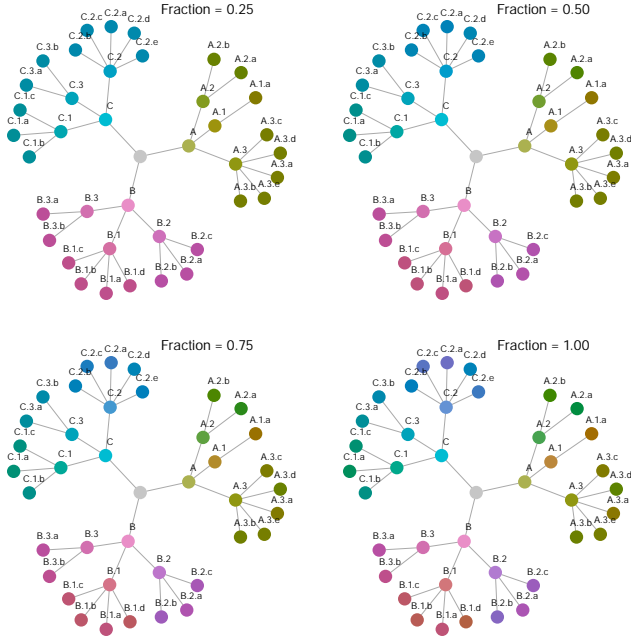


Fig. 6. Node-link diagram with different fraction values.

seen as paint pigments that are mixed towards the dark gray root node. The other method is the subtractive color method in which leaf nodes can be seen as dimmed light beams that are mixed towards the light gray root node. Here, a child node is darker and little more saturated than its parent node.

Throughout this paper, we will use the subtractive color method by default, but the additive color method can be used just as well. The node-link diagram in Figure 2 illustrates the subtractive color method. The nodes in the first hierarchical layer, A, B, and C have the brightest colors which are a little less saturated than the other colors. In Figure 8

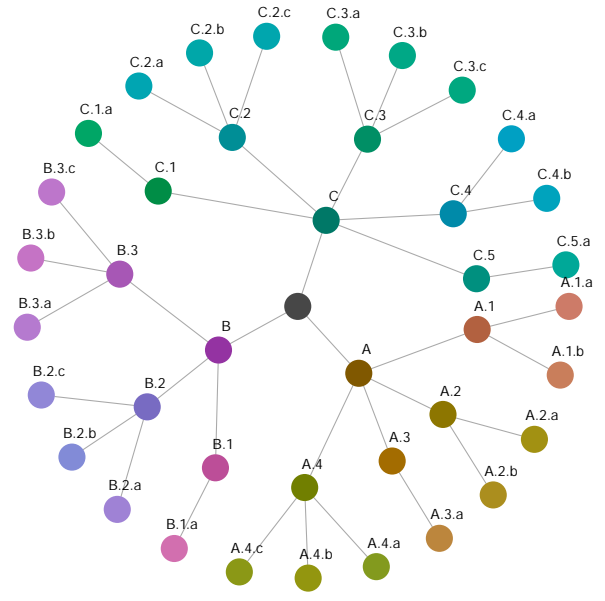


Fig. 8. The additive color method.

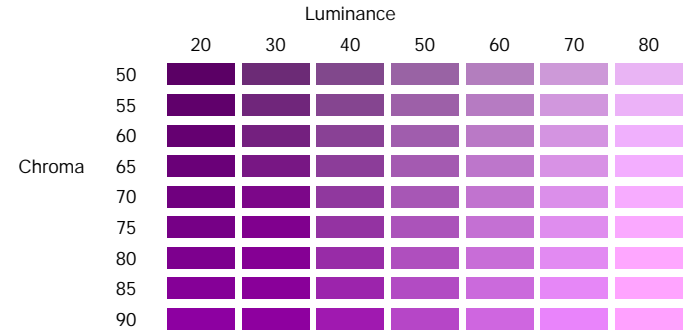


Fig. 9. Colors for different L and C values with a constant $H = 300$.

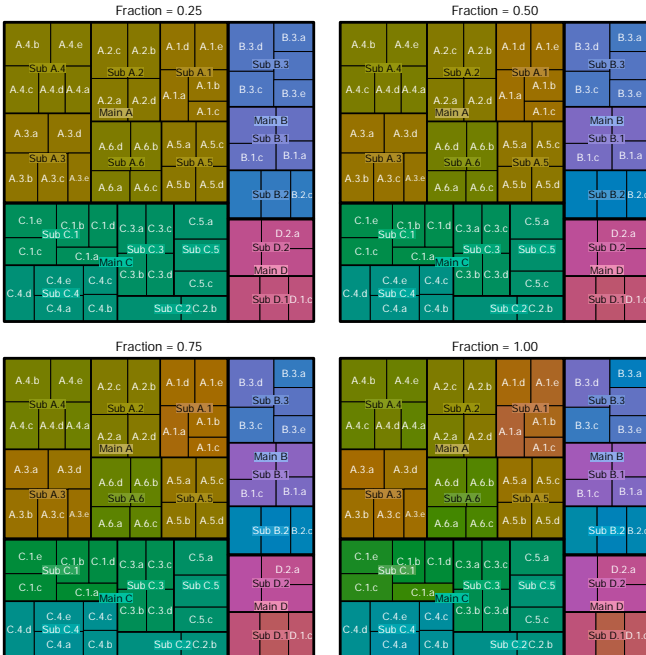


Fig. 7. Treemaps with different fraction values.

the same diagram is shown where the additive color method is applied. In this method A, B, and C are the darkest nodes (except for the root node), and also have the most saturated colors.

For the subtractive method, we let luminance decrease linearly with depth. We set the default luminance value for the first (highest) layer below the root as $L_1 = 70$. For the other layers $i = 2, \dots, d$, where d is the depth of the tree, the luminance value is defined as

$$L_i = (i - 1)\beta^L + L_1, \quad (1)$$

where the default value for the slope parameter β^L is set to -10 . In case the root node is visualized, it is colored grey. Its luminance value is specified by $L_0 = L_1 - \beta^L$. For the additive method, in which luminance increases with depth, we suggest $L_1 = 40$ and $\beta^L = 10$.

In Figure 9 a table of colors are depicted for various chroma and luminance values and a constant hue of $H = 300$. Brighter colors (with higher values of L) have the tendency to become too saturated in our opinion, for instance, the colors with $L = 70$ and $C \geq 70$. However, for dark colors, high values of C may help to discriminate them distinguish them from other dark colors with different hue values. The question therefore is, what values of C are needed for what values of L in order to distinguish the colors easily without using too much saturation.

For different pairs of C and L , color schemes with a fixed hue range from 120 and 360 are depicted in Figure 10. Among the bright color schemes (with $L = 70$) the saturation level of $C = 60$ is sufficient to discriminate the colors easily. For the dark color schemes (with $L = 30$),

saturation values of $C = 80$ or higher are not superfluous, especially because the assigned hue range is often very narrow for nodes low in the tree.

Therefore, we propose to increase C with depth for the subtractive color method. Let $C_1 = 60$ be the chroma value for the first layer. For layer $i = 2, \dots, d$ the chroma value is defined as

$$C_i = (i - 1)\beta^C + C_1, \quad (2)$$

where the slope parameter is set to $\beta^C = 5$ by default. The chroma value for the root node is irrelevant, since it is colored grey. Chroma decreases with depth in the additive method. For this we suggest $C_1 = 75$ and $\beta^C = -5$.

So per hierarchical layer i , we have specified a fixed pair of L_i and C_i based on the parameters L_1 , β^L , C_1 , and β^C . For the default values of these parameters using the subtractive color method, we depicted the pairs with a fixed hue values between 120 and 360 in Figure 11. The pairs for the additive method are by default identical, but reversed where the parameter values for first layer are $L_1 = 75$ and $C_1 = 40$.

Although we propose default parameter values for luminance and chroma, the choice of these values depends on the number of hierarchical layers in the data, and on which layer the attention is focused. The default parameter values for the subtractive method provide colors that are well distinguishable within the first three layers. Therefore, they are particularly useful for datasets up to three hierarchical layers. However, when only leaf nodes of the third layer are visualized, such as in treemaps of data that have a complete tree structure of depth three, a higher L_1 value may be preferred. Also, when the dataset contains five or more layers a higher value of L_1 may also be preferred. In these cases, we suggest L_1 to be 80 or even 90. In order to prevent colors that become too saturated, we suggest C_1 to be 55 or 50 in this situation. However, when more discrimination among the colors is needed, higher values of C_1 may be chosen.

3.3 Parameter overview

An overview of all parameters that are used in the described method is provided in Table 1. The abbreviations sub and add stand for subtractive respectively additive color method.

Due to the ranges of $[0, 100]$, the luminance and chroma parameters are restricted to the following constraints:

$$0 \leq (d - 1)\beta^L + L_1 \leq 100 \quad (3)$$

and

$$0 \leq (d - 1)\beta^C + C_1 \leq 100. \quad (4)$$

Notice that hue values are radial degrees where 360 degrees is a full circle. In order to rotate the hue range, we also allow negative numbers. Furthermore, it is also possible to set $H_{end} < H_{start}$. In that case, the direction in which hue values are assigned is counter-clockwise instead of clockwise.

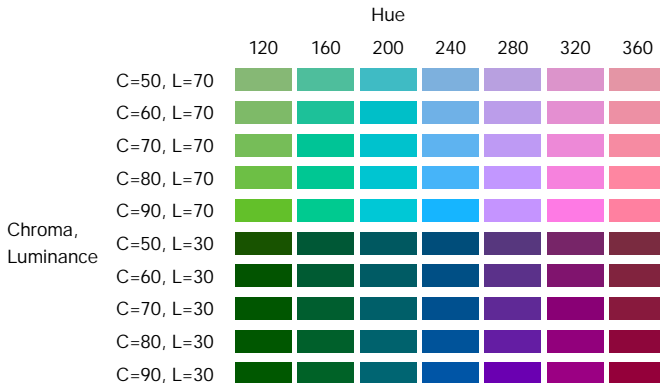


Fig. 10. Colors schemes for different pairs of L and C .

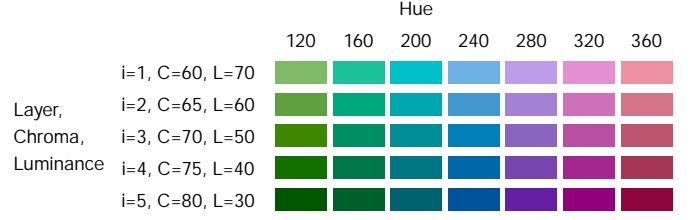


Fig. 11. Colors schemes for matched pairs of default L and C values for the top five hierarchical layers.

Parameter		Range	Default value	
Hue start	H_{start}	-360 to 360	0	
Hue end	H_{end}	-360 to 360	360	
Hue fraction	f	0 to 1	0.75 (explicit)	0.50 (implicit)
Hue permutations	perm	boolean	TRUE	
Hue reverse	rev	boolean	TRUE	
			Sub.	Add.
Luminance first level value	L_1	0 to 100	70	40
Luminance slope value	β^L		-10	10
Chroma first level value	C_1	0 to 100	60	75
Chroma slope value	β^C		5	-5

Table 1. Parameters of the Tree Colors method.

3.4 Color vision deficiency

Although Tree Colors were not developed with color blindness in mind, it is important to know whether Tree Colors are perceived adequately by people with a color vision deficiency, because that is quite common [2].

People with normal color vision, called trichromates, perceive colors by three classes of cone opsins, the S-, M- and L-cone opsins, that have absorption peaks at short (bluish), medium (greenish), respectively long (reddish) wavelengths. Colorblind people only have two classes of cone opsins, and are therefore called dichromats. It may also occur that people have all three classes of cone opsins, but that the absorption peaks of two of them are shifted closer together than normal. Those people, called anomalous trichromats, are able to see the full color spectrum, but have difficulty distinguishing particular colors.

People with color vision deficiency cannot easily differentiate colors with different hue values. Especially distinction between reddish and greenish colors are often problematic for them. If this would be the only obstacle for them to use Tree Colors, a straightforward solution would be to adjust the Tree Colors method by omitting these problematic hue ranges. However, there is a more fundamental problem for people with color vision deficiency. Since the adaption of colors by cone opsins is approximately logarithmic rather than linear, dichromacy or anomalous trichromacy will result in losing the perceptual properties of the HCL color space. In other words, people with a color vision deficiency may not perceive colors with different hue values and constant luminance and chroma values as equally bright and saturated.

Figure 12 shows how people with color vision deficiency would probably see the full hue cycle depicted in Figure 3(a). These simulated plot are created with free software tool Chrometric [9]. The left-hand side plot shows how the full hue circle is seen by anomalous trichromats with deuteranomaly, the most common type of color vision deficiency, where colors of medium wavelength (greenish) colors are not perceived well. Although all hue values seem to be distinguishable, the colors do not seem to be perceived equally bright and saturated. The plot on the right-hand side is seen by dichromats with protanopia, where the long wavelength (reddish) colors are not per-

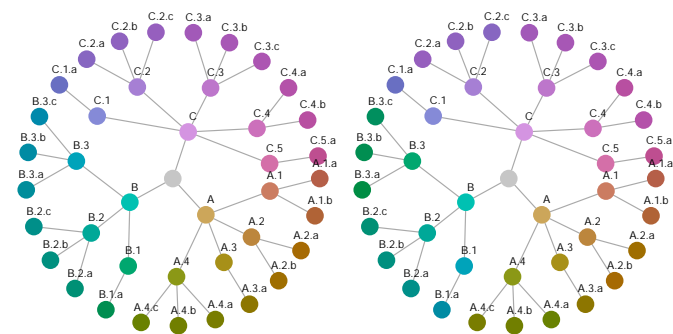


Fig. 12. Simulation of how persons with deuteranomaly (left) and protanopia (right) see the full hue circle. **TO DO Martijn**

ceived. Not only the diversity of hue values is reduced, the colors also have a large variation in brightness and saturation.

4 SOFTWARE

The Tree Colors method is implemented in the `treemap` package [28] of the statistical software environment R [21] and can be downloaded from The Comprehensive R Archive Network (CRAN). All treemaps in this paper are created directly with this package, without post-processing. The implemented layout algorithms are the ordered treemap layout algorithm (pivot by size) [1] and the squarified treemap layout algorithm [5]. By default, Tree Colors are used to emphasize the hierarchical structure of the data. However, the color attribute can also be used for a second variable or to compare two hierarchical datasets [29]. The node-link diagrams in this paper are also created with the `treemap` package. The layout of the nodes are processed with the dependency package `igraph` [8].

To visualize Tree Colors and to tune its parameters, the `treemap` package contains an interactive tool called `treecolors`. With this tool, users can create random tree structured data, and experiment with the parameters. Four visualizations can be shown: two node-link diagrams (Reingold-Tilford and Fruchterman-Reingold), a treemap and a bar chart. It also provides a table of the data that includes the color values in hexadecimal format and the HCL values of all tree nodes. **The sunburst plot is generated with `d3.js` [3] and Tree Colors.**

5 APPLICATIONS

In this section, we discuss the application of Tree Colors to tree visualizations with real-world statistical data.

5.1 Economic activity

The *Nomenclature statistique des activités économiques dans la Communauté européenne* (NACE) [10] is a classification system of economic activity that is often used for national statistics on business enterprises. In Figure 13, the NACE labels of the sector G, wholesale and retail trade, are depicted by a node-link diagram with the Fruchterman-Reingold layout algorithm [11]. Other layout algorithms, e.g. Kamada-Kawai [16], typically better express the tree structure but at the cost of having less space per node. Using Tree colors allows for a more spaced-out layout scheme by expressing tree structure in color.

Figure 14 shows the net turnover of the Dutch wholesale and retail trade enterprises in 2011 [23] in a sunburst layout [26, 27] with Tree Colors. The angle of a arc corresponds to its net turnover. A sunburst plot, which is a radial version of a layered icicle plot [17, 7], typically repeats the same qualitative color scheme for child nodes: sibling nodes have different colors, but their children use the same color scheme. This makes siblings more distinct, but makes the tree structure less visible. In contrast, Tree Colors better show the hierarchical structure of data.

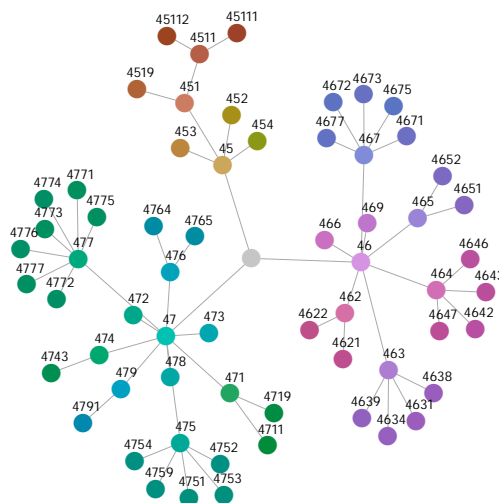


Fig. 13. Node-link diagram of all wholesale and retail trade NACE labels produced by the Fruchterman-Reingold layout algorithm.

In Figure 15, the same dataset is visualized by a treemap. The Tree Colors of the non-leaf nodes are used for the text label backgrounds. Notice that the colors of the third NACE layer nodes, for instance the pink colored 466, are brighter than the colors of the other leaf nodes. The depth of leaf nodes is more difficult to observe in treemaps than in other visualization methods such as a sunburst diagram, apart from the used color schemes.

5.2 Regional classifications

Many publications in official statistics are broken down by region, especially regarding demographics. In many situations, thematic maps are useful as a data visualization tool for spatial statistics, in particular choropleths and cartograms. However, non-cartographic methods are often sufficient for the task at hand. In those cases, the geographic location of the regions is less important for the analysis than the comparison of some specific target variable between regions. Tree Colors can improve the discrimination between the regions in a subtle way.

In Figure 16 a bar chart, created with the R package `ggplot2` [32], is shown of the Dutch population broken down by twelve provinces. For comparing the populations to each other, a bar chart is a good working horse, since length is perceived quite accurately [19]. We applied Tree Colors to add information about the geographical layout of the

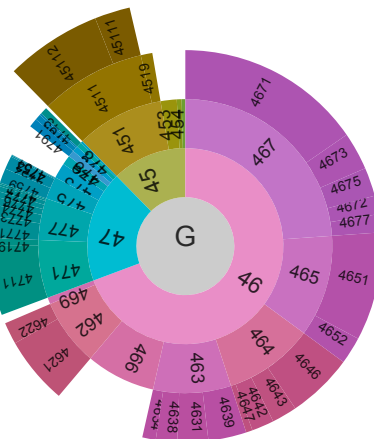


Fig. 14. Sunburst diagram with Tree Colors.

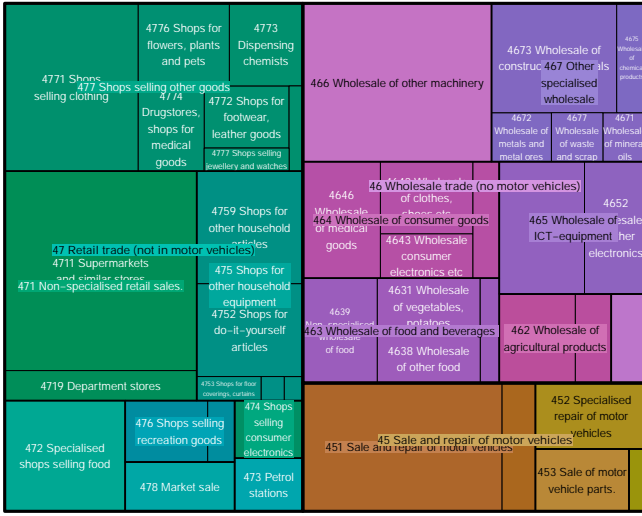


Fig. 15. Turnover among Dutch wholesale and retail trade enterprises in 2011 **TO DO Martijn: check colors and sizes (consistency with other plots)**

provinces. Typically, the provinces are grouped by the cardinal directions north, east, west, and south. We use those directions as the first hierarchical layer, and the provinces themselves as the second hierarchical layer. The obtained Tree Colors discriminate the provinces while grouping them by cardinal direction. To enhance groupings, the vertical space between any two adjacent bars that represent provinces in different cardinal directions is slightly increased.

6 USER STUDY

A user study has been conducted to evaluate our proposed method. We let participants compare Tree Colors to Main Branch Colors. Main Branch Colors form a qualitative color scale that assigns distinct qualitative colors to the children of the root and gives their offspring the same color as their parent. The colors are taken from the qualitative

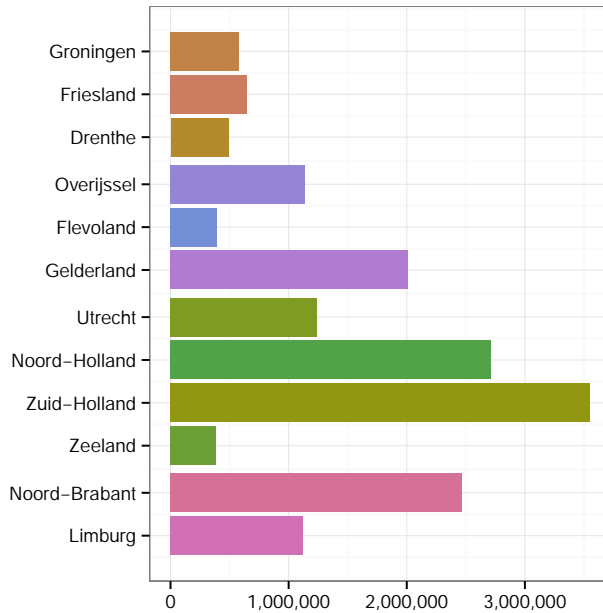


Fig. 16. Dutch population in 2012 per province

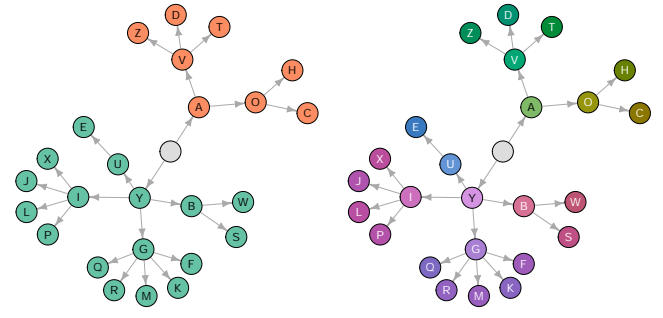


Fig. 17. Node link diagrams applied to Dataset 1 with Main Branch Colors (left) and Tree Colors (right)

ColorBrewer color schemes [4], which are user tested and popular in cartography and statistical visualizations, and hence provide a good benchmark for Tree Colors. An alternative would have been testing against a Tree Colors scheme with $f = 0$, but such color schemes are not in common use and testing three colors schemes would have complicated the user study.

6.1 Questionnaire setup

The questionnaire was taken by employees of Statistics Netherlands. Although no specific demographic characteristics were asked, the participants typically have at least a bachelor's degree in quantitative sciences. Furthermore all employees are aged from 18 to 65 years old, and gender is approximately equally divided. In order to know whether a participant has a color vision deficiency, we directly asked the participants whether they are (partially) color blind. Participants who did not know the answer to that question were tested for color vision deficiency using the Ishihara test [14].

Three visualization methods were used in the questionnaire, namely the node-link diagram, the treemap, and the bar chart. For each of the three methods, participants received questions for two charts of two different datasets, one with Tree Colors and one with Main Branch Colors.

In order to exclude the effects of all other aesthetics but color as much as possible, we distributed two different versions of the questionnaire. Each participant was randomly assigned to one version. For the two versions, the datasets for the Main Branch Colors and Tree Colors questions were swapped. Therefore, each chart was tested with both color schemes but in different groups. A node-link diagram, a treemap, and a bar chart that were included in the questionnaires are depicted in Figure 17, 18, and 19 respectively. An overview of the charts used in the two versions of the questionnaire is provided in Table 2. We alternated the used color schemes per visualization method in order to prevent a repeating systematic pattern in the questionnaire. Unfortunately, it was not possible to invert the alternating schemes, since this would require two extra versions of the questionnaire.

Method	Color scheme	Version 1	Version 2
Node-link diagram	Main Branch Colors	Dataset 1	Dataset 2
Node-link diagram	Tree Colors	Dataset 2	Dataset 1
Treemap	Main Branch Colors	Dataset 4	Dataset 3
Treemap	Tree Colors	Dataset 3	Dataset 4
Bar chart	Main Branch Colors	Dataset 5	Dataset 6
Bar chart	Tree Colors	Dataset 6	Dataset 5

Table 2. Overview of charts in the questionnaire

The three visualization methods represent three levels of hierarchical explicitness. The node-link diagram clearly is an explicit tree visualization by the layout of the nodes and by the edges, which are

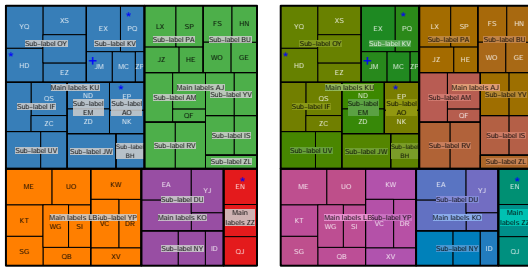


Fig. 18. Treemaps applied to Dataset 4 with Main Branch Colors (left) and Tree Colors (right)

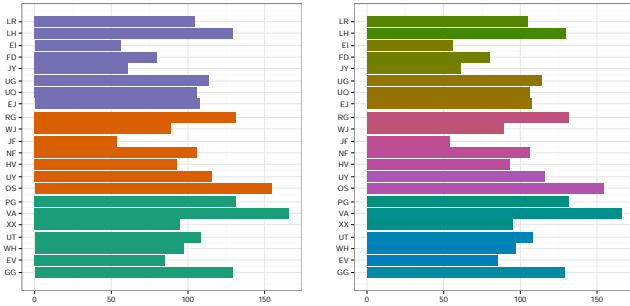


Fig. 19. Bar charts applied to Dataset 5 with Main Branch Colors (left) and Tree Colors (right)

depicted as directed arcs pointed from the root node. The treemap is an implicit visualization method, in which the hierarchical structure is less clear in comparison to the node-link diagram. Except for color, the hierarchical structure is represented by the nesting of the rectangles, the thickness of the rectangle lines, and by the label fonts. The bar chart is in essence a non-hierarchical visualization method. However, the bar charts that were included in the questionnaire contained beside color an extra subtle hierarchical element in the spacing between the bars. The bars represent the leaf nodes of the tree structure and the amount of spacing between two bars is determined by the degree of relationship.

All datasets used in the questionnaire are hierarchically structured with three hierarchical layers. The labels of the data points are randomized letters, such that participants were not able to extract information about the hierarchy from the printed labels.

The questionnaire contained reading and evaluation questions. Per chart, participants got one or two reading questions and one evaluation question:

Relations Which label(s) are most similar to X? The answer options consisted of one label from a different main branch than X, one or two labels from the same main branch but a different sub branch, and one label from the same sub branch as X. From the data structure point of view, we considered the last label as the correct answer.

Offspring How many sub-labels does main branch X have? This was an open question.

Help What do you think of the following statement? The charts colors helped me to answer the question(s) above. This question is a five-level Likert item with the answer options Strongly disagree (SD), Disagree (D), Neutral (N), Agree (A) and Strongly agree (SA).

Per visualization method, participants were asked those reading questions for two plots of different datasets, one with Main Branch Colors

and one with Tree Colors. Next, participants were asked to evaluate these two plots with three questions:

Prettiness Which chart is the prettiest?

Interpretation Which colors contributed most in interpreting the charts?

Overview Which colors provided the best overview?

Finally, participants were given the possibility to write down comments or suggestions.

6.2 User study results

We recruited 98 participants with normal color vision and 10 participants with a color vision deficiency. From the people with normal color vision, 58 participants received Version 1 of the questionnaire and 40 Version 2. Among those with a color vision deficiency, 4 participants received Version 1 and 6 participants Version 2.

The results of the reading questions are summarized in the left part of Figure 20. Per dataset the percentages of correct answers, that is, from a data structure point of view, are shown in orange for the Main Branch Colors and in blue for the Tree Colors. For each percentage, the corresponding 95% confidence interval is depicted as a line. The right part of Figure 20 shows per visualization method the distribution of answers to the question whether colors had helped in answering the reading questions.

Of all three visualization methods, the reading questions regarding the node-link diagrams received the highest percentages of correct answers for both color schemes. The reason is the questions were fairly easy to answer by the explicit tree layouts of the node-link diagrams. The questions about the offspring resulted in 100% scores for all four color-scheme-dataset combinations. As for the node-link diagrams, participants experienced more help from Tree Colors than from Main Branch Colors.

The percentages of correct answers for the treemaps were lower than for the node-link diagrams. One reason could be that people are not familiar with treemaps; it turned out the many participants also took into account other aesthetics of the rectangles, in particular aspect ratio and area size, for answering the questions. Although the percentages of correct answers between both color schemes are comparable, the Main Branch Colors scored almost significantly better than the Tree Colors on the questions about the number of sub-labels for Dataset 4. This could be caused by the limitation that hue permutations and reversals were not designed for two-dimensional visualization methods. For treemaps, two adjacent rectangles may therefore get indistinguishable hue values, such as sub-labels PA and BU in Figure 18 (left).

As for the bar charts, the majority of the participants did not observe the underlying data hierarchy when the Main Branch Colors were applied. Apparently, the spacing between the bars did not stand out clearly in comparison to other aesthetics such as color and length. For example, the question that belongs to Figure 19 (left) was which labels are most similar to UT, where the answers options are NF, XX, EV, and GG. Almost 52% of the participants chose the labels that belong to the same main branch, XX, EV and GG, and therefore only used color to answer the question. Another 28% only used length to answer the question, since they answered NF. Only 3% of the participants answered EV, which is given the data hierarchy the correct answer. When Tree Colors were applied, see Figure 19 (right), none of the participants checked XX, EV, and GG, 23% chose the equal-length bar NF, and 63% answered EV correctly. This result indicates that Tree Colors can be a valuable attribute to visualize a hierarchical data structure in non-hierarchical plots such as bar charts, line charts, and area charts.

The three evaluation questions are summarized in Figure 21 with a diverging stacked bar chart. In general, the participants liked both color schemes equally, although Tree Colors were favored for node-link diagrams.

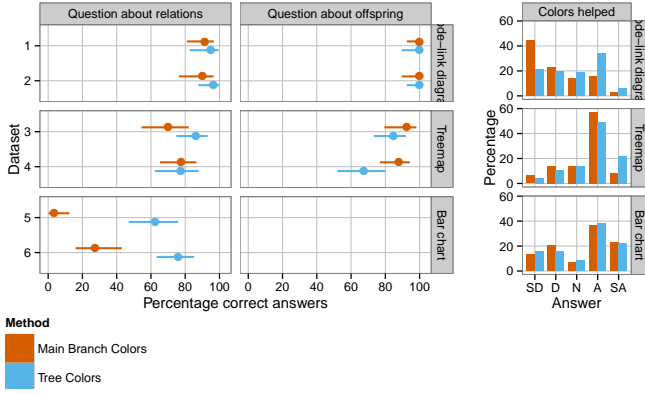


Fig. 20. Results of the reading questions

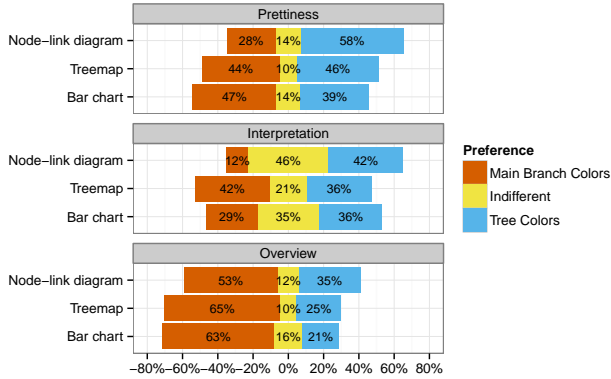


Fig. 21. Results of the evaluation questions

The charts with Main Branch Colors provided the best overview for the majority of the participants. This result is not surprising, since a good overview is obtained by discriminating the main branches. Recall that Tree Colors can be adjusted with parameter f in order to better discriminate main branches, and therefore getting a better overview at the expense of the discrimination of leaf nodes.

The results of the user study regarding the 10 participants with color vision deficiency are summarized in Table 3. By the small number of these participants, we were unable to make statistical claims from their responses. In line with the participants with normal color vision, most of them (64%) experienced a better overview with Main Branch Colors than with Tree Colors (15%).

	Node-link diagram		Treemap		Bar chart
	relations	offspring	relations	offspring	relations
M. B. C.	7	10	5	10	0
Tree Colors	7	10	5	6	3

Table 3. Numbers of correct answers to the reading questions asked to the 10 participants with color vision deficiency.

7 DISCUSSION

We proposed a method to create color schemes for tree structured data. In our opinion, this method improves both hierarchical and non-hierarchical visualizations methods when the tree structure of the data plays a role in the analysis. Tree Colors satisfy the three properties

that we described in Section 1, namely that 1) all colors of a hierarchical color scheme should be unique, 2) the colors should reflect the tree structure in terms of parent-child relationships, and 3) hierarchical depth should be encoded in color.

Although the choice to use hue to discriminate between different branches is straightforward and therefore not novel [33, 18], the actual mapping of tree structures to hue values involves two innovative techniques. First, we introduced hue gaps to obtain hue values that are grouped by branch to a certain extent, which is determined by the parameter f . The second novel technique is the permutation and reversals of the hue values, which results in a better differentiation of the nodes, both between siblings and between adjacent nodes with a different parent.

As for the hierarchical depth, we proposed a linear relation of depth with both luminance and chroma. By default we used the subtractive color method where luminance decreases and chroma increases with depth. The opposite holds for the additive color method that can be used alternatively. Further research on the preferences and usefulness of both methods is recommended.

For explicit tree visualizations such as node-link diagrams, the conducted user study suggests that Tree Colors are a useful enhancement. Although most participants answered the questions regarding the node-link diagrams correctly for both color schemes, a large part of them found Tree Colors more helpful and found node-link diagrams with Tree Colors better to interpret than with Main Branch colors. As a consequence, using Tree Colors for node-link diagrams enables relaxing a hierarchical layout of the nodes, therefore spacing-out the placements of nodes and labels.

As mentioned in Section 3.1.1. The coloring of sibling nodes is designed for layouts in which they are arranged linearly or radially. For two-dimensional visualization methods such as treemaps, two adjacent siblings can therefore get indistinguishable colors, which was also the case in the user study example. For further research, it is worthwhile to improve the permutation and reversal method for such visualization methods. Approaches to similar problems, such as the coloring of edges in a graph [15] may be useful.

More advanced user studies might reveal more insightful differences between Tree Colors and other tree coloring methods when applied to tree visualizations. It may be worthwhile to analyze response times [30] to reveal differences between the effectiveness of both color schemes, and to conduct eye tracking experiments [6], to provide insight in how the participants understand the visualized tree structure with different color schemes.

We would like to remark that although the HCL color has well defined perceptual properties, the total range of hue values is not perceived perfectly linear, especially around non-primary colors. This could introduce certain artifacts in the resulting color schemes. For instance, the blue node U in Figure 17 (right) seems to be more distinct from its parent Y than its siblings I, G, and B. Such artifacts could be overcome by rotating the total hue range with the parameters H_{start} and H_{end} .

Unfortunately, Tree Colors are not adequately perceived by people with color vision deficiency, since the range of distinguishable hue values is reduced and colors with a constant luminance and chroma value may vary in perceived brightness and saturation. There are no straightforward solutions at hand to adjust the Tree Colors method for people with color vision deficiency. Moreover, designing fixed qualitative color schemes for such people is already far from trivial [20]. Further research is needed to develop hierarchical color schemes for people with color vision deficiency. From a practical point of view, we suggest to use color vision deficiency proof qualitative color schemes proposed in literature [20, 4] as Main Branch Colors for people with color vision deficiency.

Although Tree Colors can be generated for hierarchical datasets of any size, it is still unknown how effective they are for large hierarchical datasets, both in terms of depth as in average number of siblings per node. For deep hierarchical datasets, the luminance and chroma ranges could be enlarged, and the slope parameters β^L and β^C could be made smaller. With both adjustments, the distinction between col-

ors of different hierarchical layers is reduced. For hierarchical dataset with many siblings per node, the available hue range have to be split by a large number, resulting in less distinctive colors. However, with carefully tuned parameters, Tree Colors may be effective for particular analytics with large hierarchical datasets. Evaluation of Tree Colors for large datasets is recommended.

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REFERENCES

- [1] B. B. Bederson, B. Shneiderman, and M. Wattenberg. Ordered and quantum treemaps: Making effective use of 2D space to display hierarchies. *ACM Trans. Graph.*, 21(4):833–854, 2002.
- [2] J. Birch. Worldwide prevalence of red-green color deficiency. *J Opt Soc Am A Opt Image Sci Vis.*, 29(3):313–320, 2012.
- [3] M. Bostock. D3.js. *Data Driven Documents*, 2012.
- [4] C. A. Brewer, G. W. Hatchard, and M. A. Harrower. ColorBrewer in print: A catalog of color schemes for maps. *Cartography and Geographic Information Science*, 30(1):5–32, 2003.
- [5] M. Bruls, K. Huizing, and J. van Wijk. Squarified treemaps. In *In Proceedings of the Joint Eurographics and IEEE TCVG Symposium on Visualization*, pages 33–42. Press, 1999.
- [6] M. Burch, N. Konevtsova, J. Heinrich, M. Hferlin, and D. Weiskopf. Evaluation of traditional, orthogonal, and radial tree diagrams by an eye tracking study. *IEEE Trans. Vis. Comput. Graph.*, 17(12):2440–2448, 2011.
- [7] M. Burch, M. Raschke, and D. Weiskopf. Indented pixel tree plots. In *Advances in Visual Computing*, pages 338–349. Springer, 2010.
- [8] G. Csardi and T. Nepusz. The igraph software package for complex network research. *InterJournal, Complex Systems*:1695, 2006.
- [9] M. Englund. *Chrometric*, 2010. Version 0.93.
- [10] Eurostat. NACE rev. 2 - statistical classification of economic activities. Online publication, http://epp.eurostat.ec.europa.eu/portal/page/portal/nace_rev2/introduction, 2008.
- [11] T. M. J. Fruchterman and E. M. Reingold. Graph drawing by force-directed placement. *Softw., Pract. Exper.*, 21(11):1129–1164, 1991.
- [12] IBM. Many eyes. Website, <http://www-958.ibm.com/software/analytics/labs/manyeyes/>, 2013.
- [13] R. Ihaka. Colour for presentation graphics. In *Proceedings of the 3rd International Workshop on Distributed Statistical Computing, Vienna Austria*, 2003.
- [14] S. Ishihara. *Tests for colour-blindness*. Handaya, Tokyo, Hongo Haruki-cho, 1917.
- [15] R. Jianu, A. Rusu, A. J. Fabian, and D. H. Laidlaw. A coloring solution to the edge crossing problem. *2013 17th International Conference on Information Visualisation*, 0:691–696, 2009.
- [16] T. Kamada and S. Kawai. An algorithm for drawing general undirected graphs. *Inf. Process. Lett.*, 31(1):7–15, Apr. 1989.
- [17] J. B. Kruskal and J. M. Landwehr. Icicle plots: Better displays for hierarchical clustering. *The American Statistician*, 37(2):162–168, 1983.
- [18] H.-C. Lam and I. D. Dinov. Hyperbolic Wheel: A novel hyperbolic space graph viewer for hierarchical information content. *ISRN Computer Graphics*, vol. 2012:Article ID 609234, 10 pages, 2012.
- [19] J. Mackinlay. Automating the design of graphical presentations of relational information. *ACM Trans. Graph.*, 5(2):110–141, Apr. 1986.
- [20] M. Okabe and K. Ito. Color Universal Design (CUD) - how to make figures and presentations that are friendly to colorblind people -. Online publication, <http://jfly.iam.u-tokyo.ac.jp/color/>, 2002 (modified 2008).
- [21] R Core Team. *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria, 2013. ISBN 3-900051-07-0.
- [22] E. M. Reingold and J. S. Tilford. Tidier drawings of trees. *IEEE Trans. Software Eng.*, 7(2):223–228, 1981.
- [23] Statistics Netherlands. Statline: Trade and industry. Online publication, <http://statline.cbs.nl>, 2014.
- [24] H.-J. Schulz. Treevis.net: A tree visualization reference. *IEEE Comput. Graph. Appl.*, 31(6):11–15, 2011.
- [25] B. Shneiderman. Tree visualization with tree-maps: 2-d space-filling approach. *ACM Trans. Graph.*, 11:92–99, 1992.
- [26] J. Stasko, R. Catrambone, M. Guzdial, and K. McDonald. An evaluation of space-filling information visualizations for depicting hierarchical structures. *International Journal of Human-Computer Studies*, 53(5):663–694, 2000.
- [27] J. Stasko and E. Zhang. Focus+ context display and navigation techniques for enhancing radial, space-filling hierarchy visualizations. In *Information Visualization, 2000. InfoVis 2000. IEEE Symposium on*, pages 57–65. IEEE, 2000.
- [28] M. Tennekes. *treemap: Treemap visualization*, 2014. R package version 2.2.
- [29] M. Tennekes and E. de Jonge. Top-down data analysis with treemaps. In *Proceedings of the International Conference on Information Visualization Theory and Applications, IVAPP 2011*, 2011.
- [30] Y. Wang, S. T. Teoh, and K.-L. Ma. Evaluating the effectiveness of tree visualization systems for knowledge discovery. In B. S. Santos, T. Ertl, and K. I. Joy, editors, *EuroVis*, pages 67–74. Eurographics Association, 2006.
- [31] M. Weskamp. Newsmap. Website, <http://newsmap.jp>, 2014.
- [32] H. Wickham. *ggplot2: elegant graphics for data analysis*. Springer New York, 2009.
- [33] J. Yang, M. O. Ward, and E. A. Rundensteiner. InterRing: An interactive tool for visually navigating and manipulating hierarchical structures. In *Proceedings of the IEEE Symposium on Information Visualization (InfoVis'02)*, pages 77–84, 2002.
- [34] A. Zeileis, K. Hornik, and P. Murrell. Escaping RGBland: Selecting colors for statistical graphics. *Comput. Stat. Data Anal.*, 53(9):3259–3270, 2009.